

# Combining Deep Generative Models and Multi-lingual Pretraining for Semi-supervised Document Classification

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Code: [https://github.com/cambridgeltl/mling\\_sdgms](https://github.com/cambridgeltl/mling_sdgms)



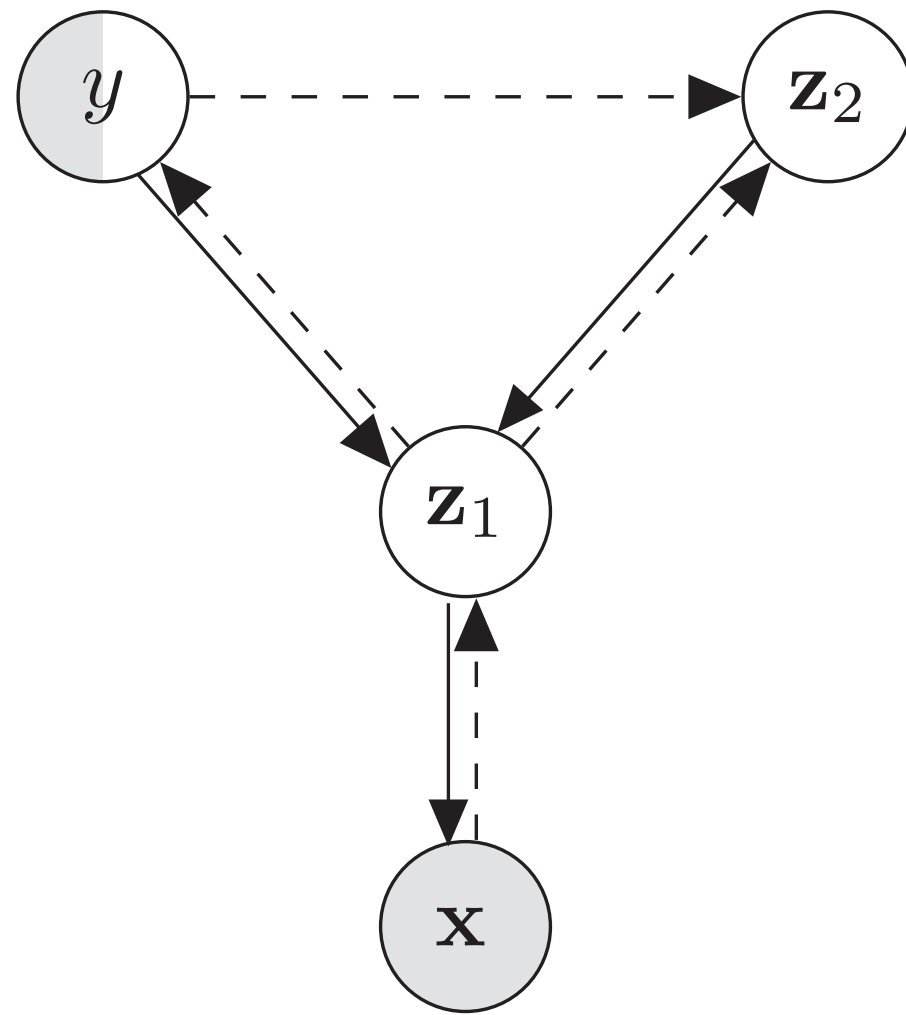
# Deep generative models+Multi-lingual Pretraining

- Deep generative models (**DGMs**)
  - capable of capturing complex data distributions at scale with rich latent representations
- Semi-supervised deep generative models (**SDGMs**)
  - leverage both *labelled* and *unlabelled* data by modelling input and output (label) together

# Deep generative models+Multi-lingual Pretraining

- Deep generative models (**DGMs**)
  - capable of capturing complex data distributions at scale with rich latent representations
- Semi-supervised deep generative models (**SDGMs**)
  - leverage both *labelled* and *unlabelled* data by modelling input and output (label) together
- Effectively use *unlabelled* data through learning shared representations across languages that can be transferred to downstream tasks
- The lack of *labelled* data still leads to inferior performance of the same model compared to those trained in languages with more labelled data such as English

# Deep generative models+Multi-lingual Pretraining

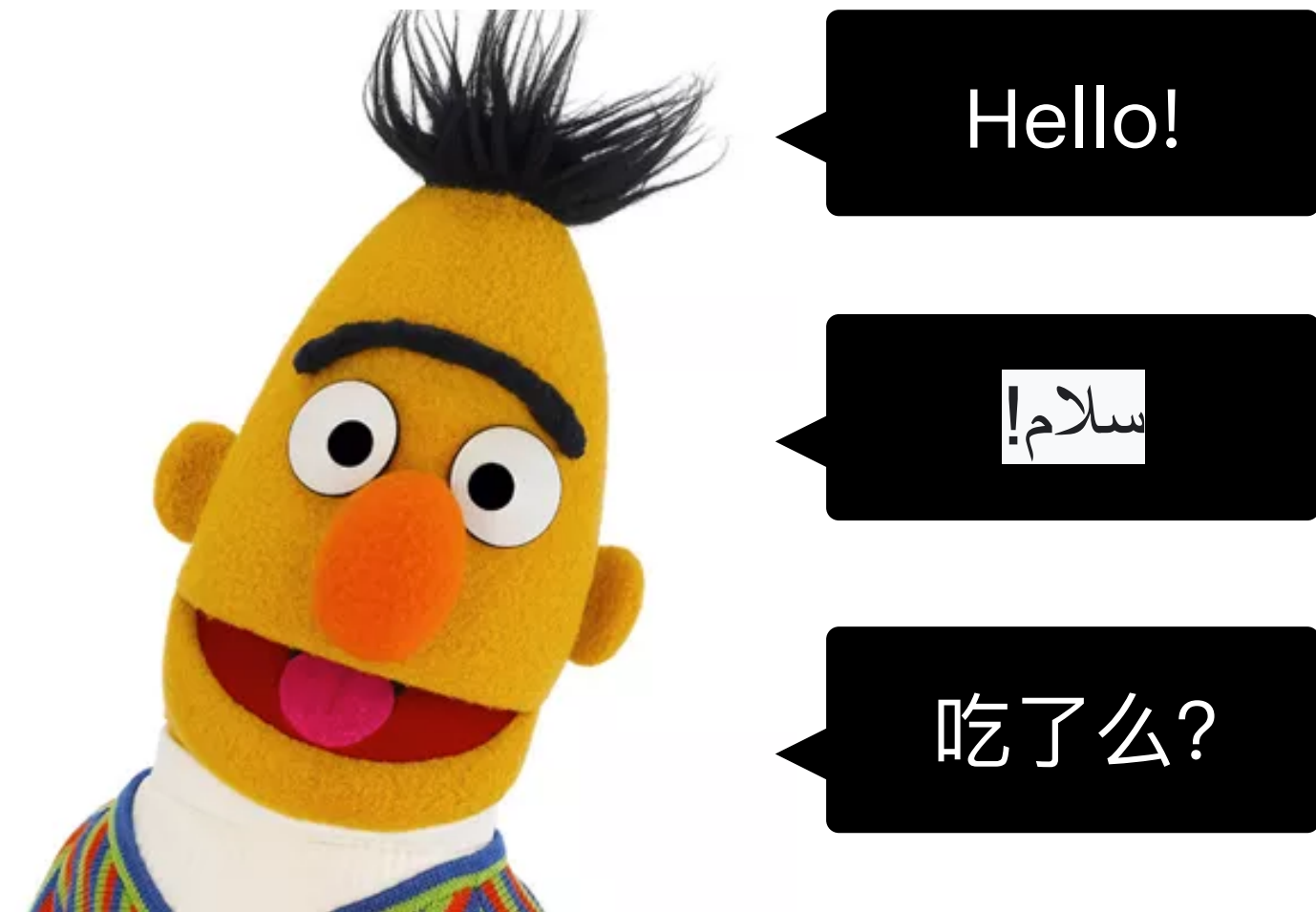
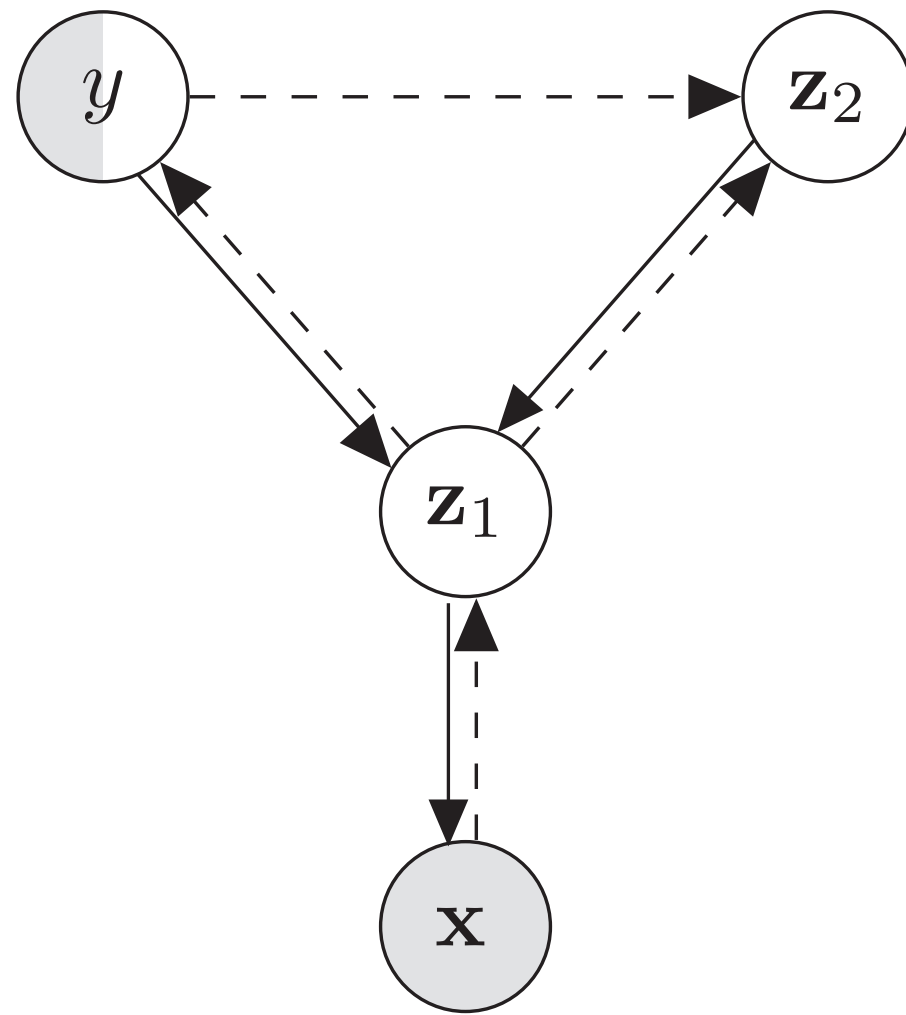


Hello!

سلام!

吃了么?

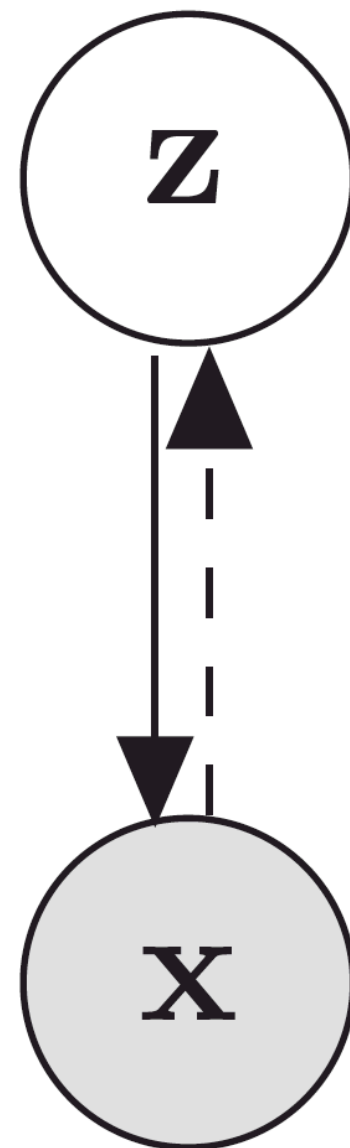
# Deep generative models+Multi-lingual Pretraining



- We bridge the gap to form a **pipeline framework** by combining both for *multi-lingual document classification*
  - The multi-lingual pretrained model serves as multi-lingual encoder
  - SDGMs can operate on top of it independently of encoding architecture

# DGMs

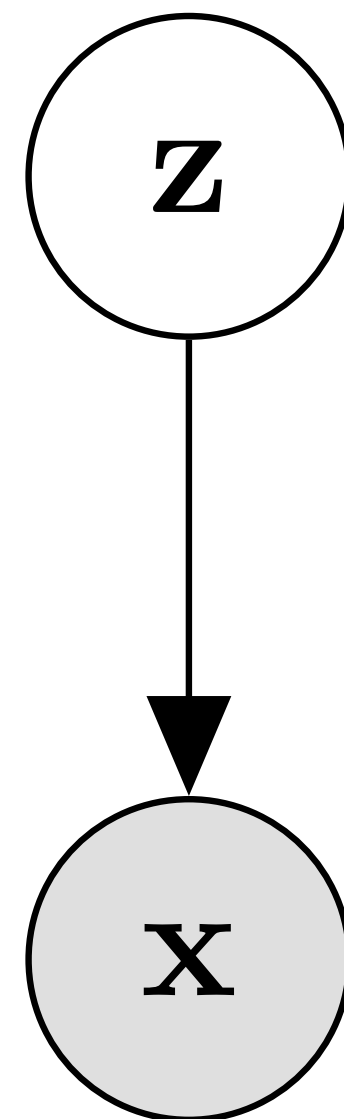
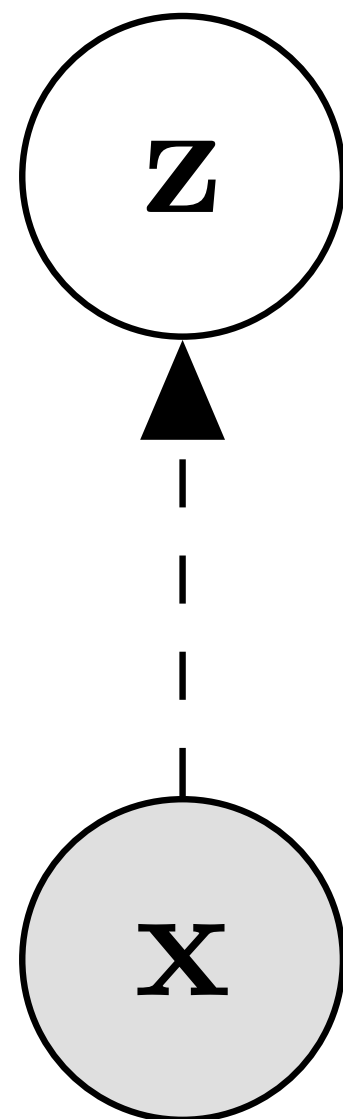
**VAE [Kingma et al. 2014]**



$$\mathbb{E}_{q_{\phi}(\mathbf{z}|\mathbf{x})} \left[ \log \frac{p_{\theta}(\mathbf{x}, \mathbf{z})}{q_{\phi}(\mathbf{z}|\mathbf{x})} \right] \leq \log p(\mathbf{x})$$

# DGMs

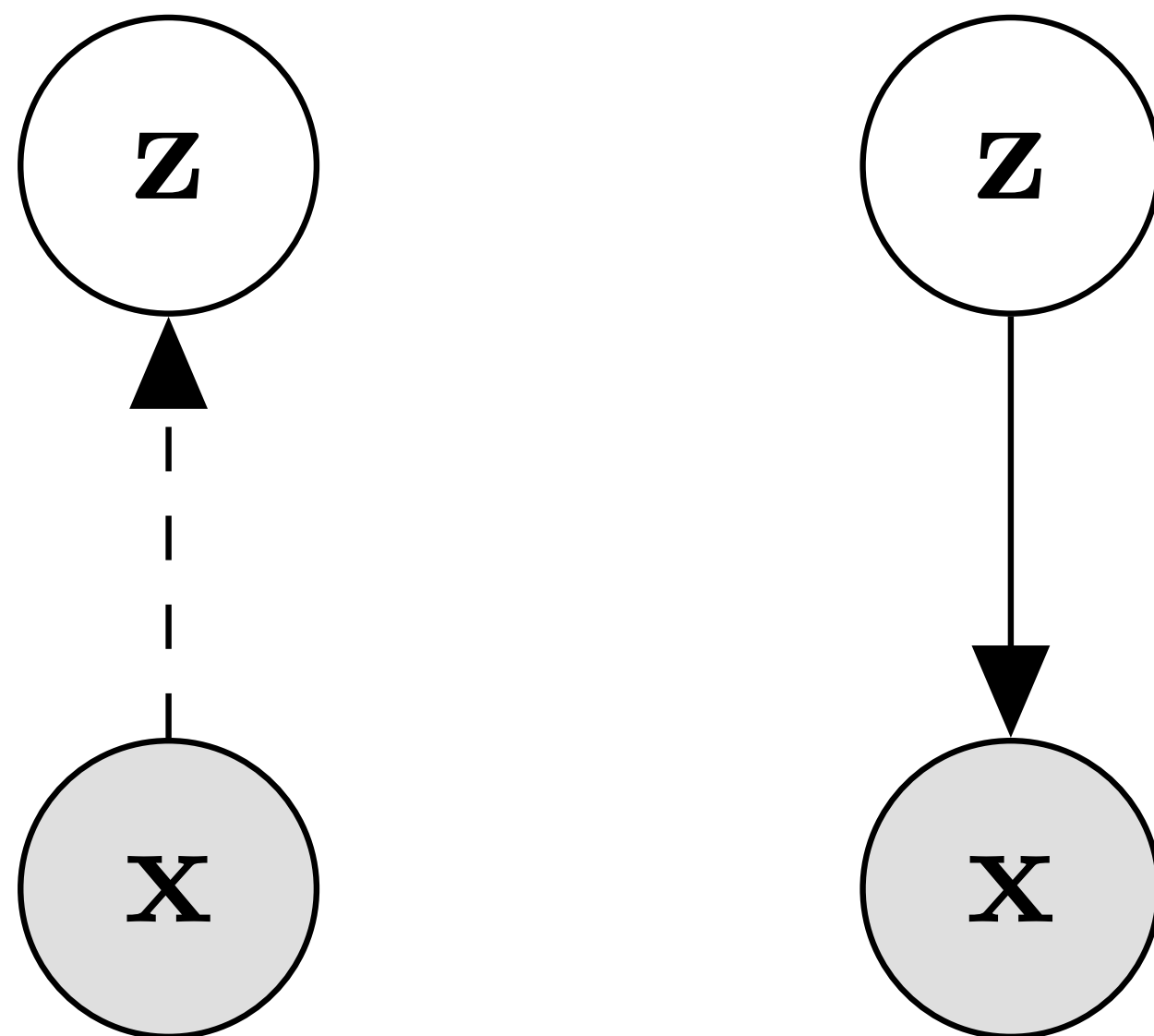
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# DGMs

**VAE [Kingma et al. 2014]**



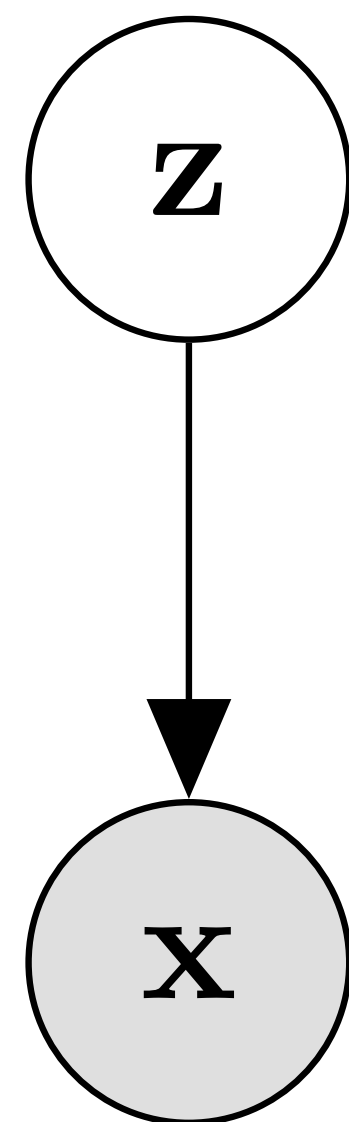
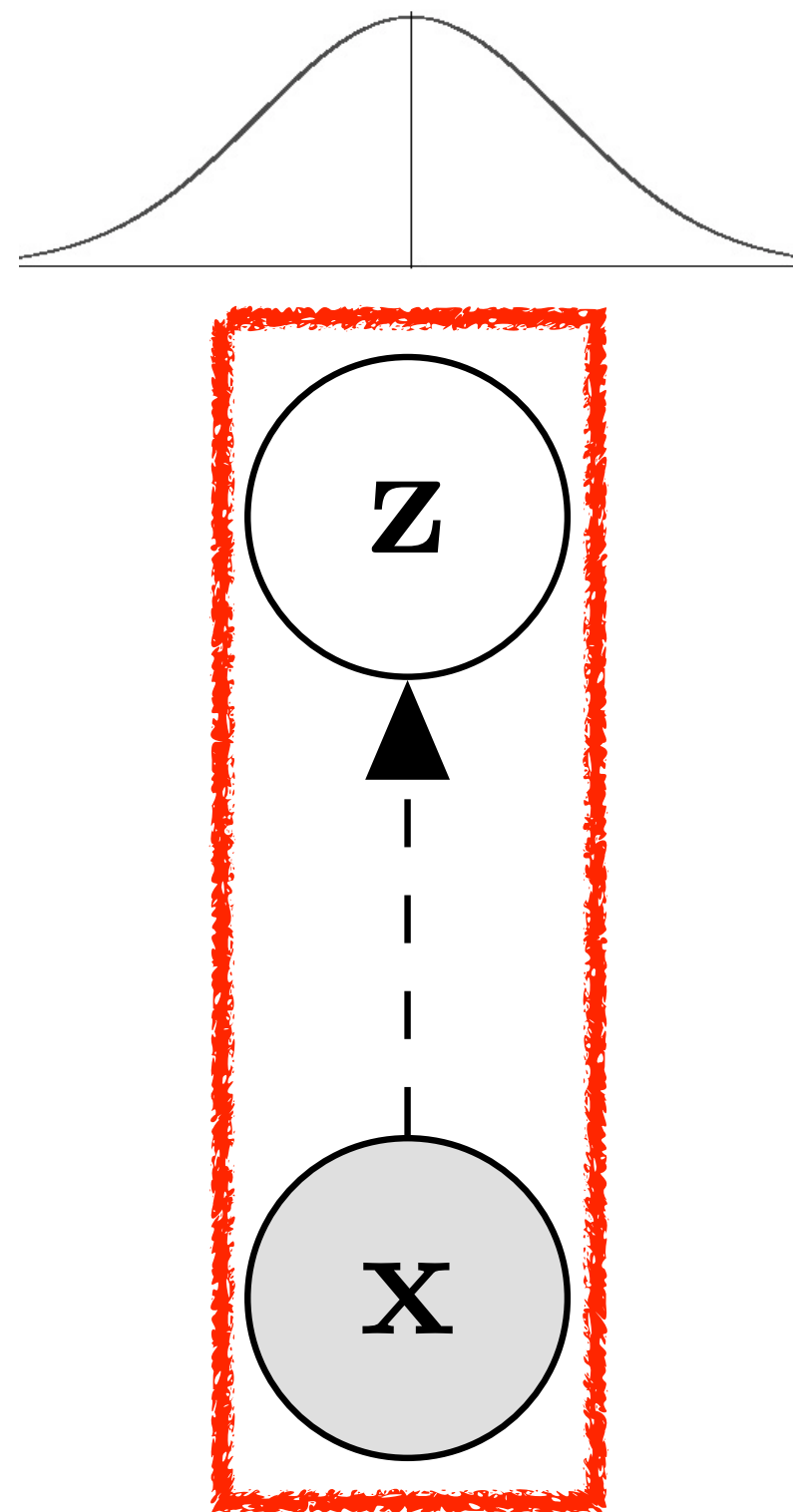
$$\mathbb{E}_{q_\phi(\mathbf{z}|\mathbf{x})} \left[ \log \frac{p_\theta(\mathbf{x}, \mathbf{z})}{q_\phi(\mathbf{z}|\mathbf{x})} \right] \leq \log p(\mathbf{x})$$

$$\underbrace{\mathbb{E}_{q_\phi(\mathbf{z}|\mathbf{x})} [\log p_\theta(\mathbf{x}|\mathbf{z})]}_{\text{Reconstruction}} - \underbrace{\text{KL}(q_\phi(\mathbf{z}|\mathbf{x}) \| p(\mathbf{z}))}_{\text{KL}}$$



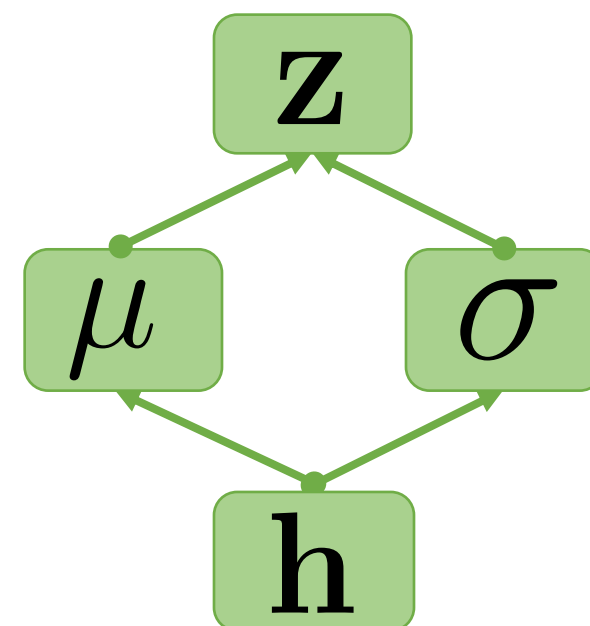
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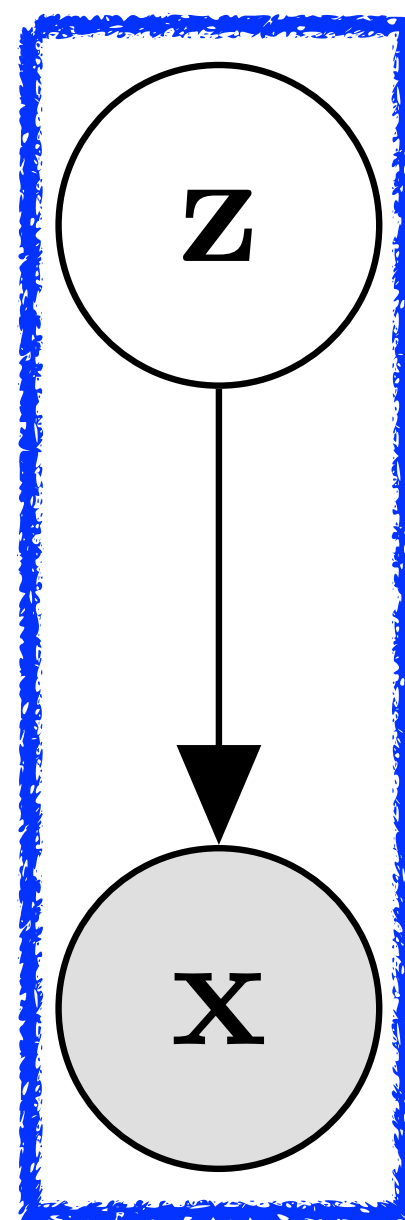
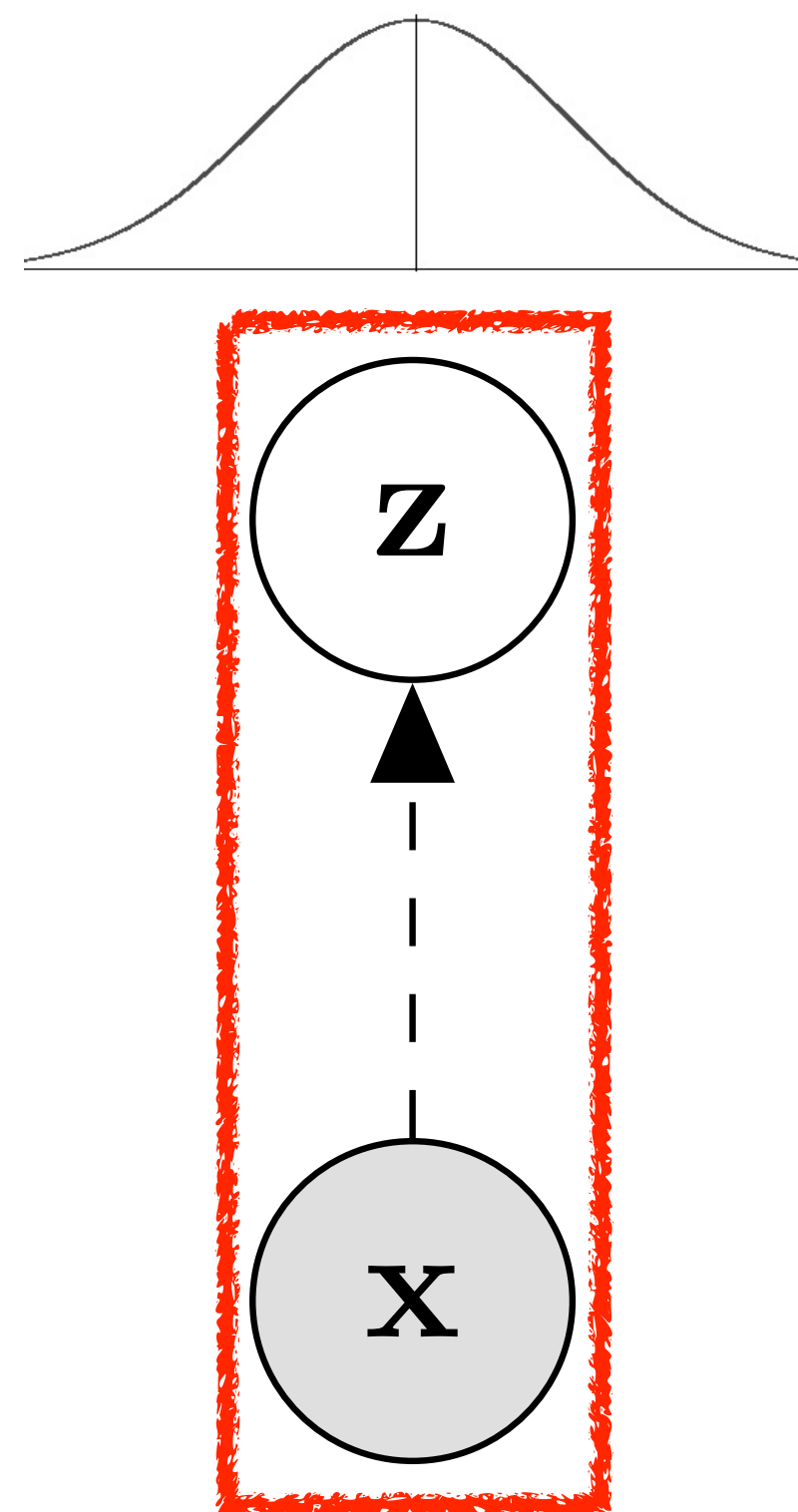
$$\underbrace{\mathbb{E}_{q_{\phi}(\mathbf{z}|\mathbf{x})} [\log p_{\theta}(\mathbf{x}|\mathbf{z})]}_{\text{Reconstruction}} - \underbrace{\text{KL}(q_{\phi}(\mathbf{z}|\mathbf{x}) \| p(\mathbf{z}))}_{\text{KL}}$$



$$q_{\phi}(\mathbf{z}|\mathbf{x}) = \mathcal{N}(\boldsymbol{\mu}_{\phi}(\mathbf{h}), \text{diag}(\boldsymbol{\sigma}_{\phi}^2(\mathbf{h})))$$

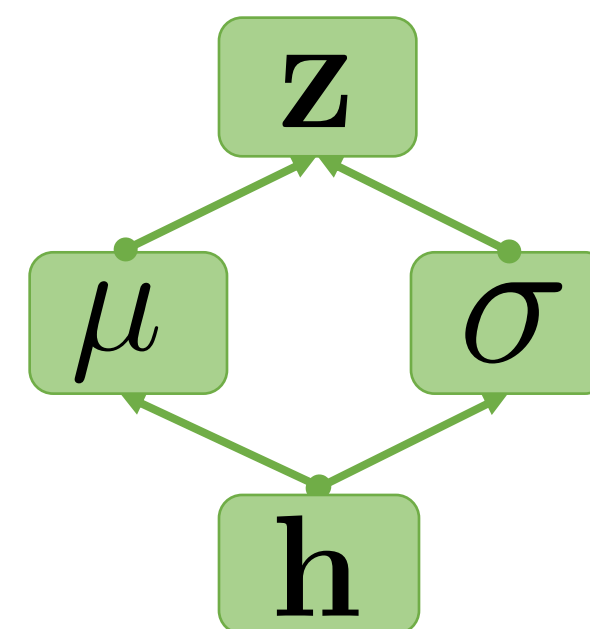
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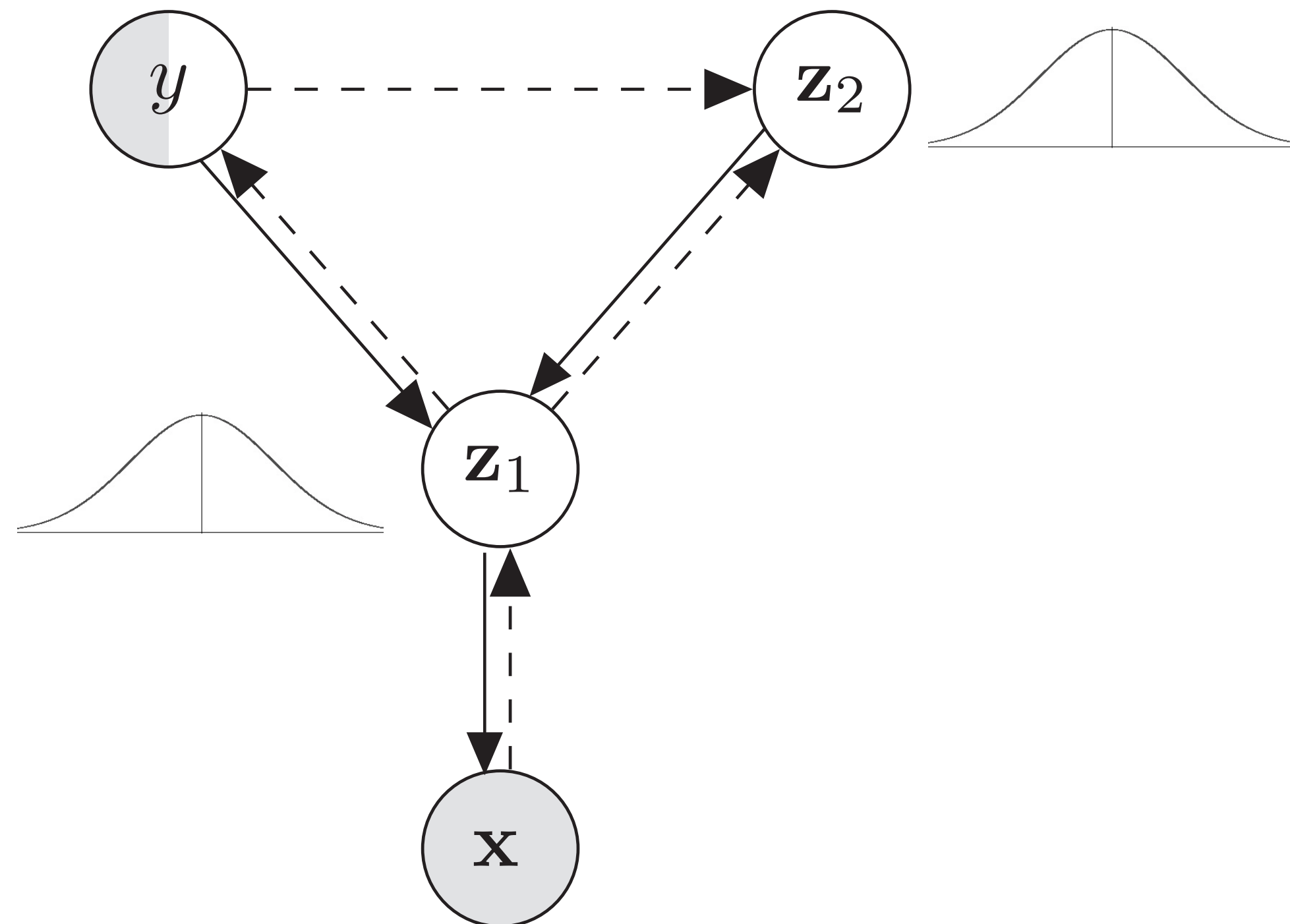
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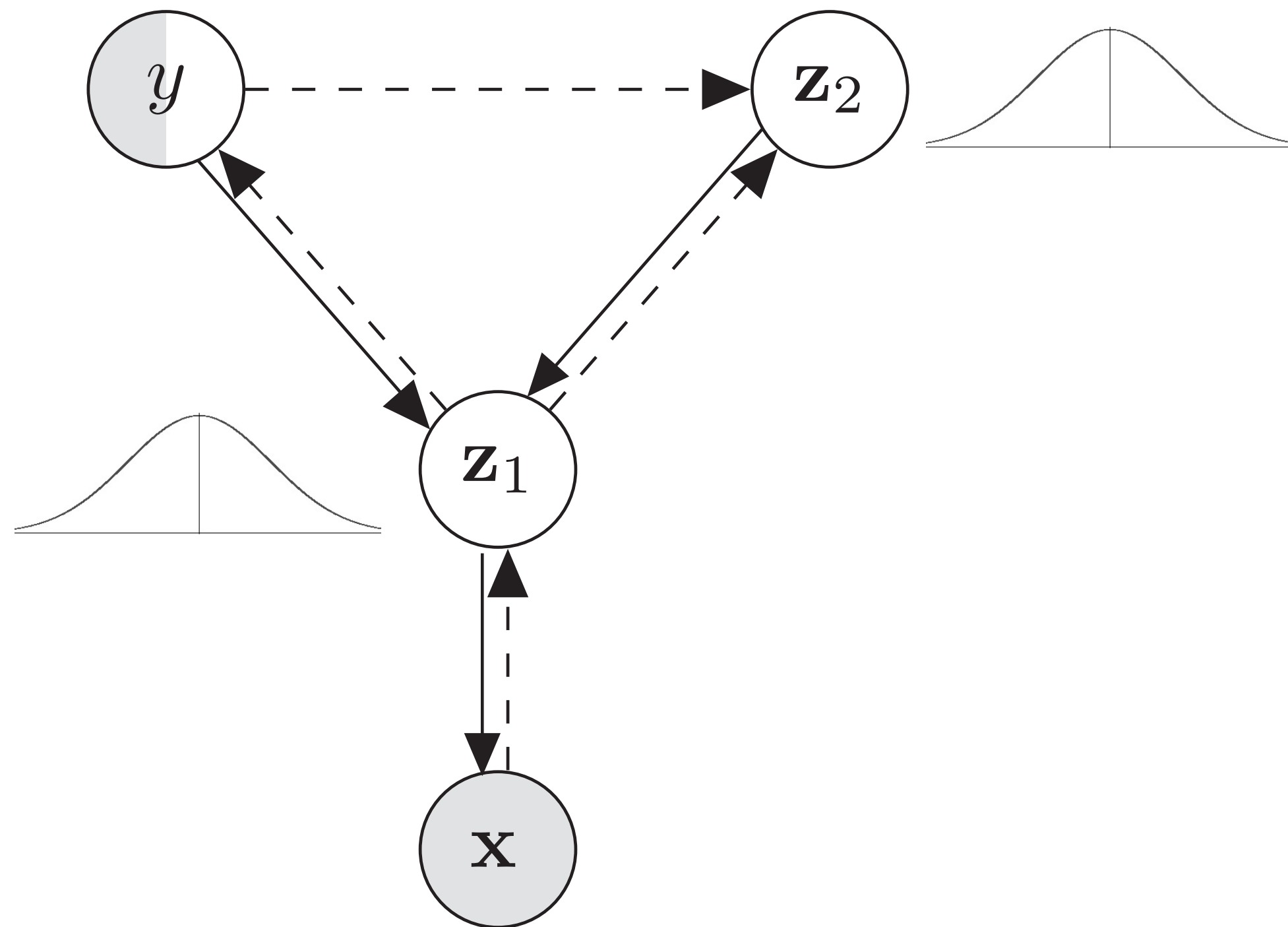


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# Our SDGM



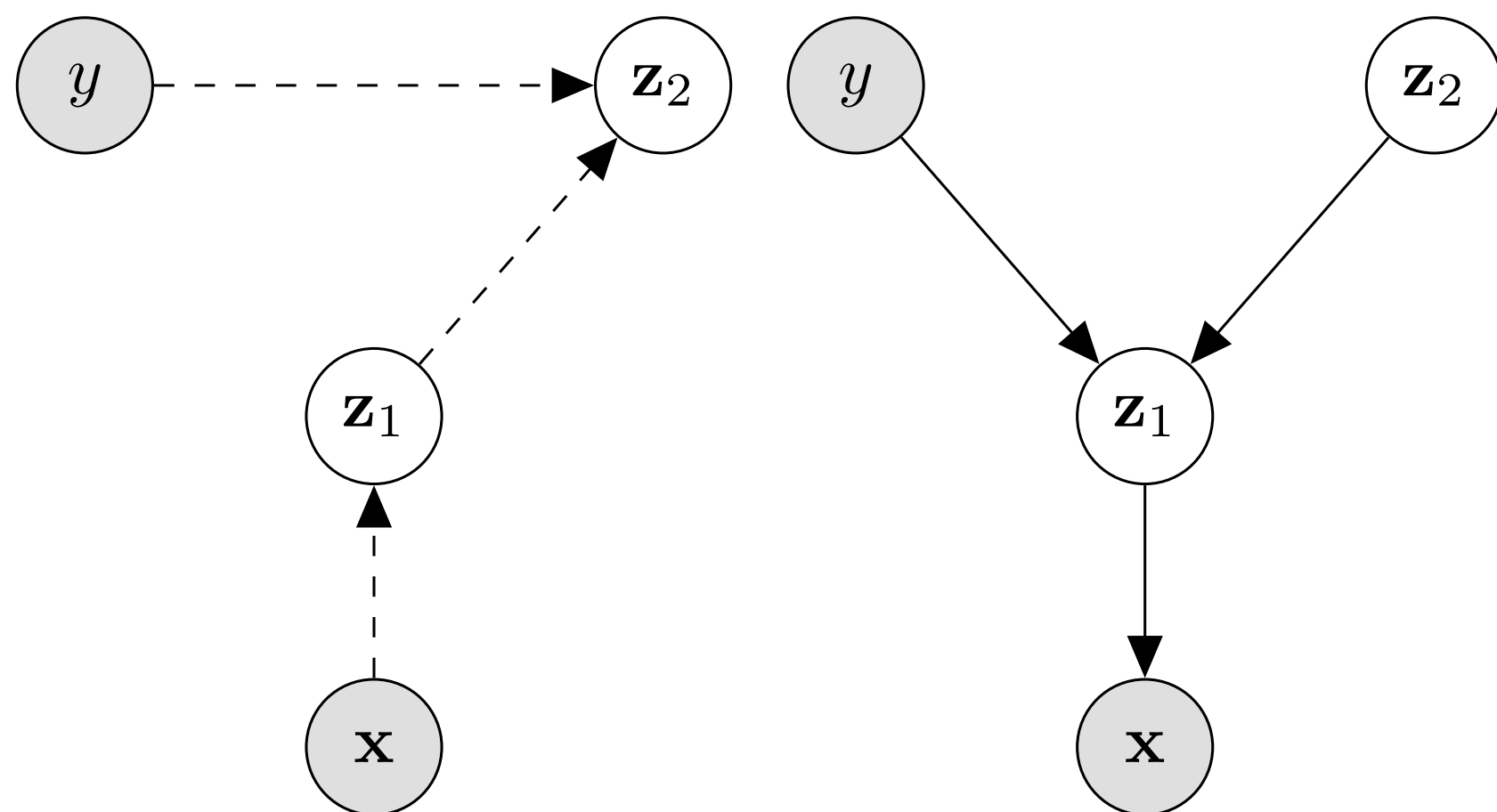
# Our SDGM



$$\mathbb{E}_{q_{\phi}(\mathbf{z}_1, \mathbf{z}_2 | \mathbf{x}, y)} \left[ \log \frac{p_{\theta}(\mathbf{x}, y, \mathbf{z}_1, \mathbf{z}_2)}{q_{\phi}(\mathbf{z}_1, \mathbf{z}_2 | \mathbf{x}, y)} \right] \leq \log p(\mathbf{x}, y)$$

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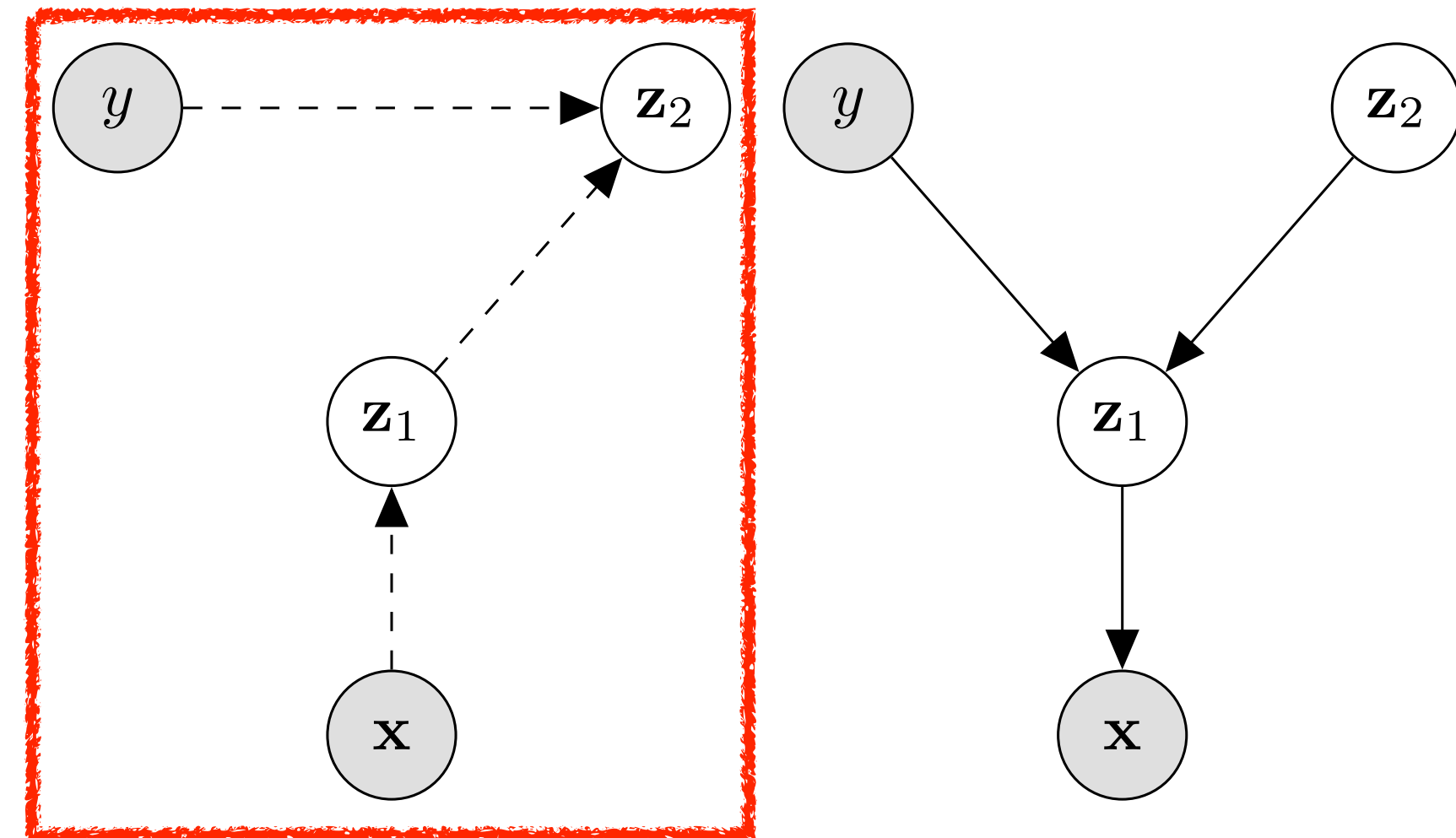
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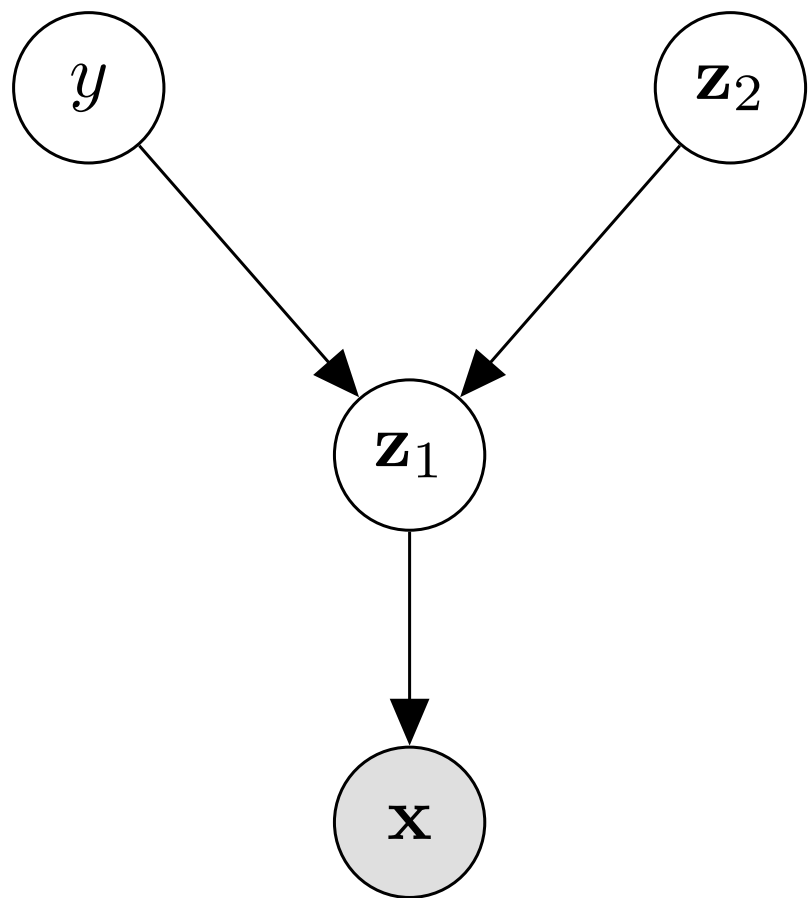
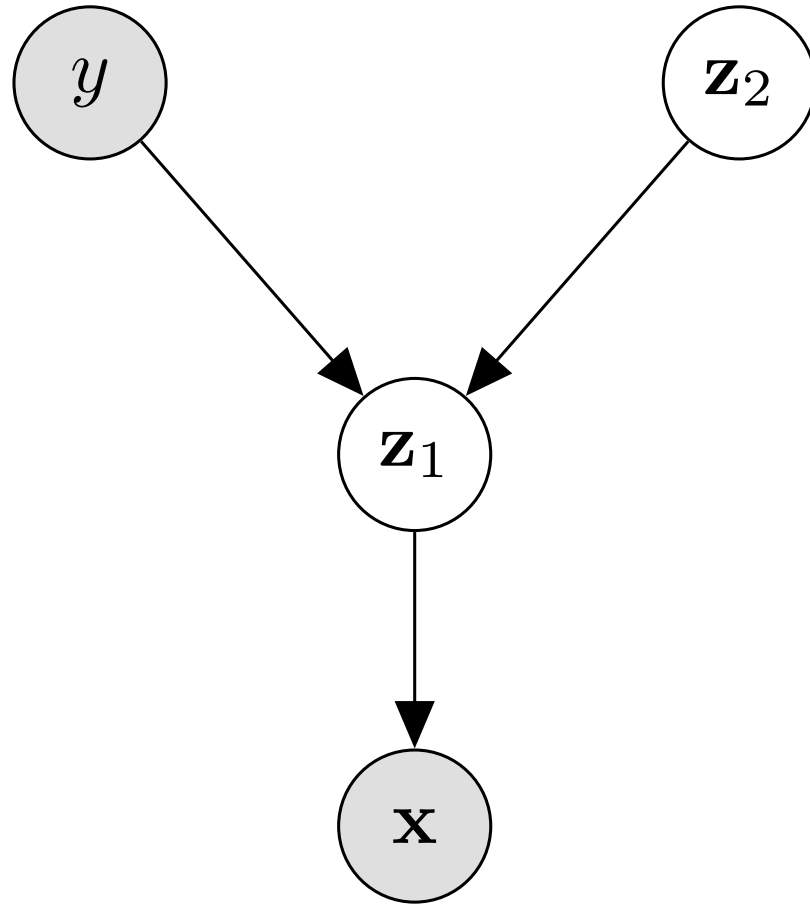
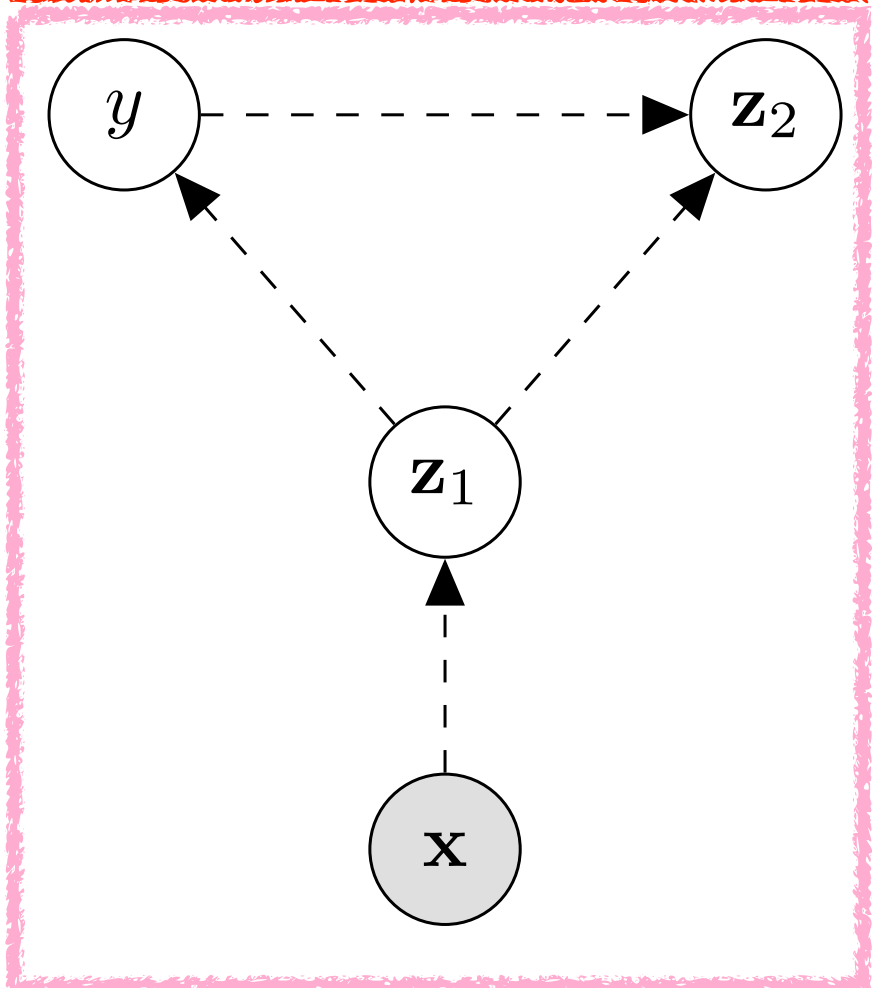
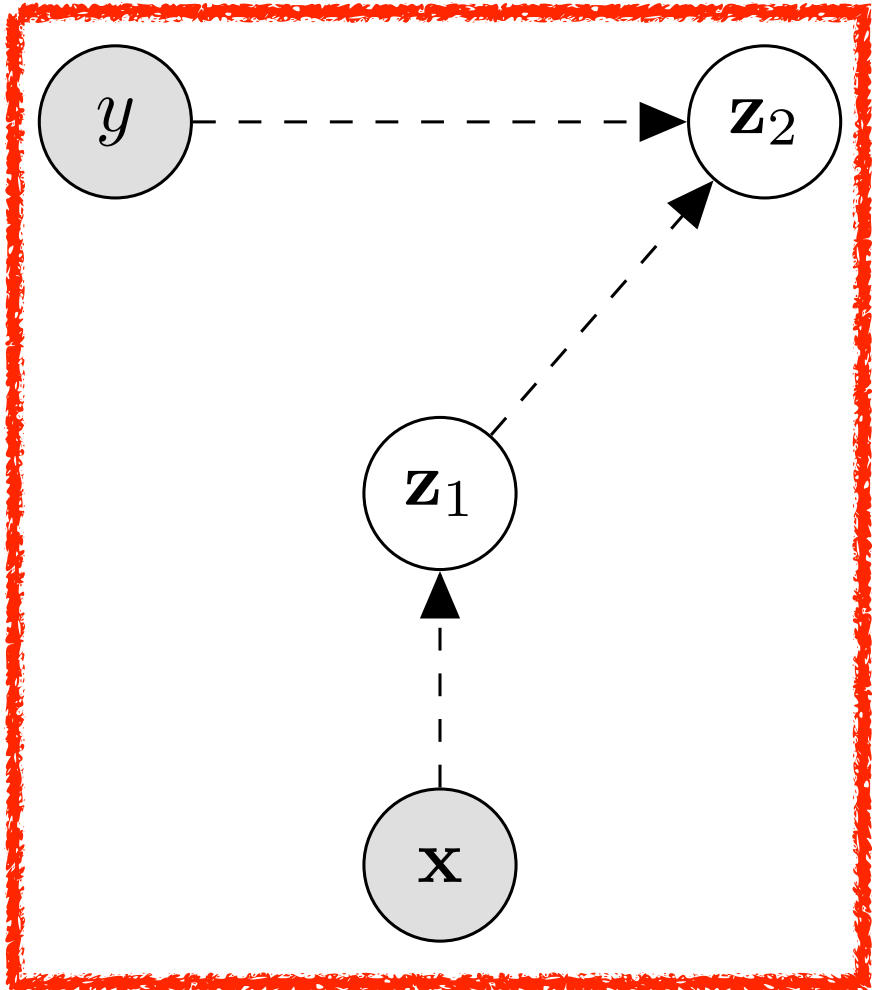


$$\mathbb{E}_{q_\phi(\mathbf{z}_1, \mathbf{z}_2 | \mathbf{x}, y)} \left[ \log \frac{p_\theta(\mathbf{x}, y, \mathbf{z}_1, \mathbf{z}_2)}{q_\phi(\mathbf{z}_1, \mathbf{z}_2 | \mathbf{x}, y)} \right] \leq \log p(\mathbf{x}, y)$$

$$\mathcal{L}(\mathbf{x}, y) = \underbrace{\mathbb{E}_{q_\phi(\mathbf{z}_1 | \mathbf{x})} [\log p_\theta(\mathbf{x} | \mathbf{z}_1)]}_{\text{Reconstruction}} - \underbrace{\mathbb{E}_{q_\phi(\mathbf{z}_1 | \mathbf{x}) q_\phi(\mathbf{z}_2 | \mathbf{z}_1, y)} \left[ \log \frac{q_\phi(\mathbf{z}_2 | \mathbf{z}_1, y)}{p(\mathbf{z}_2)} + \log \frac{q_\phi(\mathbf{z}_1 | \mathbf{x})}{p_\theta(\mathbf{z}_1 | \mathbf{z}_2, y)} \right]}_{\text{KL}} + \underbrace{\log p(y)}_{\text{Constant}}$$

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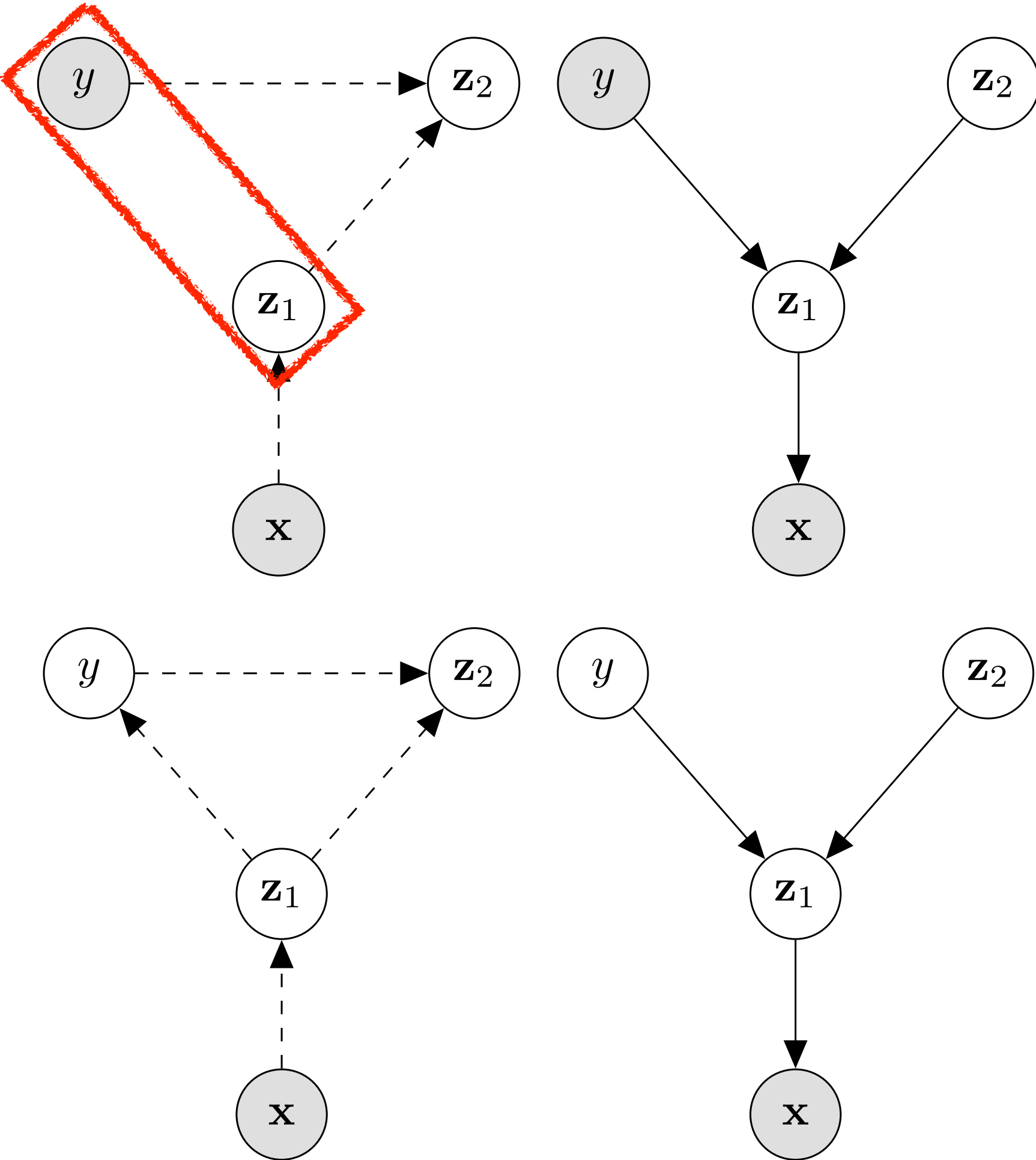
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$$\mathcal{U}(\mathbf{x}) = \underbrace{\mathbb{E}_{q_{\phi}(\mathbf{z}_1 | \mathbf{x})} [\log p_{\theta}(\mathbf{x} | \mathbf{z}_1)]}_{\text{Reconstruction}} - \underbrace{\mathbb{E}_{q_{\phi}(\mathbf{z}_1 | \mathbf{x}) q_{\phi}(y | \mathbf{z}_1) q_{\phi}(\mathbf{z}_2 | \mathbf{z}_1, y)} \left[ \log \frac{q_{\phi}(\mathbf{z}_2 | \mathbf{z}_1, y)}{p(\mathbf{z}_2)} + \log \frac{q_{\phi}(\mathbf{z}_1 | \mathbf{x})}{p_{\theta}(\mathbf{z}_1 | \mathbf{z}_2, y)} + \log \frac{q_{\phi}(y | \mathbf{z}_1)}{p(y)} \right]}_{\text{KL}}$$

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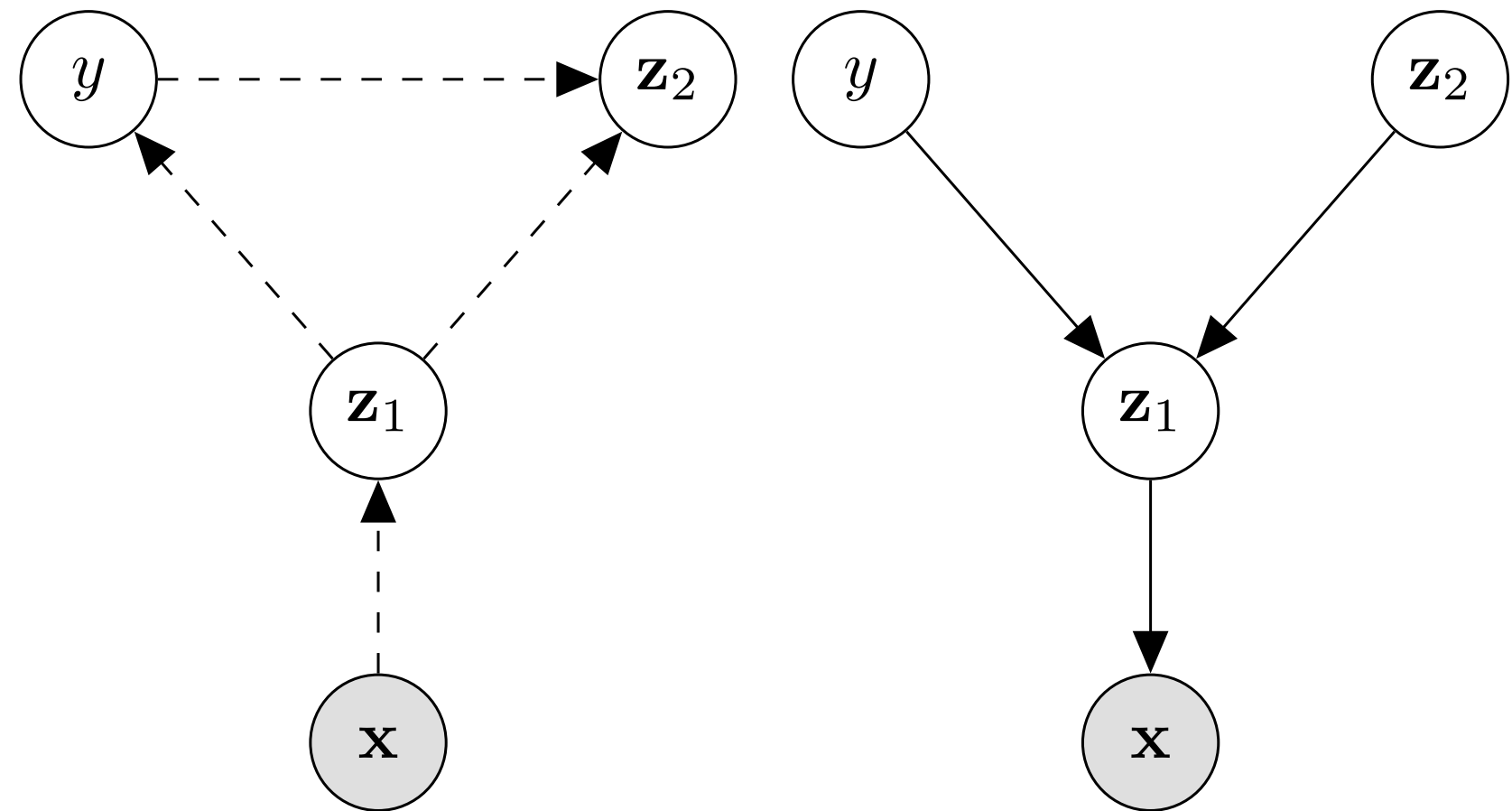
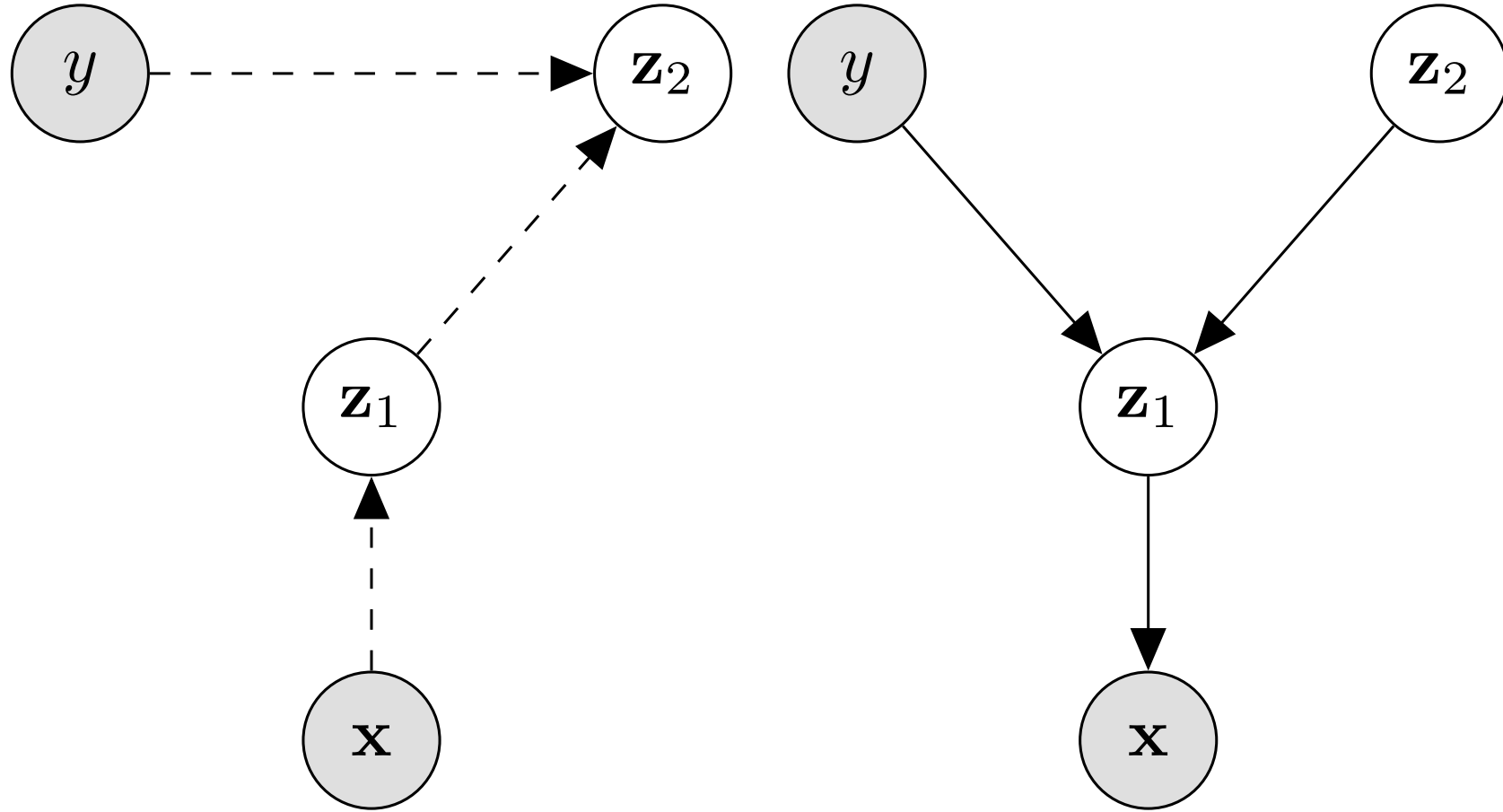
$$\mathbb{E}_{q_{\phi}(\mathbf{z}_1, \mathbf{z}_2, y | \mathbf{x})} \left[ \log \frac{p_{\theta}(\mathbf{x}, y, \mathbf{z}_1, \mathbf{z}_2)}{q_{\phi}(\mathbf{z}_1, \mathbf{z}_2, y | \mathbf{x})} \right] \leq \log p(\mathbf{x})$$

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$$\mathcal{J}_{cls}(\mathbf{x}, y) = \mathbb{E}_{q_{\phi}(\mathbf{z}_1 | \mathbf{x})} [q_{\phi}(y | \mathbf{z}_1)]$$



# Our SDGM



$$\mathbb{E}_{q_{\phi}(\mathbf{z}_1, \mathbf{z}_2 | \mathbf{x}, y)} \left[ \log \frac{p_{\theta}(\mathbf{x}, y, \mathbf{z}_1, \mathbf{z}_2)}{q_{\phi}(\mathbf{z}_1, \mathbf{z}_2 | \mathbf{x}, y)} \right] \leq \log p(\mathbf{x}, y)$$

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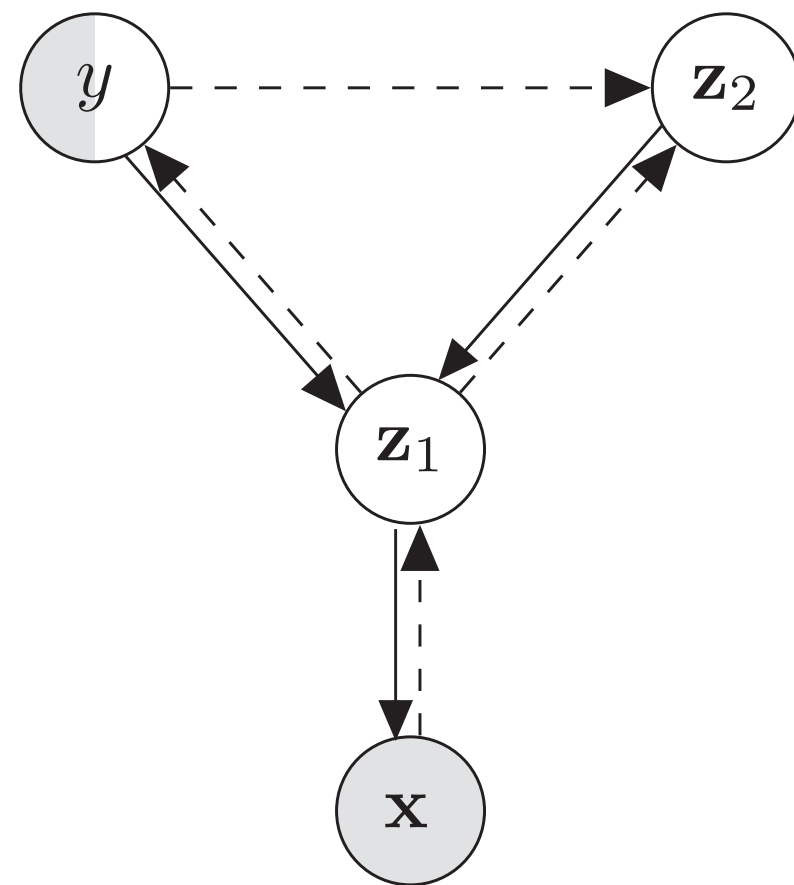
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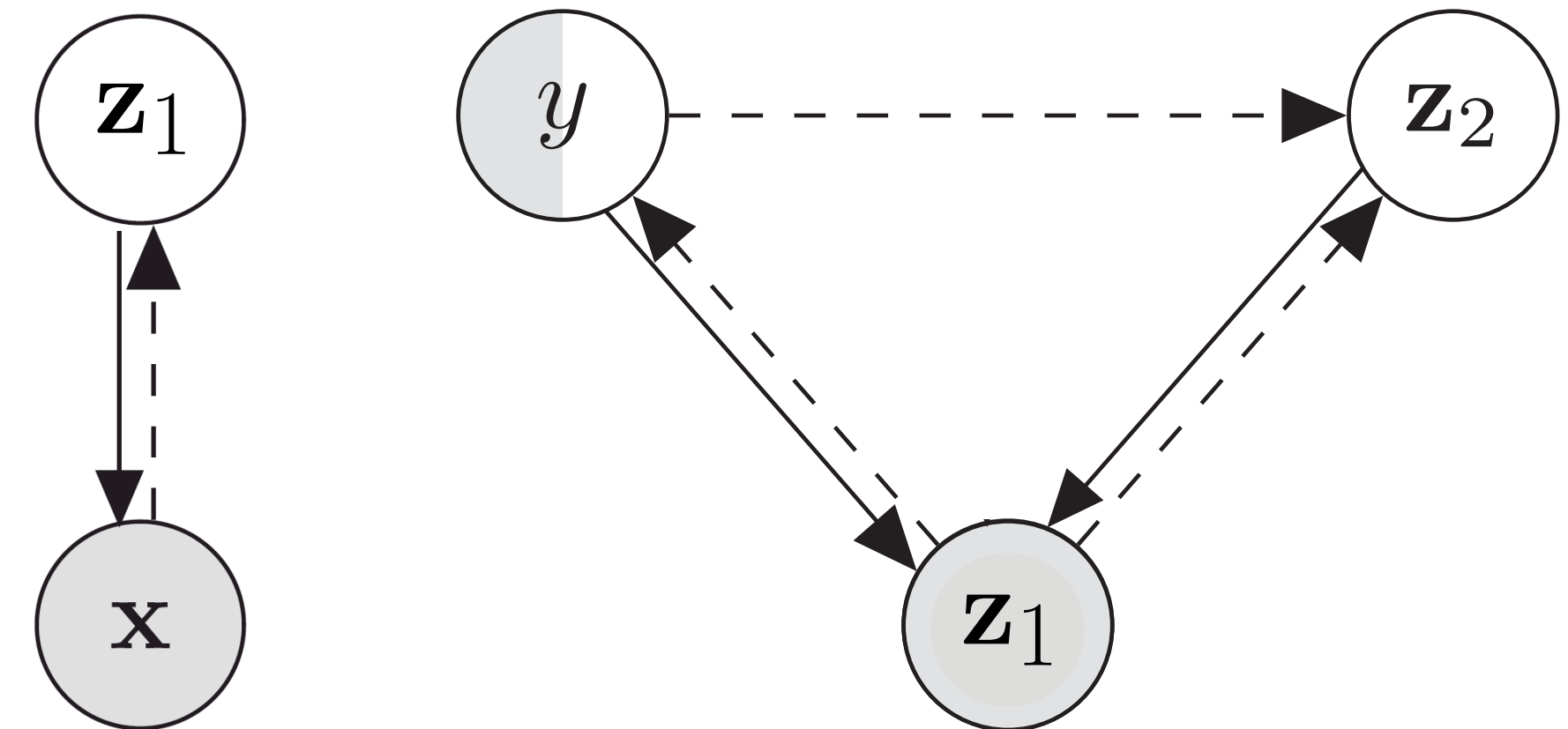
$$\mathcal{J} = \sum_{(\mathbf{x}, y) \in \mathcal{S}_l} (\mathcal{L}(\mathbf{x}, y) + \alpha \mathcal{J}_{cls}(\mathbf{x}, y)) + \sum_{\mathbf{x} \in \mathcal{S}_u} \mathcal{U}(\mathbf{x})$$

# Difference between our SDGM and M1 + M2 [Kingma et al. 2014]

**Our SDGM**

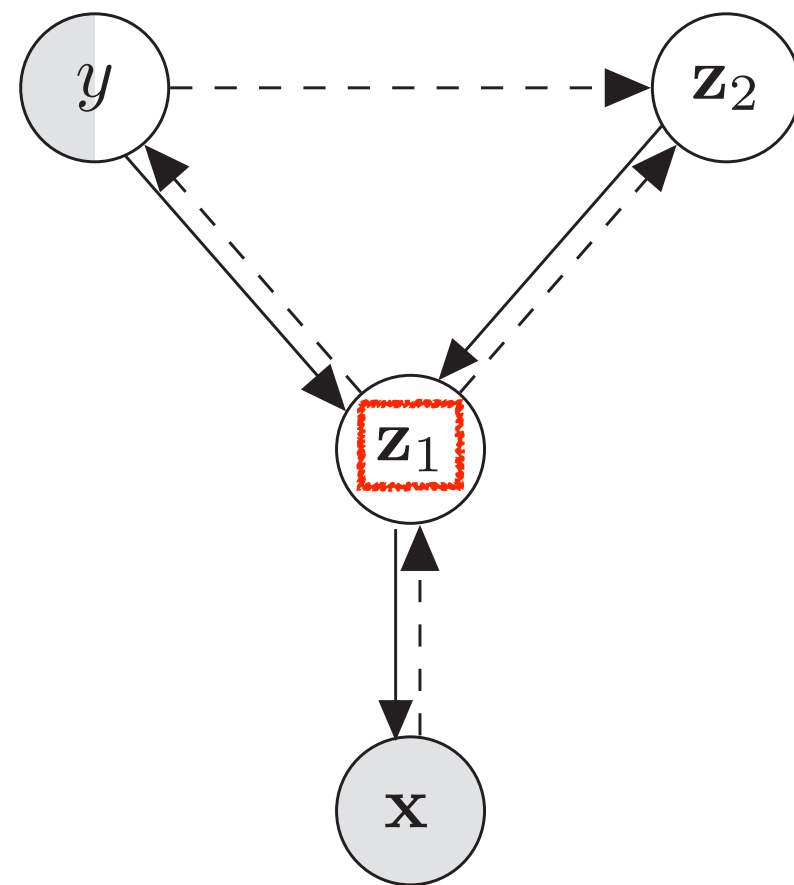


**M1+M2**

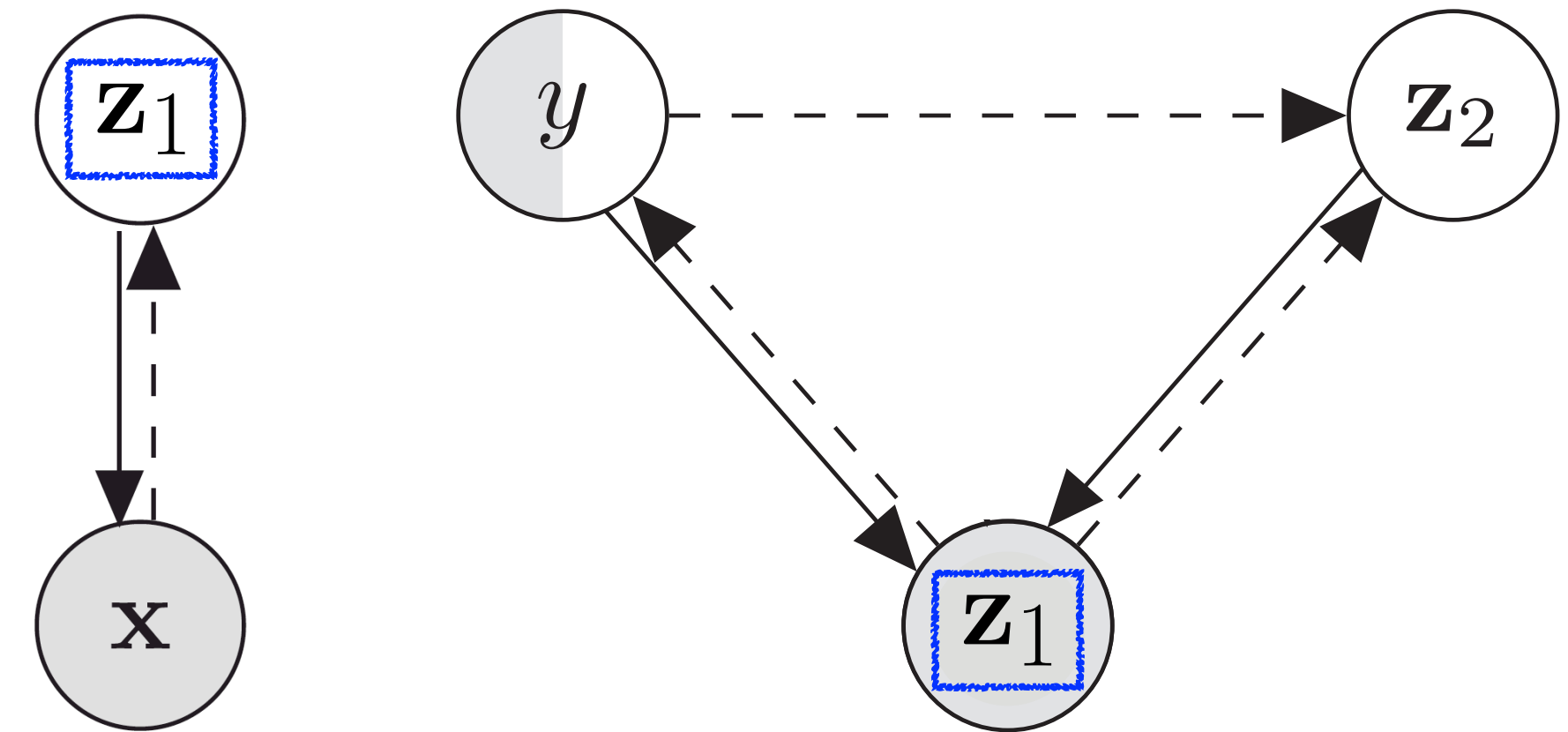


# Difference between our SDGM and M1 + M2 [Kingma et al. 2014]

**Our SDGM**



**M1+M2**



$$\mathbb{E}_{q_{\phi}(\mathbf{z}_1, \mathbf{z}_2 | \mathbf{x}, y)} \left[ \log \frac{p_{\theta}(\mathbf{x}, y, \mathbf{z}_1, \mathbf{z}_2)}{q_{\phi}(\mathbf{z}_1, \mathbf{z}_2 | \mathbf{x}, y)} \right] \leq \log p(\mathbf{x}, y)$$

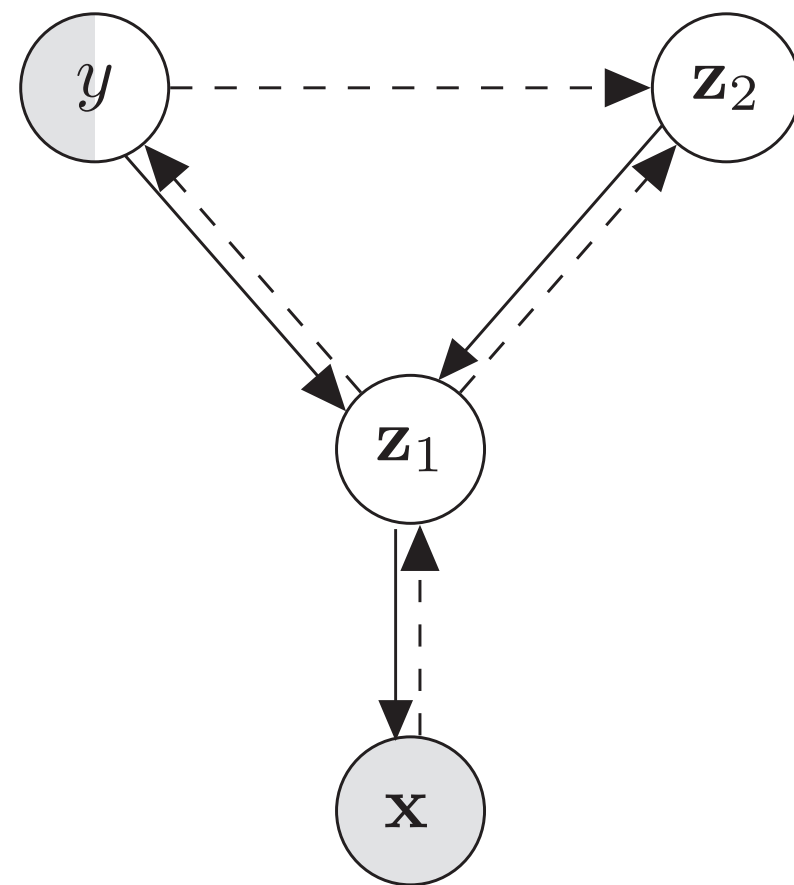
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$$\mathbb{E}_{q_{\phi}(\mathbf{z}_2 | \mathbf{z}_1, y)} \left[ \log \frac{p_{\theta}(\mathbf{z}_1, y, \mathbf{z}_2)}{q_{\phi}(\mathbf{z}_2 | \mathbf{z}_1, y)} \right] \leq \log p(\mathbf{z}_1, y)$$

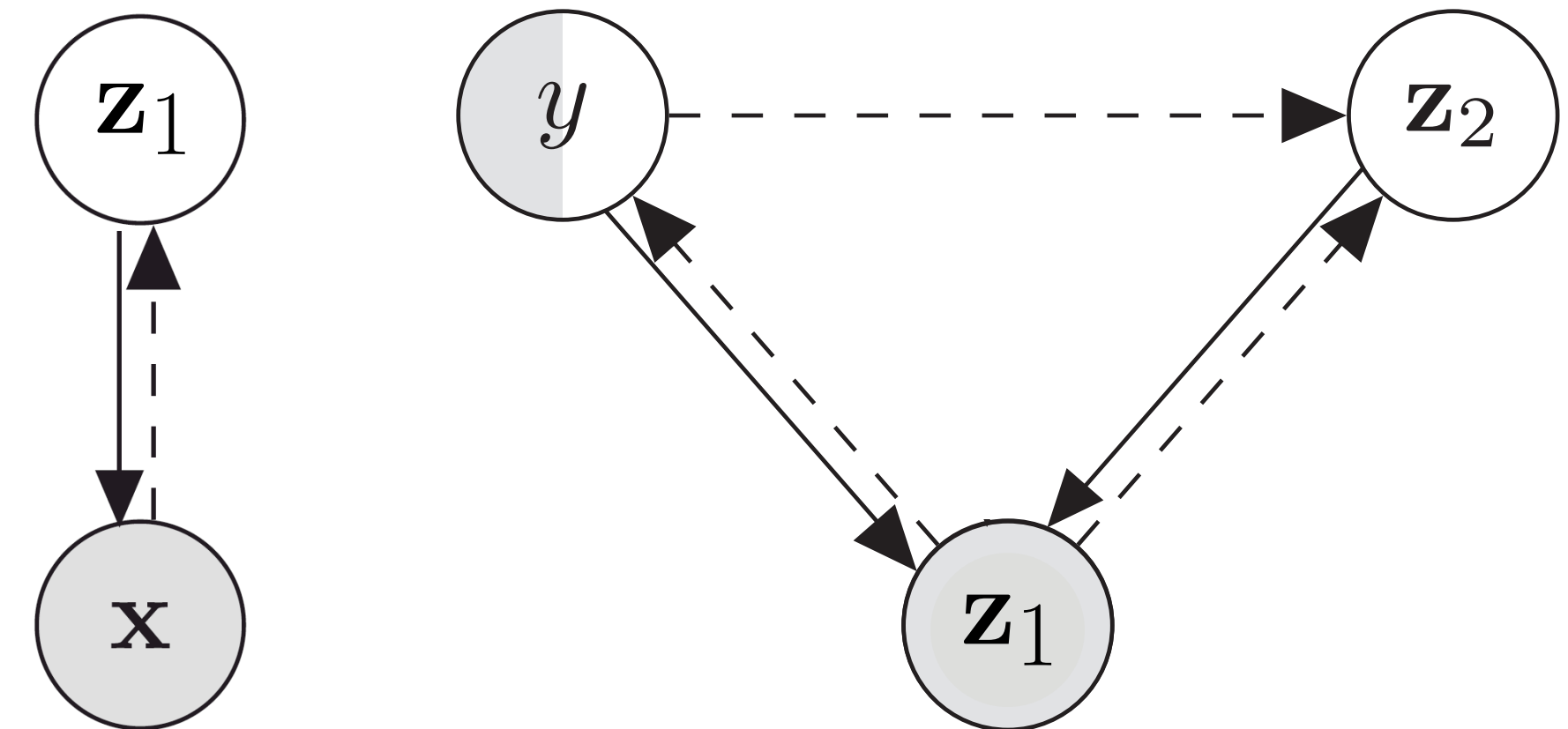
$$\mathbb{E}_{q_{\phi}(\mathbf{z}_2, y | \mathbf{z}_1)} \left[ \log \frac{p_{\theta}(\mathbf{z}_1, y, \mathbf{z}_2)}{q_{\phi}(\mathbf{z}_2, y | \mathbf{z}_1)} \right] \leq \log p(\mathbf{z}_1)$$

# Difference between our SDGM and M1 + M2 [Kingma et al. 2014]

**Our SDGM**

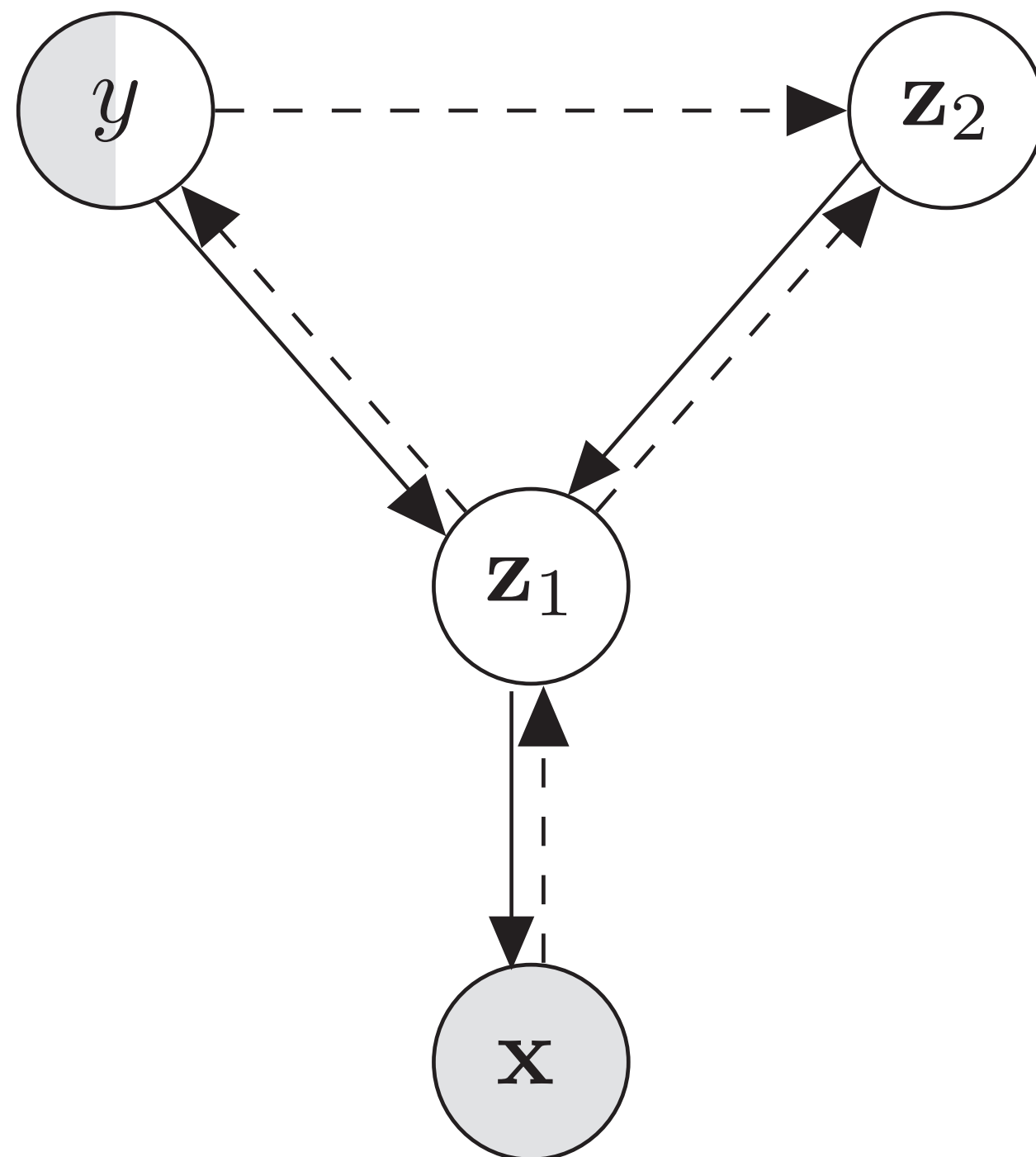


**M1+M2**

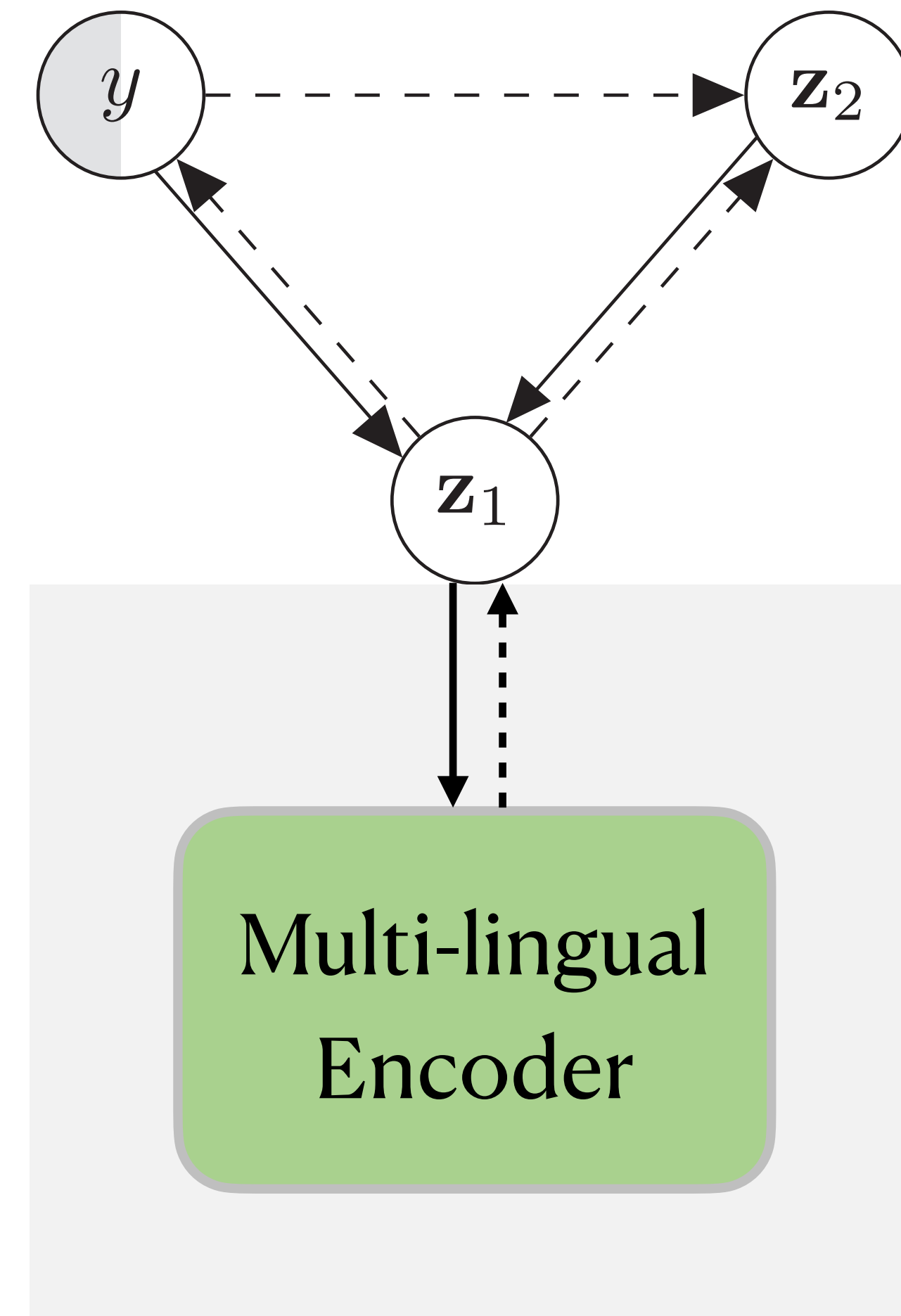
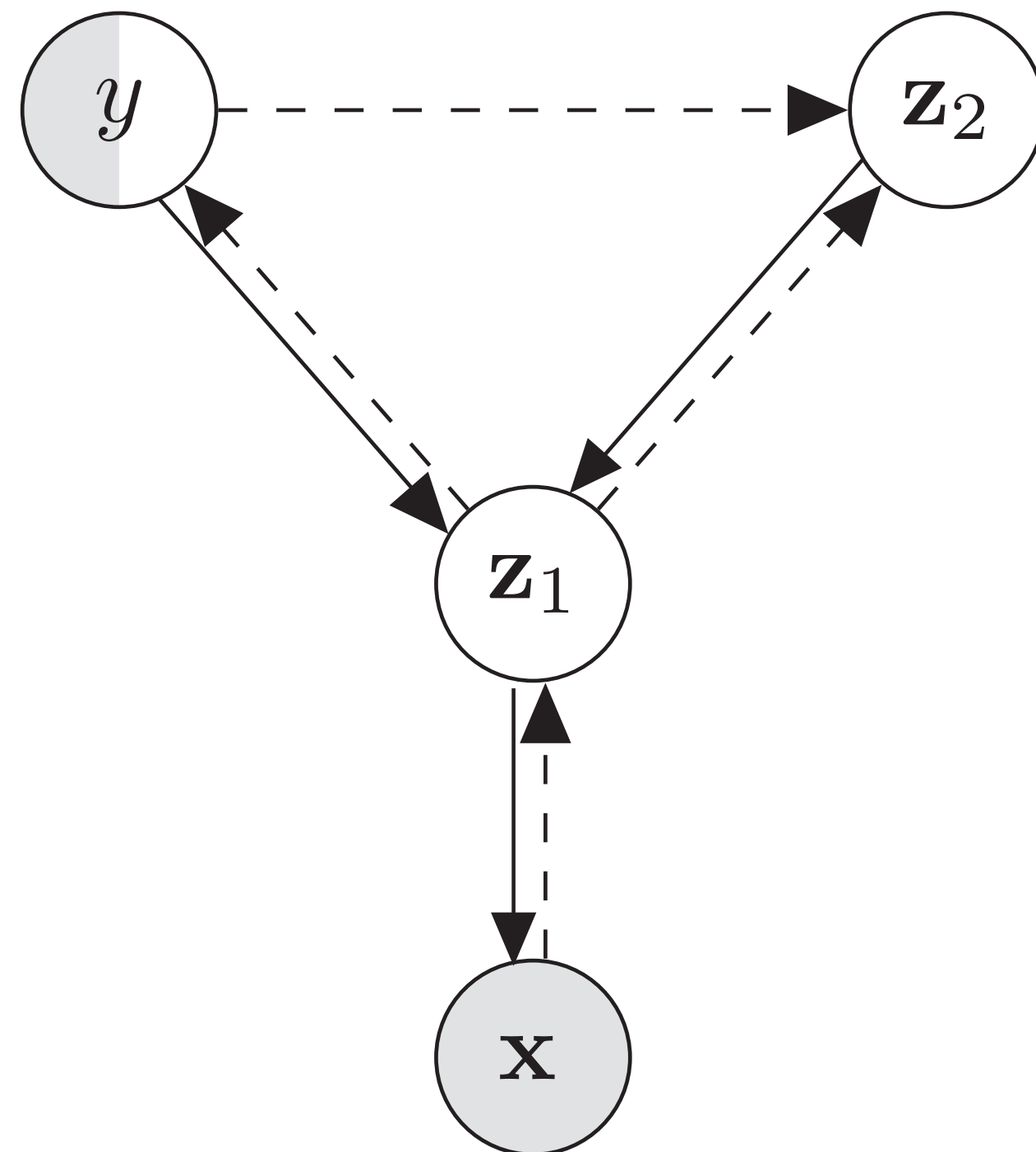


- M1 + M2
  - Layer-wise training
  - The parameters between  $x$  and  $z_1$  are fixed during semi-supervised learning
- Our SDGM
  - End-to-end training
  - Mathematical reformulation of ELBOs into reconstruction and KL terms, more stable optimisation schedule

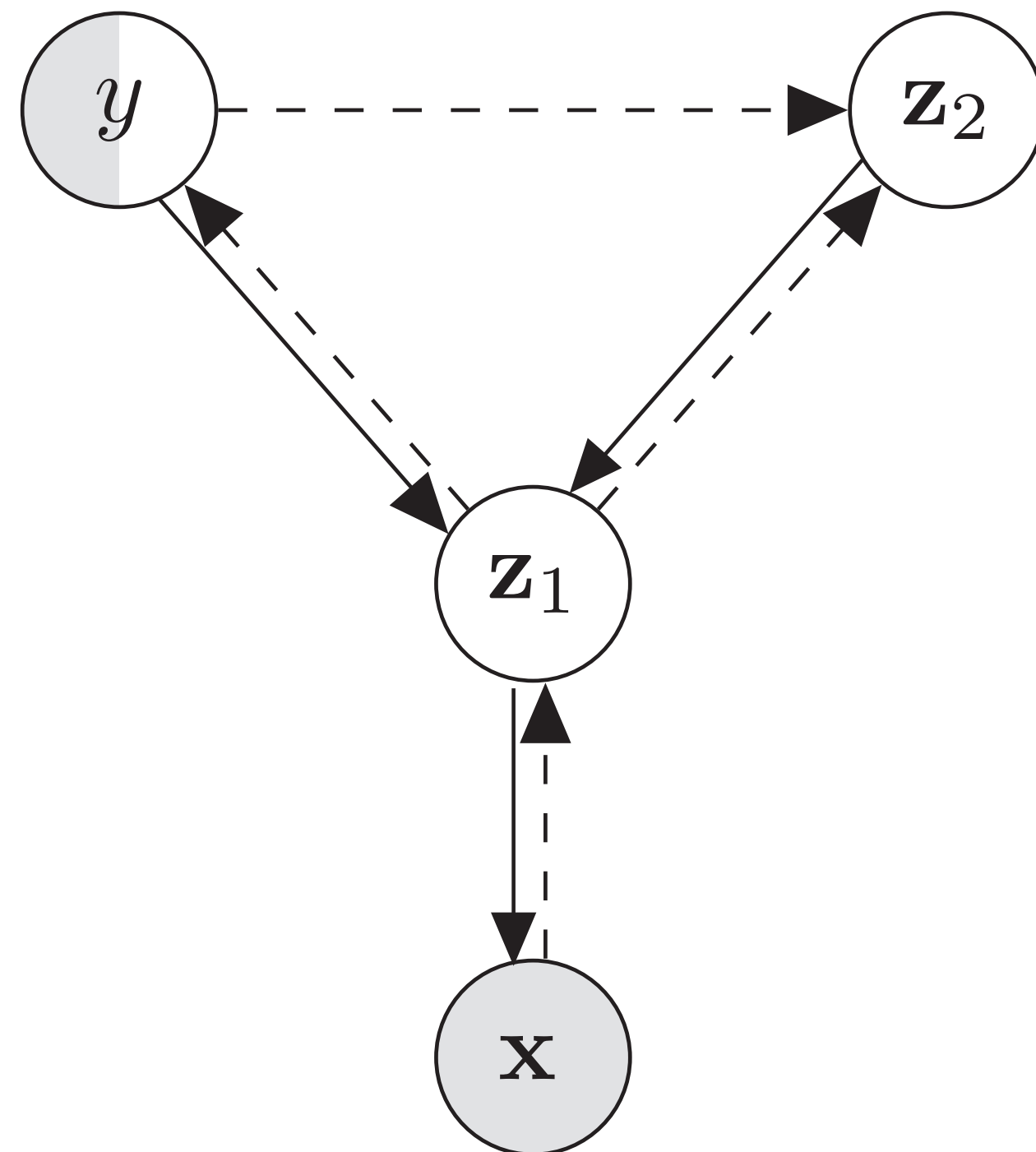
# SDGMs + Multi-lingual pretraining



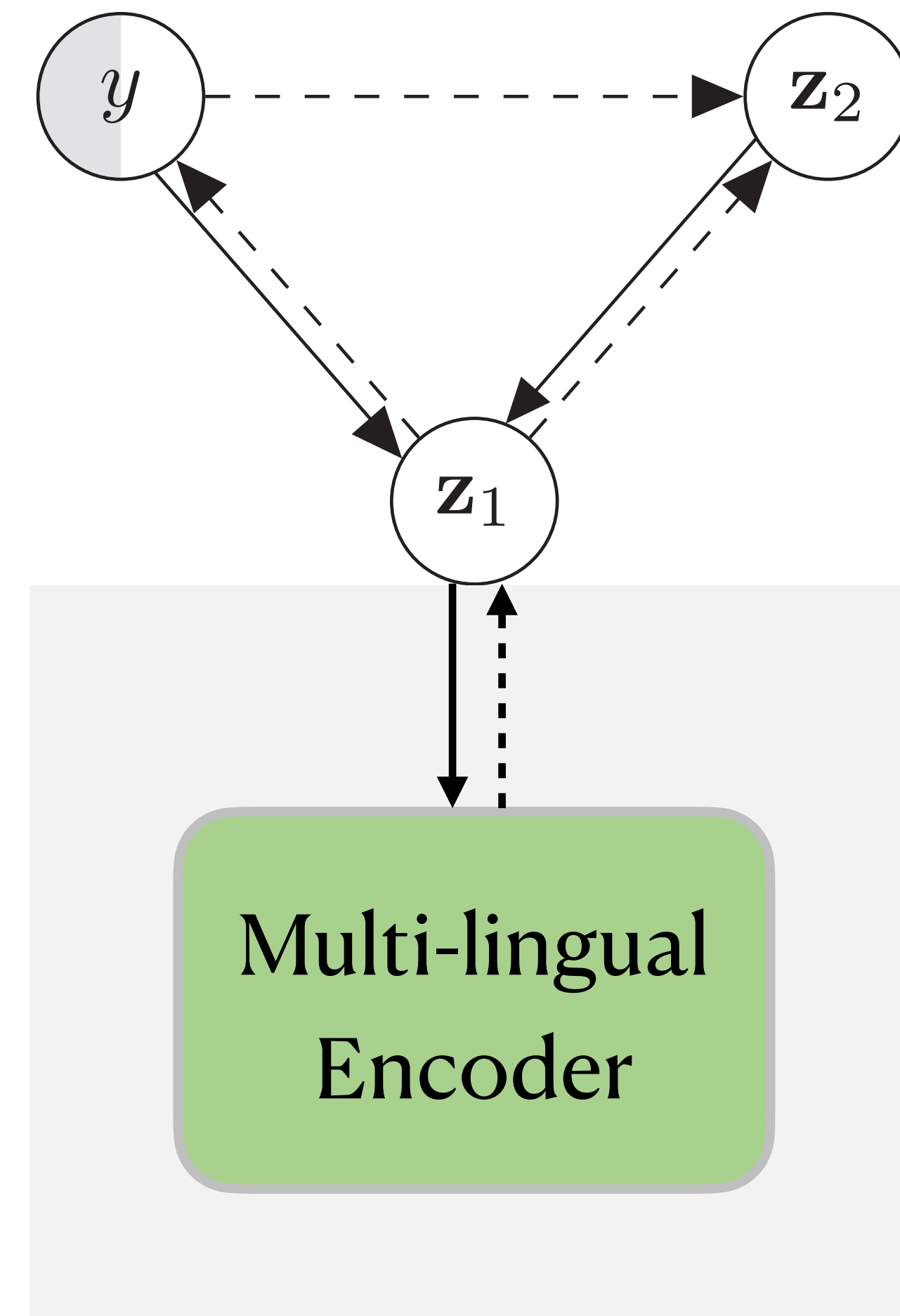
# SDGMs + Multi-lingual pretraining



# SDGMs + Multi-lingual pretraining



SDGMs can operate on top of the multi-lingual encoder *independently* of encoding architecture



# Experiments

## Document classification in multiple languages

- Multilingual document classification corpus (MLDoc; Schwenk and Li [2018])



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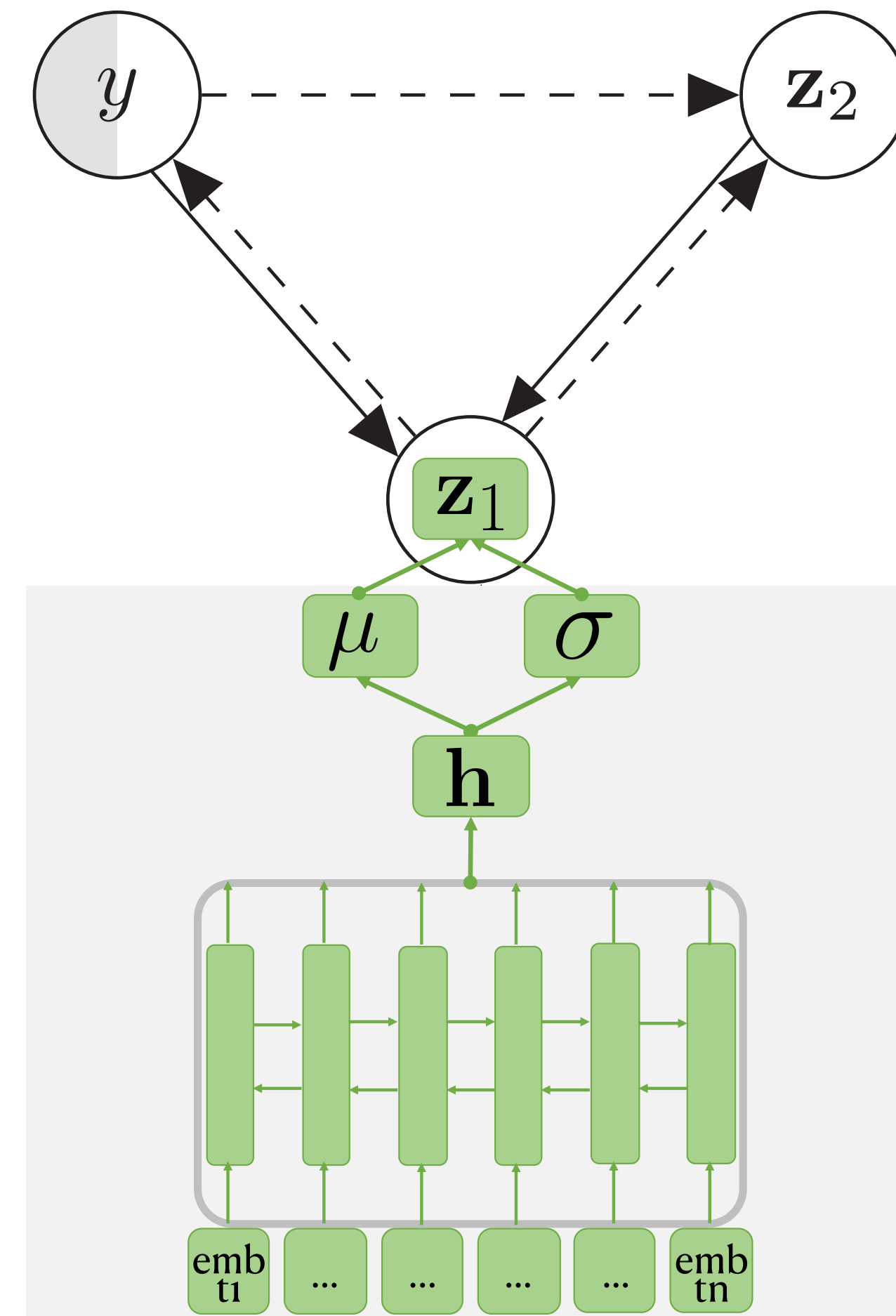
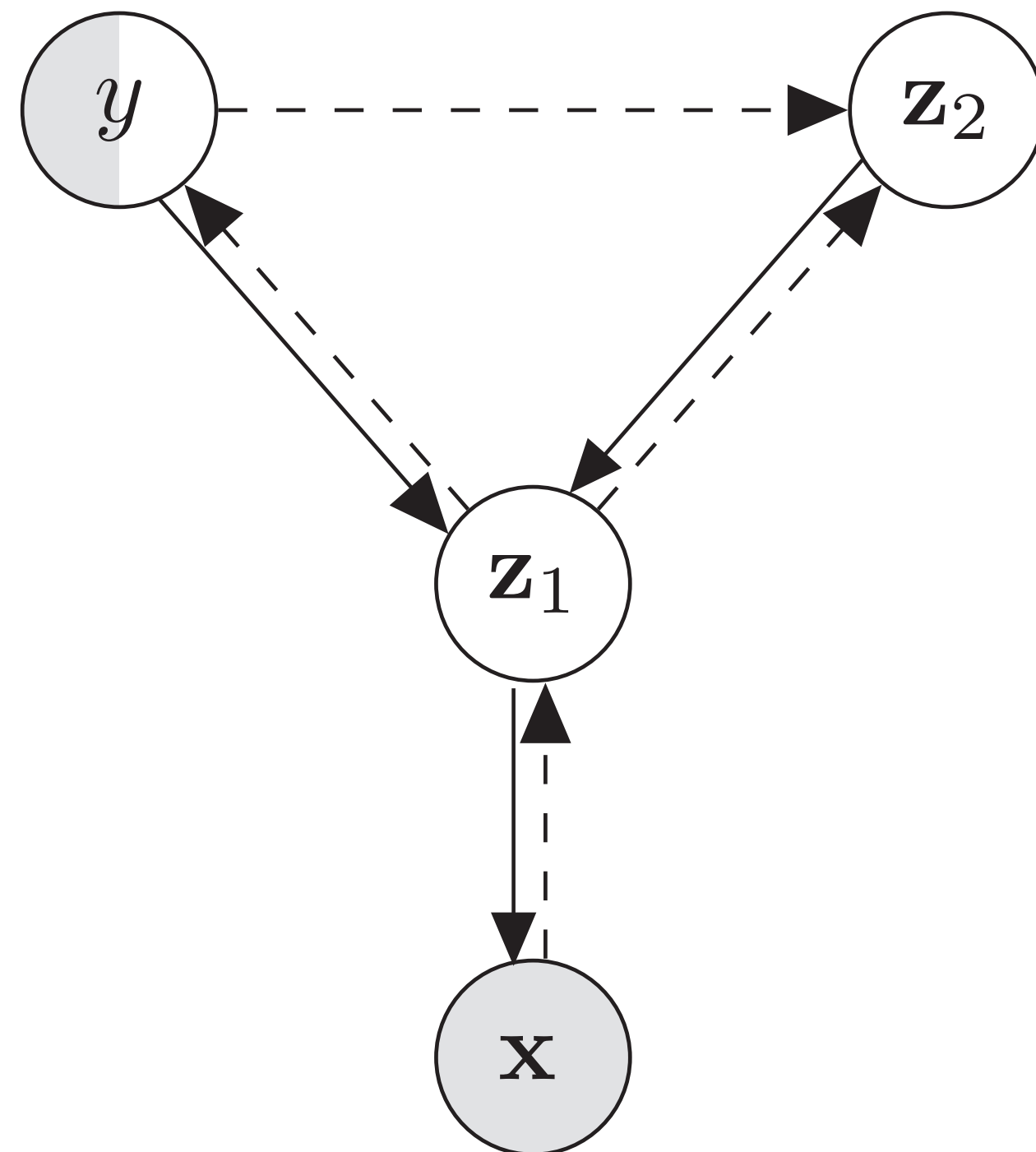
# Experiments

## Document classification in multiple languages

- Multilingual document classification corpus (MLDoc; Schwenk and Li [2018])
- Five languages in total: English (EN), German (DE), French (FR), Russian (RU), Chinese (ZH)
- For 1k training corpus, vary labelled data size, use the rest as unlabelled data

# SDGMs + Multi-lingual pretraining

Non-parallel cross-lingual VAE (NXVAE)



# Qualitative results

## EN-DE

Word pair	Lang	kNNs ( $k = 3$ )
president (EN)	EN	mr, madam, gentlemen
	DE	präsident, herr, kommissar
präsident (DE)	EN	president, mr, madam
	DE	herr, kommissar, herren
great (EN)	EN	deal, with, a
	DE	große, eine, gute
groß (DE)	EN	striking, gets, lucrative
	DE	gering, heikel, hoch
said (EN)	EN	already, as, been
	DE	gesagt, mit, dem
sagte (DE)	EN	he, rightly, said
	DE	vorhin, kollege, kommissar

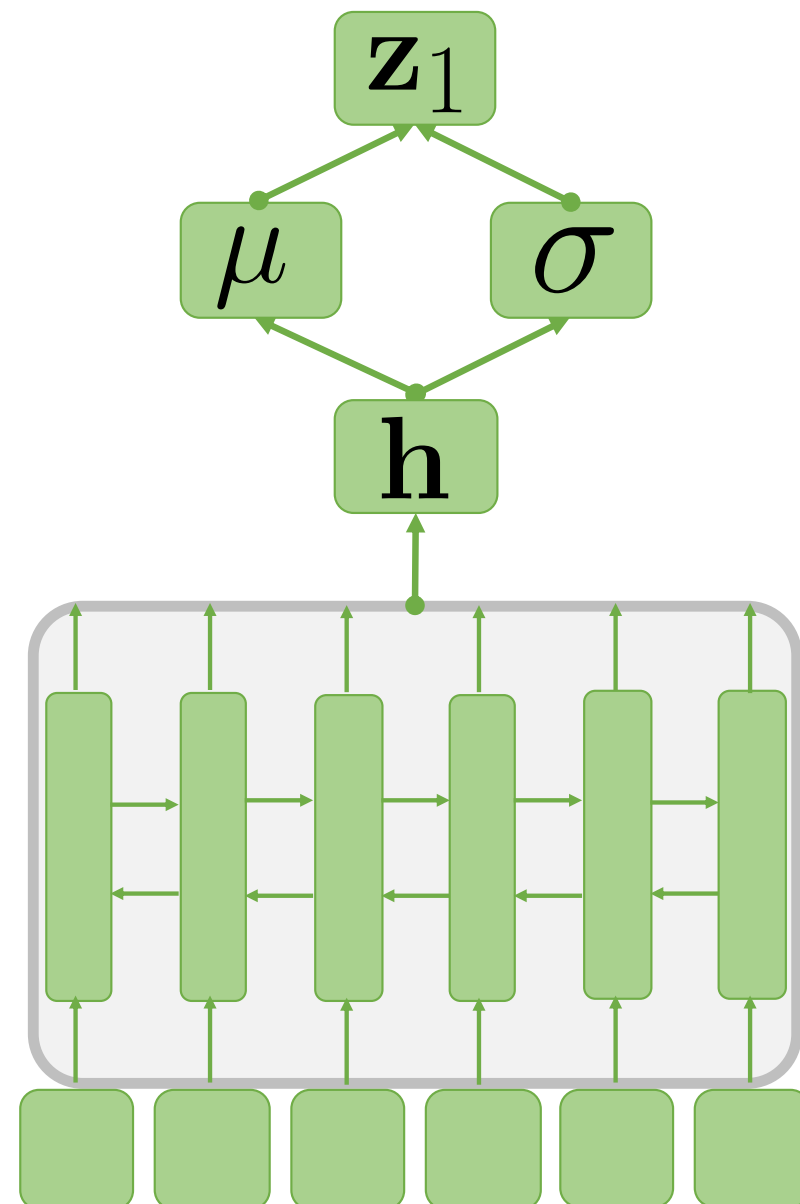
# Our SDGM-NXVAE

- Our SDGM with bag-of-word (BOW) decoder (**M<sub>1</sub> + M<sub>2</sub> + BOW**)
- Our SDGM with GRU decoder (**M<sub>1</sub> + M<sub>2</sub> + GRU**)

# Baselines - NXVAE

## Supervised models

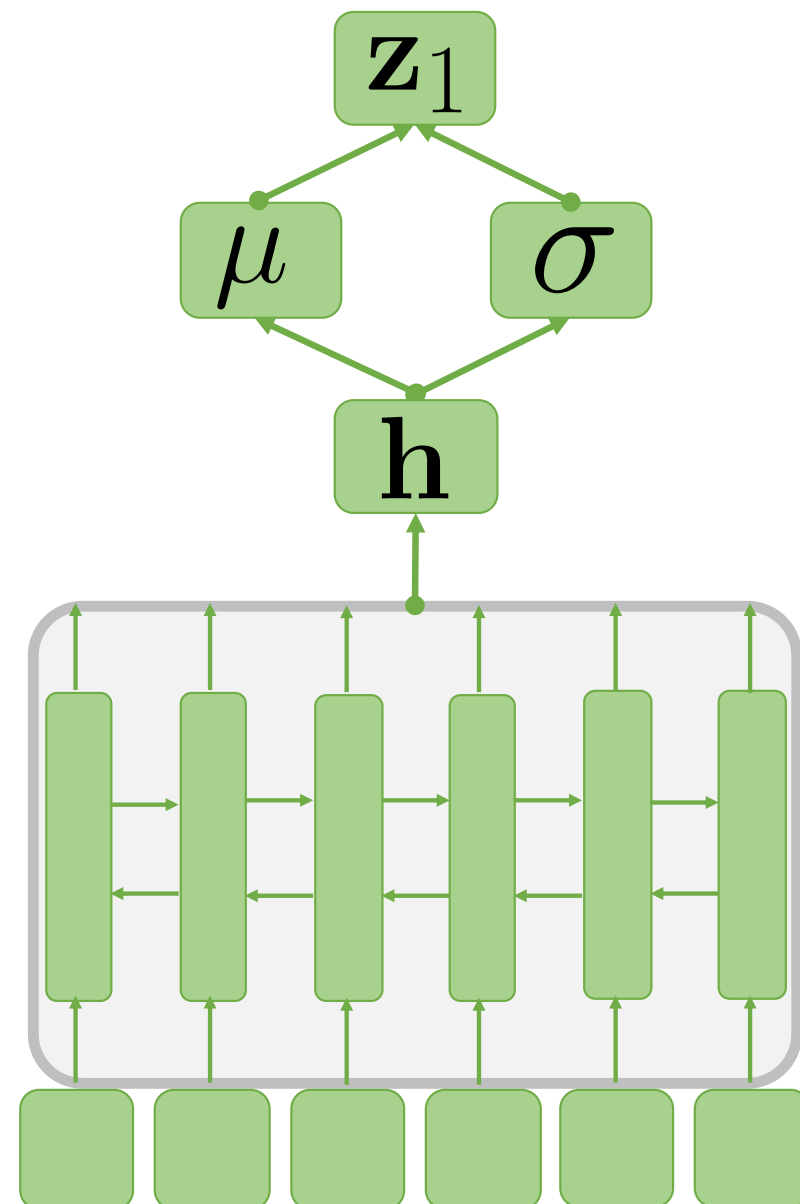
### NXVAE-Z1



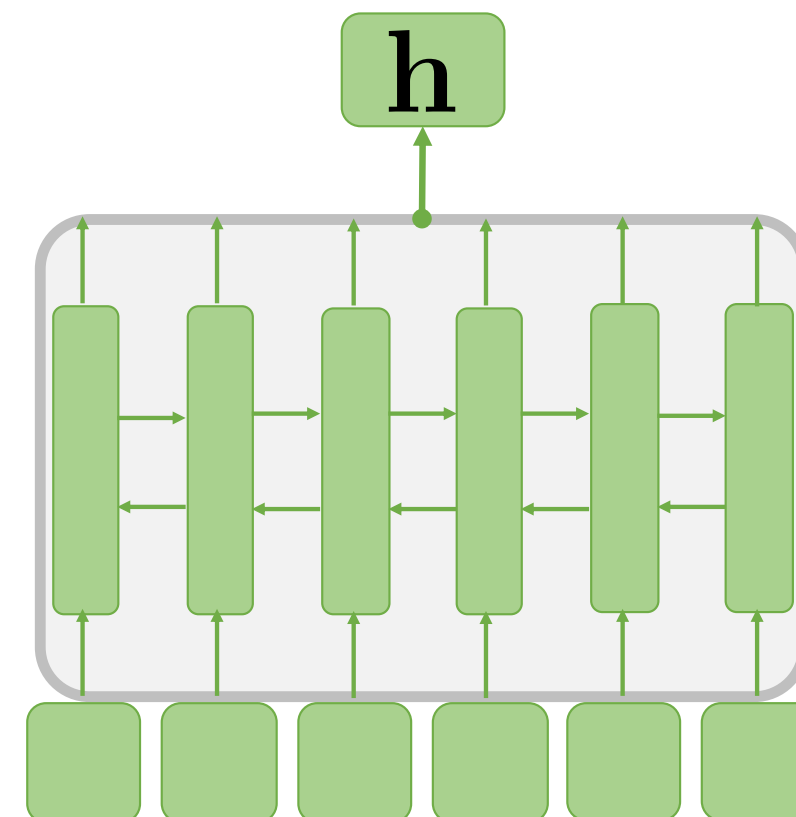
# Baselines - NXVAE

## Supervised models

**NXVAE-Z1**



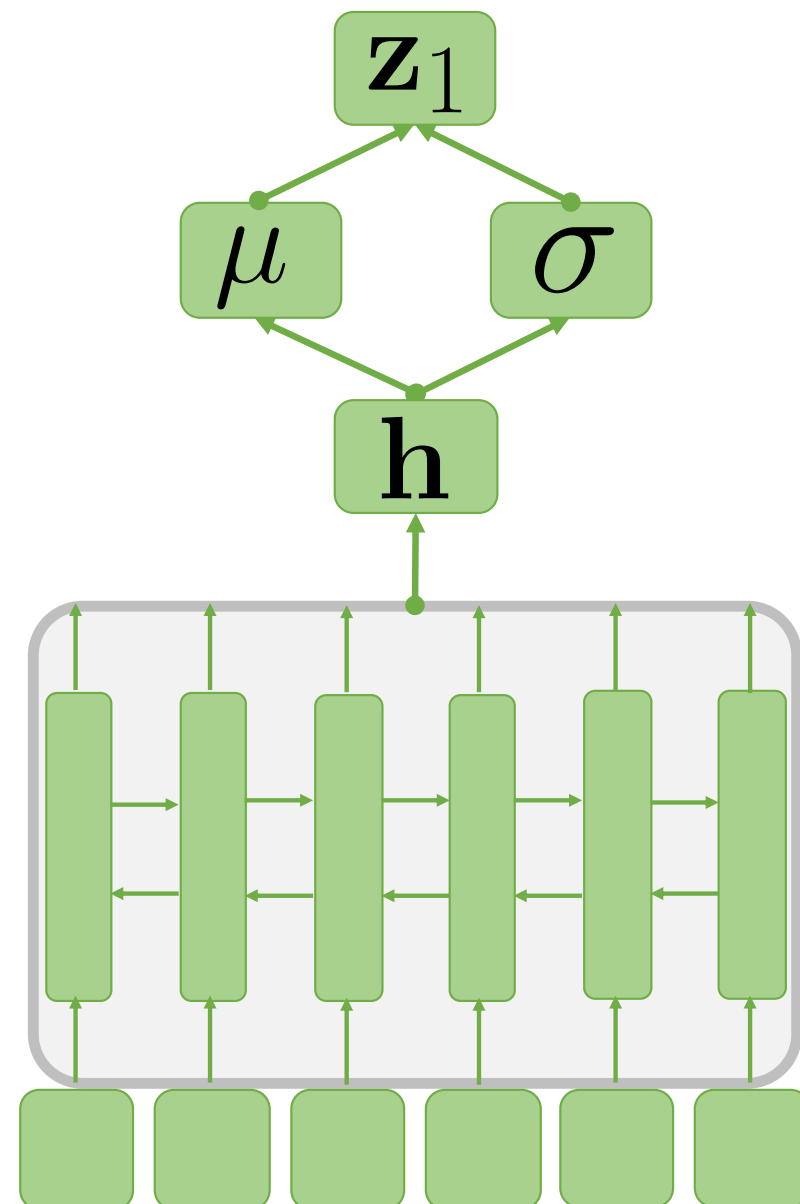
**NXVAE-h**



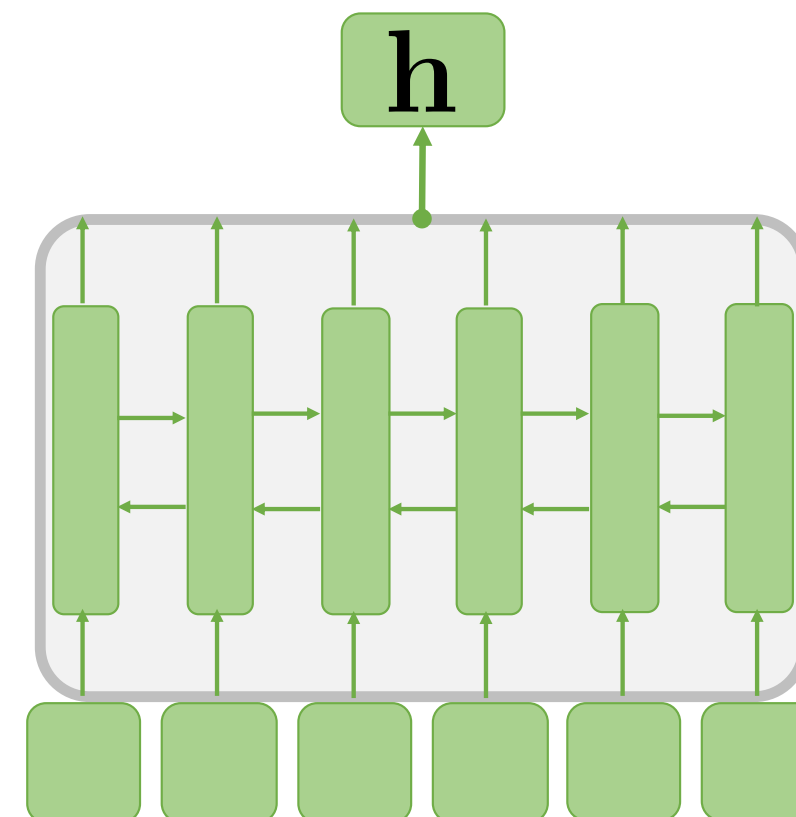
# Baselines - NXVAE

## Supervised models

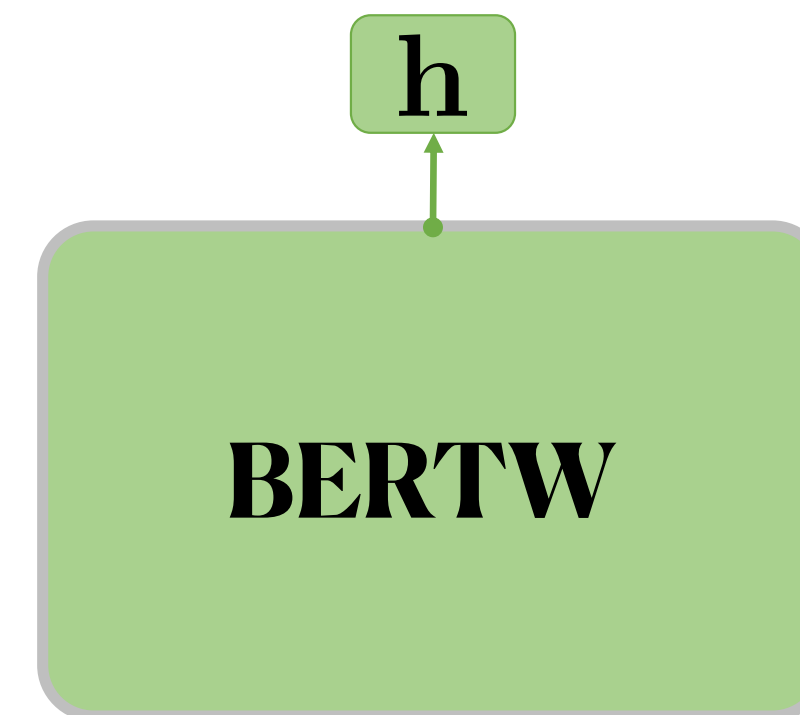
**NXVAE-Z1**



**NXVAE-h**



**BERTW**





# Baselines - NXVAE

Semi-supervised models

- $\mathbf{M_1 + M_2}$

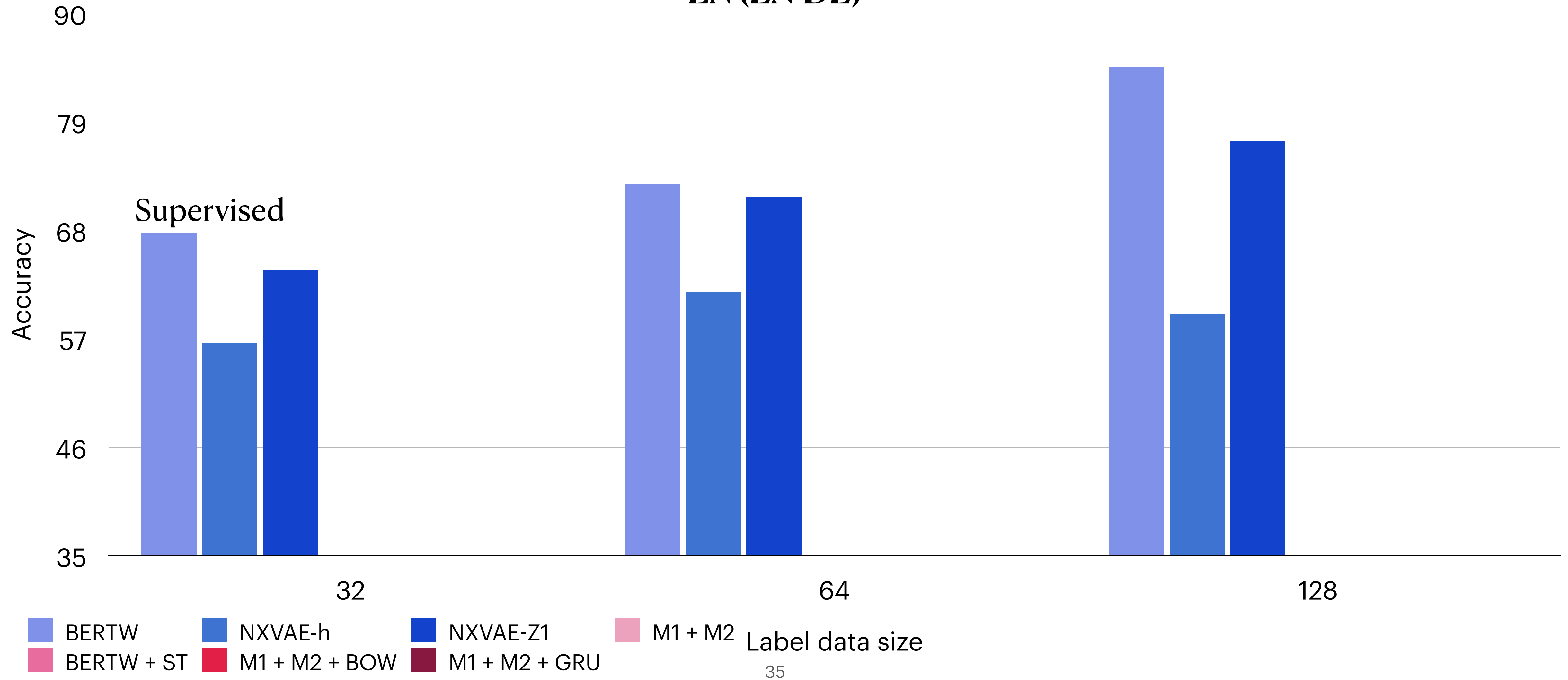
# Baselines - NXVAE

## Semi-supervised models

- **$M_1 + M_2$**
- BERTW with self-training (**BERTW + ST**)

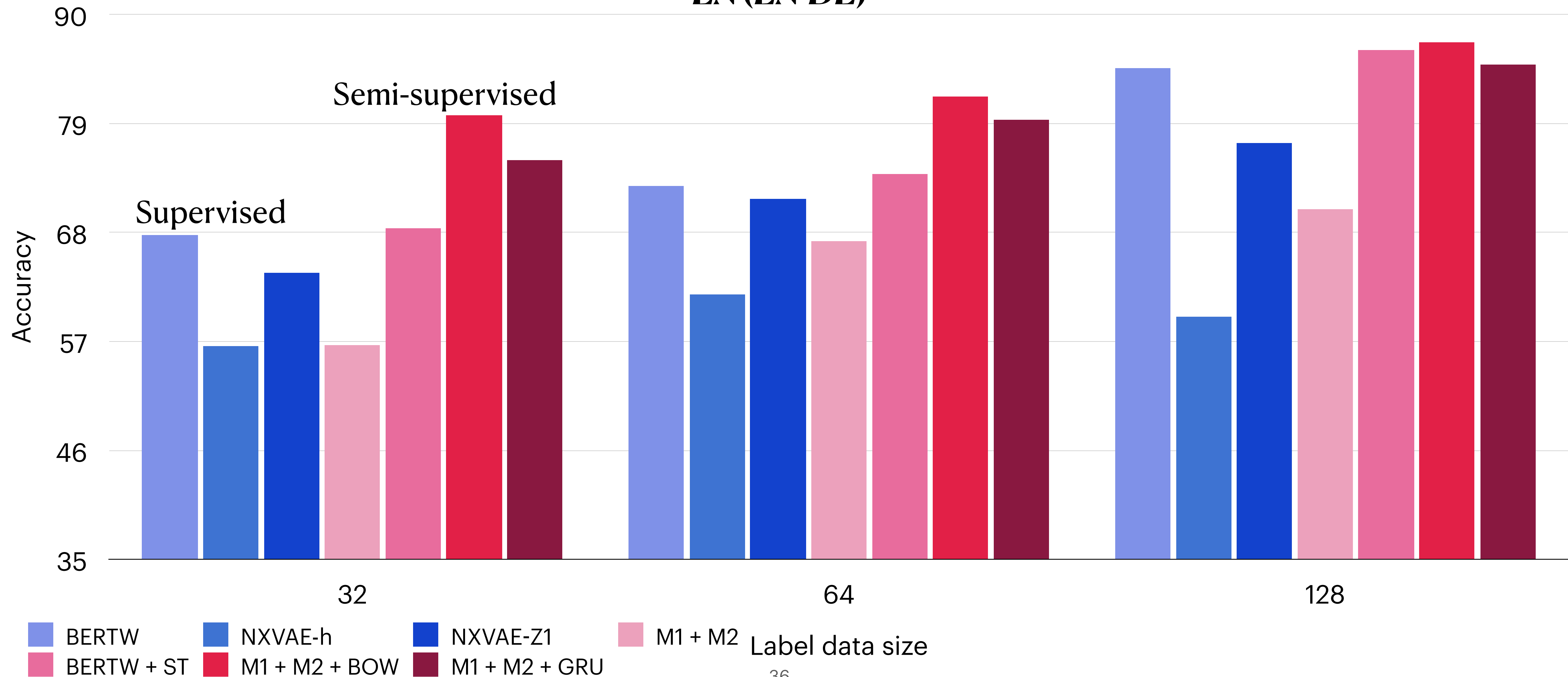
# Results

EN (EN-DE)



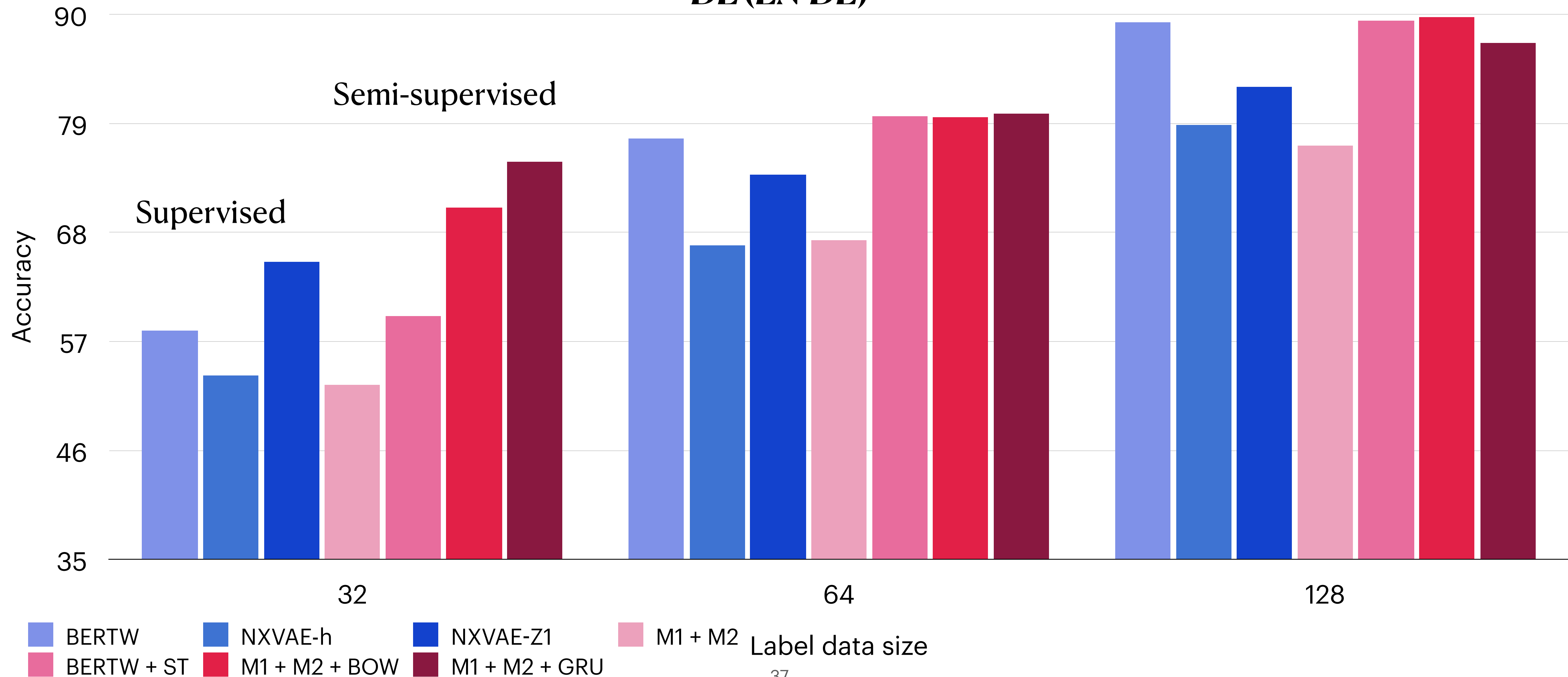
# Results

EN (EN-DE)



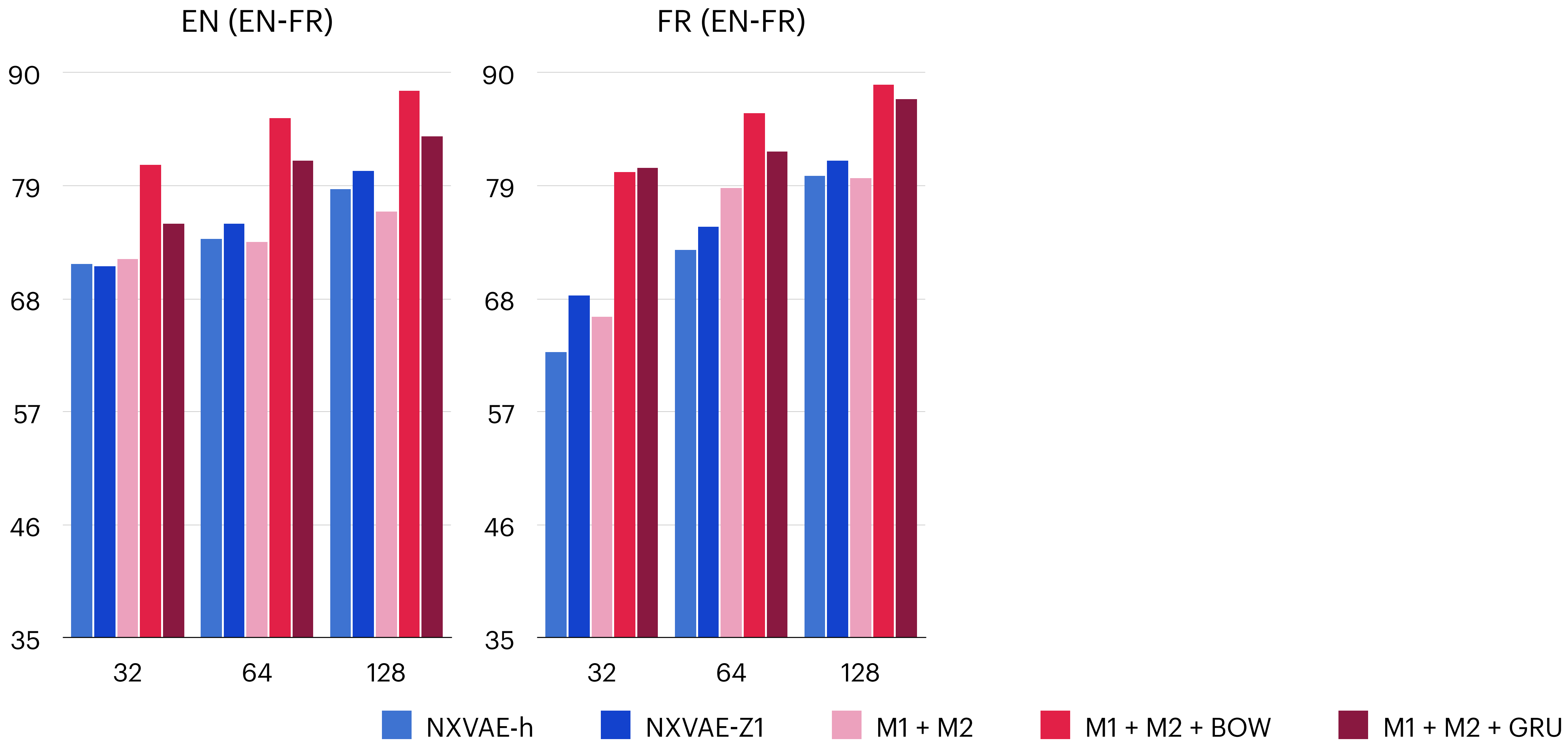
# Results

DE (EN-DE)



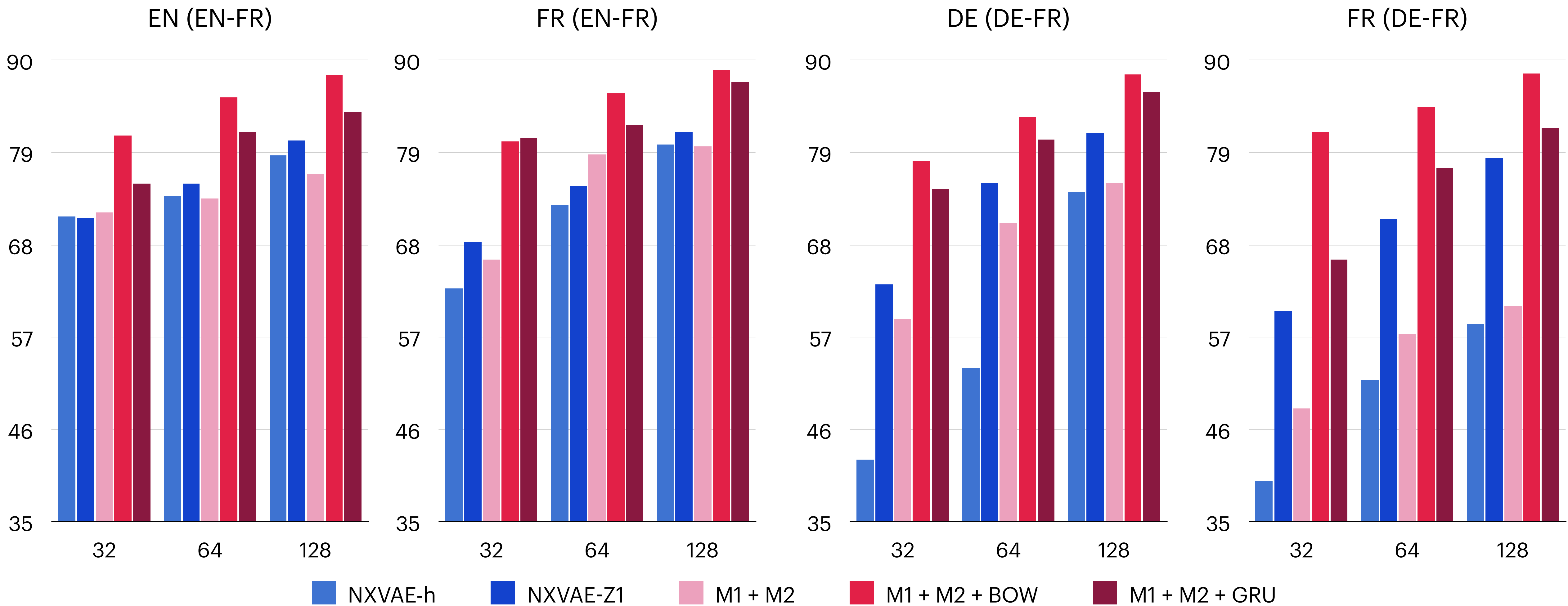
# Results

## NXVAE for EN-FR and DE-FR



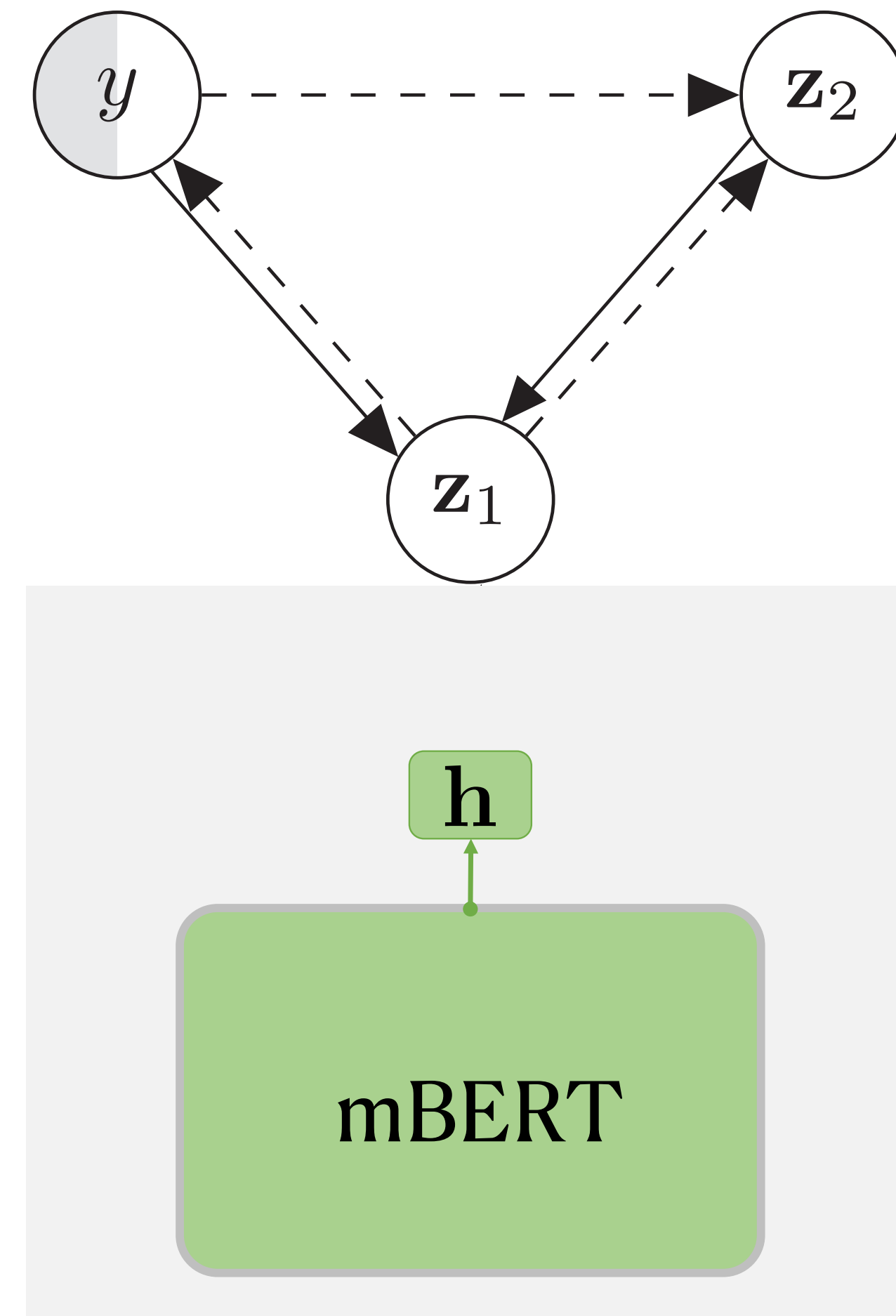
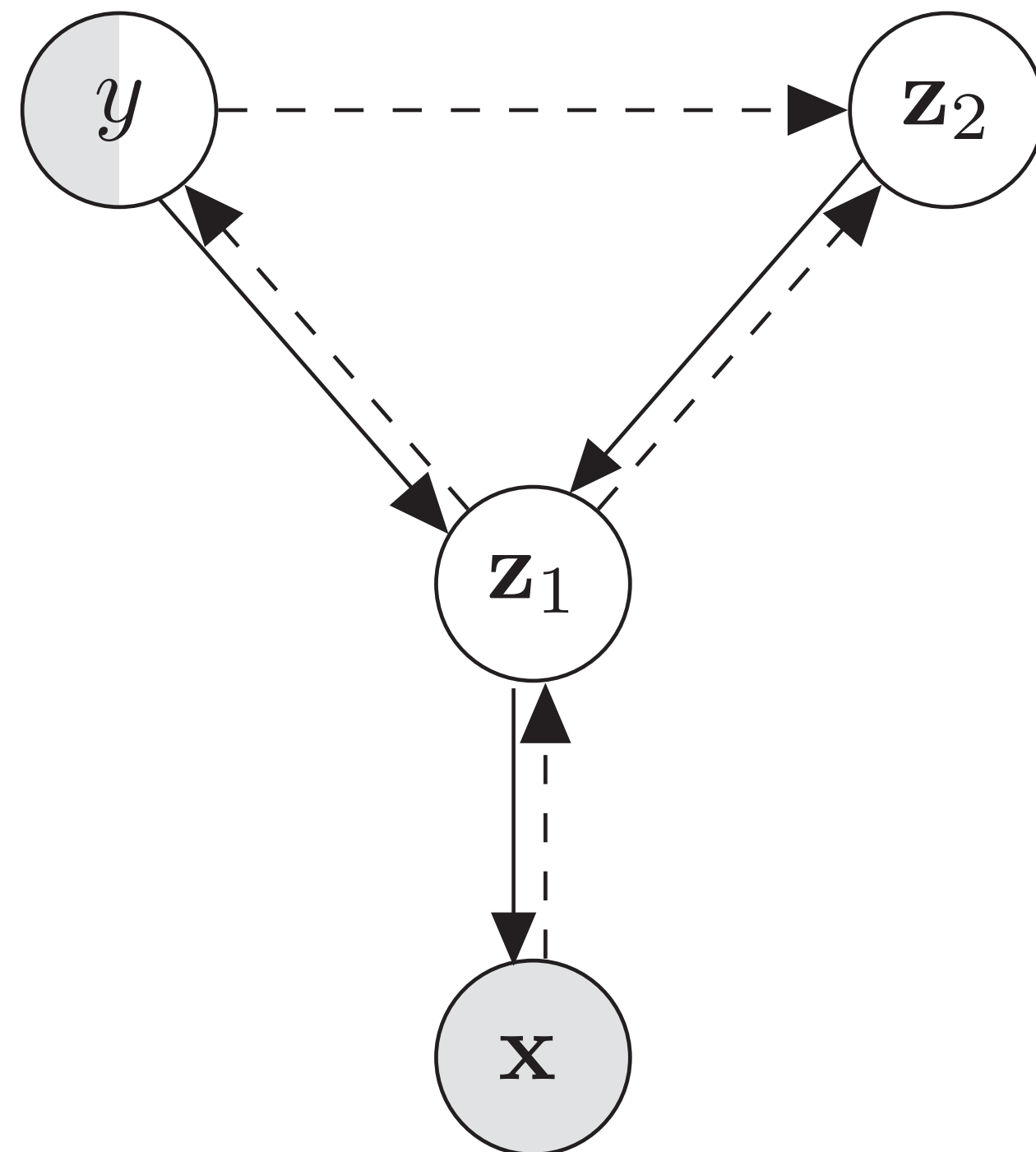
# Results

## NXVAE for EN-FR and DE-FR



# SDGMs + Multi-lingual pretraining

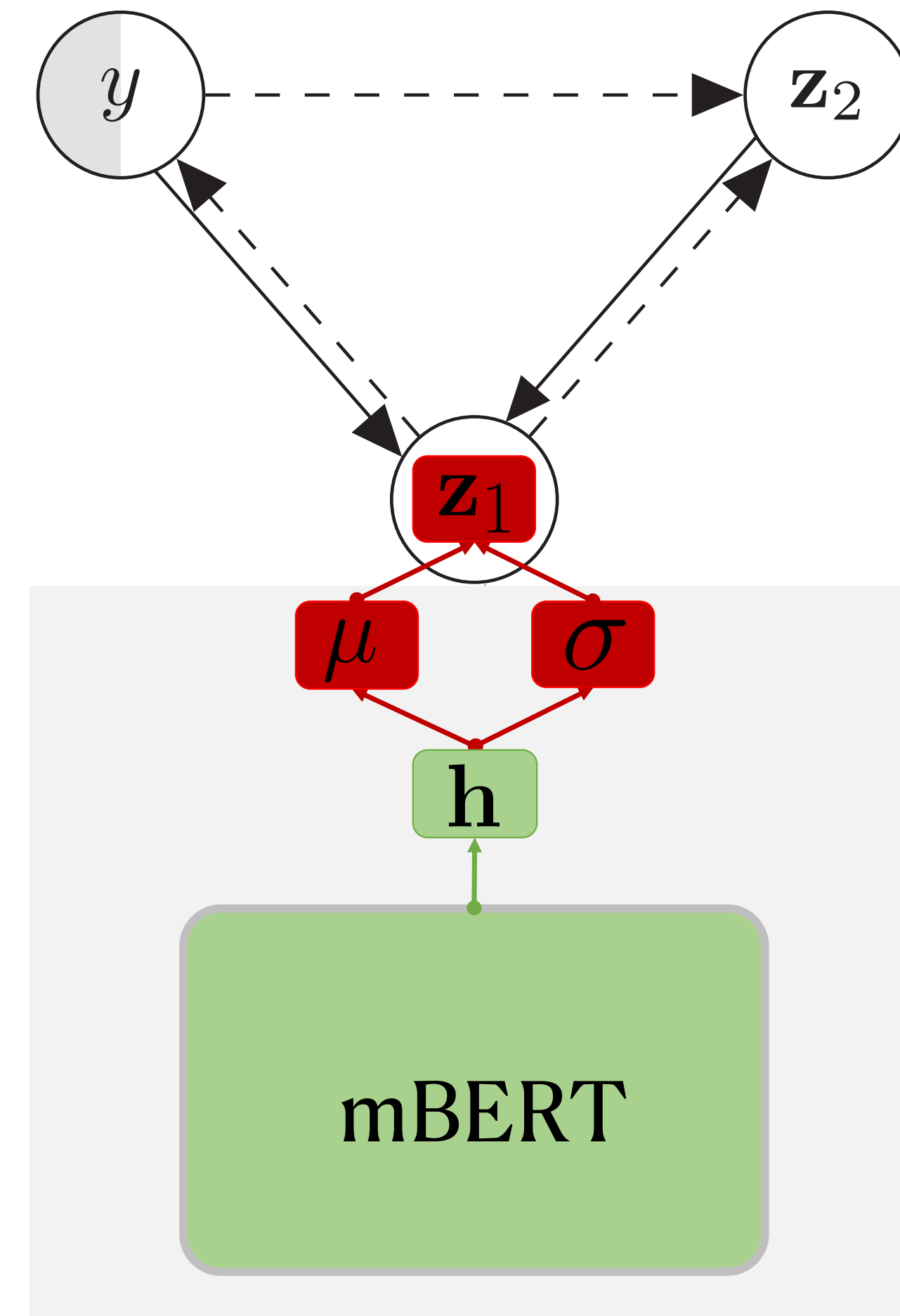
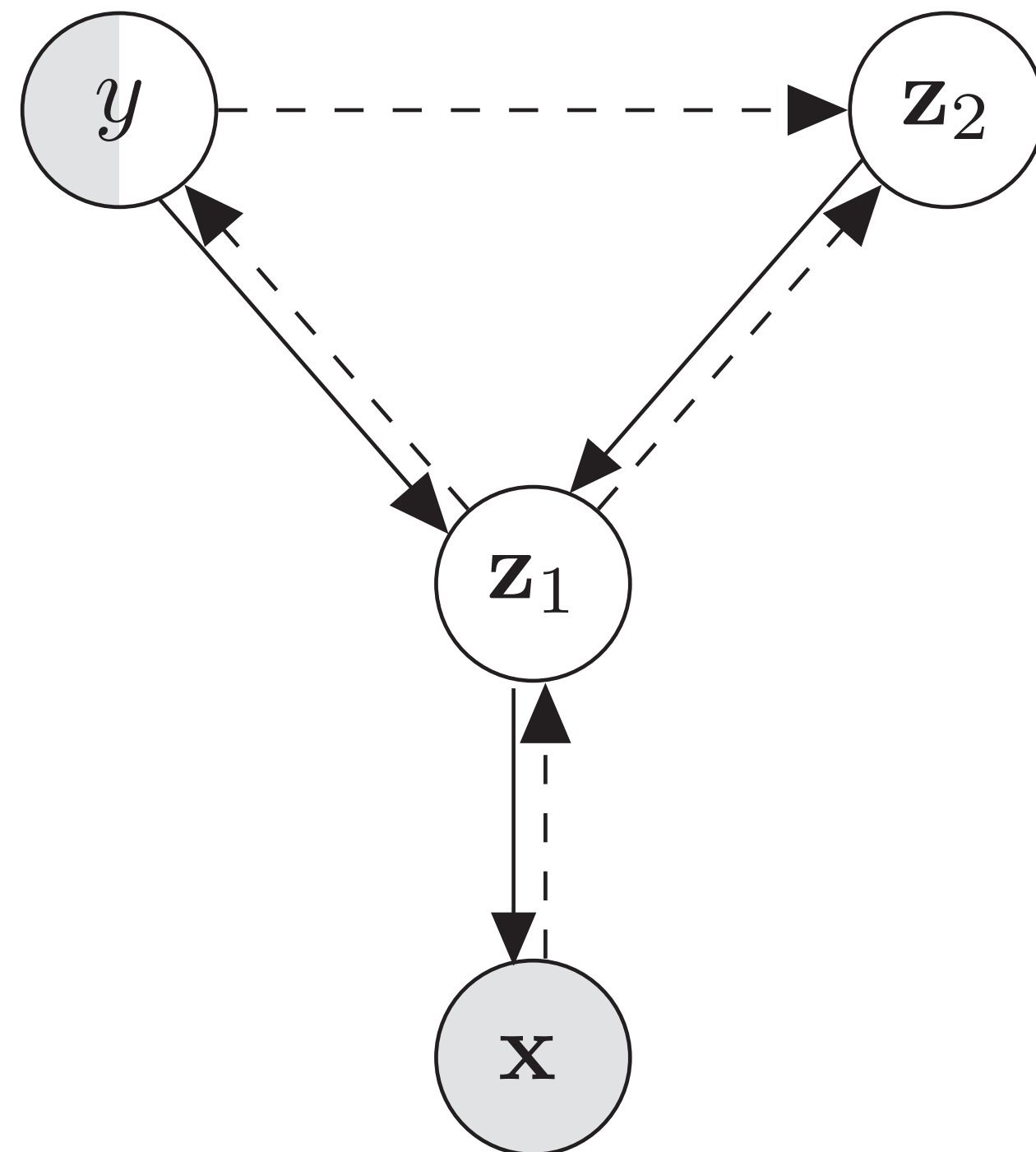
Multi-lingual BERT (mBERT)





# SDGMs + Multi-lingual pretraining

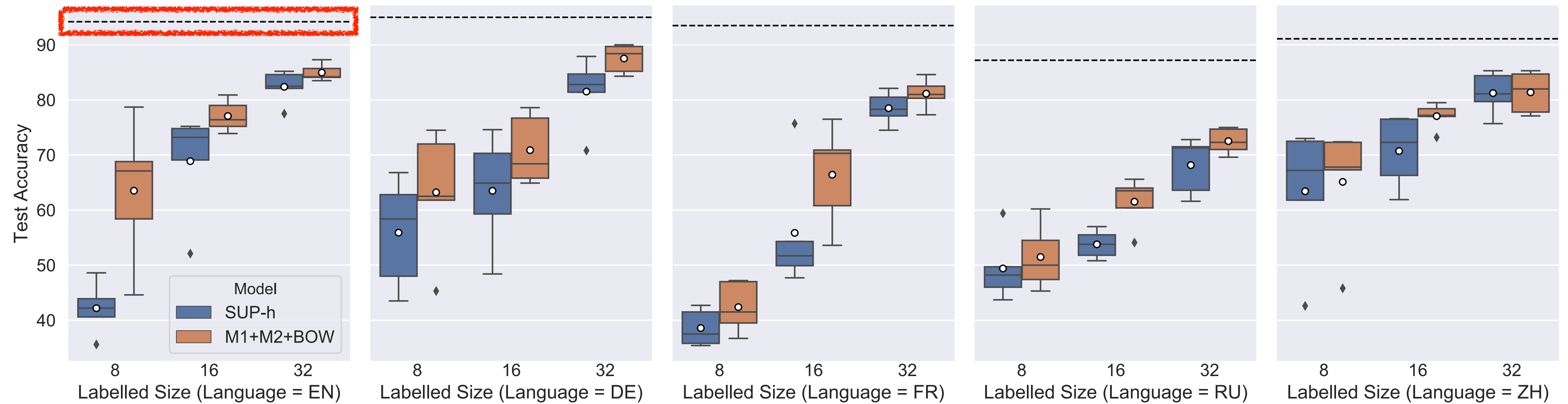
## Multi-lingual BERT (mBERT)



# Results

## mBERT

SUP-h with full training data (1k)



# Conclusion

- We bridged between multi-lingual pretraining and deep generative models to form a semi-supervised learning framework for multi-lingual document classification

# Conclusion

- We bridged between multi-lingual pretraining and deep generative models to form a semi-supervised learning framework for multi-lingual document classification
- Our framework outperformed competitive baseline models, including supervised mBERT
- The benefits of SDGMs are orthogonal to the encoding architecture, opening up a new avenue for SDGMs in low-resource NLP

# Thank you! Questions?

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