

2) $x^2 + y^2$

$$x^2 + y^2$$

$$(1)^2 + 3^2$$

3) ~~$x^2 + y^2$~~

$$\sqrt{x^2 + y^2} \rightarrow 1300$$

4) $\sqrt{y^3 - x^2}$

$$\sqrt{3^3 - 2^2}$$

$$3\sqrt{3} - 4$$

5) $|x - y|$

$$\text{abs } (x - y)$$

$$= 10$$

6) $((2, 3, 4, 5))^2$

$$4 + 9 + 16 + 25$$

7) $((4, 5, 6, 8))^3$

$$64 \quad 125 \quad 216 \quad 512$$

8) $-4 \quad C(2, 3, 5, 7)$

$$-4 \quad -9 \quad -25$$

$$* C(-2, -3, -5, -7)$$

$$-28$$

Basics of R Software

- 1) R is a software for data analysis and statistical computing
- 2) This software is used for effective data handling and output storage is possible
- 3) It is capable of graphical display
- 4) It is a free software.

$$1) 2^2 + \sqrt{25} + 35$$

$$\rightarrow 2^2 + \text{sqrt}(25) + 35 \\ [1] 44.$$

$$2) 2 * 5 * 3 + 62 \div 5 + \sqrt{49}$$

$$\rightarrow 2 * 5 * 3 + 62 / 5 + \text{sqrt}(49) \rightarrow 49.4$$

$$3) \text{sqrt}(46 + 4 * 2 + 9 / 5) \rightarrow \sqrt{76 + 8 + 1.8} \rightarrow 9.26$$

$$4) 42 + |-10| + 7^2 + 3 * 9$$

$$\rightarrow 42 + \text{abs}(-10) + 7^2 + 3 * 9 \rightarrow 128$$

$$5) x = 20$$

$$y = 30$$

$$x + y \\ [1] 50$$

Find the sum, prod, max, min, of the values
 $c = (5, 8, 6, 7, 9, 10, 15, 5)$

$$\begin{bmatrix} 1 & 5 \\ 2 & 6 \\ 3 & 7 \\ 4 & 8 \end{bmatrix}$$

$x <- \text{matrix}(\text{nrow} = 4, \text{ncol} = 2,$
 $\text{data} = c(1, 2, 3, 4, 5, 6, 7, 8))$

$$x = \begin{bmatrix} 1 & 4 & 7 \\ 2 & 5 & 8 \\ 3 & 6 & 9 \end{bmatrix} \quad y = \begin{bmatrix} 2 & 4 & 10 \\ -2 & 8 & -11 \\ 10 & 6 & 12 \end{bmatrix}$$

$$\begin{aligned} & 6x + y \\ & x \times y \\ & 2x + 3y \end{aligned}$$

Q8

$x = ((2, 4, 6, 1, 3, 5, 7, 18, 16, 14, 17, 19, 18, 3, 2, 5, 0, 13, 9, 4, 18, 10, 12))$

$a = \text{table}(x)$.

$\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$

$a = \text{table}(x)$.

$\text{random}(a)$.

Can the following be p.d.f?

$$f(x) = \begin{cases} 2-x & ; 1 \leq x \leq 2 \\ 0 & \text{o.w.} \end{cases}$$

To prove :- $\int_1^2 (2-x) dx = 1$

$$\begin{aligned} & \int_1^2 2dx - \int_1^2 xdx \\ &= 2x \Big|_1^2 - \frac{x^2}{2} \Big|_1^2 \\ &= (4-2) - (2 - 0.5) \\ &= 2 - 1.5 \\ &= 0.5 \end{aligned}$$

Hence it is ~~not~~ a p.d.f.

$$f(x) = \begin{cases} 3x^2 & ; 0 \leq x \leq 1 \\ 0 & \text{o.w.} \end{cases}$$

To prove :- $\int_0^1 3x^2 dx = 1$.

$$\int_0^1 3x^2 dx$$

$$\begin{aligned} &= \frac{3x^3}{3} \Big|_0^1 \\ &= 1 - 0. \end{aligned}$$

Hence it is a p.d.f.

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$$3) f(x) = \begin{cases} \frac{3x}{2} (1 - \frac{x}{2}), & 0 \leq x \leq 2 \\ 0 & \text{o.w.} \end{cases}$$

$$\rightarrow \int_0^2 \frac{3x}{2} \left(1 - \frac{x}{2}\right) dx$$

$$= \left[\frac{3x^2}{4} \left(x - \frac{x^2}{4} \right) \right]_0^2$$

$$= \frac{12}{4} - 2 = 0.$$

$$= 3 - 2$$

$$= 1$$

Q2) Can the following be p.m.f

(i)	x	1	2	3	4	5
	p(x)	0.2	0.3	-0.1	0.5	0.1

$$\nexists \int p(x) = 1.$$

Hence it is a p.m.f.

(ii)	x	0	1	2	3	4	5
	p(x)	0.1	0.3	0.2	0.2	0.1	0.1

Q3)	$P(X \leq 2)$, $P(2 \leq X \leq 4)$, $P(\text{at least } 4)$, $(P 3 \leq X \leq 6)$																
	<table border="1"> <tbody> <tr> <td>x</td><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td></tr> <tr> <td>p(x)</td><td>0.1</td><td>0.1</td><td>0.2</td><td>0.2</td><td>0.1</td><td>0.2</td><td>0.1</td></tr> </tbody> </table>	x	0	1	2	3	4	5	6	p(x)	0.1	0.1	0.2	0.2	0.1	0.2	0.1
x	0	1	2	3	4	5	6										
p(x)	0.1	0.1	0.2	0.2	0.1	0.2	0.1										

$$i) P(X \leq 2).$$

$$P(0) + P(1) = 0.1 + 0.1 = 0.2.$$

$$\text{i)} P(2 \leq X \leq 4).$$

$$P(2) + P(3) + P(4)$$

$$= 0.2 + 0.2 + 0.1$$

$$= 0.5$$

$$\text{ii)} P(4) + P(5)$$

$$= 0.1 + 0.2$$

$$= 0.3$$

$$\text{iii)} P(9) + P(5)$$

$$= 0.1 + 0.2$$

$$= 0.3$$

Q4) Prob = ~~(0.1, 0.1, 0.2, 0.2, 0.1, 0.2, 0.1)~~.

1)	X	0	1	2	3	4	5	6
	P(X)	0.1	0.1	0.2	0.2	0.1	0.2	0.1

2)	X	10	12	14	16	18
	P(X)	0.2	0.35	0.15	0.2	0.1

$$\text{Ans1)} F(x) = 0 \quad \text{if } x < 0.$$

$$= 0.1 \quad \text{if } 0 \leq x < 1$$

$$= 0.2 \quad \text{if } 1 \leq x < 2$$

$$= 0.4 \quad \text{if } 2 \leq x < 3$$

$$= 0.6 \quad \text{if } 3 \leq x < 4$$

$$= 0.7 \quad \text{if } 4 \leq x < 5$$

$$= 0.9 \quad \text{if } 5 \leq x < 6$$

$$= 1.0 \quad \text{if } x \geq 6$$

$$\text{Ans2)} F(x) = 0. \quad \text{if } x < 0.$$

$$= 0.2 \quad \text{if } 0 \leq x < 12$$

$$= 0.55 \quad \text{if } 12 \leq x < 14$$

$$= 0.70 \quad \text{if } 14 \leq x < 16$$

$$= 0.90 \quad \text{if } 16 \leq x < 18$$

$$= 1.0 \quad \text{if } x \geq 18$$

Practical-3.

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Probability distribution and B.D

- i) Find PPF of the foll CDF and draw the graph.

x	10	20	30	40	50
$f(x)$	0.15	0.25	0.3	0.2	0.1

$$\begin{aligned} \rightarrow P(x) &= 0 && \text{if } x < 10 \\ &= 0.15 && 10 \leq x < 20 \\ &= 0.40 && 20 \leq x < 30 \\ &= 0.70 && 30 \leq x < 40 \\ &= 0.90 && 40 \leq x < 50 \\ &= 1.0 && x \geq 50 \end{aligned}$$

$$\Rightarrow x = (10, 20, 30, 40, 50)$$

prob = (0.15, 0.25, 0.3, 0.2, 0.1)
 cumsum (prob)

$$[1] 0.15 \quad 0.40 \quad 0.70 \quad 0.90 \quad 1.0$$

$\rightarrow \text{plot}(x, \text{cumsum(prob)}, \text{xlab} = \text{"values"}, \text{ylab} = \text{"probability"}, \text{main} = \text{"graph of cdf of S"})$

Binomial distribution

2) Suppose there are 12 mcq's in a test + each question has 3 options and only one of them is correct. Find the probability of having at least 5 correct answers (2) at most 6 correct answers

$$\rightarrow n = 12, p = 1/3, q = 2/3$$

x = total no. of correct ans

$\sim WB(n, p)$

$$n = 12, p = 1/3, q = 2/3, x = 5 \text{ or } 6$$

$$n = 12; p = 1/3; q = 2/3; x = 5 \text{ or } 6$$

[1] 18

$$\Rightarrow p_{\text{binom}}(5, 2, 1/3)$$

$$0.05318022$$

$$\Rightarrow p_{\text{binom}}(4, 12, 1/3)$$

$$0.9274443$$

3) There are 10 members in a committee, the probability of any one attending a meeting is 0.9. Find the probability

(i) If member attended

(ii) At least 3 members attended

(iii) At most 6 members attended.

Given that

$$n = 10, p = 0.9, q = 0.1$$

x = Total no. of member attended.

$$x \sim B(n, p)$$

$$n = 10, p = 0.9, q = 0.1$$

$$\geq n = 10, p = 0.9, q = 0.1$$

$$\geq \text{dbinom}(7, 10, 0.9)$$

$$[1] 0.05739$$

$$> 1 - \text{pbinom}(5, 10, 0.9)$$

$$[1] 0.99836$$

$$> \text{pbinom}(6, 10, 0.9)$$

$$[1] 0.0127952$$

4) Find the C.d.f and draw the graph

X	0	1	2	3	4	5	6
$p(x)$	0.1	0.1	0.2	0.2	0.1	0.2	0.1

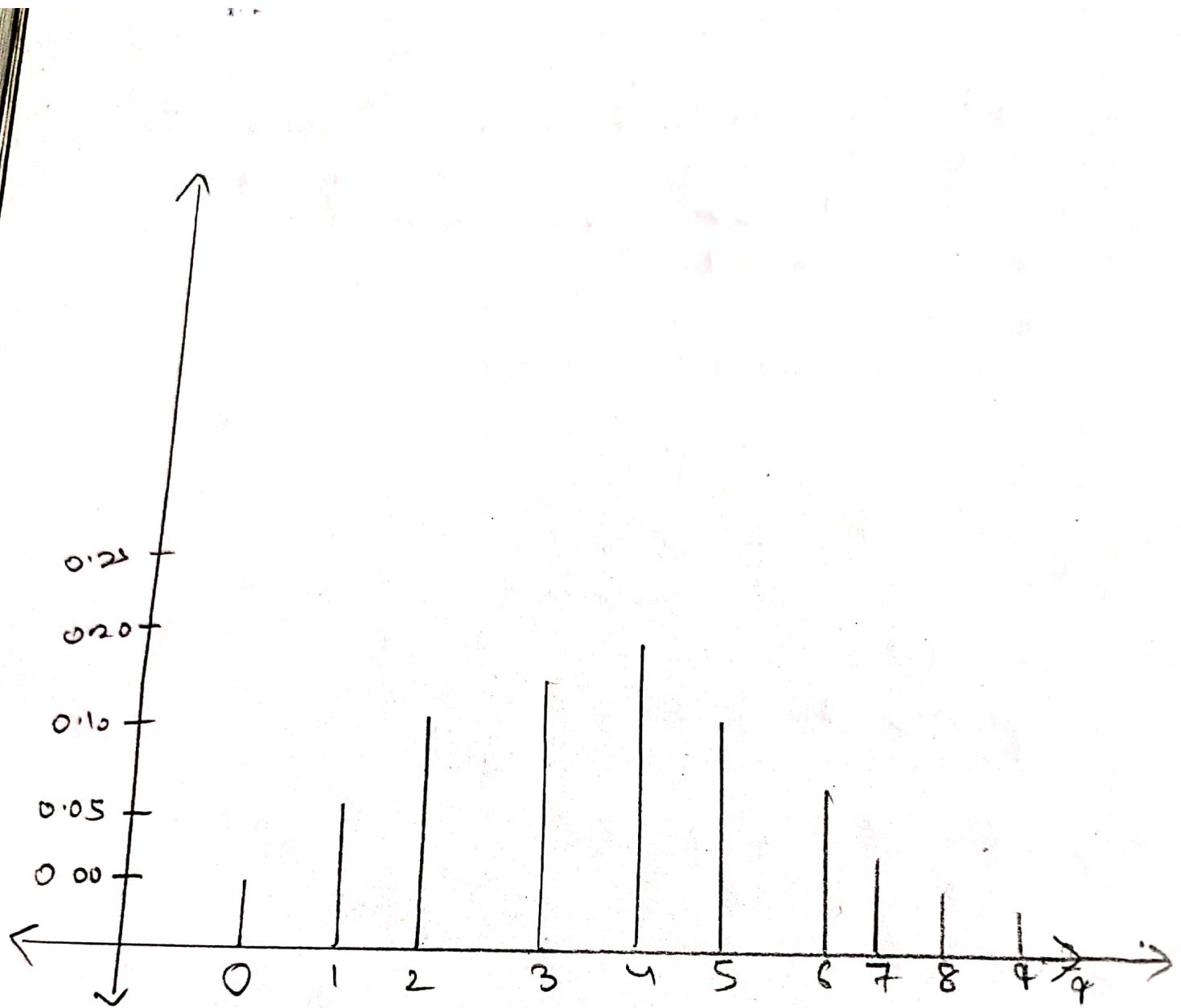
$$\rightarrow x = c(1, 2, 3, 4, 5, 6)$$

$$> prob = c(0.1, 0.1, 0.2, 0.2, 0.1, 0.2, 0.1)$$

$$> cumsum(prob)$$

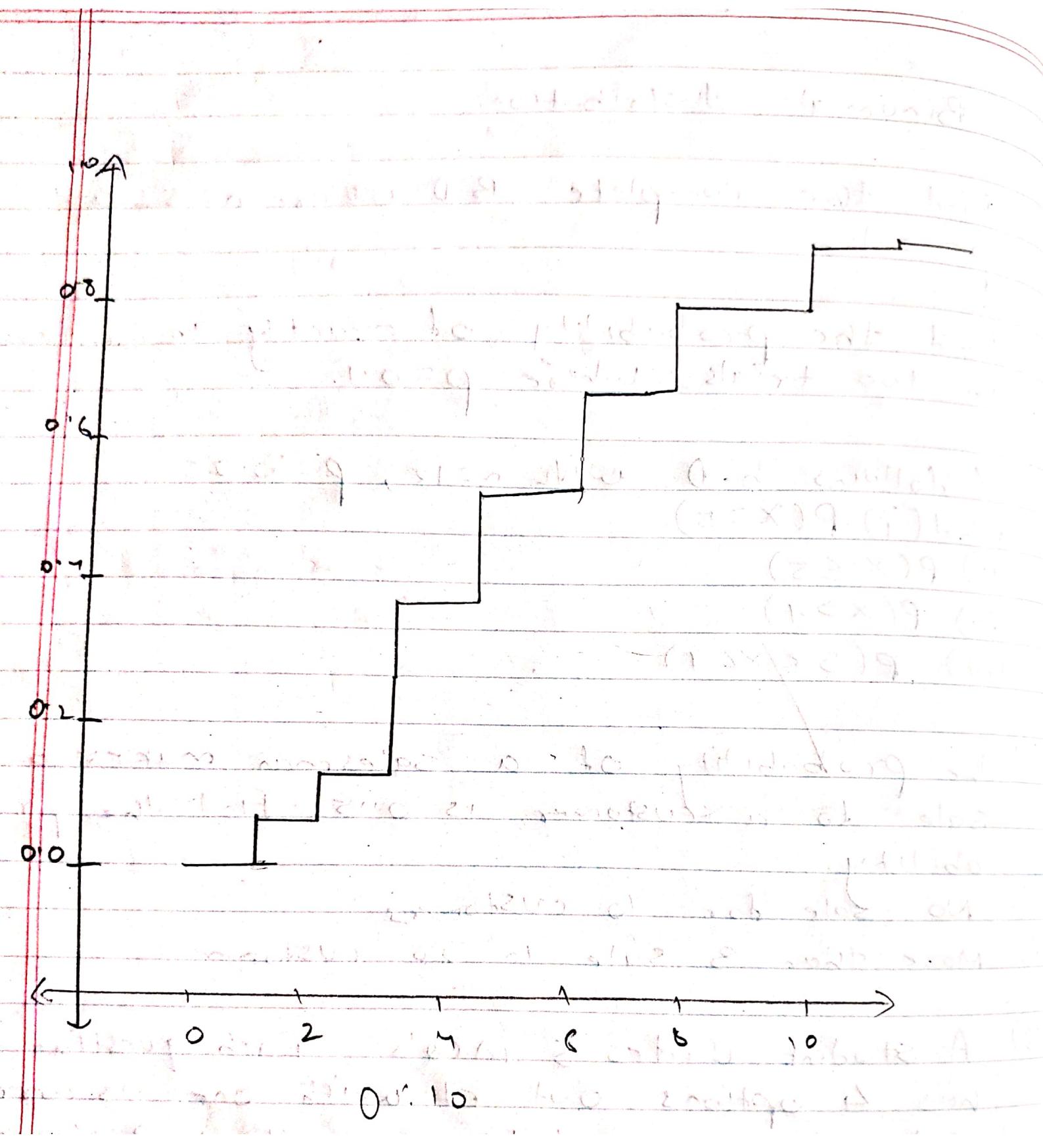
$$[1] 0.1 0.2 0.4 0.6 0.7 0.9 1.0$$

> plot(x, cumsum(prob), xlab = "values",
ylab = "probability", main = "graph of C.d.f")



Binomial distribution.

- 1) Find the complete B.D where $n=5$ and $p=0.1$.
- 2) Find the probability of exactly 10 success in 100 trials where $p=0.1$.
- 3) X follows b.D with $n=12$, $p=0.25$
 Find (i) $P(X=5)$
 (ii) $P(X \leq 5)$
 (iii) $P(X > 7)$
 (iv) $P(5 < X < 7)$
- 4) The probability of a salesman makes a sale to a customer is 0.15. Find the probability.
 (i) No sale for 10 customers.
 (ii) More than 3 sale in 20 customer.
- 5) A student writes 5 MCQ's. Each question has 4 options out of which one is correct. Calculate the probability for atleast 3 correct answers.
- 6) X follows B.D $n=10$, $p=0.4$. Plot the graph of P.M.F and C.D.F.



$$P(X=x) = d\text{binom}(x, n, p)$$

$$P(X \leq x) = P\text{binom}(x, n, p)$$

$$P(X \geq x) = P\text{binom}(x, n, p)$$

find the value of x for which the prob

is given as p , the command is

$$\text{binom}(p, n, p).$$

$$n=5, p=0.1.$$

$$(i) d\text{binom}(0:5, 5, 0.1). \\ 0.59049 \quad 0.32805 \quad 0.07290 \quad 0.00810 \quad 0.00045 \quad 0.00001$$

$$) n=100, p=0.1, x \geq 10.$$

$$d\text{binom}(10, 100, 0.1)$$

$$\rightarrow 0.138653.$$

$$) n=12, p=0.25, x \geq 5.$$

$$(i) d\text{binom}(5, 12, 0.1)$$

$$\rightarrow 0.1032414.$$

$$(ii) P(X \leq 5)$$

$$d\text{binom}(0:5, 12, 0.1)$$

$$(iii) P(X > 7)$$

$$1 - P\text{binom}(7, 12, 0.25)$$

$$) n=10, p=0.15, x \leq 0.$$

$$(i) P\text{binom}(0, 10, 0.15).$$

$$\rightarrow 0.1968744.$$

$$(ii) n=20, p=0.15 (x \geq 3)$$

$$1 - P\text{binom}(x \leq 3) = 1 - P\text{binom}(3, 20, 0.15)$$

$$\rightarrow 0.3522748.$$

$$5) P(X \geq 3)$$

$$= 1 - P(X \leq 2)$$

$$\approx 1 - P\text{binom}(2, 5, 1/4)$$

$$= 0.1035156.$$

$$6) n=10, p=0.4.$$

$$X \sim \text{Bin}(n, p).$$

prob = dbinom(X, n, p).

cumprob = pbisnom(X, n, p).

d = data.frame("x values" = X, "probability" = prob, print(d).

plot(X, prob, "b").

plot(X, cumprob, "s").

\rightarrow X-values probability.

2	0.0256
3	0.1024
4	0.2048
5	0.2304
6	0.192
7	0.1024
8	0.0256
9	0.0064
10	0.0016
11	0.0004

Practical - 5 :

- 1) $P[X=x] = dnorm(x, \mu, \sigma)$
- 2) $P[X \leq x] = pnorm(x, \mu, \sigma)$
- 3) $P[X > x] = 1 - pnorm(x, \mu, \sigma)$
- 4) $P(X_1 < x_1 < x_2) = pnorm(x_2, \mu, \sigma) - pnorm(x_1, \mu, \sigma)$
- 5) $P[X \leq x] = P_i ; qnorm(P_i, \mu, \sigma)$
- 6) $rnorm(n, \mu, \sigma)$

To find value of x so that

$$P[X \leq x] = P_i ; qnorm(P_i, \mu, \sigma)$$

i) $X \sim N(\mu=50, \sigma^2=100)$

i) $P(X \leq 40)$

ii) $P(X > 55)$

iii) $P(42 \leq X \leq 60)$

iv) $P(X \leq 10, X \geq 60)$

Generate 10 random nos from a normal distrib. with mean $\mu=60$, $S.D=5$. Also calculate the Sample mean, median, variance and

Draw the graph of Standard normal distribution

$$\text{3) } \begin{array}{cccc} 60.76603 & 60.02772 & 59.49480 & 52.13985 \\ 62.58680 & 63.70532 & 60.48170 & 58.03257 \end{array}$$

$$\text{mean}(x) = 59.50901$$

$$v = (n-1) \times \text{var}(x)/\alpha$$

$$v = 9.301891$$

$$\text{sd} = \sqrt{v} \\ = 3.0499$$

$$\text{J) } a = \text{pnorm}(40, 50, 10)$$

cat ("p(x ≤ 40) is = ", a)

$$0.1586553$$

$$p(x < 40) \text{ is } 0.158655$$

$$\text{i) } b = 1 - \text{pnorm}(55, 50, 10)$$

~~$$\text{cat("p(x > 55) is = ", b)}$$~~

~~$$p(x > 55) \text{ is } 0.03085375$$~~

$$0.3085375$$

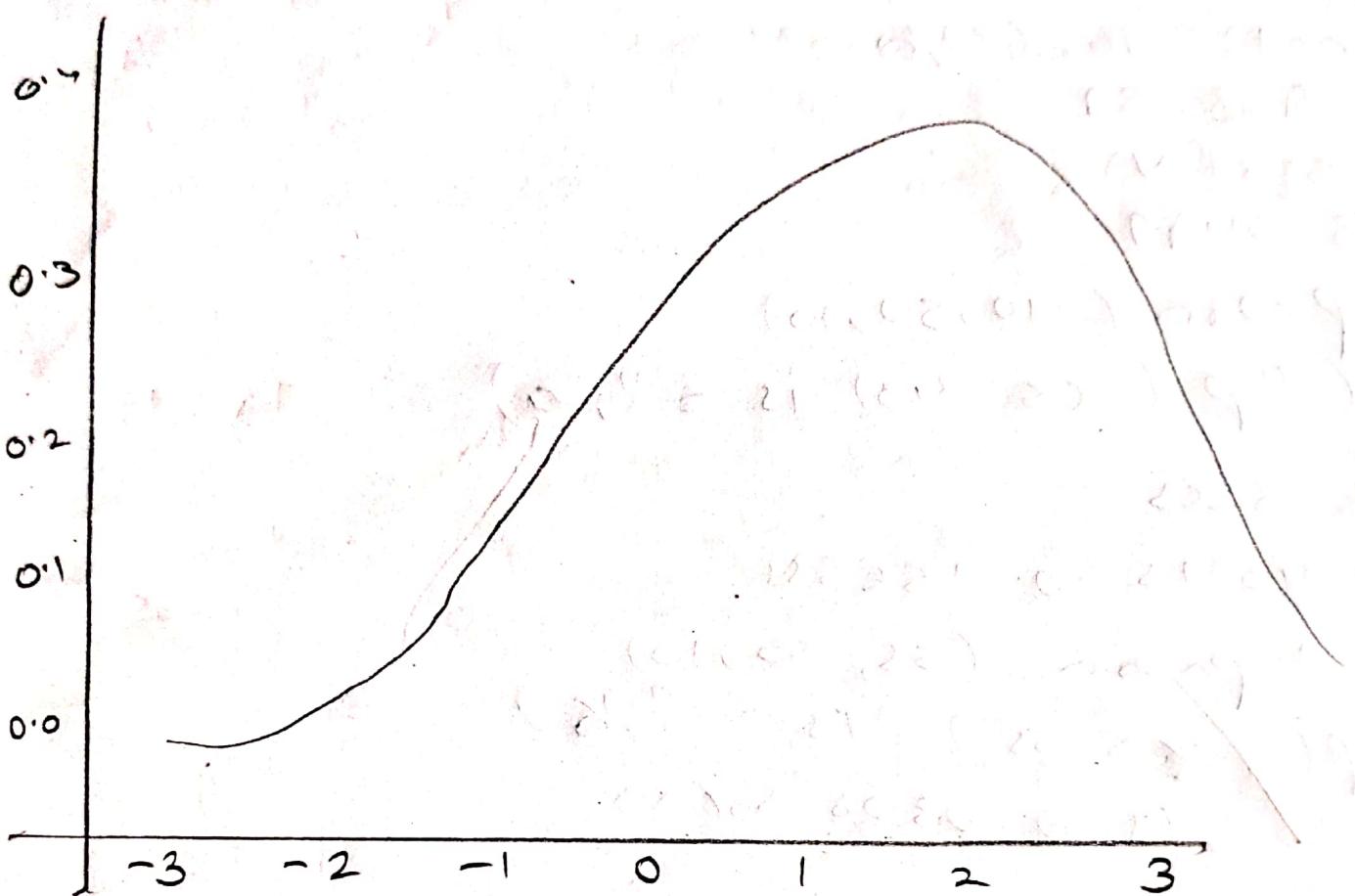
$$\text{iii) } (= \text{pnorm}(60, 50, 10) - \text{pnorm}(42, 50, 10))$$

$$0.6274893$$

$$\text{2) } a = \text{pnorm}(110, 100, 6)$$

$$0.9522076$$

$$b = \text{pnorm}(95, 100, 6)$$



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x = seq(-3, 3, by = 0.1)

> x

y = dnorm(x)

y = dnorm(x) /

> plot(x, y, sub = "evals", sub = "prob",
main = "standard normal graph")

Practical - 6.

Test the hypothesis (H_0) $H_0: \mu = 10$ against $H_1: \mu \neq 10$.
 A sample of size 400 is selected which gives the mean 10.2 and standard deviation 2.25. Test the hypothesis at 5% level of significance.

$H_0: \mu = 10$ against $H_1: \mu \neq 10$.

10.2 2.25 S.Y.

$\mu_0 = 10$; $\bar{m}_x = 10.2$, $S_d = 2.25$; $n = 400$.

$Z_{cal} = (\bar{m}_x - \mu_0) / (S_d / (\sqrt{n})) = 1.777$
 cat (Z_{cal} is ≈ 1.777 , 2(a1))

pvalue = $2^{-|Z|} (1 - \text{pnorm}(\text{abs}(Z_{cal})))$

pvalue = 0.0754

Test the hypothesis $H_0: \mu = 75$ against $H_1: \mu \neq 75$.

A Sample of size 100 is selected and the sample mean is 80 with a S.D of 3. Test the hypothesis at 5% level of significance.
 $H_1: \mu \neq 75$ against $H_1: \mu \neq 75$.

$\mu_0 = 75$ $\bar{m}_x = 80$.

$S_d = 2.25$

$n = 100$

Test the hypothesis $H_0: \mu = 25$ against $H_1: \mu \neq 25$ at 5% level of significance. Full Sample of 30 is selected

20, 24, 24, 35, 30, 46, 26, 27, 10, 20, 30, 37,
 35, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30,
 31, 27, 15, 19, 22, 20, 18.

mean (\bar{x}).
 $n = \text{length}(x)$.

$$\text{variance} = (n-1) \cdot \text{var}(x)/n.$$

variance.

$$5.2622.$$

$$Sd = \sqrt{\text{variance}}$$

7.0895

5) Experience has proved that 20% students
 of a college smokes out of a sample of
 400 students reveal that out of 400 only
 50 smoke. Test the hypothesis that the
 experience gives the correct proportion or
 not.

Test the hypothesis $H_0: p = 0.1$ against $H_1: p \neq 0.1$.
A sample of 200 is selected and the sample proportion is calculated. Test the hypothesis
by significance.

$$P = 0.1$$
$$\rho = 0.50$$
$$Q = 1 - P$$
$$Z_{\text{cal}} = (p - P) / (\text{sqrt}(P \cdot Q / n))$$
$$= 2.4$$

P-value $= 2 * (1 - \text{prob}(Z > |Z_{\text{cal}}|))$.

$$\text{pvalue} = 0.0163$$

Practical-7
Large sample tests

A study calculated noise level in 2 hospital's noise level into hypothesis that the not

	Hos. A	Hos. B
No. of Sample obs.	84	34
mean is	61	59
S.D	7	8

H_0 : The noise levels are same

$$n_1 = 84$$

$$n_2 = 34$$

$$m_x = 61$$

$$m_y = 59$$

$$Sdx = 7$$

$$Sdy = 8$$

$$Z = (m_x - m_y) / \sqrt{(Sdx^2/n_1) + (Sdy^2/n_2)}$$

cat("Z calculated is ", z)

$$pvalue = 2 * (1 - pnorm(abs(z)))$$

Since value < 0.05 we reject H_0 at 5% level of significance

$$z = 1.273$$

$$pvalue = 0.1291361$$

2) 2 random samples of size 1000 and 2000 are drawn from 2 populations with mean of 67.5 and 68 respectively and with the same S.D of 2.5. Test the hypothesis that the mean of 2 populations are equal.

H_0 is the same.

	A	B		A	B
No. of obs	1000	2000	No. of obs	1000	2000
mean	67.5	68	mean	67.5	68
S.D.	2.5	2.5	S.D.	2.5	2.5

$$n_1 = 1000$$

$$n_2 = 2000$$

$$m_x = 67.5$$

$$m_y = 68$$

$$sdx = 2.5$$

$$sdy = 2.5$$

$$z = \frac{(m_x - m_y)}{\sqrt{(\frac{sdx^2}{n_1} + \frac{sdy^2}{n_2})}}$$

$$= -5.163$$

$$p\text{-value} = 2 * (1 - \text{norm.cdf}(z))$$

$$= 2 * 4.14564e-07$$

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In FYBSC 20% of a random sample of 400 students had defective eyesight, the SYBSC class had 15.5%. Of 500 sample had the same defect, is the difference of proportion is same?

H_0 the proportion of the population are equal.

$$n_1 = 400$$

$$n_2 = 500$$

$$p_1 = 0.2$$

$$p_2 = 0.155$$

$$p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$= 0.175$$

$$q = 1 - p$$

$$= 0.825$$

$$z = (p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$$

$$z = 1.76547$$

Cut ("z calculated is", z)

$$p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z)))$$

$$= 0.07748$$

Q8

From each of the box of the apples, a sample size of 200 is collected. It is found that there are 44 bad apples in the first sample and 30 bad, 2nd sample. The 2 boxes are equivalent in terms of no. of bad apples.

H₀ is that 2 boxes are equivalent

$$n_1 = 200$$

$$n_2 = 200$$

$$p_1 = 44/200$$

$$p_2 = 30/200$$

$$p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$q = 1 - p$$

$$p = 0.185$$

$$q = 0.815$$

$$Z = (p_1 - p_2) / \text{sqrt}(p * q * (1/n_1 + 1/n_2))$$

$$Z = 2.54946$$

$$\text{Pvalue} = 2 * (1 - \text{norm.pdf}(Z))$$

$$\approx 0.0104$$

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Q) In MA class out of the sample of 60 mean height is 63.5 inch, with a SD of 2.5. In an M.COM class of 50 students, mean height of 69.5 inches with a SD of 2.5, test the hypothesis that the mean of MA and M.COM class are same.

The mean height of MA and M.COM are equal
~~H₀ is - the two classes are equivalent.~~

$$n_1 = 60$$

$$n_2 = 50$$

$$p_1 = 0.041$$

$$p_2 = 0.05$$

$$p = \frac{(n_1 * p_1 + n_2 * p_2)}{n_1 + n_2}$$
$$\approx 0.04509$$

$$q = 1 - p$$

$$\approx 0.954$$

$$z = \frac{(p_1 - p_2)}{\sqrt{p_1 q_1 (1/n_1 + 1/n_2)}}$$

$$z = -0.22650$$

Practical - 8

Small sample test

The tens are selected and height are found to be 63, 63, 68, 69, 71, 71, 72 cms. Test hypothesis that mean height are 66 cms or not at 1.

$$H_0: \text{Mean} = 66 \text{ cms.}$$

$$\geq \text{mean} = 66$$

$$\geq x = (63, 63, 68, 69, 71, 71, 72)$$

t-test (x)

One sample test t-test:

data: x

$$t = 47.94, df = 6, P\text{value} = 5.22 \times 10^{-9}$$

alternative hypothesis: mean is not equal to 95 percent confidence interval

$$64.86479 \quad 71.62092$$

Sample estimates

mean of x

$$68.14286$$

P-value < 0.01 is rejected on in 1% level of significance.

Two random sample was drawn from 2 different population

Sample 1 = 8, 10, 12, 11, 16, 15, 8, 7

Sample 2 = 20, 15, 18, 9, 8, 10, 11, 12.

Let the hypothesis that there is no difference between the hypothesis that there is no difference in 2 mean at s.r. level of significance.

H_0 : there is no difference in the population mean

$x = c(8, 10, 12, 11, 16, 15, 8, 7)$

$y = c(20, 15, 18, 9, 8, 10, 11, 12)$

t-test(x, y)

With 2 sample t-test

data: x and y

$t = -0.36247$, $df = 13$, $p\text{-value} = 0.7225$

alternative hypothesis: true difference in mean is not equal to 5. $\sqrt{9.2718} = 3.692718$

Sample estimates:

mean of x and mean of y

12.125

12.875

$p\text{-value}$ 20.01 is accepted in 1% on 12. level of significance

3) Following are the weight of 10 people.

Before = (100, 125, 95, 96, 98, 102, 118, 104, 107, 110)

After = (95, 80, 95, 98, 90, 100, 110, 85, 100, 105)

H₀: The diet program is not affective.

$x = (100, 125, 95, 96, 98, 102, 115, 104, 107, 110)$

$y = (95, 80, 95, 98, 90, 100, 110, 85, 100, 105)$

t-test(x, y, paired = TRUE, alternative = "Tc")

Paired t-test

data x and y.

t = 2.3215, df = 9, p-value = 0.9773

alternative hypothesis : true difference in means is less than 0.95 percent confidence interval.

-Int 17.89635

Sample estimates

mean of the differences

10.

pvalue < 0.01 is accepted in H₀ on 1% level of significance.

R / n²

Q) Marks before and after a training program is given below.

before = 20, 25, 32, 28, 27, 36, 35, 25

after = 30, 35, 32, 37, 37, 40, 40, 23

Test the hypothesis that training program is effective or not.

H₀: The training program is not effective.

$X = \{20, 25, 32, 28, 27, 36, 35, 25\}$

$Y = \{30, 35, 32, 37, 37, 40, 40, 23\}$

t-test (X, Y , paired = T, alternative = "greater", paired t test).

data X and Y .

$t = -3.858$, $Df = 7$, p-value = 0.9842

alternative hypothesis true difference it means is greater than 0.95 percent confidence interval

-8.96 ± 3.99

Sample estimate

mean of the difference

-5.75

p-value < 0.01 is accepted in H₀ and H₁.

S) 2 random sample were drawn from 2 normal population and the value are

A = 66, 67, 75, 76, 82, 84, 88, 90, 92

B = 64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97

Test whether the population have same variance at 5% level of significance

Q3

H₀: variances of the population are equal

$$x = (66, 67, 73, 76, 82, 84, 88, 90, 92)$$

$$y = (64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97)$$

Var test(x, y)

Test to compare 2 variances.

data: x and y.

F = 0.70686, num df = 8, denom df = 6

p-value = 0.6359 95% confidence interval

0.1833662 3.0360393

Sample estimates

ratio of variances

0.7088567

6. H₀: population mean = ss

n = 100

$\bar{x} = ss$

$s^2 = ss$

$s = \sqrt{ss}$

$$z(\alpha) = (\bar{x} - \mu_0) / (s / \sqrt{n})$$

PValue = 2 * (1 - pnorm(z(0.05)))

PValue

= 1.8213e-05

Practical 9

Chi square:

Q) Use the foll data to test whether the cleanliness of the home depends upon the child or not.

Condition of home

	Clean	Dirty
Clean	70	50
fairly clean	80	20
dirty	35	45

$$X = \{70, 80, 35, 50, 20, 45\}$$

$$m = 3$$

$$n = 2$$

$$Y = \text{matrix}(X, nrow=m, ncol=n)$$

$$Y = \text{chisq}(\text{frest}(Y))$$

Since p-value is less than 0.05 we accept H_0 at 5% level of significance

$$\chi^2 = 25.648, df = 2, p\text{-value} = 2.698$$

Table below shows the relation between maths and computer of CIS students

	Maths		
	HG	MG	LG
HG	56	51	12
MG	47	163	38
LG	14	42	85

H_0 : Performance between maths and computer are independent

$$m = 3$$

$$n = 3$$

$y = \text{matrix}(x, \text{row} = m, \text{col} = n)$

$PV = \text{chi}^2 \text{sq. test}(y)$

$\chi^2 \text{-squared} = 145.75, df = 4, P\text{-value} < 2.2e-11$

3) Perform ANOVA for the following data

Variables	Observations
A	50, 52
B	53, 55, 53
C	60, 58, 57, 51
D	52, 54, 54, 55

H₀: The means of variety ABCD are equal

$$x_1 = c(50, 52)$$

$$x_2 = c(53, 55, 53)$$

$$x_3 = c(60, 58, 57, 51)$$

$$x_4 = c(52, 54, 54, 55)$$

de stack (list (b₁ = x₁, b₂ = x₂, b₃ = x₃, b₄ = x₄))
names(d)

One way test (values = indep, data = d, var. equal = T)
One-way analysis of means

data: values and ind

F = 11.735, num df = 3, denom df = 1, p-value = 0.003

anova = oov (values ~ ind, data = d)

anova:

Call:

oov (formula = values ~ ind, data = d)

Terms:

ind Residuals

1.8

Sum of squares 71.06410 18.16667
 Degr. of freedom 3 9

Residual standard error: 1.420746

Estimated effects may be unbalanced

> summary (anova)

	Df	Sum Sq	mean Sq	F value	Pr(>F)
Ind	3	71.06	23.6873	11.73	0.00183 **
Residuals	9	18.17	2.019		

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ''

4) Perform anova on the following table.

Types observations

A 6, 7, 8

B 4, 6, 5

C 8, 6, 10

D 6, 7, 9

a = c(6, 7, 8)

b = c(4, 6, 5)

c = c(8, 6, 10)

d = c(6, 7, 9)

d = stack (list (b1=a, b2=b, b3=c, b4=d))
 names(d)

oneway. test (values ~ ind, data = d, var - equal = T)

One-way analysis of means

data: values and ind

F = 2.6667, num-df = 3, denom df = 8, p-value = 0.1187

anova = aov (values ~ ind, data = d)

anova

call:

aov (formula = values ~ ind, data = d)

aova

Call: aov (formula = values ~ ind, data = d)

Terms:

	ind	Residuals
Sum of squares	1.8	1.8
Deg of freedom	3	8

Residual standard error : 1.5

Estimated effects may be unbalanced

7 summary (anova)

Df	Sum Sq	Mean Sq	F value	Pr(>F)
ind	3	1.8	6.00	2.667 0.119
Residuals	8	1.8	2.25	

2

Practical - 10

Aim: Non parametric test

following are the amounts of sulphur oxide emitted by a factory.

70, 50, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, 15, 23, 24, 26.

Apply sign test to test the hypothesis that the population median is 21.5. Against the alternative it is less than 21.5.

$$H_0: \text{Population median} = 21.5$$

$$H_1: \text{It is less than } 21.5$$

$$n = c(15, 17, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, 15, 23, 24, 26)$$

$$m = 21.5$$

$$sp = \text{length}(x \in \{x > m\})$$

$$sn = \text{length}(x \in \{x < m\})$$

$$\eta = sp + sn$$

$$[1] 20$$

$$pv = \text{pbinom}(sp, n, 0.5)$$

$$pv$$

$$= 0.4119015$$

If the alternative is greater than median

$$pv = \text{pbinom}(sn, n, 0.5)$$

for the observation 12, 17, 31, 28, 43, 40, 55, 49, 70, 63. Apply sign test to test population median is 25 against the alternative is more than 25.

$$x = c(12, 17, 31, 28, 43, 40, 55, 49, 70, 63)$$

$$m = 25$$

$$sp = \text{length}(x[x > m])$$

$$sn = \text{length}(x[x < m])$$

$$n = sp + sn$$

$$n = 10$$

$$pv = \text{pbinom}(sn, n, 0.5)$$

$$pv$$

$$[1] 0.0546575$$

For the foll data, 60, 65, 63, 87, 61, 71, 58, 51, 48, 66, Test the hypothesis using Wilcoxon Sign rank test. For testing the hypothesis that the median is 60 against the alternative it is greater than 60.

H_0 is 60

H_1 is greater than 60

$$x = c(60, 65, 63, 87, 61, 71, 58, 51, 48, 66)$$

wilcox.test(x, alter="greater", mu=60).

$$N = 28$$

$$\text{P-value} = 0.2386$$

If the alternative is less $\&$ alter="less", mu=—).

If the alternative is not equal to μ_0

wilcox.test(x, "2.sided")

- Q4) Using Wilcox. test , test the hypothesis , the median is 12 against the alternative (less than 12)
12, 13, 10, 20, 15, 5, 1, 7, 6, 11, 9, 20
 $V = 25$
 $p\text{-value} = 0.2521$