ELEC 4700

ASSIGNMENT 3 – MONTE CARLO/ FINITE DIFFERENCE METHOD

Submitted By:

Jarikre Efe Jeffery

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Introduction:

Part 1:

The differential equations that represent the network in the time domain using KCL (Summation of I=0 at the node) can be found below:

Equations:

$$\begin{split} V_1 &= V_{in} \\ G_1(V_2 - V_1) + C \frac{d(V_2 - V_1)}{dt} + G_2 V_2 - I_L &= 0 \\ V_2 - V_3 - L \frac{dI_L}{dt} &= 0 \\ -I_L + G_3 V_3 &= 0 \\ V_4 - \alpha I_3 &= 0 \\ G_3 V_3 - I_3 &= 0 \\ G_4(V_O - V_4) + G_O V_O &= 0 \end{split}$$

Matrices:

Equations in the frequency domain can be found below:

To the frequency domain: Date V, = Vin G, (V2-V2) + C Jus (V2-V2) + Gold - I1=0	
V, = Vin G, (V2-V2) + C) w (V2-V2) + GoVb - I, = 0	
$\frac{1}{1+\frac{1}{2}}\frac{1}$	
V ₄ - «I ₈ = 0	
G3V3 - I3 -0	
Gy (Vo-Vy) + GoVo = 0	

Programming section:

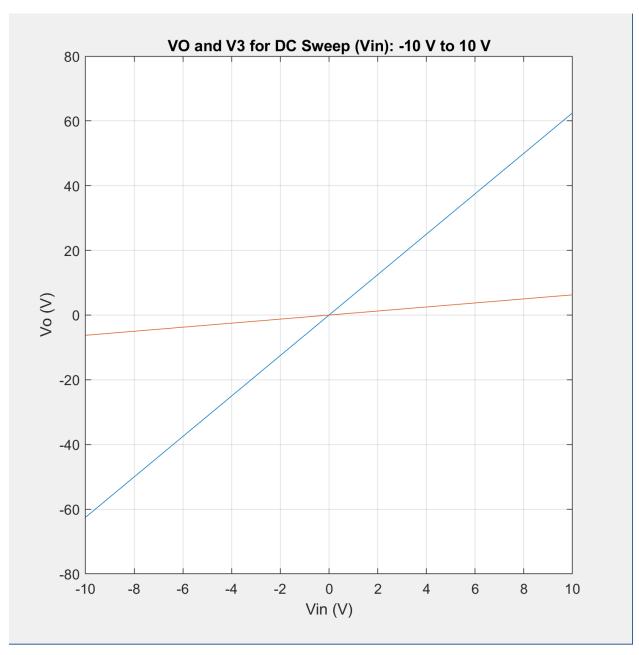


Figure 1: DC Sweep of the input voltage

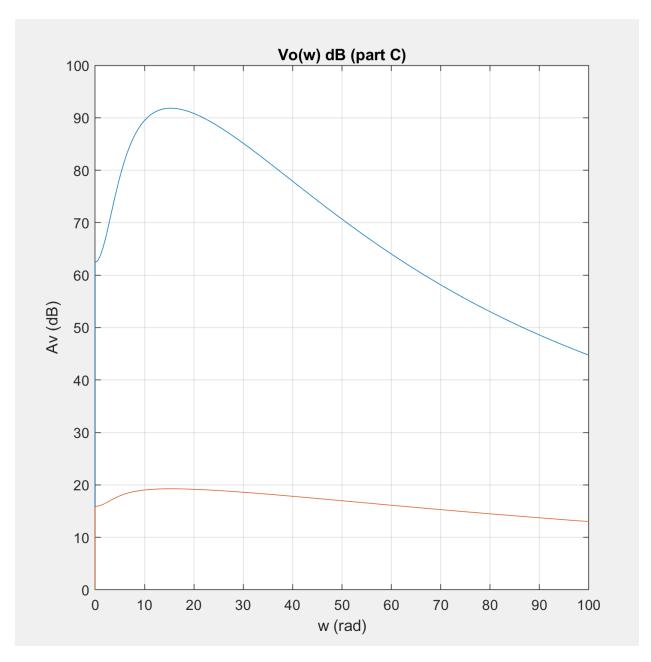


Figure 2: Ac plot of Vo as a fuction of w

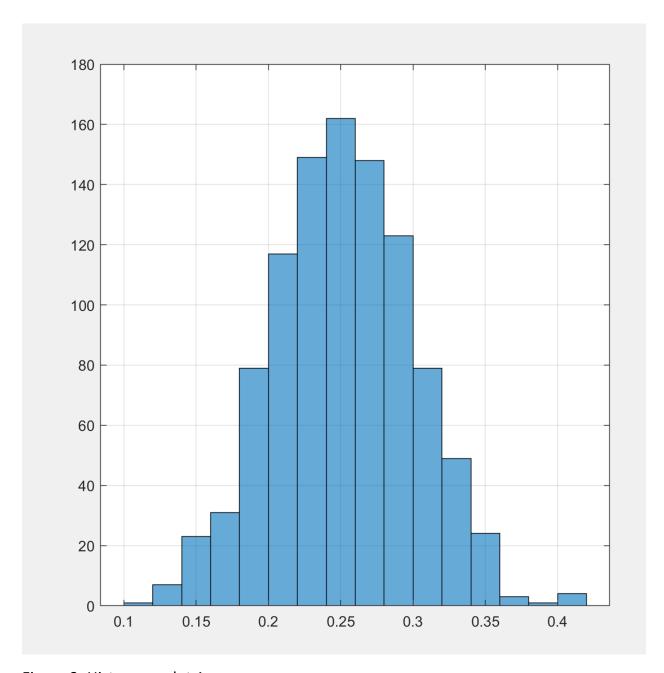


Figure 3: Histogram plot 1

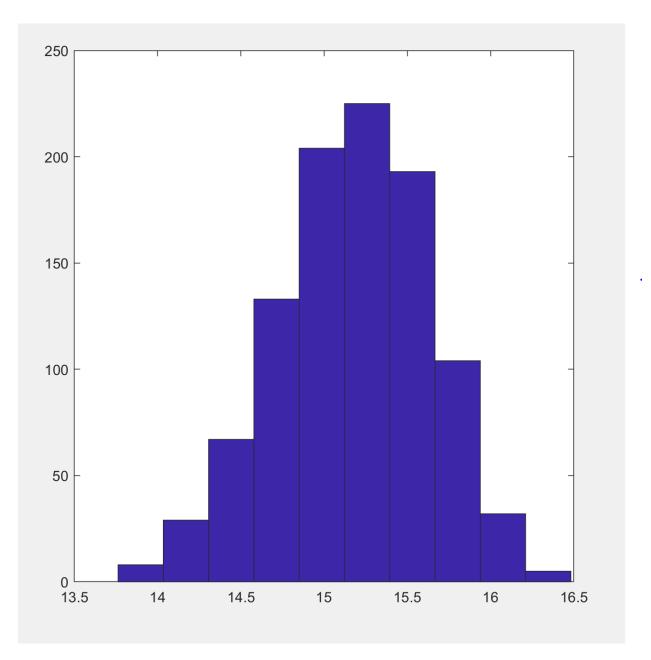


Figure 4: Histogram plot 2

Transient Simulation:

The circuit can be simulated in the time domain by solving the equation of CdV/dt + GV = F

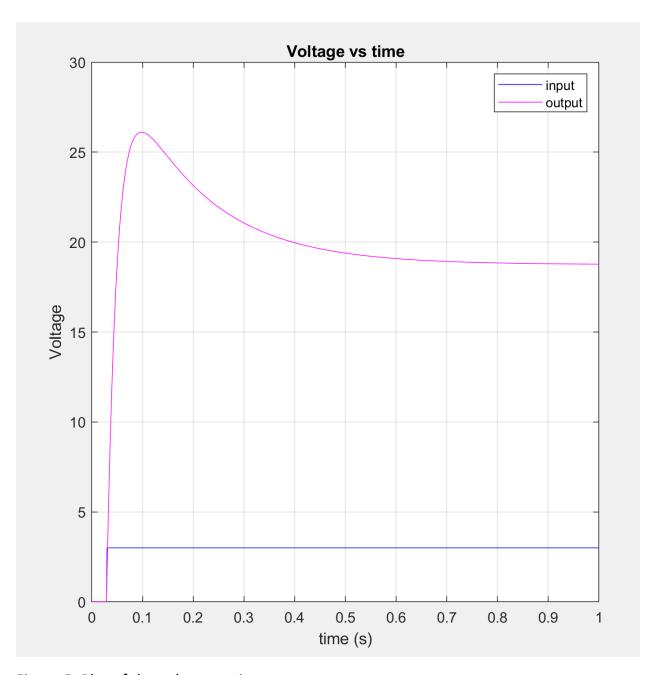


Figure 5: Plot of the voltage vs time

- a.) By inspection the circuit is a low pass filter
- b.) We should expect the frequency response to cut off high frequencies and allow only the low frequencies to go through.
- d.) Part v: As the time step is increased the accuracy of the simulation is decreased.

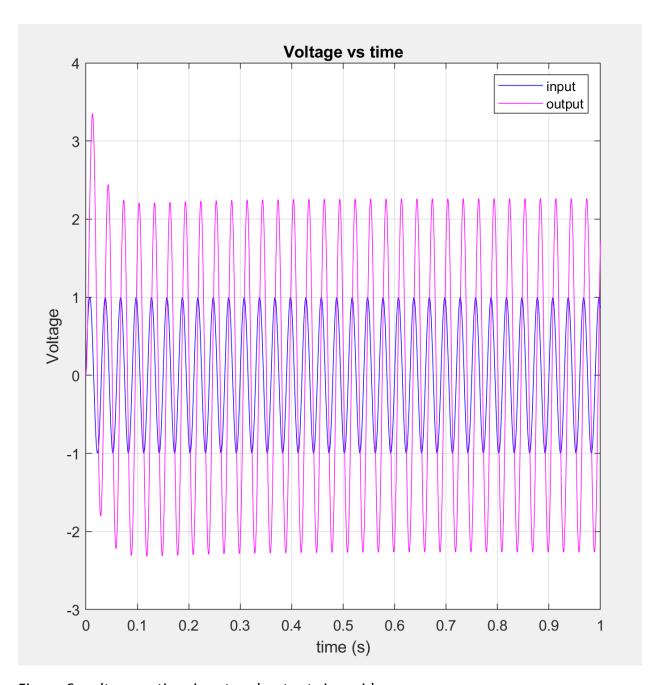


Figure 6: voltage vs time input and output sinusoid

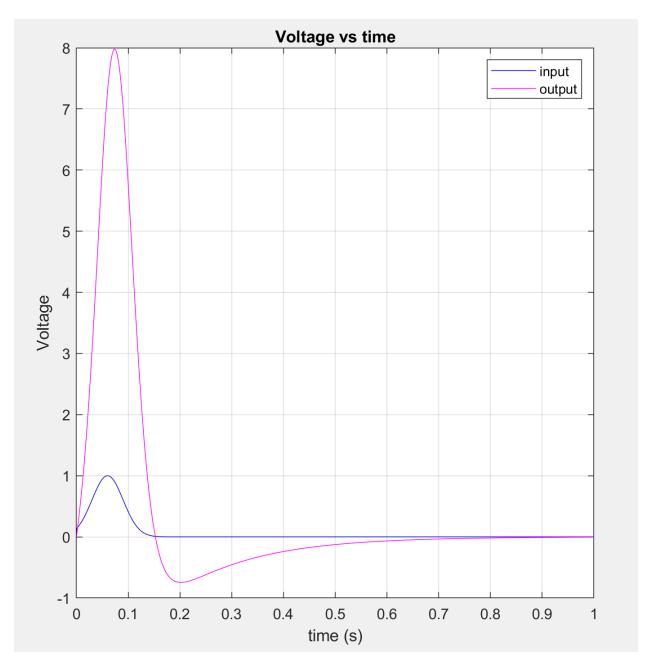


Figure 7: voltage vs time with input and output

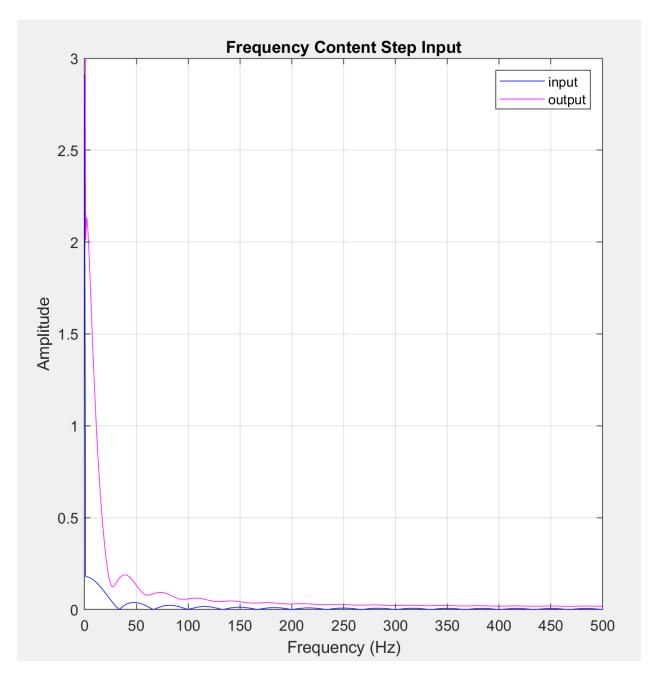


Figure 8: frequency content step input

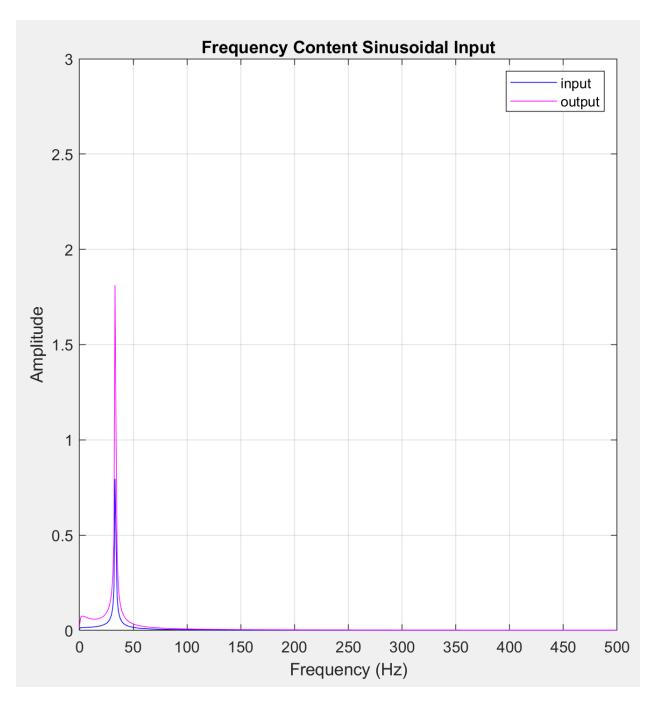


Figure 9: Frequency content sinuisoidal input

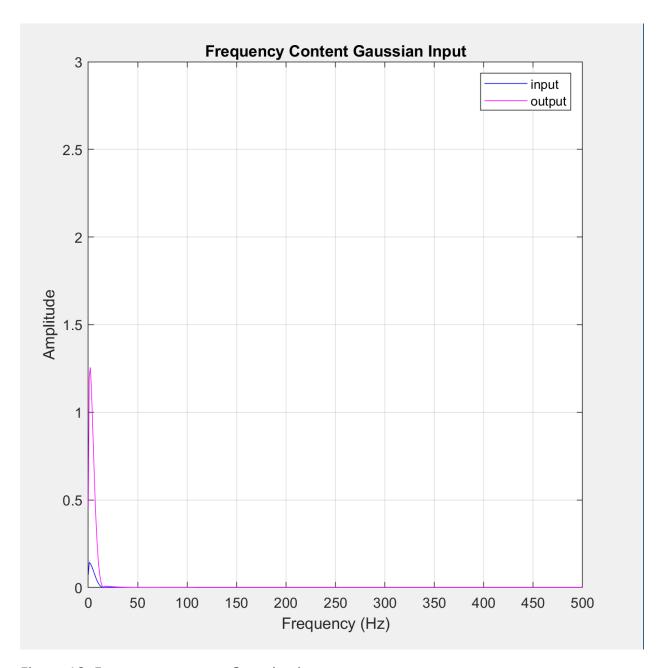


Figure 10: Frequency content Gaussian input

C matrix:

C1 =							
0.2500	-0.2500	0	0	0	O	0	0
-0.2500	0.2500	0	0	0	0	0	0
0	0	0.0000	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	-0.2000	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0

Note That Cn1 = 0.00001

Varying Cn:

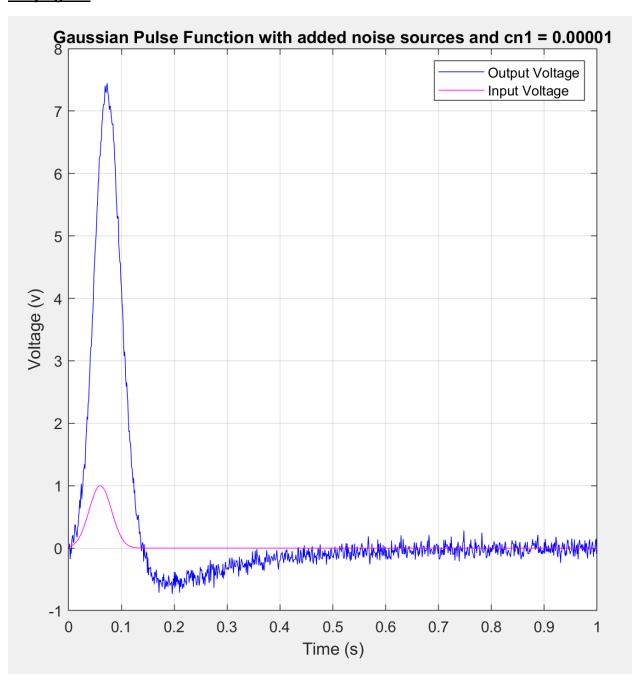


Figure 11: Gaussian Pulse function with added noise sources and cn1 = 0.00001

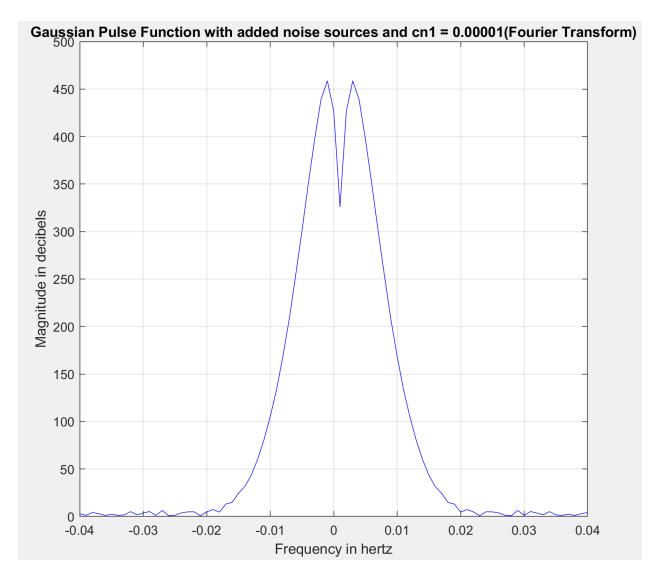


Figure 12: Gaussian Pulse function with added noise sources and cn1=0.00001 fourier transform

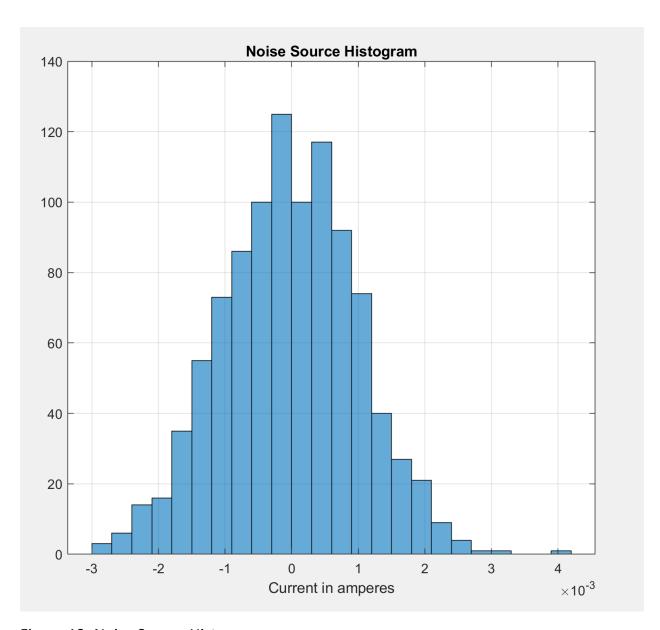


Figure 13: Noise Source Histogram

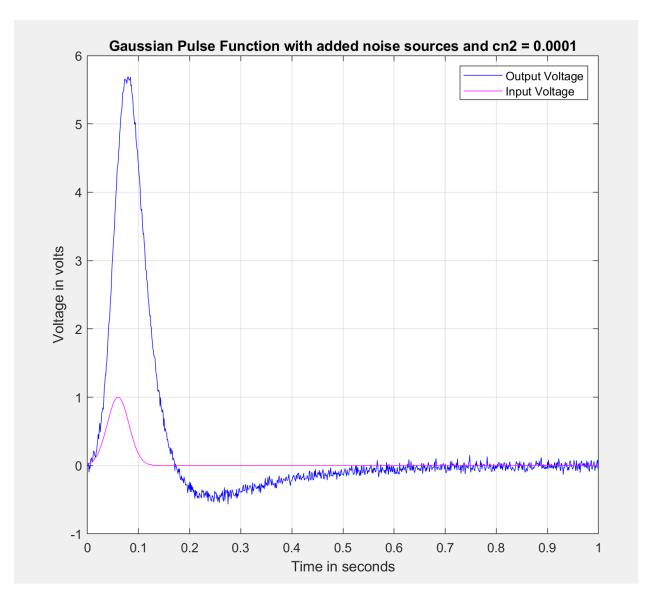


Figure 14: Gaussian Pulse function with added noise sources and cn2=0.0001

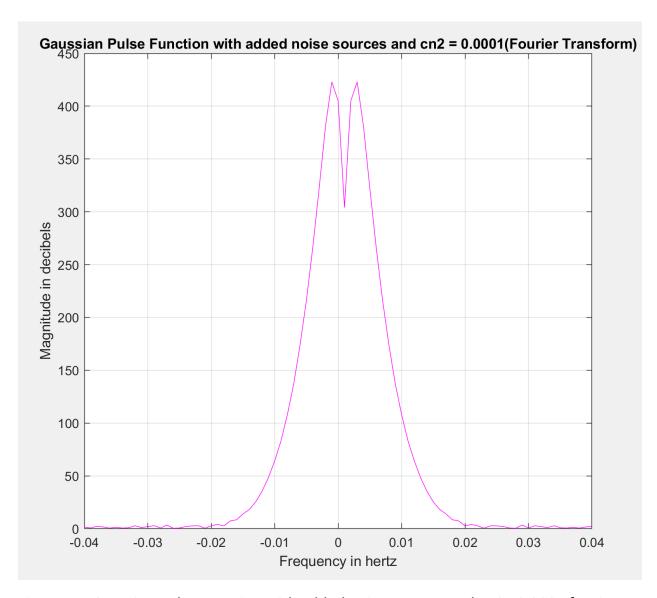


Figure 15: Gaussian Pulse Function with added noise sources and cn2 =0.0001 fourier transform

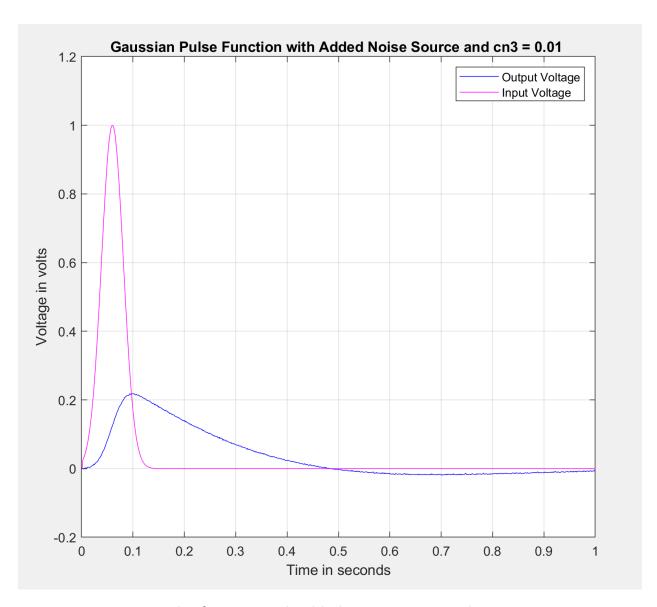


Figure 16: Gaussian Pulse function with added noise sources and cn3=0.01

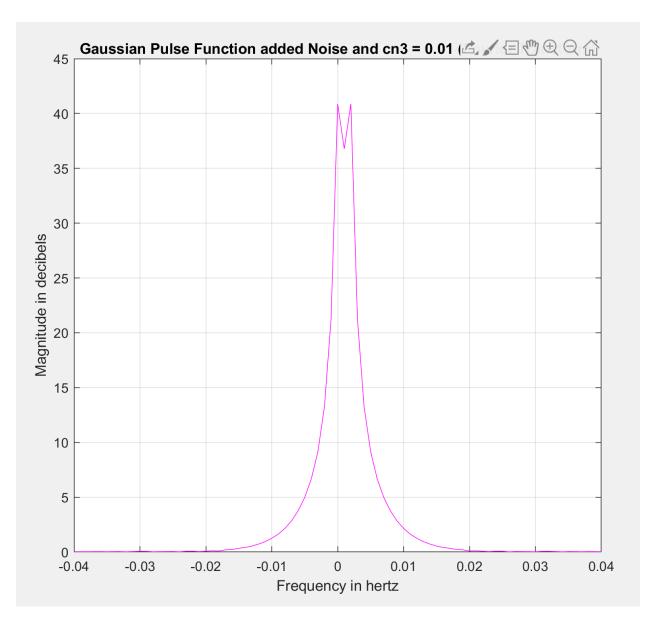


Figure 17: Gaussian Pulse function with added noise sources and cn3=0.01 fourier transform

We can conclude that as cn gets larger the bandwidth tends to get smaller.

Varying the timestep:

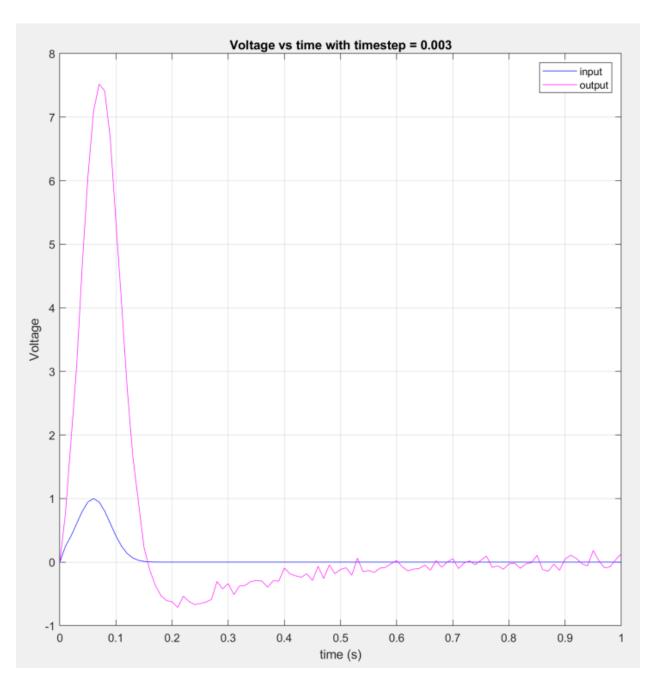


Figure 18: Plot when time step equals 0.003

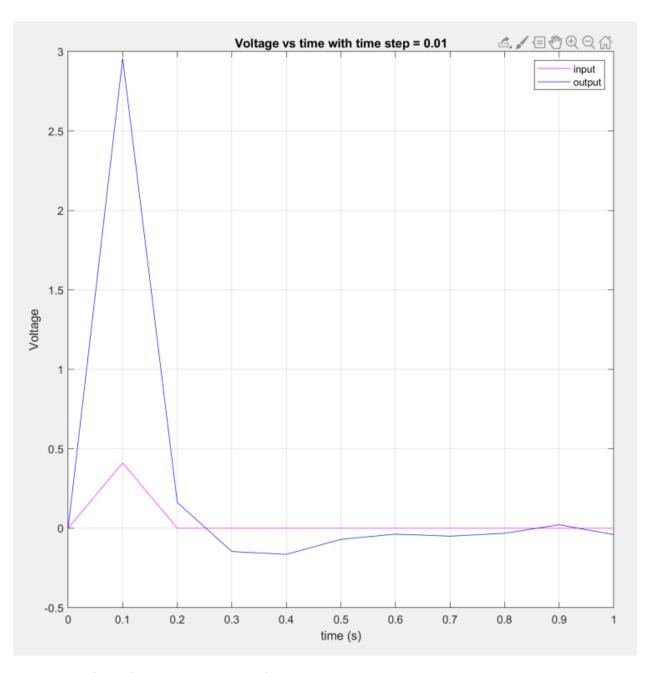


Figure 19: Plot when timestep equals 0.01

What I seemed to have observed was that as the time step is increased the accuracy of the simulation decreases.

Non-Linearity:

In order to implement this in MATLAB we would need to add another matrix to represent or contain the equations for the non-linear elements. A column vector B(V) would need to be added. When that has been added, because the system is

now non-linear it can't be solved by simple gaussian elimination and instead the newton Raphson numerical method would need to be used instead.

Appendix section:

```
clc
clear
clearvars
set(0,'DefaultFigureWindowStyle','docked')
% Name:Jarikre Efe Jeffery
% Student Number: 101008461
% Part 3: Programming
G = zeros(6, 6);
%Resistances:
R1 = 1;
R2 = 2;
R3 = 10;
R4 = 0.1;
R0 = 1000;
%Conductances:
G1 = 1/R1;
G2 = 1/R2;
G3 = 1/R3;
G4 = 1/R4;
G0 = 1/R0;
%Additional Parameters:
a = 100;
Cval = 0.25;
L = 0.2;
vi = zeros(100, 1);
vo = zeros(100, 1);
v3 = zeros(100, 1);
G(1, 1) = 1;
G(2, 1) = G1; G(2, 2) = -(G1 + G2); G(2, 6) = -1;
```

```
G(3,3) = -G3; G(3,6) = 1;
G(4, 3) = -a*G3; G(4, 4) = 1;
G(5, 5) = -(G4+G0); G(5, 4) = G4;
G(6, 2) = -1; G(6, 3) = 1;
C = zeros(6, 6);
C(2, 1) = Cval; C(2, 2) = -Cval;
C(6, 6) = L;
F = zeros(6, 1);
v = 0;
for vin = -10:0.1:10
  v = v + 1;
  F(1) = vin;
  Vm = G\backslash F;
  vi(v) = vin;
  vo(v) = Vm(5);
  v3(v) = Vm(3);
end
figure(1)
plot(vi, vo);
hold on;
plot(vi, v3);
title('VO and V3 for DC Sweep (Vin): -10 V to 10 V');
xlabel('Vin (V)')
ylabel('Vo(V)')
grid on
vo2 = zeros(1000, 1);
W = zeros(1000, 1);
Avlog = zeros(1000, 1);
for freq = linspace(0, 100, 1000)
  v = v+1;
```

```
Vm2 = (G+1j*freq*C)\F;
  W(v) = freq;
  vo2(v) = norm(Vm2(5));
  Avlog(v) = 20*log10(norm(Vm2(5))/10);
end
figure(3)
plot(W, vo2)
hold on;
plot(W, Avlog)
grid on
title('Vo(w) dB (part C)')
xlabel('w (rad)')
ylabel('Av (dB)')
figure(4)
semilogx(W,vo2)
title('Vo(w) dB (part C)')
xlabel('w (rad)')
ylabel('Av (dB)')
grid on
w = pi;
CC = zeros(1000,1);
GG = zeros(1000,1);
for i = 1:1000
  crand = Cval + 0.05*randn();
  C(2, 1) = crand;
  C(2, 2) = -crand;
  C(3, 3) = L;
  Vm3 = (G+(1i*w*C))\F;
  CC(i) = crand;
  GG(i) = 20*log10(abs(Vm3(5))/10);
end
figure(5)
histogram(CC)
grid on
```

```
figure(6)
grid on
hist(GG)
clc
clear
clearvars
set(0,'DefaultFigureWindowStyle','docked')
% Transient simulation
R1 = 1;
R2 = 2;
C = 0.25;
L = 0.2;
R3 = 10;
a = 100;
R4 = 0.1;
R0 = 1000;
G = zeros(7,7);
Cm = zeros(7,7);
% Conductance value
G(1,1) = 1;
G(2,1) = -1/R1;
G(2,2) = 1/R1 + 1/R2;
G(2,6) = 1;
G(3,3) = 1/R3;
G(3,6) = -1;
G(4,3) = 1/R3;
G(4,7) = -1;
G(5,4) = -1/R4;
G(5,5) = 1/R4 + 1/R0;
G(6,2) = 1;
G(6,3) = -1;
G(7,4) = 1;
G(7,7) = -a;
% Capacitance value
Cm(2,1) = -C;
Cm(2,2) = C;
Cm(6,6) = -L;
V1 = zeros(7,1);
V2 = zeros(7,1);
```

```
V3 = zeros(7,1);
V \text{ node1}(1) = 0;
V \text{ node2}(1) = 0;
V \text{ node3}(1) = 0;
delta = 0.001;
A = (Cm/delta) + G;
F index1 = zeros(7,1);
F_{index2} = zeros(7,1);
F index33 = zeros(7,1);
Vo node1(1) = 0;
Vo node2(1) = 0;
Vo node3(1) = 0;
i = 1;
for j = delta:delta:1
  if j >= 0.03
    F index1(1) = 3;
  end
  F index2(1) = \sin(2*pi*j/0.03);
  F_{index33(1)} = exp(-0.5*((j - 0.06)/0.03)^2);
  V1 = A(Cm*V1/delta + F index1);
  V2 = A(Cm*V2/delta + F_index2);
  V3 = A\setminus(Cm*V3/delta + F index33);
  V \text{ node1}(i+1) = V1(1);
  V_node2(i+1) = V2(1);
  V_node3(i+1) = V3(1);
  Vo_node1(i+1) = V1(5);
  Vo node2(i+1) = V2(5);
  Vo node3(i+1) = V3(5);
  i = i+1;
end
figure(7)
plot(0:delta:1,V_node1,'b')
hold on
plot(0:delta:1,Vo node1,'m')
title('Voltage vs time')
xlabel('time (s)')
ylabel('Voltage')
legend('input','output')
```

```
grid on
figure(8)
plot(0:delta:1,V node2,'b')
hold on
plot(0:delta:1,Vo node2,'m')
title('Voltage vs time')
xlabel('time (s)')
ylabel('Voltage')
legend('input','output')
grid on
figure(9)
plot(0:delta:1,V node3,'b')
hold on
plot(0:delta:1,Vo node3,'m')
title('Voltage vs time')
xlabel('time (s)')
ylabel('Voltage')
legend('input','output')
grid on
% Convert to frequency domain by taking the fourier transform
step in = fft(V node1); %fft -> Fast fourier transform
P mag2 in = abs(step in/1000);
P 1 in = P mag2 in(1:1000/2+1);
P_1_in(2:end-1) = 2*P_1_in(2:end-1);
sample_f = (1/delta)*(0:(1000/2))/1000;
% Plot figure
figure(10)
plot(sample f,P 1 in,'b')
step out = fft(Vo node1);
P2 out = abs(step out/1000);
P1 out = P2 out(1:1000/2+1);
P1_out(2:end-1) = 2*P1_out(2:end-1);
sample f = (1/delta)*(0:(1000/2))/1000;
hold on
plot(sample f,P1 out,'m')
title('Frequency Content Step Input')
xlabel('Frequency (Hz)')
ylabel('Amplitude')
ylim([0 3])
```

```
legend('input','output')
grid on
% The fourier transform of the step input signal givess us a sinc function.
% This makes sense as we know that by taking the fourier transform of a step signal we
should get a sinc function.
% The High Frequency components are attenuated due to the fact that the filter
% is a low pass filter
step in = fft(V node2); %Take fourier transform
P mag2 in = abs(step_in/1000);
P_1_in = P_mag2_in(1:1000/2+1);
P 1 in(2:end-1) = 2*P 1 in(2:end-1); % Calculate singel ended spectrum
figure(11)
plot(sample f,P 1 in,'b')
grid on
step out = fft(Vo node2);
P2 out = abs(step out/1000);
P1_out = P2_out(1:1000/2+1);
P1 out(2:end-1) = 2*P1 out(2:end-1);
hold on
plot(sample f,P1 out,'m')
title('Frequency Content Sinusoidal Input')
xlabel('Frequency (Hz)')
ylabel('Amplitude')
ylim([0 3])
legend('input','output')
step in = fft(V node3); %Take fourier transform
P mag2 in = abs(step in/1000);
P 1 in = P mag2 in(1:1000/2+1);
P 1 in(2:end-1) = 2*P 1 in(2:end-1); % Calculate single ended spectrum
figure(12)
plot(sample f,P 1 in,'b')
grid on
step out = fft(Vo node3);
P2 out = abs(step out/1000);
P1_out = P2_out(1:1000/2+1);
P1 out(2:end-1) = 2*P1 out(2:end-1);
hold on
plot(sample f,P1 out,'m')
title('Frequency Content Gaussian Input')
```

```
xlabel('Frequency (Hz)')
ylabel('Amplitude')
ylim([0 3])
legend('input','output')
clc
clearvars
set(0,'DefaultFigureWindowStyle','docked')
R1 = 1;
R2 = 2;
R3 = 10;
R4 = 0.1;
Ro = 1000;
C = 0.25;
L = 0.2;
a = 100;
cn1 = 0.00001;
cn2 = 0.0001;
cn3 = 0.01;
C1(1,:)=[C-C000000];
C1(2,:)=[-C C O O O O O O];
C1(3,:)=[0 \ 0 \ cn1 \ 0 \ 0 \ 0 \ 0];
C1(4,:)=[0\ 0\ 0\ 0\ 0\ 0\ 0];
C1(5,:)=[00000000];
C1(6,:)=[0\ 0\ 0\ 0\ 0\ -L\ 0\ 0];
C1(7,:)=[0\ 0\ 0\ 0\ 0\ 0\ 0];
C1(8,:)=[00000000];
C1
C2(1,:)=[C-C000000];
C2(2,:)=[-C C O O O O O O];
C2(3,:)=[0 0 cn2 0 0 0 0 0];
C2(4,:)=[0 0 0 0 0 0 0 0];
C2(5,:)=[0\ 0\ 0\ 0\ 0\ 0\ 0];
C2(6,:)=[0\ 0\ 0\ 0\ 0\ -L\ 0\ 0];
C2(7,:)=[0\ 0\ 0\ 0\ 0\ 0\ 0];
C2(8,:)=[0\ 0\ 0\ 0\ 0\ 0\ 0];
```

```
C3(1,:)=[C-C000000];
C3(2,:)=[-C C O O O O O O];
C3(3,:)=[0 \ 0 \ cn3 \ 0 \ 0 \ 0 \ 0];
C3(4,:)=[0 0 0 0 0 0 0 0];
C3(5,:)=[0\ 0\ 0\ 0\ 0\ 0\ 0];
C3(6,:)=[0\ 0\ 0\ 0\ 0\ -L\ 0\ 0];
C3(7,:)=[0\ 0\ 0\ 0\ 0\ 0\ 0];
C3(8,:)=[0 0 0 0 0 0 0 0];
C3
G(1,:)=[1-1000001];
G(2,:)=[-1 1.5 0 0 0 1 0 0];
G(3,:)=[0 \ 0 \ 0.1 \ 0 \ 0 \ -1 \ 0 \ 0];
G(4,:)=[0\ 0\ 0\ 10\ -10\ 0\ 1\ 0];
G(5,:)=[0\ 0\ 0\ -10\ 10.0010\ 0\ 0\ 0];
G(6,:)=[0\ 1\ -1\ 0\ 0\ -L\ 0\ 0];
G(7,:)=[0\ 0\ -10\ 1\ 0\ 0\ 0\ 0];
G(8,:)=[10000000];
G
F = [
  0 ;
  0 ;
  0 ;
  0 ;
  0 ;
  0 ;
  0 ;
  0 ;
  ];
% Given these values from lab manual
delta = 0.001;
standard_deviation = 0.03;
d = 0.06;
```

```
m = 1;
c s = zeros(1,1000);
f_l = zeros(8,1,1000);
for i=1:1:1000
  f I(8,1,i) = \exp(-((i*delta - d)/standard deviation)^2);
  f_{l}(3,1,i) = -0.001*randn;
  c_s(i) = f_l(3,1,i);
end
VL 1 = zeros(8,1,1000);
VL 2 = zeros(8,1,1000);
VL 3 = zeros(8,1,1000);
for i = 2:1:1000
  index1 = C1/delta + G;
  index2 = C2/delta + G;
  index3 = C3/delta + G;
  VL_1(:,:,i) = index1\(C1*VL_1(:,:,i-1)/delta +f_l(:,:,i));
  VL 2(:,:,i) = index2\(C1*VL 2(:,:,i-1)/delta +f l(:,:,i));
  VL 3(:,:,i) = index3\(C1*VL 3(:,:,i-1)/delta +f l(:,:,i));
end
Vol_1(1,:) = Vl_1(5,1,:);
ViL_1(1,:) = VL_1(1,1,:);
Vol 2(1,:) = VL 2(5,1,:);
ViL 2(1,:) = VL 2(1,1,:);
VoL_3(1,:) = VL_3(5,1,:);
ViL_3(1,:) = VL_3(1,1,:);
figure(13)
plot((1:1000).*delta, VoL_1(1,:),'b')
hold on
plot((1:1000).*delta, ViL 1(1,:),'m')
title('Gaussian Pulse Function with added noise sources and cn1 = 0.00001')
```

```
xlabel('Time (s)')
ylabel('Voltage (v)')
grid on
legend('Output Voltage','Input Voltage')
hold off
figure(14)
histogram(c_s)
title('Noise Source Histogram')
grid on
xlabel('Current in amperes')
figure(15)
FF = abs(fftshift(fft(Vol 1(1,:))));
plot(((1:length(FF))/1000)-0.5,FF,'b')
xlabel('Frequency in hertz')
ylabel('Magnitude in decibels')
grid on
xlim([-0.04 \ 0.04])
title('Gaussian Pulse Function with added noise sources and cn1 = 0.00001(Fourier
Transform)')
% CN 2 -----
figure(16)
plot((1:1000).*delta, VoL_2(1,:),'b')
hold on
plot((1:1000).*delta, ViL 2(1,:),'m')
title('Gaussian Pulse Function with added noise sources and cn2 = 0.0001')
xlabel('Time in seconds')
ylabel('Voltage in volts')
grid on
legend('Output Voltage','Input Voltage')
hold off
figure(17)
FF = abs(fftshift(fft(VoL_2(1,:))));
plot(((1:length(FF))/1000)-0.5,FF,'m')
xlabel('Frequency in hertz')
ylabel('Magnitude in decibels')
```

```
grid on
xlim([-0.04 0.04])
title('Gaussian Pulse Function with added noise sources and cn2 = 0.0001(Fourier
Transform)')
figure(18)
plot((1:1000).*delta, VoL_3(1,:),'b')
hold on
plot((1:1000).*delta, ViL 3(1,:),'m')
title('Gaussian Pulse Function with Added Noise Source and cn3 = 0.01')
xlabel('Time in seconds')
ylabel('Voltage in volts')
grid on
legend('Output Voltage','Input Voltage')
hold off
figure(19)
FF = abs(fftshift(fft(Vol 3(1,:))));
plot(((1:length(FF))/1000)-0.5,FF,'m')
xlabel('Frequency in hertz')
ylabel('Magnitude in decibels')
grid on
xlim([-0.04 0.04])
title('Gaussian Pulse Function added Noise and cn3 = 0.01 (Fourier Transform)')
% Varying timestep
%Varying timestep:
clc
clear
clearvars
set(0,'DefaultFigureWindowStyle','docked')
R1 = 1;
R2 = 2;
C = 0.25;
L = 0.2;
R3 = 10;
a = 100;
R4 = 0.1;
R0 = 1000;
G = zeros(7,7);
```

```
C_{mat} = zeros(7,7);
G(1,1) = 1;
G(2,1) = -1/R1;
G(2,2) = 1/R1 + 1/R2;
G(2,6) = 1;
G(3,3) = 1/R3;
G(3,6) = -1;
G(4,3) = 1/R3;
G(4,7) = -1;
G(5,4) = -1/R4;
G(5,5) = 1/R4 + 1/R0;
G(6,2) = 1;
G(6,3) = -1;
G(7,4) = 1;
G(7,7) = -a;
C mat(2,1) = -C;
C_{mat(2,2)} = C;
C_{mat}(6,6) = -L;
G
C mat
F = zeros(7,1);
V = zeros(7,1);
%Circuit with noise
In = 0.001; % as provided in assignment manual
Cn = 0.00001; % as provided in assignment manual
C \text{ mat}(3,3) = Cn;
G
C_mat
delta = 0.001;
A_transpse = C_mat/delta + G;
F = zeros(7,1);
V = zeros(7,1);
Vo_index(1) = 0;
Vi_index(1) = 0;
```

```
ii = 1;
for t = delta:delta:1
  F(1) = \exp(-0.5*((t - 0.06)/0.03)^2);
  F(3) = In*normrnd(0,1);
  V = A transpse(C mat*V/delta + F);
  Vi index(ii + 1) = F(1);
  Vo_index(ii + 1) = V(5);
  ii = ii + 1;
end
X input = fft(Vi index);
P2 input = abs(X input/1000);
P1 input = P2 input(1:1000/2+1);
P1 input(2:end-1) = 2*P1 input(2:end-1);
f = (1/delta)*(0:(1000/2))/1000;
X output = fft(Vo index);
P2 output = abs(X output/1000);
P1_output = P2_output(1:1000/2+1);
P1 output(2:end-1) = 2*P1 output(2:end-1);
f = (1/delta)*(0:(1000/2))/1000;
C sml = C mat;
C med = C mat;
C_big = C_mat;
C_sml(3,3) = 0;
C_{med}(3,3) = 0.001;
C big(3,3) = 0.1;
V \text{ sml} = zeros(7,1);
V med = zeros(7,1);
V big = zeros(7,1);
Vo sml(1) = 0;
Voutput_med(1) = 0;
Vout big(1) = 0;
Vi index(1) = 0;
ii = 1;
for t = delta:delta:1
  F(1) = \exp(-0.5*((t - 0.06)/0.03)^2);
  F(3) = In*normrnd(0,1);
  V sml = (C sml/delta + G)(C sml*V sml/delta + F);
```

```
V \text{ med} = (C \text{ med/delta} + G)(C \text{ med*}V \text{ med/delta} + F);
   V big = (C_big/delta + G)\(C_big*V_big/delta + F);
   Vo sml(ii + 1) = V sml(5);
   Voutput med(ii + 1) = V med(5);
   Vout big(ii + 1) = V big(5);
   Vi index(ii + 1) = F(1);
   ii = ii + 1;
end
delta1 = 0.01;
Vinput SmlStep(1) = 0;
Voutput SmlStep(1) = 0;
V = zeros(7,1);
ii = 1;
for t = delta1:delta1:1
   F(1) = \exp(-0.5*((t - 0.06)/0.03)^2);
   F(3) = In*normrnd(0,1);
   V = (C \text{ mat/delta1} + G) (C \text{ mat*V/delta1} + F);
   Voutput SmlStep(ii + 1) = V(5);
   Vinput SmlStep(ii + 1) = F(1);
   ii = ii + 1;
end
delta2 = 0.1;
Vinput_bigStep(1) = 0;
Voutput_bigStep(1) = 0;
V = zeros(7,1);
ii = 1;
for t = delta2:delta2:1
   F(1) = \exp(-0.5*((t - 0.06)/0.03)^2);
   F(3) = In*normrnd(0,1);
   V = (C \text{ mat/delta2} + G) (C \text{ mat*V/delta2} + F);
   Voutput_bigStep(ii + 1) = V(5);
   Vinput bigStep(ii + 1) = F(1);
   ii = ii + 1;
end
figure(20)
plot(0:delta1:1,Vinput SmlStep,'b')
hold on
```

```
plot(0:delta1:1,Voutput_SmlStep,'m')
title('Voltage vs time with timestep = 0.003')
xlabel('time (s)')
ylabel('Voltage')
legend('input','output')
grid on

figure(21)
plot(0:delta2:1,Vinput_bigStep,'m')
hold on
plot(0:delta2:1,Voutput_bigStep,'b')
title('Voltage vs time with time step = 0.01')
xlabel('time (s)')
ylabel('Voltage')
legend('input','output')
grid on
```