The pollination trade-off

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Changes

- Use AICc instead of AIC (no change in results)
- To keep signature of phenology, absolute flower counts (log-transformed) are used instead of relative abundances 10
- Columns in the trait matrix for phenology are scaled so that it doesn't count 5 times as much as other 11 traits 12
 - Boostraping resampling worked

To do

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- References to the introduction 15
- Discussion from bullet-points to actual paragraphs. I will do that once we all agree with the quantitative 16 methodology and getting some contributions for the interpretation of the results 17
- Spell-check everything 18
 - Write the abstract

Questions

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- Feel free to come back here after you've read the manuscript. Thanks!
- Originality: Currently the plants phenology are included in the traits. The relative abundance of the 22 plant in each of the five a survey months is included as a trait. This allows to maintain the model 23 simple and it could be easily argued that phenological strategy can be considered as another trait. 24 However I'm not convinced that it is a good idea to keep them together, especially because differences 25 in phenology is a rather intuitive factor/strategy to overcome competition for pollination. Do you think I should separate traits from phenology? If yes, should I use the same "originality" approach to 27 determine how different each species is?
 - Traits: Currently I don't mention much traits in the discussion. I think the trait component is valuable and interesting but sadly at the moment the data quality is poor. Only 4 traits have been compiled: growth form, longevity, flower colour, and whether the plant is native to the region. It won't be possible to gather all of the traits used by Coux et al. (2016) from the literature but hopefully it is for a good proportion of them. Daniel and Jason, could we discuss options here?
 - Conspecific pollen: Previously I used, as Hugo did in his papers, the gain in conspecific pollen in

- open flowers relative to the amount of in bagged flowers as the indication of the "quantity" of the
 pollination service. After thinking more about the limitations of this metric (pollinators also take pollen
 from stigmas, some plants are not self-fertile, different maturation times for male/female organs, etc.) I
 decided it would be best to include both the total and the relative pollen amounts in the manuscript.
 This add more nuance to the story and interpretation which is not cool, but I think together they
 overcome each other's problems. What do you think about it?
- Naming: I currently use absolute and relative pollen gain as names for the two previous metrics. I think it's OK but I feel there might be better options. Any ideas?
- Quantity & quality: This version of the paper uses quantity/quality to frame the results. I think
 that's pretty neat. However, different studies define quantity and quality in different ways. Hugo for
 example used the relative amount of conspecific pollen as an indication of quantity and the amount of
 heterospecific pollen for quality. We discussed earlier that a good indication could be the proportion
 of heterospecific pollen instead. What do you think? Should I ditch quantity/quality and stick to
 conspecific/heterospecific pollen instead? Should I stay with the current definitions of quantity and
 quality of pollination? This probably needs meeting/Skype, but it would be good to think about it.
- Pollen transfer: Currently all I'm using from the pollen transfer networks is the share of a plant in
 the pollen pool. That fits nice with the density hypothesis but its rather simplistic. Any ideas?
- Pollen in bagged flowers: Jason, you mentioned that pollen in bagged flowers can be due to selfing or wind. You meant wind moving flowers and that causing pollen to be deposited on stigmas? Wouldn't that count as selfing too?

55 Introduction

Pollination systems play a disproportionally important role in food production and maintenance of global biodiversity. In the context of animal pollination, the support to biodiversity is fundamentally achieved by virtue of intra-species facilitation—the positive feedback loops that exist between plants that share pollinators or pollinators that share plants. Facilitation is able to promote species coexistence because it offsets the effects of direct competition for resources. Indeed, studies that are fundamental to our current knowledge of mutualism predict that an upper limit to biodiversity is achieved when the number of mutualistic partners is maximised in a community. And yet, fully connected natural pollination communities do not exist.

This is so, because sharing a mutualistic partner also has costs. The end result is that, when the cumulative costs have a negative impact on fitness, species also start competing for mutualistic partners. The possible negative effects of competition for pollinators have been long recognised and widely documented. Based mainly on two-species systems, it is currently clear that they have the potential to drive the evolution of flower phenologies, morphologies and reproductive strategies as well as driving ecological differentiation. However, these competitive interactions between species pairs do not occur in isolation. Plants often occur in communities in which multiple competitive interactions operate simultaneously and lead to emergent phenomena not observed at smaller scales.

Perhaps the most obvious ecological factor influencing the cost of sharing pollinators is the species degree—the number of interaction partners. Yet, evidence at the community scale of the mutualistic trade-off—the extent to which species degree affects the benefit—is scarce, to say the least. Furthermore, although the relationship between degree and the costs of the pollination service is relatively intuitive, elucidating the 74 magnitude of the trade-off at the community scale has been elusive because multiple other factors like traits, abundance, and the share of the pollen pool might be involved. For instance, recent empirical evidence suggest that species with original traits (far from the community centroid) generally have fewer interaction partners. This evidence is aligned with the intuitive rationale that a species that interacts with few species benefits strongly from each of them, whereas a species that interacts with a large number of species does so comparatively weakly. If evolutionary specialisation occur by changing traits to focus on fewer but better partners, we should expect a reduction of competition for pollination in species with original traits. Alternatively, it might also be the case that density is the dominant force driving pollen transfer. Abundant species might experience a dilution of the available pollinators but might also comprise a greater component of the pollen source pool being transported by pollinators. In this case, a potential reduction in the quantity of pollination could be compensated by an increase in the quality of pollination.

Here, we explore the role that competition for pollinators plays on the quantity and quality of the pollination service and look for the signature of the mutualistic trade-off in diverse natural communities. To tease apart the multiple factors that operate at the community scale we use data that describes both the structure of the interactions and the pollen flows that occur within it, all while accounting for the traits of the species that integrate the community. Specifically, we first estimate the gain on pollen that can be attributed to the mutualistic interactions. Second, we investigate whether there is a relationship between this gain (of both conspecific and heterospecific pollen and by extension the quantity and quality of pollination) and the species degree, functional originality, abundance, and contribution to the pollen pool, which together describe the role of the plant species and the ecological context. Third, and finally, we explore how these variables shape the quantity and quality of pollination and ultimately the competition for pollinators.

96 Methods

Elucidating how the mechanisms and drivers of facilitation scales to the community level and its theoretical consequences has been elusive in part because of the large amounts of data required. Previous studies focus on the final picture of interspecific pollen transfer that is obtained by examining the pollen deposited on flower stigmas. However, as we have described, teasing apart competition for pollinators and evaluating whether there is a trade-off between the number of partners and the mutualistic benefit also requires data that describes the structure of the interactions and the pollen flows that occur within it, while accounting for the traits of the species that integrate the community. Here, we examine a comprehensive data set that includes information about pollen deposition, transfer, visitation, species abundance, and species traits across diverse communities in the Argentinian Pampas.

Data collection

We performed sampling in three locations, each located in a distinct region of the Argentinian Pampas. The sampling locations are distributed across a gradient of precipitation with a humid temperate climate in the eastward Flooding Pampas and an drier as we move inland and westward towards the Pampean Grasslands.

Across all sites, annual mean temperatures range between 14.8 and 15.8 Celsius.

In each location, we sampled two restored and two agricultural fragments. However, due to the lack of available sites in the Flooding Pampas, it was only possible to sample one restored site. We visited each fragment in November 2010 and February 2011. In each of these visits we gathered information related to

abundance, plant-pollinator visitation, pollen transfer, and pollen deposition.

Abundance was estimated using two 50 m randomly located transects in each fragment. In a first sampling 115 we counted all units of floral attraction that were found in a 2 m wide strip. In a second sampling we counted and collected all floral visitors while walking at a pace of 10 m per minute (Memmott 1999; Marrero et al. 117 2014). We constructed quantitative visitation networks using information about the floral visitors collected during abundance transects (Marrero et al. 2014). In addition, we also constructed qualitative visitation 119 networks during independent two hour observations of floral visits across each fragment. We estimated pollen transfer by examining the pollen loads present on the collected floral visitors (Marrero et al. 2017). Where 121 the pollen count on an individual was estimated to be less than 2,000 grains, we identified every grain to the species level whenever possible and to pollen complexes when it was not. When the pollen count was 123 above 2,000 grains, we classified approx. 50% of pollen and total pollen counts were extrapolated (Bosch et 124 al. 2009). If more than 10 pollen grains from a plant species were identified, we assumed that pollination 125 service between the plant and the pollinator existed. Finally, we analysed pollen deposition in a subset of the 126 plant community (Marrero et al. 2016). This subset comprised between three and nine of the most common 127 entomophilus species that were flowering during the sampling period while ensuring that the chosen species 128 covered a wide range on a specialization-generalization gradient. In the selected plants we removed all flowers except buds that were expected to go into inflorescence on the next day. A quarter of these buds were bagged 130 to prevent animal pollination. Two days after inflorescence, we analysed the pollen grains in the flowers' pistils and classified them between conspecific and heterospecific pollen. 132

More details about the study sites, data collection, and laboratory protocols can be found in Marrero *et al.* (2014, 2016, and 2017).

$_{ ext{35}}$ Data analysis

At the community scale, sharing mutualistic partners might induce competition for pollination mainly trough
two mechanisms. The first is competition for visits, where plants with more attractive flowers reduce the
number of visits for those less attractive. Competition for visits affects the quantity of the pollination service
as it induces a reduction in the amount of conspecific pollen received by flowers. The second, more subtle,
mechanism is interspecific pollen transfer, where even receiving a visit might not translate into net facilitation.
Interspecific pollen transfer affects the quality of the pollination service because a focal plant might receive
pollen from a different species, or conversely pollen from the focal plant might be lost to different species.

Generally speaking the larger the proportion of conspecific relative to heterospecific pollen the higher the

quality of the pollination service.

We explore the quantity of pollination service by examining two metrics. First, we use the absolute amount 145 of conspecific pollen (pollen counts per stigma) found on flowers open to animal pollination. Second, we use the relative amount of conspecific pollen—the difference between the absolute amount and the that from 147 flowers that were bagged. We use both metrics simultaneously because, in the one hand, the relative amount acknowledges that autogamus self-pollination can occur and hence might be a better indication of the pollen 149 that has been actually deposited by mutualistic partners. On the other, self-pollination is an adaptive trait (Kalisz & Vogler 2003) and some plants are not self-fertile, even if their pollen gets deposited on the stigma. 151 Both metrics complement each other and provide a complete picture of the quantitative aspect of pollination service. Similarly, to explore the quality of pollination we examine the relationship that exists between both 153 the absolute and relative amount of conspecific pollen and heterospecific pollen. We use the relative amount 154 of heterospecific pollen for our calculations. However, because the amount of heterospecific pollen in bagged 155 flowers was negligible, results are almost identical if we use the absolute amounts. 156

To study the amounts of deposited pollen, which are needed to construct our metrics of pollination quantity and quality, we use three sets of linear fixed models (using the R package nlme 3.1–131, Pinheiro et al. 2018)—two for conspecific pollen (absolute and relative) and one for heterospecific pollen. This modelling approach allowed us to simultaneously explore whether there is a relationship between the benefit of animal pollination and several ecological variables that can affect the mutualistic trade-off. In addition, to estimate and incorporate the uncertainty associated to our results we used a combination of multi-model inference and bootstrap resampling.

Each model set was based on the same one hundred bootstrap resamples of the deposition data. We used bootstrap resampling because, as open and bagged flowers were not paired, this allowed us to directly model the *gain* in pollen density rather than density itself. In each data replicate we randomly sampled with replacement a number of open flowers within each community-species combination and an equal number of closed flowers. We then log-transformed the pollen densities to improve normality and minimise the impact of outliers (Figure S1), this generally offered better results that a generalised linear model with poisson (or quasiposson) error structure. Finally, for the models of the relative amounts of pollen we calculated the difference between the pollen density among treatments.

As predictors in all model sets, we included species degree, the plant relative abundance, the plant species' share on the pollen pool, and the species' functional originality. Species degree was calculated from combining the quantitative and qualitative visitation networks and corresponds to the number of animal species that were

observed to visit the plant species in the community where it was sampled. The plant's relative abundance
we simply aggregated the flower counts for each plant species in the community. As with the deposition
data, we found that log-transforming the abundance counts drastically improved normality (Figure ??). The
species' share of the pollen pool was calculated as the proportion of pollen of that species in the pollen counts
being carried by pollinators from the community.

Functional originality is defined as the distance of a species from the community trait average—the centroid of 180 functional space of the community (Laliberté & Legendre 2010; Coux et al. 2016). Specifically, we recorded morphological traits that relate to plant type (herb, shrub, climber), life cycle (annual, perennial), flower 182 colouration, and whether the species is native in the study region or not. As phenology has been shown to 183 be a key mechanisms of niche differentiation among plants, we also included the plant abundance in each 184 of the survey months (November to March) as an additional trait in our analysis. This approach allowed 185 us to integrate the originality in phenological niche alongside the originality on other functional traits. All 186 traits were scaled to have a mean of zero and a standard deviation of one prior to calculating the centroid 187 of the functional space. The species-specific functional coordinates were calculated using the R package FD 188 1.0-12 (Laliberté & Legendre 2010; Laliberté et al. 2014). To facilitate comparison across model estimates. 189 we scaled all independent variables to have a mean of zero and a standard deviation of one.

In all three sets of models we first evaluated a set of candidate random effects which included random 191 intercepts for plant species as well as random slopes for the relationship between degree and pollen gain. In 192 addition we also tested for random intercepts that assumed that the plant species grouping was hierarchically nested in either their community, the land use, and the locality. We selected the best random structure by 194 comparing the median Akaike Information Criterion (AIC) of evaluated models. After determining the best random structure, we then focused on the model's fixed structure composed by our explanatory variables. We 196 used multi-model inference to calculate the relative importance of each variable and its mean effect on pollen density. First we fitted all possible combinations of explanatory variables to the same bootstrap resamples 198 used previously. This yielded one hundred models for each "candidate formula"—a particular combination of 199 explanatory variables. We then determined the likelihood of each candidate formula and its relative weight by 200 calculating the median Δ AIC of the one hundred models that constitute it. As AIC is only useful to compare 201 models with the same response variable, the ΔAIC of each candidate formula was calculated independently 202 for each bootstrap resample. Calculating the median value of each candidate formula allowed us to estimate 203 the relative importance of the explanatory variables using the standard methods of adding the median weight of the candidate models that included the variable. 205

To calculate the effect that each variable had on the gain of conspecific and heterospecific pollen we sampled

from the estimated coefficients in each candidate model proportional to the median likelihood of each set. In
other words, the estimated coefficients from more likely candidate constitute a larger share of the distribution
of coefficients. When a variable was not included in a model set we setted the estimate of its coefficient in
the model to zero. We expect some of our predictors to be correlated to each other. Estimating the models
using multiple combinations of explanatory variables also allowed us to evaluate the potential collinearity
between them. To do so we inspect how the effect of the explanatory variables changed across candidate
formulae, when one or more of them were removed in turns.

After calculating the effects of the ecological variables in heterospecific and conspecific pollen densities, we
can now evaluate their effect in the quality and quantity of pollination. For the quantity of pollination, we
simply calculated the mean value of the distribution of the effect for both the absolute and relative conspecific
pollen densities. Again, we used bootstrap resampling from the coefficient distributions to calculate the
confidence intervals of the mean. For the quality of pollination, we calculated the mean difference between a
sample of the distribution of the effects of conspecific pollen and a sample of those of heterospecific pollen
gain. Similar to the mean effects on the quantity of pollination, we used bootstrap resampling to calculate
confidence intervals of the means.estimated by the relationship that exists between the gain in conspecific
and heterospecific pollen.

23 Results

We found that, for both the model sets of conspecific and heterospecific pollen, the random structure that
was best supported by the data was the one that included plant species nested in community as the grouping
factors (Table S1). When looking at the relative amount of conspecific pollen gained, we observe that
only 41% of species in their communities observed a significant increase in conspecific pollen density when
comparing open and bagged flowers (Table S2). We also observed a positive relationship between the gain in
heterospecific pollen and both the relative and absolute gain of conspecific pollen (Figure 1). The slope of
the relationship is such that across plant species in their communities heterospecific pollen is gained slower
than the absolute amount of conspecific pollen but faster than the amount of conspecific pollen relative to

In addition, AIC scores of the candidate model sets indicated that the species' share in the pollen pool, the functional originality, and the species relative abundance were the most important variables determining the gain in both conspecific and heterospecific pollen (Figure 2). Note that relative abundance plays a more important role determining the gain in heterospecific pollen than the gain in both the absolute and relative

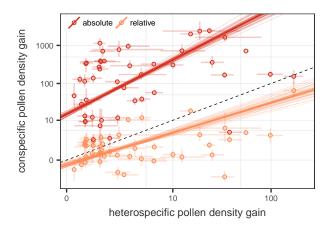


Figure 1: The interplay between the gain on heterospecific and conspecific pollen. Each dot indicates the predicted median gains for a species in its community (which correspons to the selected random effects in all of our models). The horizontal and vertical bars under each dot indicate the 0.05 bootstrap confidence intervals of the estimates. The solid lines indicate the overall relationship in each of the bootstrap replicates and were calculated by sampling the predictions from 100 conspecific/heterospecific model pairs and estimated the relationship by fitting an standardised major axis (SMA) to each pair (we used the R package smatr 3.4-3, Warton et al. 2012). The dashed line indicates the isoline at which heterospecific pollen is gained at the same rate than conspecific pollen.

amounts of conspecific pollen. Surprisingly, the species degree was comparatively less important for predicting pollen gain as it was only included in models with relatively large AICc values (Table S3).

Overall we observed that species degree and abundance had a negative relationship with the gain of both absolute and relative conspecific pollen (Figure 2). Functional originality had a weak negative relationship with the absolute gain of conspecific pollen but a small positive effect on the relative gain. The plant's share in the community pollen pool, had opposite effects, with a positive relationship with the absolute gain and a negative relationship with the relative gain of conspecific pollen. Although relative abundance, degree, and the share in the pollen pool were positively correlated (Figure S3), the effect that each of them had on conspecific pollen was relatively similar among models that included all or just some of these three explanatory variables (Figure S4).

The gain in heterospecific pollen was negatively related to the species abundance but positively to the species' share in the pollen pool, functional originality, and degree (Figure 2). Compared to the models of conspecific pollen, the collinearity in the explanatory variables had a larger impact in the models of heterospecific pollen. For instance, when the species abundance was not accounted for, both the species' share in the pollen pool and its functional originality have a negative relationship with the gain in heterospecific pollen (Figure S4).

Using the results from the models of conspecific and heterospecific pollen gain we then examined the

Using the results from the models of conspecific and heterospecific pollen gain we then examined the relationship between the explanatory variables and the quantity and quality of pollination (Figure 3). Degree,

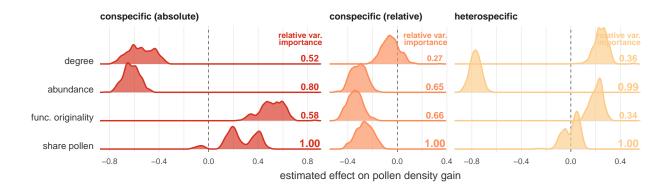


Figure 2: Distribution of effect estimates of models of conspecific (absolute and relative to the potential selfing) and heterospecific pollen density gain. Results are only shown for models that included explanatory variable. The median relative variable impotance of the four variables for each model set is shown next to each distribution. Variable importance was calculated as the sum of the median Akaike weights (Table S3) of each candidate model set that includes the variable.

mean effect on pollination service					
quantity		degree	abundance	func. originality	share pollen
	rel.	-0.014 [-0.022, -0.008]	-0.202 [-0.226, -0.176]	-0.22 [-0.247, -0.191]	-0.265 [-0.276, -0.255]
	abs.	-0.288 [-0.335, -0.247]	-0.501 [-0.545, -0.454]	0.294 [0.248, 0.343]	0.255 [0.234, 0.275]
quality	rel.	-0.102 [-0.122, -0.08]	0.563 [0.532, 0.594]	-0.288 [-0.323, -0.256]	-0.269 [-0.281, -0.257]
	abs.	-0.319 [-0.368, -0.274]	0.266 [0.219, 0.318]	0.176 [0.116, 0.225]	0.165 [0.142, 0.188]

Figure 3: Mean relative effect of ecological variables on the quantity and quality of pollination. Results are shown for values calculated with both the absolute gain in pollen density (abs.) and the gain relative to selfing (rel.). Bootstrap confidence intervals of the mean (at the 0.05 level) are shown in square brackets.

had a negative, albeit relatively small, effect on both the quantity and quality of pollination. The species relative abundance has a large positive effect to the quality of pollination accompanied by a relatively smaller negative impact on the quantity. Finally, the plant's functional originality and its share in the pollen pool have a moderate positive impact on its quantity but also a negative impact on the quality.

58 Discussion

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 We did find a trade-off between the number of partners a species interacts with and the mutualistic service. Interacting with more species alone is often accompanied by a decreases in both the quantity and quality of pollination.

- However, the effect and importance of this trade-off is comparatively small when considering other factors that describe the species niche and its ecological settings.
- We found that animal pollination only brings a small amount of extra conspecific pollen (compared selfing) if any. This relatively small difference is probably very important because, first, some plants simply aren't self-fertile, even if their pollen gets deposited on the stigma. Second, in some flowers there is temporary separation in the maturation of the sexes (dichogamy) that favours cross-pollination as, evolutionary, it has been shown to be a better strategy than cloning.
 - Overall it seems like density seems to be a dominant force behind pollen transfer. If you have many individuals of your species, you get fewer visits (dilution of the pollinators flying around), which is reflected in a smaller amount of deposited pollen. We show that abundant plants also tend to comprise a greater component of the pollen source pool and so the end result is that get more conspecific pollen per visit than heterospecific pollen.
 - Our result of the comparatively weak effect of the mutualistic trade-off is important because it is fundamentally related to the way we understand and mathematically represent mutualistic systems. Some of the most widely used theoretical models of pollination account for the negative effects of mutualism by adjusting the mutualistic benefit of an interaction so that it can be negatively affected by the number of mutualistic partners—the species degree. This approach, considerably simplifies the mathematical treatment of competition for pollinators. However we show that care must be taken because the negative effects of the mutualistic trade-off in both the quantity and quality of pollination can be offset by density mechanisms. Species with large degrees also tend be abundant and prolific pollen producers.

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