1. What is the running time of each of the code fragments? Give your answers in Big-O notation.

```
for (i = 1; i \le n; i += 2)
  k++;
for (i = 1; i <= n; i *= 2)
  k++;
for (i = n; i \ge 1; i /= 20){
  j = m;
  while (j \ge 1)
    j -= 20;
}
i = 0;
while (i < n * n * n)
  i = i + (2 * n);
```

```
int factorial(int n){
    if (n < = 1)
        return 1;
    return n * factorial(n - 1);
}</pre>
```

```
void hanoi (int n, char source, char dest, char space){
    if (n > 0){
        hanoi(n-1, source, spare, dest);
        hanoi(n-1, spare, dest, source);
    }
}
```

4. Write a recurrence equation for the following function and solve it using the repeated substitution method? Consider the $\underline{\text{WORST CASE}}$.

```
int binarySearch(int A[], int key, int low, int high){
    if (low > high)
        return -1;
    int mid = (low + high) / 2;
    if (A[mid] == key)
        return mid;
    if (A[mid] > key)
        return binarySearch(A, key, low, mid - 1);
    return binarySearch(A, key, mid + 1, high);
}
```

```
void foo(int n){
    if (n > 1){
        foo(n / 2);
        foo(n / 2);
    }
}
```

```
void bar(int n){
    if (n > 1){
        bar(n / 2);
        bar(n / 2);
        for (int i = 1; i < n; i++)
              cout << i << endl;
    }
}</pre>
```