

Lab W1D5

Question 1. Goal of this question is to understand inversions.

In Slide 13 (Lesson 4), you have been introduced to inversions. In fact it has the following example.

Example. The array $arr = \{34, 8, 64, 51, 32, 21\}$ has nine inversions:

$(34, 8), (34, 32), (34, 21), (64, 51), (64, 32),$

$(64, 21), (51, 32), (51, 21), (32, 21).$

Apply Bubble Sort on array arr . List all inversions and the number of inversions **after each iteration of the outer loop**. (Please complete the table. Add/delete rows as required.)

| Iteration | inversions | # inversions |
|-----------|--|--------------|
| 0 | $(34, 8), (34, 32), (34, 21), (64, 51), (64, 32), (64, 21), (51, 32), (51, 21), (32, 21).$ | 9 |
| | | |
| | | |

Total number of inversions for Bubble Sort =

Apply Selection Sort on array arr . List all inversions and the number of inversions **after each iteration of the outer loop**. (Please complete the table. Add/delete rows as required.)

| Iteration | inversions | # inversions |
|-----------|--|--------------|
| 0 | $(34, 8), (34, 32), (34, 21), (64, 51), (64, 32), (64, 21), (51, 32), (51, 21), (32, 21).$ | 9 |
| | | |
| | | |

Total number of inversions for Selection Sort =

Apply Insertion Sort on array arr . List all inversions and the number of inversions **after each iteration of the outer loop**. (Please complete the table. Add/delete rows as required.)

| Iteration | inversions | # inversions |
|-----------|--|--------------|
| 0 | $(34, 8), (34, 32), (34, 21), (64, 51), (64, 32), (64, 21), (51, 32), (51, 21), (32, 21).$ | 9 |
| | | |
| | | |

Total number of inversions for Insertion Sort =

Question 2. Aim of this question is to understand amortized cost analysis.

Consider the following sequence of operations:

add, add, add, add, clear, add, add, add, add, add, add, clear, add, add, add, add, clear, add, add, add, add, add, add, add, add, add, clear.

- (a) What is the actual total cost?
- (b) What is the average actual cost?
- (c) What is the amortized total cost?
- (d) What is the average amortized cost?