Elec 4700

Assignment 3 – Monte Carlo/ Finite Difference Method

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Introduction:

The purpose of this experiment involved combining the Monte Carlo simulation and Finite difference method from the past two assignments and seeing what happens when there's a field pushing the electrons.

Part 1:

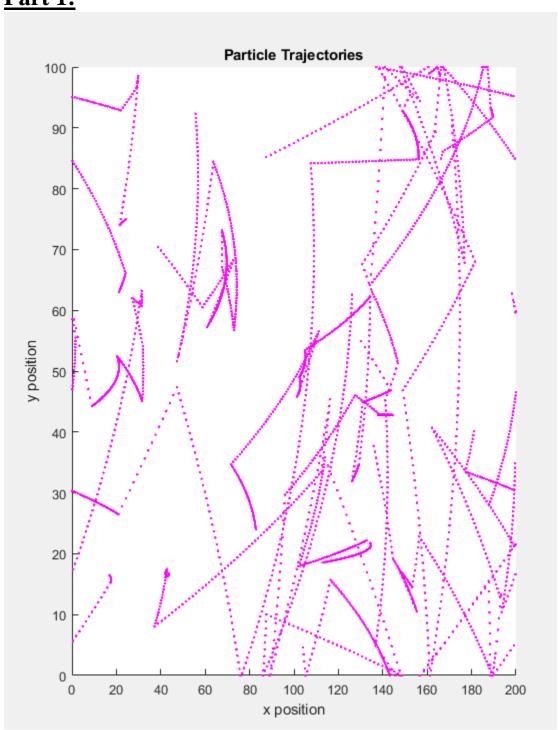


Figure 1: Particle trajectory without bottleneck

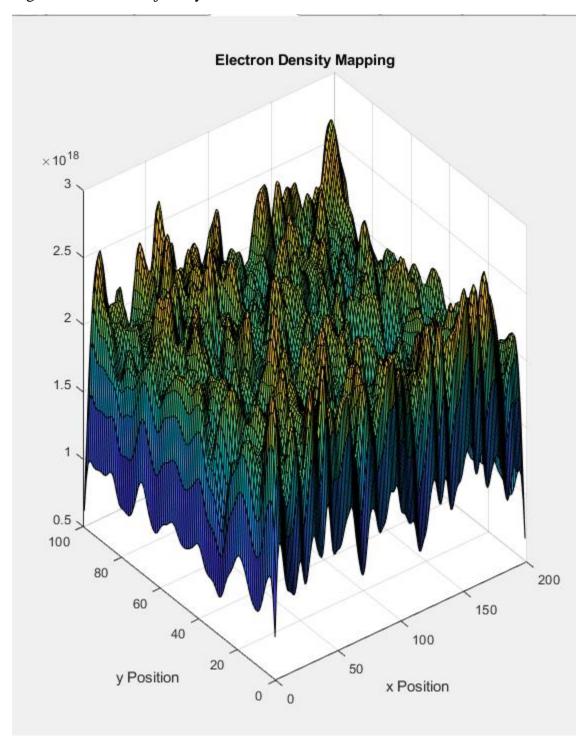


Figure 2: Electron Density Mapping.

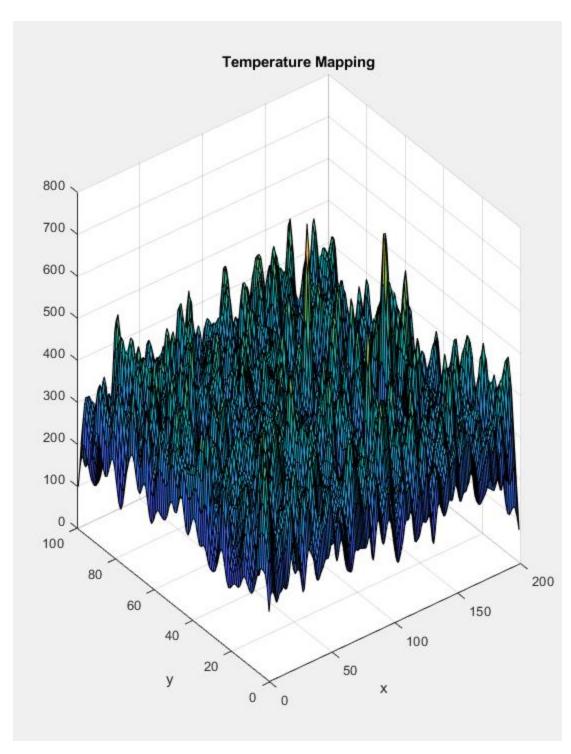


Figure 3: Temperature mapping

The relationship between the electron drift current density and the average carrier velocity is a linear relationship. This can be arrived at from the equation: J = V*n*q*Ny.

Where V is the average carrier velocity of the particles, n is the electron Charge Concentration which was provided to us in the assignment instruction as 10^{15} cm⁻², Q is the electron Charge, Ny is the length of the y boundary.

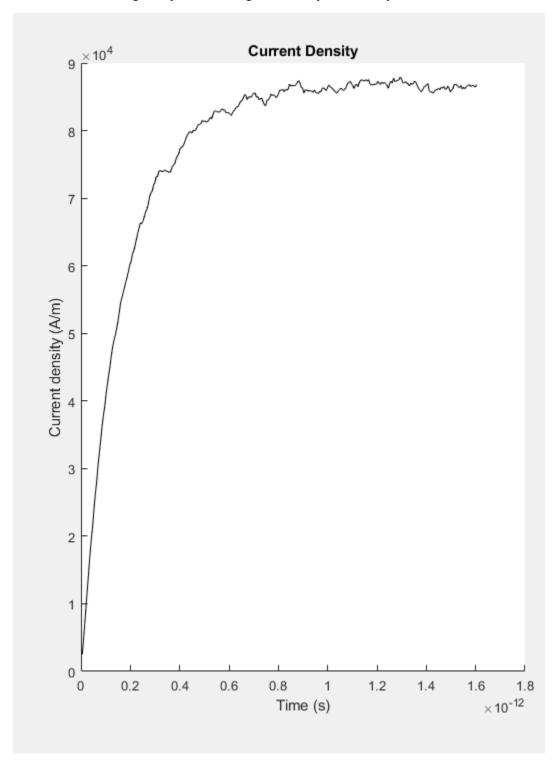


Figure 4: Current Density vs Time

As we can see from the plot above, the behavior of the current is as follows the current rises until it gets to a point where it saturates. What causes the saturation of the current is rethermalization which is resetting the velocities of the particles and this is caused by the scattering (rethermalization occurs as a result of the simulation getting to a point where the amount of scattering of the electrons begins to cancel out the acceleration of the electrons).

The electric field E, Force on the charge F and Acceleration A From the calculations found in the simulations are: $E = 5x10^5$ V/m, $F = 8.01 \times 10^{-14}$ Newtons and $A = 3.38 \times 10^{17}$ m/s².

```
Command Window

The electric field of the charge is 500000.000000 V/m.

The force on the charge is 8.010883e-14 N.

The acceleration of the charge is 338234619754597888.000000 m/s^2.

fx >>
```

Figure 5: Electric Field, Acceleration and Force on charge from MATLAB command Line.

<u>Part 2:</u>

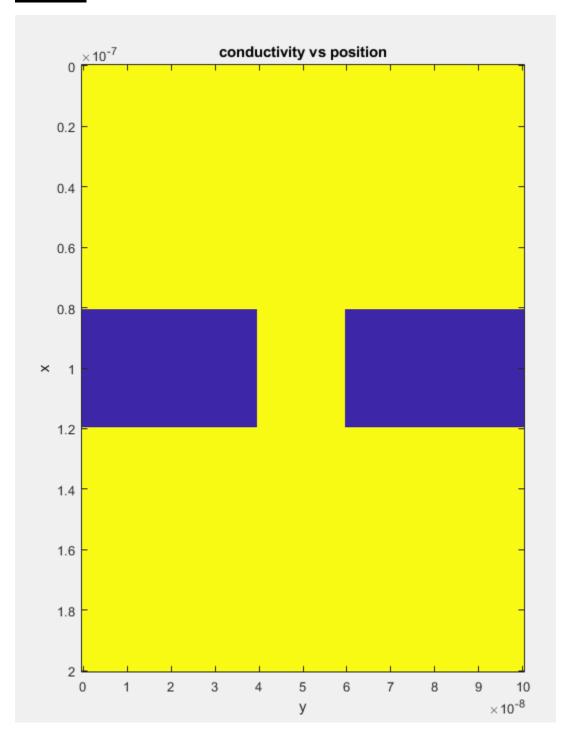


Figure 6: Conductivity vs Position

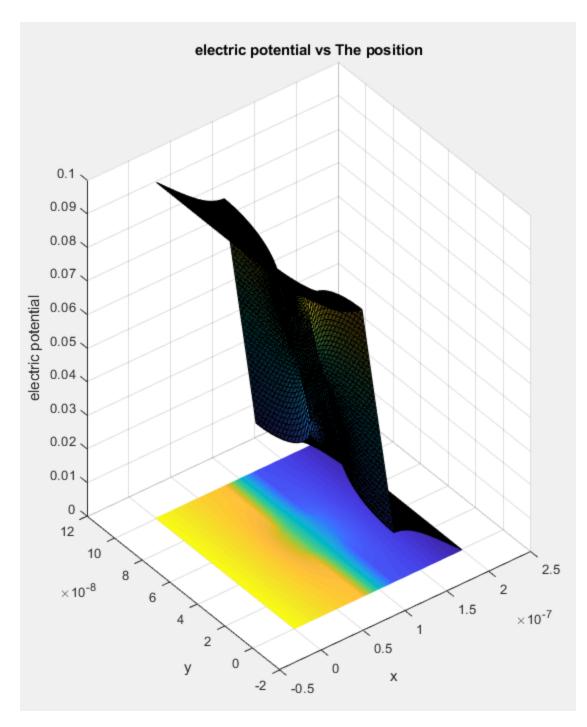


Figure 7: Electric potential vs Position

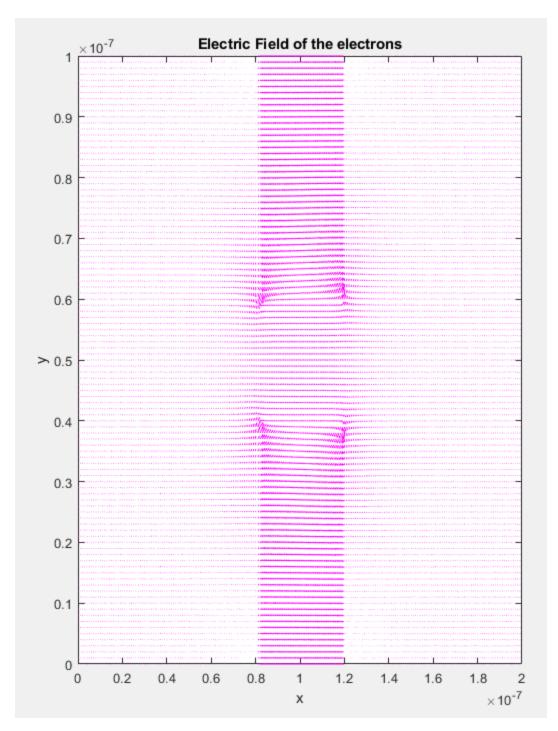


Figure 8: Electric field of the electrons

Part 3:

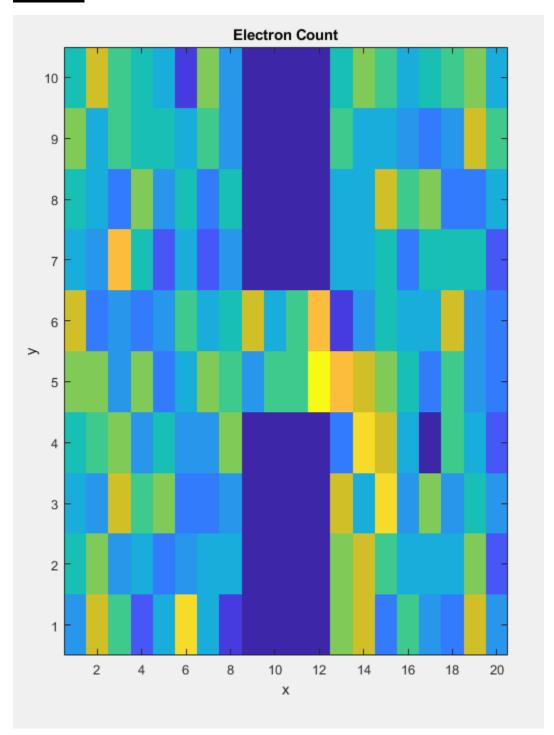


Figure 9: Density mapping

The density mapping was plot using imagesc function in MATLAB which is why it appears as seen as above. The density mapping from figure 9 above is basically telling us where the electrons are most concentrated as the simulation is taking place.

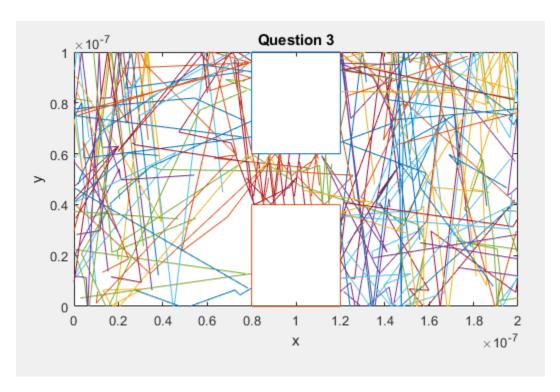


Figure 10: particle trajectory

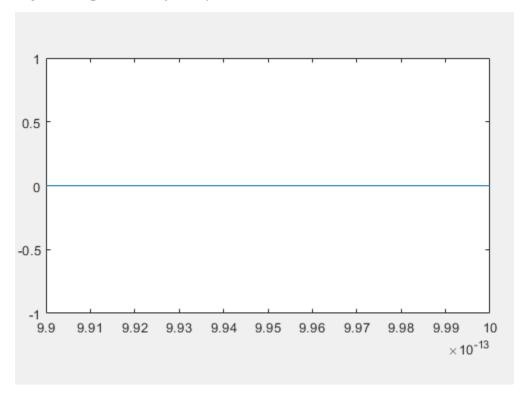


Figure 11: Temperature vs time step

This was what was gotten from our simulation at first but after slight modifications to our code we were able to get something similar to what the ideal plot should look like in theory. Ideally the temperature vs time step should look more like figure 12 below, that is it should fluctuate around a constant value.

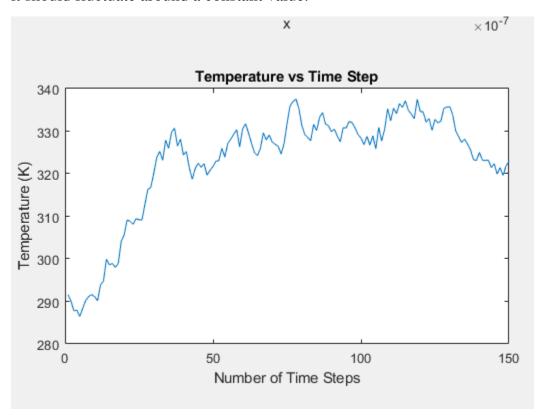


Figure 12: Temperature vs time step

The next step to make the simulation more accurate would be to increase the number of particles in the simulation, as by doing this we would be able to get a more accurate result. Another way would be to use a finer mesh in the simulation.

Conclusion:

In conclusion, the assignment was a success we were able to combine both assignment two and assignment 1 together and add a field into the setup in order to see what happens to the electrons. We were also able to see the relationship between the electron drift current density and carrier velocity of the electrons.

Appendix:

Question 1 and Question 2:

```
clc
clear
set(0,'DefaultFigureWindowStyle','docked')
% Jarikre Efe Jeffery
%101008461
% Part 1: Start with the Monte Carlo Simulator from Assignment 1 without
% the bottleneck from those assignments
wid x = 200e-9; % width
len y = 100e-9; % length
Voltage x = 0.1; % Voltage across x dimension
Voltage y = 0; % Voltage applied across y
Charge electron = -1.60217662e-19; % Charge of electrons
electron conc = 1e15*100^2; % Density of electrons
m0 = 9.10938356e-31; % electron rest mass
effective m = 0.26*m0; % effective mass of electrons
Temperature = 300; % temperature in Kelvin
Boltz const = 1.38064852e-23; % Boltzmann Constant
Thermal v = sqrt(2*Boltz const*Temperature/effective m); % Thermal velocity
of the electrons
mean free path = Thermal v*0.2e-12; % Mean free path
specular top bound = 0; % capable of being specular or diffusive
specular bottom bound = 0; % capable of being specular or diffusive
time step = len y/Thermal v/100;
num iterations = 300;
size_p = 40000;
pp = 10;
pscat = 1 - exp(-time step/0.2e-12);
vel = makedist('Normal', 'mu', 0, 'sigma',
sqrt(Boltz const*Temperature/effective m));
Display m = 0;
% Using the relationship E = V/D to calculate the electric field.
electricfield x = Voltage x/wid x;
electricfield y = Voltage y/len y;
electricfield total = electricfield x + electricfield y;
fprintf('The electric field of the charge is %f V/m.\n',electricfield_total);
% The force on each electron is the sum of its individual components.
x force = Charge electron*electricfield x;
y force = Charge electron*electricfield y;
total force = abs(x force + y force);
fprintf('The force on the charge is %d N.\n', total force);
acceleration = total force/effective m; % Using the relationship of f=ma we
can calculate the accelration of the particle.
fprintf('The acceleration of the charge is %f m/s^2.\n',acceleration);
% The current formula is J = vnqNy. This formula shows the relationship
% between the electron drift current density and average carrier velocity
% Spoke to TA and he insisted on using this since matbe performing
% integration might complicate things.
change vx = x force*time step/effective m;
change vy = y force*time step/effective m;
```

```
change vx = change vx.*ones(size p,1);
change vy = change vy.*ones(size p,1);
positions = zeros(size p, 4);
traj = zeros(num iterations, pp*2);
temporary a = zeros(num iterations, 1);
J = zeros(num iterations, 2);
% Initializing the positions of the particles
for i = 1:size p
   theta = rand*2*pi;
    positions(i,:) = [wid x*rand len y*rand random(vel) random(vel)];
temperature plot = animatedline;
figure(2);
current plot = animatedline;
title('Current Density');
xlabel('Time (s)');
ylabel('Current density (A/m)');
% Iterate through the simulation
for i = 1:num iterations
    positions(:,3) = positions(:,3) + change vx;
    positions(:,4) = positions(:,4) + change vy;
    positions(:,1:2) = positions(:,1:2) + time_step.*positions(:,3:4);
    j = positions(:,1) > wid x;
    positions(j,1) = positions(j,1) - wid x;
    j = positions(:,1) < 0;
    positions(j,1) = positions(j,1) + wid x;
    j = positions(:,2) > len y;
    if(specular top bound)
        positions(j,2) = 2*len y - positions(j,2);
        positions (j,4) = -positions(j,4);
    else
        positions (j, 2) = len y;
        v = sqrt(positions(j,3).^2 + positions(j,4).^2);
        theta = rand([sum(j),1])*2*pi;
        positions(j,3) = v.*cos(theta);
        positions(j,4) = -abs(v.*sin(theta));
    end
    j = positions(:,2) < 0;
    if(specular bottom bound)
        positions(j,2) = -positions(j,2);
        positions(j,4) = -positions(j,4);
        positions(j,2) = 0;
        v = sqrt(positions(j,3).^2 + positions(j,4).^2);
        theta = rand([sum(j),1])*2*pi;
        positions(j,3) = v.*cos(theta);
        positions(j, 4) = abs(v.*sin(theta));
    end
    j = rand(size p, 1) < pscat;</pre>
    positions(j,3:4) = random(vel, [sum(j),2]);
```

```
temporary a(i) = (sum(positions(:,3).^2) +
sum(positions(:,4).^2))*effective m/Boltz const/2/size p;
    for j=1:pp
        traj(i, (2*j):(2*j+1)) = positions(j, 1:2);
    J(i, 1) = Charge electron.*electron conc.*mean(positions(:,3));
    J(i, 2) = Charge electron.*electron conc.*mean(positions(:,4));
    addpoints(temperature plot, time step.*i, temporary a(i));
    addpoints(current plot, time step.*i, J(i,1));
    if(Display m \&\& mod(i,5) == 0)
        figure(1);
        hold off;
        plot(positions(1:pp,1)./1e-9, positions(1:pp,2)./1e-9, 'o');
        axis([0 wid x/1e-9 0 len y/1e-9]);
        hold on;
        title('Particle Trajectories');
        % x and y positions are in nanometers
        xlabel('x position');
        ylabel('y position');
        pause (0.05);
    end
end
figure(1);
title('Particle Trajectories');
%x and y positions are in nanometers
xlabel('x position');
ylabel('y position');
axis([0 \text{ wid } x/1e-9 \ 0 \text{ len } y/1e-9]);
hold on;
for i=1:pp
    plot(traj(:,i*2)./1e-9, traj(:,i*2+1)./1e-9, 'm.');
electron conc = hist3(positions(:,1:2),[200 100])';
N = 20;
sigma = 1.5;
[x,y] = meshgrid(round(-N/2):round(N/2), round(-N/2):round(N/2)); % in order
to use the surf function later
f = \exp(-x.^2/(2*sigma^2) - y.^2/(2*sigma^2));
f=f./sum(f(:));
figure(3);
electron conc = conv2(electron conc,f,'same');
electron conc =
electron conc/(len y./size(electron conc,1)*wid x./size(electron conc,2));
surf(conv2(electron conc,f,'same'));
% contourmode (conv2 (electron conc, f)
title('Electron Density Mapping');
% x and y positions are in nanometers
xlabel('x Position');
ylabel('y Position');
% Temperature mapping
```

```
sum x = zeros(ceil(wid x/1e-9), ceil(len y/1e-9));
sum y = zeros(ceil(wid x/1e-9), ceil(len y/1e-9));
temp num = zeros(ceil(wid x/1e-9), ceil(len y/1e-9));
% electron velocity
for i=1:size p
    x = floor(positions(i, 1)/1e-9);
    y = floor(positions(i,2)/1e-9);
    if(x==0)
        x = 1;
    end
    if(y==0)
        y=1;
    sum y(x,y) = sum y(x,y) + positions(i,3)^2;
    sum x(x,y) = sum x(x,y) + positions(i,4)^2;
    temp num(x,y) = temp num(x,y) + 1;
end
temporary a = (sum x + sum y).*effective m./Boltz const./2./temp num;
temporary a(isnan(temporary_a)) = 0;
temporary a = temporary a';
N = 20;
sigma = 1.5;
[x,y] = meshgrid(round(-N/2):round(N/2), round(-N/2):round(N/2)); % useful to
use the surf function
f=\exp(-x.^2/(2*sigma^2)-y.^2/(2*sigma^2));
f=f./sum(f(:));
figure (4);
surf(conv2(temporary a,f,'same'));
% contourmode(conv2(temporary a,f,'same'));
title('Temperature Mapping');
xlabel('x');
ylabel('y');
clc
clear
set(0,'DefaultFigureWindowStyle','docked')
% Jarikre Efe Jeffery
%101008461
% Part 2: Use The Finite Difference Method in Assignment 2 to calculate the
% electric field and then provide a field for the Monte Carlo bottleneck
% Simulation
length y = 200e-9;
width x = 100e-9;
Len box = 40e-9;
Wid box = 40e-9;
meshspace = 1e-9;
num x = round(length y/meshspace + 1);
num y = round(width x/meshspace + 1);
conductivity outside = 1;
```

```
conductivity inside = 1e-2;
% Conductivity mapping
conductivity_mapping = zeros(num_x,num_y);
for i = 1:num x
   for j = 1:num y
       if (i-1)>0.5*(length_y-Len_box)/meshspace&&(i-
1) <0.5*(length y+Len box)/meshspace&&((j-1)<Wid_box/meshspace||(j-1)<
1) > (width x-Wid box) / meshspace)
           conductivity mapping(i,j) = conductivity inside;
       else
           conductivity mapping(i,j) = conductivity outside;
       end
   end
end
figure (5)
imagesc([0 width x],[0 length y],conductivity mapping);
xlabel('y')
ylabel('x')
title('conductivity vs position')
G matrix = sparse(num x*num y);
B matrix = zeros(1, num x*num y);
for i = 1:num x
    for j = 1:num y
        n = j + (i-1) * num y;
        n1 = j + (i - 1) * length y;
        nxm1 = j + ((i-1) - 1) * length y;
        nxp1 = j + ((i+1) - 1) * length y;
        nym1 = (j-1) + (i - 1) * length y;
        nyp1 = (j+1) + (i - 1) * length y;
        if i == 1
        n1 = j + (i - 1) * length y;
        nxm1 = j + ((i-1) - 1) * length y;
        nxp1 = j + ((i+1) - 1) * length y;
        nym1 = (j-1) + (i - 1) * length y;
        nyp1 = (j+1) + (i - 1) * length y;
            G_{matrix}(n,n) = 1;
            B_{matrix}(n) = 0.1;
        elseif i == num x
        n1 = j + (i - 1) * length y;
        nxm1 = j + ((i-1) - 1) * length_y;
        nxp1 = j + ((i+1) - 1) * length_y;
        nym1 = (j-1) + (i - 1) * length y;
        nyp1 = (j+1) + (i - 1) * length_y;
        G \text{ matrix}(n,n) = 1;
        elseif j == 1
        n1 = j + (i - 1) * length y;
        nxm1 = j + ((i-1) - 1) * length y;
```

```
nxp1 = j + ((i+1) - 1) * length y;
        nym1 = (j-1) + (i - 1) * length y;
        nyp1 = (j+1) + (i - 1) * length y;
        nxm = j + (i-2)*num y;
        nxp = j + i*num y;
        nyp = j+1 + (i-1)*num y;
        rxm = (conductivity_mapping(i,j) + conductivity_mapping(i-1,j))/2;
        rxp = (conductivity mapping(i,j) + conductivity mapping(i+1,j))/2;
        ryp = (conductivity mapping(i,j) + conductivity mapping(i,j+1))/2;
             G \text{ matrix}(n,n) = -(rxm + rxp + ryp);
            G \text{ matrix}(n, nxm) = rxm;
            G \text{ matrix}(n, nxp) = rxp;
             G_{matrix}(n,nyp) = ryp;
        elseif j == num_y
            nxm = j + (i-2)*num y;
            nxp = j + i*num y;
            nym = j-1 + (i-\overline{1}) * num y;
            n1 = j + (i - 1) * length_y;
            nxm1 = j + ((i-1) - 1) * length_y;
            nxp1 = j + ((i+1) - 1) * length y;
            nym1 = (j-1) + (i - 1) * length y;
            nyp1 = (j+1) + (i - 1) * length y;
            rxm = (conductivity mapping(i,j) + conductivity mapping(i-
1,j))/2;
            rxp = (conductivity mapping(i,j) +
conductivity mapping(i+1,j))/2;
             rym = (conductivity mapping(i,j) + conductivity mapping(i,j-
1))/2;
            G \text{ matrix}(n,n) = -(rxm + rxp + rym);
            G \text{ matrix}(n, nxm) = rxm;
            G \text{ matrix}(n, nxp) = rxp;
            G \text{ matrix}(n, nym) = rym;
        else
            nxm = j + (i-2)*num_y;
            nxp = j + i*num_y;
            nym = j-1 + (i-1)*num_y;
            nyp = j+1 + (i-1)*num y;
            n1 = j + (i - 1) * length y;
        nxm1 = j + ((i-1) - 1) * length y;
        nxp1 = j + ((i+1) - 1) * length y;
        nym1 = (j-1) + (i - 1) * length_y;
        nyp1 = (j+1) + (i - 1) * length y;
             rxm = (conductivity mapping(i,j) + conductivity mapping(i-
1,j))/2;
             rxp = (conductivity_mapping(i,j) +
conductivity_mapping(i+1,j))/2;
             ryp = (conductivity_mapping(i,j) +
conductivity_mapping(i,j+1))/2;
             rym = (conductivity_mapping(i,j) + conductivity_mapping(i,j-
1))/2;
```

```
G \text{ matrix}(n,n) = -(rxm + rxp + rym + ryp);
            G \text{ matrix}(n, nxm) = rxm;
            G \text{ matrix}(n, nxp) = rxp;
            G matrix(n,nym) = rym;
            G_{matrix}(n, nyp) = ryp;
        end
    end
end
% set up matrix and solve
V = G matrix\B matrix';
Voltage map = zeros(num_x,num_y);
for i = 1:num x
    for j = 1:num y
        n = j + (i-1) * num y;
        Voltage map(i,j) = V(n);
    end
end
[X, Y] = meshgrid(0:meshspace:length y,0:meshspace:width x);
figure(6)
surf(X',Y',Voltage map)
hold on
imagesc([0 length y],[0 width x], Voltage map')
xlabel('x')
ylabel('y')
zlabel('electric potential')
title('electric potential vs The position')
hold off
[electricfield y, electricfield x] = gradient(Voltage map, meshspace);
electricfield x = -electricfield x;
electricfield y = -electricfield y;
figure(7)
quiver(X',Y',electricfield x,electricfield y)
xlim([0 length y])
ylim([0 width x])
xlabel('x')
ylabel('y')
title('Electric Field of the electrons')
Question 3:
clc
clear
set(0, 'DefaultFigureWindowStyle', 'docked')
% Jarikre Efe Jeffery
%101008461
% Part 3: Use the coupled simulations to investigate the "device" and
% extract simple trajectories
global C
global Ecount
```

```
global Vx Vy Vtotal x y
Ecount =1000;
C.mo = 9.10938215e-31;
C.k = 1.3806504e-23;
electron charge = -1.60217662e-19;
Temperature =300;
effective m = 0.26 * C.mo;
Length = 200e-9;
Width = 100e-9;
Thermal v = sqrt((2*C.k*Temperature)/effective m);
time_step = 10e-15;
frame = 100*time step;
x = zeros(Ecount, 2);
y = zeros(Ecount, 2);
Temperature = zeros(1,2);
Time = 0;
VisibleEcount = 50;
tmn = 0.2e-12;
PScat = 1 - exp(-time step/tmn);
V Histogram = zeros(Ecount, 1);
bottleneck X = [80e-9 \ 80e-9 \ 120e-9 \ 120e-9 \ 80e-9];
bottleneck Y1 = [100e-9 60e-9 60e-9 100e-9 100e-9];
bottleneck Y2 = [40e-9 \ 0 \ 0 \ 40e-9 \ 40e-9];
Specular = true;
Inside Box = true;
Mapping S = 10e-9;
Density Mapping = zeros(Width/Mapping S, Length/Mapping S);
Temperature Mapping = zeros(Width/Mapping S, Length/Mapping S);
wid x = 30;
len_y = 20;
change x = Length/wid x;
change y = Width/len y;
conduction outside = 1;
conduction inside = 01e-2;
conductivity = zeros(wid x,len y);
G matrix = sparse (wid x*len y, wid x*len y);
V matrix = zeros(1, wid x*len y);
Voltage x = 0.1;
for i = 1:wid x
    for j = 1:len_y
        n = j + (i - 1) *len_y;
        nxm = j + ((i-1) - 1)*len y;
        nxp = j + ((i+1) - 1)*len y;
        nym = (j-1) + (i - 1) *len y;
        nyp = (j+1) + (i - 1)*len y;
        if (i > (0.3*wid x) \mid \mid i < (0.6*wid x)) && (j > (0.6*len y) \mid \mid j <
(0.3*len y))
            conductivity(i,j) = conduction inside;
            conductivity(i,j) = conduction outside;
        end
```

```
end
for i = 1:wid x
    for j = 1:len y
         n = j + (i - 1) *len_y;
        nxm = j + ((i-1) - \overline{1})*len y;
        nxp = j + ((i+1) - 1)*len y;
        nym = (j-1) + (i - 1)*len y;
        nyp = (j+1) + (i - 1)*len y;
         if (i == 1)
        n = j + (i - 1) *len y;
        nxm = j + ((i-1) - 1)*len y;
        nxp = j + ((i+1) - 1)*len y;
        nym = (j-1) + (i - 1) *len y;
        nyp = (j+1) + (i - 1)*len y;
             V matrix(n) = Voltage x;
             G_{matrix}(n,n) = 1;
        elseif (i == wid x)
        n = j + (i - 1) * len y;
        nxm = j + ((i-1) - \overline{1}) *len y;
        nxp = j + ((i+1) - 1)*len y;
        nym = (j-1) + (i - 1)*len y;
        nyp = (j+1) + (i - 1)*len y;
             V \text{ matrix}(n) = 0;
             G matrix (n,n) = 1;
        elseif (j == 1)
         n = j + (i - 1) * len y;
        nxm = j + ((i-1) - 1)*len y;
        nxp = j + ((i+1) - 1)*len y;
        nym = (j-1) + (i - 1)*len y;
        nyp = (j+1) + (i - 1)*len y;
             G = -((conductivity(i,j) + conductivity(i-1,j))/2) -
((conductivity(i,j) + conductivity(i+1,j))/2) - ((conductivity(i,j) + conductivity(i,j)) + conductivity(i,j))
conductivity(i,j+1)/2;
             G \text{ matrix}(n, nxm) = ((conductivity(i,j) + conductivity(i-1,j))/2);
             G \text{ matrix}(n, nxp) = ((conductivity(i,j) + conductivity(i+1,j))/2);
             G \text{ matrix}(n, nyp) = ((conductivity(i,j) + conductivity(i,j+1))/2);
        elseif (j == len y)
        n = j + (i - 1) *len y;
        nxm = j + ((i-1) - 1)*len y;
        nxp = j + ((i+1) - 1)*len y;
        nym = (j-1) + (i - 1) *len y;
        nyp = (j+1) + (i - 1)*len y;
             G matrix(n,n) = -((conductivity(i,j) + conductivity(i-1,j))/2) -
((conductivity(i,j) + conductivity(i+1,j))/2) - ((conductivity(i,j) + conductivity(i,j)) + conductivity(i,j))
conductivity(i,j-1)/2;
             G \text{ matrix}(n,nxm) = ((conductivity(i,j) + conductivity(i-1,j))/2);
             G matrix(n,nxp) = ((conductivity(i,j) + conductivity(i+1,j))/2);
             G \text{ matrix}(n,nym) = ((conductivity(i,j) + conductivity(i,j-1))/2);
        else
        n = j + (i - 1) * len y;
        nxm = j + ((i-1) - 1)*len_y;
        nxp = j + ((i+1) - 1)*len y;
        nym = (j-1) + (i - 1) *len y;
        nyp = (j+1) + (i - 1) *len y;
             G matrix(n,n) = -((conductivity(i,j) + conductivity(i-1,j))/2) -
((conductivity(i,j) + conductivity(i+1,j))/2) - ((conductivity(i,j) + conductivity(i,j)) + conductivity(i,j))
conductivity(i,j-1)/2 - ((conductivity(i,j) + conductivity(i,j+1)/2);
```

```
G \text{ matrix}(n, nxm) = ((conductivity(i,j) + conductivity(i-1,j))/2);
            G \text{ matrix}(n, nxp) = ((conductivity(i,j) + conductivity(i+1,j))/2);
            G_{matrix}(n, nym) = ((conductivity(i,j) + conductivity(i,j-1))/2);
            G \text{ matrix}(n, nyp) = ((conductivity(i,j) + conductivity(i,j+1))/2);
        end
    end
end
Solution = G matrix\V matrix';
surface = zeros(wid x, len y);
for i = 1:wid x
    for j = 1:len y
        n = j + (i - 1) *len y;
        nxm = j + ((i-1) - 1) * len_y;
        nxp = j + ((i+1) - 1) * len y;
        nym = (j-1) + (i - 1) * len y;
        nyp = (j+1) + (i - 1) * len y;
        surface(i,j) = Solution(n);
    end
end
[Electricfield x, Electricfield y] = gradient(-surface);
Force x = electron charge*Electricfield x;
Force y = electron charge*Electricfield y;
Acceleration x = Force x / effective m;
Acceleration_y = Force_y /effective_m;
for i = 1:Ecount
    x(i,1) = rand()*200e-9;
    y(i,1) = rand()*100e-9;
    Inside Box = true;
    while Inside Box == true
        if (x(i) \ge 40e-9 \&\& x(i) \le 120e-9) \&\& (y(i) \ge 60e-9 ||...
                y(i) <= 40e-9)
            x(i,1) = rand * 200e-9;
            y(i,1) = rand * 100e-9;
            Inside Box = false;
        end
    end
end
for i = 1:Ecount
Vx(1:Ecount) = Thermal v * randn;
Vy(1:Ecount) = Thermal v * randn;
end
figure(8)
subplot(2,1,1);
plot(bottleneck X, bottleneck Y1, bottleneck X, bottleneck Y2)
axis([0 Length 0 Width]);
title('Question 3');
xlabel('x');
ylabel('y');
hold on;
```

```
while Time < frame
    subplot(2,1,1)
    for j = 1:Ecount
        leaking = true;
        if PScat> rand
                Vx(j) = Thermal_v * randn;
                Vy(j) = Thermal v * randn;
        end
        x index = round((x(j,2)/Length) * 30);
        y index = round((y(j,2)/Width)*20);
        if x index < 1
            x index = 1;
        elseif x_{index} > 30
                x index = 30;
        end
        if y index < 1</pre>
            y index = 1;
        elseif y index > 20
            y_index = 20;
        Vx(j) = Vx(j) + Acceleration x(x index, y index)*time step;
        Vy(j) = Vy(j) + Acceleration_y(x_index,y_index)*time_step;
        x(j,2) = x(j,1);
        y(j,2) = y(j,1);
        x(j,1) = x(j,1) + (time step * Vx(j));
        y(j,1) = y(j,1) + (time step * Vy(j));
        if (x(j,1) \ge 80e-9 \&\& x(j,1) \le 120e-9) \&\& y(j,1) \ge 60e-9
                 if y(j,2) < 60e-9
                     \nabla y(j) = -\nabla y(j);
                     y(j,1) = 60e-9;
                     y(j,2) = 60e-9;
                 elseif x(j,2) < 80e-9
                     Vx(j) = -Vx(j);
                     x(j,1) = 80e-9;
                     x(j,2) = 80e-9;
                 elseif x(j,2) > 120e-9
                     Vx(j) = -Vx(j);
                     x(j,1) = 120e-9;
                     x(j,2) = 120e-9;
                 end
            if Specular == true
                x(j,1) = x(j,2) + Vx(j) *time step;
                y(j,1) = y(j,2) + Vy(j) *time step;
            else
             Vx(j) = Thermal v * randn;
             Vy(j) = Thermal v * randn;
```

```
while leaking == true
         if(x(j,2) < 80e-9 \&\& Vx(j) >= 0) || ...
                  (x(j,2) > 120e-9 \&\& Vx(j) \le 0) || ...
                  (y(j,2) < 60e-9 \&\& Vy(j) >= 0)
             Vx(j) = Thermal_v * randn;
             Vy(j) = Thermal_v * randn;
         else
             leaking = false;
         end
     end
     x(j,1) = x(j,2) + Vx(j)*time step;
     y(j,1) = y(j,2) + Vy(j) *time step;
    end
end
if (x(j,1) \ge 80e-9 \&\& x(j,1) \le 120e-9) \&\& y(j,1) \le 40e-9
        if y(j,2) > 40e-9
            \nabla y(j) = -\nabla y(j);
            y(j,1) = 40e-9;
            y(j,2) = 40e-9;
        elseif x(j,2) < 80e-9
            Vx(j) = -Vx(j);
            x(j,1) = 80e-9;
            x(j,2) = 80e-9;
        elseif x(j,2) > 120e-9
            Vx(j) = -Vx(j);
            x(j,1) = 120e-9;
            x(j,2) = 120e-9;
        end
    if Specular == true
        x(j,1) = x(j,2) + Vx(j) *time step;
        y(j,1) = y(j,2) + Vy(j)*time_step;
    else
     Vx(j) = Thermal v * randn;
     Vy(j) = Thermal v * randn;
     while leaking == true
         if(x(j,2) < 80e-9 \&\& Vx(j) >= 0) || ...
                  (x(j,2) > 120e-9 \&\& Vx(j) \le 0) \mid | \dots
                  (y(j,2) > 40e-9 \&\& Vy(j) \le 0)
             Vx(j) = Thermal v * randn;
             Vy(j) = Thermal_v * randn;
         else
              leaking = false;
         end
     end
     x(j,1) = x(j,2) + Vx(j) *time step;
     y(j,1) = y(j,2) + Vy(j) *time step;
    end
end
if x(j,1) > Length
    x(j,2) = 0;
    x(j,1) = time_step * Vx(j);
end
if x(j,1) < 0
    x(j,2) = Length;
    x(j,1) = x(j,2) + (time step * Vx(j));
end
```

```
if y(j,1) > Width \mid \mid y(j,1) < 0
            \nabla y(j) = -\nabla y(j);
        end
        XPlot = [x(j,2) x(j,1)];
        YPlot = [y(j,2) y(j,1)];
        if j < VisibleEcount</pre>
        plot(XPlot, YPlot);
        end
       VTotal = sqrt(Vx(j)^2 + Vy(j)^2);
    end
    AvgTemperature = Temperature(1,2)/Ecount;
    TemperaturePlot = [Temperature(1,1) AvgTemperature];
    TimePlot = [(Time - time step) Time];
    subplot(2,1,2);
    plot(TimePlot, TemperaturePlot);
    Temperature(1,1) = AvgTemperature;
    AvgTemperature = 0;
    Temperature (1,2) = 0;
    pause (1e-19)
    Time = Time + time step;
for i = 1:(Length/Mapping S)
    for j = 1: (Width/Mapping S)
        for m = 1:Ecount
            if(x(m,1) > Mapping S*(i-1)) && ...
                     (x(m,1) < Mapping S*(i)) && ...
                     (y(m,1) > Mapping S*(j-1)) && ...
                     (y(m,1) < Mapping S*(j))
                Vtotal(m) = sqrt(Vx(m)^2 + Vy(m)^2);
                 Density Mapping(j, i) = Density Mapping(j, i) + 1;
                 Temperature Mapping(j, i) = Temperature Mapping(j,i) + ...
                     (effective m*Vtotal(m)^2)/(2*C.k);
            end
            Temperature Mapping(j,i) =
Temperature Mapping(j,i)/Density Mapping(j,i);
        end
    end
end
figure (9)
imagesc(Density Mapping)
title('Density mapping of all electrons in the frame')
xlabel('x');
ylabel('y');
set(gca, 'Ydir', 'Normal')
title('Electron Count')
```