

1) Find inner product of given vectors.

$$\mathbf{R}^3 \quad x = (2, -3, 1), \quad y = (1, 5, -6)$$

2) Inner product of polynomials can be calculated as

$$p(x), q(x) \in P_n(\mathbf{R})$$

$$\langle p(x), q(x) \rangle = \int_0^1 p(x) \cdot q(x) \, dx$$

Calculate inner product of given polynomials;

$$P_2(\mathbf{R}) \quad p(x) = 3x^2 + 2x + 5, \quad q(x) = x + 1$$

3) Calculate inner product of given vectors

$$M_{2 \times 2} \quad A = \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix}, \quad B = \begin{pmatrix} 2 & 0 \\ 1 & -3 \end{pmatrix}$$

4) Find angle between two vectors in $M_{2 \times 2}$ space.

$$M_{2 \times 2} \quad A = \begin{pmatrix} 1 & 2 \\ 0 & -1 \end{pmatrix}, \quad B = \begin{pmatrix} -1 & 0 \\ 2 & 3 \end{pmatrix}$$

5) Show that given vectors are orthogonal and find orthonormal basis vectors.

$$\mathbf{R}^3 \quad x_1 = (1, 0, 3), \quad x_2 = (0, 2, 0), \quad x_3 = (-3, 0, 1)$$

6) Find orthonormal basis vectors in \mathbf{R}^3 from given vectors in \mathbf{R}^3

$$E = \{ (1, 1, 1), (1, 0, 2), (1, 2, 3) \}$$