

No

Date

$$1. P(n) = 2 + 4 + 6 + \dots + 2n = n(n+1)$$

$$\bullet n = 1$$

$$P(1) = 2 + 4 + 6 + \dots + 2n = 1(1+1)$$

$$2(1) = 1(2)$$

$$2 = 2 \quad \checkmark$$

$$\bullet P(n+1)$$

$$P(n) = 2 + 4 + 6 + \dots + 2n = n(n+1)$$

$$P(n+1) = 2 + 4 + 6 + \dots + 2n + 2(n+1) = (n+1)((n+1)+1)$$

$$n(n+1) + 2(n+1) = (n+1)((n+1)+1)$$

$$n^2 + n + 2(n+1) = n+1(n+2)$$

$$n^2 + 3n + 2 = n^2 + 3n + 2 \quad \checkmark$$

$$2. P(n) = 1 + 4 + 9 + \dots + n^2 = \frac{1}{6} n(n+1)(2n+1)$$

$$\cdot n = 1$$

$$P(1) = 1 + 4 + 9 + \dots + n^2 = \frac{1}{6} 1(1+1)(2(1)+1)$$

$$1^2 = \frac{1}{6} 1(2)(3)$$

$$1 = 1 \checkmark$$

$$\cdot P(n+1)$$

$$P(n) = 1 + 4 + 9 + \dots + n^2 = \frac{1}{6} n(n+1)(2n+1)$$

$$P(n+1) = 1 + 4 + 9 + \dots + n^2 + (n+1)^2 = \frac{1}{6} (n+1)((n+1)+1)(2(n+1)+1)$$

$$= \frac{1}{6} n(n+1)(2n+1) + (n+1)^2 = \frac{1}{6} (n+1)(n+2)(2n+3)$$

$$(n+1) \left(\frac{1}{6} n(2n+1) + n+1 \right) = \frac{1}{6} (n+1)(n+2)(2n+3)$$

$$(n+1) \left(\frac{2}{6} n^2 + \frac{1}{6} n + n + 1 \right) = \frac{1}{6} (n+1)(n+2)(2n+3)$$

$$(n+1) \left(\frac{2}{6} n^2 + \frac{7}{6} n + 1 \right) = \frac{1}{6} (n+1)(n+2)(2n+3)$$

$$(n+1) \frac{1}{6} (2n^2 + 7n + 6) = \frac{1}{6} (n+1)(n+2)(2n+3)$$

$$\frac{1}{6} (n+1)(n+2)(2n+3) = \frac{1}{6} (n+1)(n+2)(2n+3) \checkmark$$

$$3. P(n) = 2 + 6 + 12 + \dots + n(n+1) = \frac{1}{3} n(n+1)(n+2)$$

$$\cdot n = 1$$

$$P(1) = 2 + 6 + 12 + \dots + n(n+1) = \frac{1}{3} 1(1+1)(1+2)$$

$$2 = \frac{1}{3} 1(2)(3)$$

$$2 = 2 \checkmark$$

$$\cdot P(n+1)$$

$$P(n) = 2 + 6 + 12 + \dots + n(n+1) = \frac{1}{3} n(n+1)(n+2)$$

$$P(n+1) = 2 + 6 + 12 + \dots + n(n+1) + (n+1)(n+2) = \frac{1}{3} (n+1)(n+2)(n+3)$$

$$\frac{1}{3} n(n+1)(n+2) + (n+1)(n+2) = \frac{1}{3} (n+1)(n+2)(n+3)$$

$$n(n+1)(n+2) + 3(n+1)(n+2) = (n+1)(n+2)(n+3)$$

$$(n^3 + n^2 + 2n^2 + 2n + n^2) + (3n^2 + 6n + 3n + 6) = (n^3 + 6n^2 + 11n + 6)(n+3)$$

$$(n^3 + 2n^2 + 2n + n^2) + (3n^2 + 6n + 3n + 6) = n^3 + 6n^2 + 11n + 6$$

$$n^3 + 6n^2 + 11n + 6 = n^3 + 6n^2 + 11n + 6 \checkmark$$