1 EQUILIBRIUM SYSTEM

Preferences:

$$E_0 \sum_{t=0}^{\infty} \beta^t a_t [\log(c_t) - \chi n_t^{1+\eta}/(1+\eta)]$$

Budget Constraint:

$$c_t + b_t/(i_t \bar{s}) = w_t n_t + b_{t-1}/\pi_t + d_t$$

1.1 ART MODEL   Equilibrium system (11 equations):

$$c_t = [1 - \varphi(\pi_t^{gap} - 1)^2/2]y_t \tag{1}$$

$$i_t^* = \bar{\imath}(\pi_t^{gap})^{\phi_\pi} \exp(\sigma_\nu \nu_t) \tag{2}$$

$$i_t = \max\{1, i_t^*\} \tag{3}$$

$$\lambda_t = c_t \tag{4}$$

$$w_t = \chi n_t^{\eta} \lambda_t \tag{5}$$

$$1 = \beta E_t[(\lambda_t/\lambda_{t+1})(s_t i_t/(\bar{\pi} \pi_{t+1}^{gap} g_{t+1}))] \tag{6}$$

$$\varphi(\pi_t^{gap} - 1)\pi_t^{gap} = 1 - \theta + \theta w_t/z_t + \beta \varphi E_t[(\lambda_t/\lambda_{t+1})(\pi_{t+1}^{gap} - 1)\pi_{t+1}^{gap}(y_{t+1}/y_t)] \tag{7}$$

$$y_t = z_t n_t \tag{8}$$

$$g_t = (1 - \rho_g)\bar{g} + \rho_g g_{t-1} + \sigma_\varepsilon \varepsilon_t \tag{9}$$

$$s_t = (1 - \rho_s)\bar{s} + \rho_s s_{t-1} + \sigma_\upsilon \upsilon_t \tag{10}$$

$$z_t = g_t z_{t-1} \tag{11}$$

Variables: $\{c, i^*, i, \lambda, w, \pi^{gap}, y, n, g, s, z\}$

De-trended Equilibrium System (10 equations):

$$\tilde{c}_t = [1 - \varphi(\pi_t^{gap} - 1)^2/2]\tilde{y}_t \tag{1}$$

$$i_t^* = \bar{\imath}(\pi_t^{gap})^{\phi_\pi} \exp(\sigma_\nu \nu_t) \tag{2}$$

$$i_t = \max\{1, i_t^*\} \tag{3}$$

$$\tilde{\lambda}_t = \tilde{c}_t \tag{4}$$

$$\tilde{w}_t = \chi n_t^{\eta} \tilde{\lambda}_t \tag{5}$$

$$1 = \beta E_t[(\tilde{\lambda}_t/\tilde{\lambda}_{t+1})(s_t i_t/(\bar{\pi} \pi_{t+1}^{gap} g_{t+1}))] \tag{6}$$

$$\varphi(\pi_t^{gap} - 1)\pi_t^{gap} = 1 - \theta + \theta \tilde{w}_t + \beta \varphi E_t[(\tilde{\lambda}_t/\tilde{\lambda}_{t+1})(\pi_{t+1}^{gap} - 1)\pi_{t+1}^{gap}(\tilde{y}_{t+1}/\tilde{y}_t)] \tag{7}$$

$$\tilde{y}_t = n_t \tag{8}$$

$$g_t = (1 - \rho_g)\bar{g} + \rho_g g_{t-1} + \sigma_\varepsilon \varepsilon_t \tag{9}$$

$$s_t = (1 - \rho_s)s_t + \rho_s s_{t-1} + \sigma_\upsilon \upsilon_t \tag{10}$$

Variables: $\{\tilde{c}, i^*, i, \tilde{\lambda}, \tilde{w}, \pi^{gap}, \tilde{y}, n, g, s, z\}$

Log-linear Equilibrium System:

$$\hat{c}_t = \hat{y}_t \tag{1}$$

$$\hat{\imath}_t^n = \phi_\pi \hat{\pi}_t + \sigma_\nu \nu_t \tag{2}$$

$$\hat{\imath}_t = \hat{\imath}_t^n \tag{3}$$

$$\hat{\lambda}_t = \hat{c}_t \tag{4}$$

$$\hat{w}_t = \eta \hat{n}_t + \hat{\lambda}_t \tag{5}$$

$$\hat{\lambda}_t + \hat{\imath}_t + s_t = E_t \hat{\lambda}_{t+1} + E_t \hat{\pi}_{t+1} \tag{6}$$

$$\varphi \hat{\pi}_t = (\theta - 1)\hat{w}_t + \beta \varphi E_t \hat{\pi}_{t+1} \tag{7}$$

$$\hat{y}_t = \hat{n}_t \tag{8}$$

1.2 GUST ET AL MODEL   Equilibrium system (13 equations):

$$c_t = [1 - \varphi(\pi_t^{gap} - 1)^2/2]y_t \tag{1}$$

$$i_t^* = (i_{t-1}^*)^{\rho_i}(\bar{\imath}(\pi_t^{gap})^{\phi_\pi})^{1-\rho_i}\exp(\sigma_\nu\nu_t) \tag{2}$$

$$i_t = \max\{1, i_t^*\} \tag{3}$$

$$\lambda_t = c_t \tag{4}$$

$$w_t = \chi n_t^\eta \lambda_t \tag{5}$$

$$V_{\lambda,t} = \beta E_t[(1/\lambda_{t+1})(s_t i_t/(\bar{\pi}\pi_{t+1}^{gap}g_{t+1}))] \tag{6}$$

$$1/\lambda_t = V_{\lambda,t} \tag{7}$$

$$V_{\pi,t} = 1 - \theta + \theta w_t/z_t + \beta\varphi E_t[(\lambda_t/\lambda_{t+1})(\pi_{t+1}^{gap} - 1)\pi_{t+1}^{gap}(y_{t+1}/y_t)] \tag{8}$$

$$\varphi(\pi_t^{gap} - 1)\pi_t^{gap} = V_{\pi,t} \tag{9}$$

$$y_t = z_t n_t \tag{10}$$

$$g_t = (1 - \rho_g)\bar{g} + \rho_g g_{t-1} + \sigma_\varepsilon\varepsilon_t \tag{11}$$

$$s_t = (1 - \rho_s)\bar{s} + \rho_s s_{t-1} + \sigma_\upsilon\upsilon_t \tag{12}$$

$$z_t = g_t z_{t-1} \tag{13}$$

Variables: $\{c, i^*, i, \lambda, w, \pi^{gap}, V_\lambda, y, V_\pi, n, g, s, z\}$

De-trended Equilibrium System (12 equations):

$$\tilde{c}_t = [1 - \varphi(\pi_t^{gap} - 1)^2/2]\tilde{y}_t \tag{1}$$

$$i_t^* = (i_{t-1}^*)^{\rho_i}(\bar{\imath}(\pi_t^{gap})^{\phi_\pi})^{1-\rho_i}\exp(\sigma_\nu\nu_t) \tag{2}$$

$$i_t = \max\{1, i_t^*\} \tag{3}$$

$$\tilde{\lambda}_t = \tilde{c}_t \tag{4}$$

$$\tilde{w}_t = \chi n_t^\eta \tilde{\lambda}_t \tag{5}$$

$$\tilde{V}_{\lambda,t} = \beta E_t[(1/\tilde{\lambda}_{t+1})(s_t i_t/(\bar{\pi}\pi_{t+1}^{gap}g_{t+1}))] \tag{6}$$

$$1/\tilde{\lambda}_t = \tilde{V}_{\lambda,t} \tag{7}$$

$$\tilde{V}_{\pi_t} = 1 - \theta + \theta\tilde{w}_t + \beta\varphi E_t[(\tilde{\lambda}_t/\tilde{\lambda}_{t+1})(\pi_{t+1}^{gap} - 1)\pi_{t+1}^{gap}(\tilde{y}_{t+1}/\tilde{y}_t)] \tag{8}$$

$$\varphi(\pi_t^{gap} - 1)\pi_t^{gap} = \tilde{V}_{\pi,t} \tag{9}$$

$$\tilde{y}_t = n_t \tag{10}$$

$$g_t = (1 - \rho_g)\bar{g} + \rho_g g_{t-1} + \sigma_\varepsilon\varepsilon_t \tag{11}$$

$$s_t = (1 - \rho_s)s_t + \rho_s s_{t-1} + \sigma_\upsilon\upsilon_t \tag{12}$$

Variables: $\{\tilde{c}, i^*, i, \tilde{\lambda}, \tilde{w}, \pi^{gap}, \tilde{V}_\lambda, \tilde{y}, \tilde{V}_\pi, n, g, s, z\}$

Log-linear Equilibrium System:

$$\hat{c}_t = \hat{y}_t \tag{1}$$

$$\hat{i}_t^n = \rho_i \hat{i}_{t-1}^n + (1 - \rho_i)\phi_\pi \hat{\pi}_t + \sigma_\nu \nu_t \tag{2}$$

$$\hat{i}_t = \hat{i}_t^n \tag{3}$$

$$\hat{\lambda}_t = \hat{c}_t \tag{4}$$

$$\hat{w}_t = \eta \hat{n}_t + \hat{\lambda}_t \tag{5}$$

$$\hat{V}_{\lambda,t} = \hat{i}_t + s_t - E_t \hat{\lambda}_{t+1} - E_t \hat{\pi}_{t+1} \tag{6}$$

$$-\hat{\lambda}_t = \hat{V}_{\lambda,t} \tag{7}$$

$$\hat{V}_{\pi,t} = (\theta - 1)\hat{w}_t + \beta\varphi E_t \hat{\pi}_{t+1} \tag{8}$$

$$\varphi \hat{\pi}_t = \hat{V}_{\pi,t} \tag{9}$$

$$\hat{y}_t = \hat{n}_t \tag{10}$$