

1 EQUILIBRIUM SYSTEM

Preferences:

$$E_0 \sum_{t=0}^{\infty} \beta^t a_t [\log(c_t - hc_{t-1}^a) - \chi n_t^{1+\eta}/(1+\eta)]$$

Budget Constraint:

$$c_t + b_t/(i_t(1+\bar{s})) = w_t n_t + b_{t-1}/\pi_t + d_t$$

Equilibrium system (11 equations):

$$a_t \lambda_t = c_t - hc_{t-1}^a \quad (1)$$

$$w_t = \chi a_t n_t^\eta \lambda_t \quad (2)$$

$$1 = \beta(1+\bar{s})E_t[(\lambda_t/\lambda_{t+1})(i_t/(\bar{\pi}\pi_{t+1}^{gap}))] \quad (3)$$

$$y_t = z_t n_t \quad (4)$$

$$\varphi(\pi_t^{gap} - 1)\pi_t^{gap} = 1 - \theta + \theta w_t/z_t + \beta\varphi E_t[(\lambda_t/\lambda_{t+1})(\pi_{t+1}^{gap} - 1)\pi_{t+1}^{gap}(y_{t+1}/y_t)] \quad (5)$$

$$c_t = [1 - \varphi(\pi_t^{gap} - 1)^2/2]y_t \quad (6)$$

$$i_t = \max\{1, i_t^*\} \quad (7)$$

$$i_t^* = (i_{t-1}^*)^{\rho_i} (\bar{i}(\pi_t^{gap})^{\phi_\pi} (c_t/(\bar{g}c_{t-1}))^{\phi_c})^{1-\rho_i} \exp(\sigma_\nu \nu_t) \quad (8)$$

$$g_t = (1 - \rho_g)\bar{g} + \rho_g g_{t-1} + \sigma_\varepsilon \varepsilon_t \quad (9)$$

$$a_t = 1 - \rho_a + \rho_a a_{t-1} + \sigma_v v_t \quad (10)$$

$$z_t = g_t z_{t-1} \quad (11)$$

Variables: $\{\lambda, w, c, y, n, i, i^*, \pi^{gap}, g, a, z\}$

De-trended Equilibrium System (10 equations):

$$a_t \tilde{\lambda}_t = \tilde{c}_t - h\tilde{c}_{t-1}/g_t \quad (12)$$

$$\tilde{w}_t = \chi a_t n_t^\eta \tilde{\lambda}_t \quad (13)$$

$$1 = \beta(1+\bar{s})E_t[(\tilde{\lambda}_t/\tilde{\lambda}_{t+1})(i_t/(\bar{\pi}\pi_{t+1}^{gap}g_{t+1}))] \quad (14)$$

$$\tilde{y}_t = n_t \quad (15)$$

$$\varphi(\pi_t^{gap} - 1)\hat{\pi}_t^{gap} = 1 - \theta + \theta \tilde{w}_t + \beta\varphi E_t[(\tilde{\lambda}_t/\tilde{\lambda}_{t+1})(\pi_{t+1}^{gap} - 1)\pi_{t+1}^{gap}(\tilde{y}_{t+1}/\tilde{y}_t)] \quad (16)$$

$$\tilde{c}_t = [1 - \varphi(\pi_t^{gap} - 1)^2/2]\tilde{y}_t \quad (17)$$

$$i_t = \max\{1, i_t^*\} \quad (18)$$

$$i_t^* = (i_{t-1}^*)^{\rho_i} (\bar{i}(\pi_t^{gap})^{\phi_\pi} (g_t \tilde{c}_t/(\bar{g}\tilde{c}_{t-1}))^{\phi_c})^{1-\rho_i} \exp(\sigma_\nu \nu_t) \quad (19)$$

$$g_t = (1 - \rho_g)\bar{g} + \rho_g g_{t-1} + \sigma_\varepsilon \varepsilon_t \quad (20)$$

$$a_t = 1 - \rho_a + \rho_a a_{t-1} + \sigma_v v_t \quad (21)$$

Variables: $\{\tilde{\lambda}, \tilde{w}, \tilde{c}, \tilde{y}, n, i, i^*, \pi^{gap}, g, a\}$

Log-linear Equilibrium System:

$$(1 - h/g)(\hat{a}_t + \hat{\lambda}_t) = \hat{c}_t + (h/g)(\hat{g}_t - \hat{c}_{t-1}) \quad (22)$$

$$\hat{w}_t = \hat{a}_t + \eta \hat{n}_t + \hat{\lambda}_t \quad (23)$$

$$\hat{\lambda}_t + \hat{i}_t = E_t \hat{\lambda}_{t+1} + E_t \hat{\pi}_{t+1} + E_t \hat{g}_{t+1} \quad (24)$$

$$\hat{y}_t = \hat{n}_t \quad (25)$$

$$\varphi \hat{\pi}_t = (\theta - 1) \hat{w}_t + \beta \varphi E_t \hat{\pi}_{t+1} \quad (26)$$

$$\hat{c}_t = \hat{y}_t \quad (27)$$

$$\hat{i}_t = \hat{i}_t^n \quad (28)$$

$$\hat{i}_t^n = \rho_i \hat{i}_{t-1}^n + (1 - \rho_i) \phi_\pi \hat{\pi}_t + (1 - \rho_i) \phi_c (\hat{g}_t + \hat{c}_t - \hat{c}_{t-1}) + \sigma_\nu \nu_t \quad (29)$$