

Fixed point:

$$Ebond = \beta \sum_w (\lambda_t / \lambda_{t+1}) / (g_{t+1} \bar{\pi} \pi_{t+1}^{gap}) \quad (1)$$

$$Ecap = \beta \sum_w (\lambda_t / \lambda_{t+1}) (r_{t+1}^k + (1 - \delta) q_{t+1}) / g_{t+1} \quad (2)$$

$$Einv = \beta \sum_w (\lambda_t / \lambda_{t+1}) q_{t+1} (x_{t+1}^g)^2 (x_{t+1}^g - 1) / g_{t+1} \quad (3)$$

$$Eppc = \beta \sum_w (\lambda_t / \lambda_{t+1}) (\pi_{t+1}^{gap} - 1) \pi_{t+1}^{gap} (y_{t+1} / y_t) \quad (4)$$

$$x\_up(3) = Ecap \quad (5)$$

$$\lambda_t = 1 / (s_t i_t Ebond / (\bar{\pi} \lambda_t)) \quad (6)$$

$$c_t = \lambda_t + \bar{h} c_t / g_t \quad (7)$$

$$var = (1 - \bar{g} Einv) / x\_up(3) \quad (8)$$

$$x_t^g = 1 / (3 \sqrt{7 - 6var} + 2) \quad (9)$$

$$x_t = x_t^g \bar{g} x_t / g_t \quad (10)$$

$$y_t = c_t + x_t \quad (11)$$

$$x\_up(2) = (y_t / (k_t / g_t)^\alpha)^{1/(1-\alpha)} \quad (12)$$

$$RHS = 1 - \theta + \theta m c_t + \varphi Eppc \quad (13)$$

$$x\_up(1) = (1 + \sqrt{(\varphi + 4RHS) / \varphi}) / 2 \quad (14)$$

$$LHS = \varphi (\pi_{t+1}^{gap} - 1) \pi_{t+1}^{gap} - (1 - \theta) - \varphi Eppc \quad (15)$$

$$x\_up(4) = LHS / \theta \quad (16)$$

De-trended Equilibrium System:

$$\tilde{y}_t = (\tilde{k}_{t-1}/g_t)^\alpha n_t^{1-\alpha} \quad (1)$$

$$r_t^k = \alpha m c_t g_t \tilde{y}_t / \tilde{k}_{t-1} \quad (2)$$

$$\tilde{w}_t = (1 - \alpha) m c_t \tilde{y}_t / n_t \quad (3)$$

$$\tilde{y}_t^{gdp} = [1 - \varphi(\pi_t^{gap} - 1)^2/2] \tilde{y}_t \quad (4)$$

$$y_t^g = g_t \tilde{y}_t^{gdp} / (\bar{g} \tilde{y}_{t-1}^{gdp}) \quad (5)$$

$$i_t^* = (i_{t-1}^*)^{\rho_i} (\bar{l}(\pi_t^{gap})^{\phi_\pi} (y_t^g)^{\phi_y})^{1-\rho_i} \exp(\sigma_i \varepsilon_{i,t}) \quad (6)$$

$$i_t = \max\{1, i_t^*\} \quad (7)$$

$$\tilde{\lambda}_t = \tilde{c}_t - h \tilde{c}_{t-1} / g_t \quad (8)$$

$$\tilde{w}_t = \chi n_t^\eta \tilde{\lambda}_t \quad (9)$$

$$\tilde{c}_t + \tilde{x}_t = \tilde{y}_t^{gdp} \quad (10)$$

$$x_t^g = g_t \tilde{x}_t / (\bar{g} \tilde{x}_{t-1}) \quad (11)$$

$$\tilde{k}_t = (1 - \delta)(\tilde{k}_{t-1}/g_t) + \tilde{x}_t(1 - \nu(x_t^g - 1)^2/2) \quad (12)$$

$$1 = \beta E_t[(\tilde{\lambda}_t/\tilde{\lambda}_{t+1})(s_t i_t / (\bar{\pi} \pi_{t+1}^{gap} g_{t+1}))] \quad (13)$$

$$q_t = \beta E_t[(\tilde{\lambda}_t/\tilde{\lambda}_{t+1})(r_{t+1}^k + (1 - \delta)q_{t+1})/g_{t+1}] \quad (14)$$

$$1 = q_t[1 - (x_t^g - 1)^2/2 - (x_t^g - 1)x_t^g] + \beta \bar{g} E_t[q_{t+1}(\tilde{\lambda}_t/\tilde{\lambda}_{t+1})(x_{t+1}^g)^2(x_{t+1}^g - 1)/g_{t+1}] \quad (15)$$

$$\varphi(\pi_t^{gap} - 1)\pi_t^{gap} = 1 - \theta + \theta m c_t + \beta \varphi E_t[(\tilde{\lambda}_t/\tilde{\lambda}_{t+1})(\pi_{t+1}^{gap} - 1)\pi_{t+1}^{gap}(\tilde{y}_{t+1}/\tilde{y}_t)] \quad (16)$$

$$g_t = \bar{g} + \sigma_g \varepsilon_{g,t} \quad (17)$$

$$s_t = (1 - \rho_s)s_t + \rho_s s_{t-1} + \sigma_s \varepsilon_{s,t} \quad (18)$$

$$m p_t = \sigma_i \varepsilon_{i,t} \quad (19)$$

Variables:  $\{\tilde{c}, \tilde{n}, \tilde{x}, \tilde{k}, \tilde{y}^{gdp}, \tilde{y}, x^g, y^g, \tilde{w}, r^k, \pi, i, i^n, q, m c, \tilde{\lambda}, g, s, m p\}$