

1) Write the matrix of the linear transformation with respect to the standard base.

$$T : \mathbb{R} \rightarrow \mathbb{R}^2$$
$$T(x) = (x, 3x)$$

2) Write the matrix of the linear transformation with respect to the given base.

$$T : \mathbb{R}^2 \rightarrow \mathbb{R}^2$$
$$T(x, y) = (x + y, x - y)$$

Base vectors $\{ (1, 1), (1, 0) \}$ in \mathbb{R}^2

3) $T : \mathbb{R}^3 \rightarrow \mathbb{R}^3$ linear transformation matrix with respect to the standard base is given below.

$$\begin{pmatrix} 1 & 2 & 0 \\ 2 & 3 & 1 \\ -1 & 1 & 0 \end{pmatrix}$$

Which one is $T(x, y, z)$?

- A. (x, y, z) B. $(x + y, 2x - 1, -1 + x - y)$
C. $(x + 2y, 2x + 3y + z, -x + y)$ D. $(x + 2x - y, 2x + 3y + z, y)$
E. $(x, x + 3y + 2z, -x + 2y - 5z)$

4) $E = \{ (1, 1, 1), (1, 1, 0), (1, 0, 0) \}$, $E' = \{ (1, 0, 0), (0, -1, 1), (-1, 0, 1) \}$ standart bases in \mathbb{R}^3 are given. Find the base transformation matrix from E to E' .

5) $T, S : \mathbb{R}^2 \rightarrow \mathbb{R}^2$
 $T(x, y) = (x + y, x)$
 $S(x, y) = (y, x + y)$
What is $(S \circ T)(x, y)$?