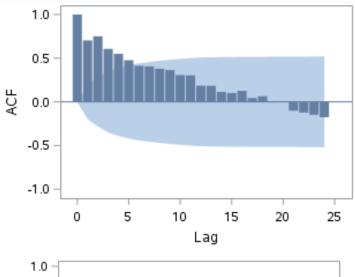
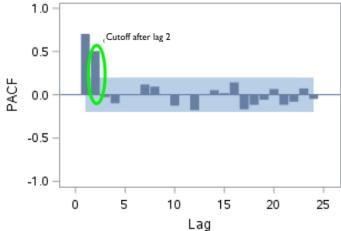


# Homework 2

#### PROBLEM 1)

|        | Autocorrelation Check for White Noise |    |            |                  |       |        |        |        |        |  |  |
|--------|---------------------------------------|----|------------|------------------|-------|--------|--------|--------|--------|--|--|
| To Lag | Chi-Square                            | DF | Pr > ChiSq | Autocorrelations |       |        |        |        |        |  |  |
| 6      | 225.32                                | 6  | <.0001     | 0.703            | 0.750 | 0.607  | 0.549  | 0.476  | 0.413  |  |  |
| 12     | 299.96                                | 12 | <.0001     | 0.406            | 0.379 | 0.364  | 0.307  | 0.303  | 0.185  |  |  |
| 18     | 309.40                                | 18 | <.0001     | 0.184            | 0.114 | 0.101  | 0.126  | 0.043  | 0.064  |  |  |
| 24     | 319.78                                | 24 | <.0001     | -0.006           | 0.002 | -0.101 | -0.122 | -0.148 | -0.176 |  |  |

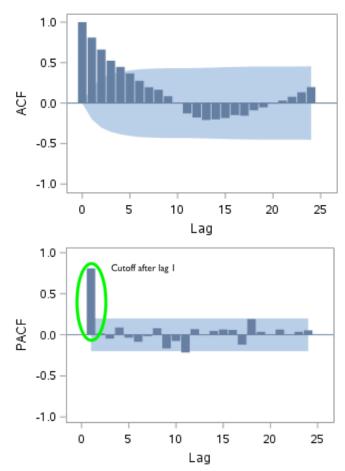




This series was generated by an AR(2) process because the ACF seems to decay exponentially to zero and the PACF has a cutoff after lag 2.

## PROBLEM 2)

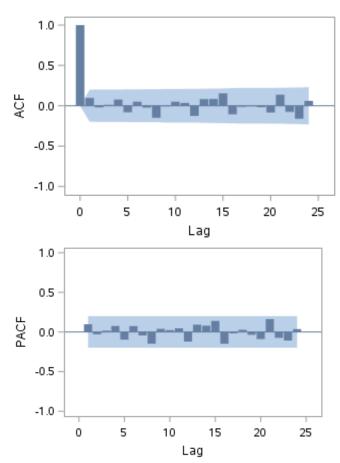
|        | Autocorrelation Check for White Noise |    |            |                  |        |        |        |        |        |  |  |
|--------|---------------------------------------|----|------------|------------------|--------|--------|--------|--------|--------|--|--|
| To Lag | Chi-Square                            | DF | Pr > ChiSq | Autocorrelations |        |        |        |        |        |  |  |
| 6      | 187.68                                | 6  | <.0001     | 0.810            | 0.661  | 0.525  | 0.447  | 0.367  | 0.275  |  |  |
| 12     | 201.34                                | 12 | <.0001     | 0.196            | 0.164  | 0.085  | 0.007  | -0.127 | -0.178 |  |  |
| 18     | 222.08                                | 18 | <.0001     | -0.208           | -0.201 | -0.184 | -0.148 | -0.155 | -0.089 |  |  |
| 24     | 231.02                                | 24 | <.0001     | -0.053           | -0.007 | 0.031  | 0.078  | 0.133  | 0.198  |  |  |



This series was generated by an **AR(1)** process because the ACF seems to decay exponentially to zero and the PACF has a cutoff after lag 1.

#### PROBLEM 3)

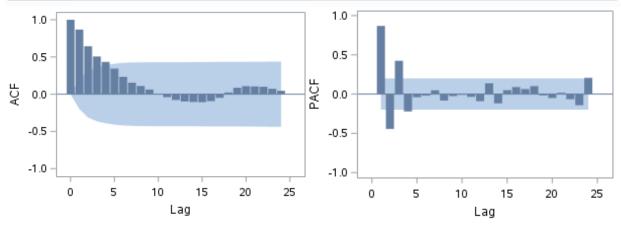
|        | Autocorrelation Check for White Noise |    |            |                  |        |        |        |        |        |  |  |
|--------|---------------------------------------|----|------------|------------------|--------|--------|--------|--------|--------|--|--|
| To Lag | Chi-Square                            | DF | Pr > ChiSq | Autocorrelations |        |        |        |        |        |  |  |
| 6      | 2.66                                  | 6  | 0.8498     | 0.097            | -0.019 | 0.012  | 0.078  | -0.080 | 0.051  |  |  |
| 12     | 7.46                                  | 12 | 0.8260     | -0.023           | -0.149 | -0.008 | 0.051  | 0.035  | -0.125 |  |  |
| 18     | 13.38                                 | 18 | 0.7684     | 0.083            | 0.084  | 0.154  | -0.105 | -0.013 | -0.008 |  |  |
| 24     | 21.44                                 | 24 | 0.6126     | -0.017           | -0.084 | 0.137  | -0.076 | -0.160 | 0.061  |  |  |



This series was generated by **random shocks**. By looking at the PACF and ACF, it is difficult to define which process was used. However, when we check the Autocorrelation Check for White Noise chart, we can observe that all the p-values are above 0.05 meaning that all this series was generated by random shocks.

### PROBLEM 4)

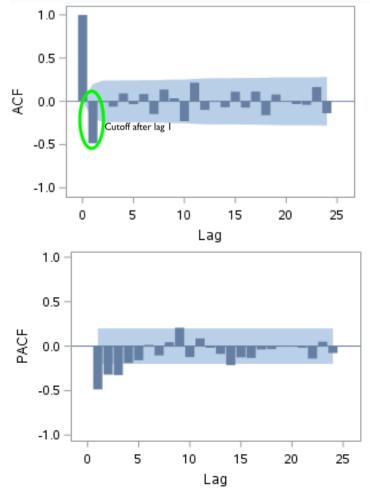
|        | Autocorrelation Check for White Noise |    |            |                  |        |        |        |        |        |  |  |
|--------|---------------------------------------|----|------------|------------------|--------|--------|--------|--------|--------|--|--|
| To Lag | Chi-Square                            | DF | Pr > ChiSq | Autocorrelations |        |        |        |        |        |  |  |
| 6      | 188.16                                | 6  | <.0001     | 0.868            | 0.644  | 0.506  | 0.434  | 0.344  | 0.233  |  |  |
| 12     | 193.48                                | 12 | <.0001     | 0.154            | 0.110  | 0.062  | 0.005  | -0.040 | -0.078 |  |  |
| 18     | 198.69                                | 18 | <.0001     | -0.098           | -0.104 | -0.107 | -0.093 | -0.048 | 0.023  |  |  |
| 24     | 204.85                                | 24 | <.0001     | 0.087            | 0.108  | 0.104  | 0.100  | 0.073  | 0.046  |  |  |



Both graphs(ACF and PACF) appear to be exponentially decaying to zero with the PACF graph alternating between positive and negative numbers. I classify this series as being generated by an **ARMA(1,1)** process.

## PROBLEM 5)

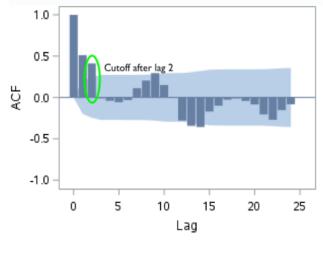
|        | Autocorrelation Check for White Noise |    |            |                  |        |        |        |        |        |  |  |
|--------|---------------------------------------|----|------------|------------------|--------|--------|--------|--------|--------|--|--|
| To Lag | Chi-Square                            | DF | Pr > ChiSq | Autocorrelations |        |        |        |        |        |  |  |
| 6      | 26.76                                 | 6  | 0.0002     | -0.486           | -0.009 | -0.062 | 0.092  | -0.032 | 0.085  |  |  |
| 12     | 43.88                                 | 12 | <.0001     | -0.146           | 0.136  | 0.035  | -0.230 | 0.215  | -0.099 |  |  |
| 18     | 51.37                                 | 18 | <.0001     | 0.004            | -0.069 | 0.111  | -0.073 | 0.113  | -0.160 |  |  |
| 24     | 58.71                                 | 24 | <.0001     | 0.080            | -0.002 | -0.032 | -0.040 | 0.165  | -0.137 |  |  |

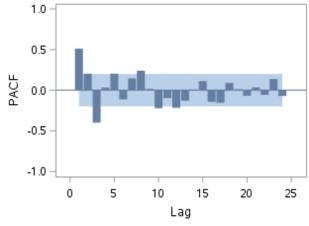


This series was generated by a **MA(1)** because the ACF has a cutoff after lag 1 and the PACF seems to decay exponentially to zero.

## PROBLEM 6)

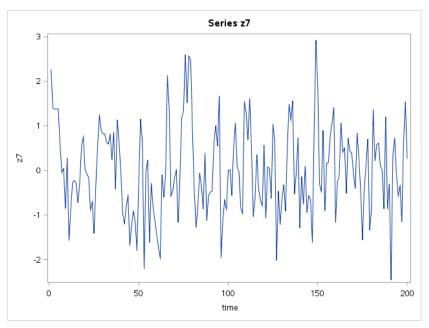
|        | Autocorrelation Check for White Noise |    |            |                  |        |        |        |        |        |  |  |
|--------|---------------------------------------|----|------------|------------------|--------|--------|--------|--------|--------|--|--|
| To Lag | Chi-Square                            | DF | Pr > ChiSq | Autocorrelations |        |        |        |        |        |  |  |
| 6      | 45.68                                 | 6  | <.0001     | 0.512            | 0.412  | -0.010 | -0.039 | -0.057 | -0.030 |  |  |
| 12     | 73.20                                 | 12 | <.0001     | 0.112            | 0.204  | 0.294  | 0.151  | -0.006 | -0.279 |  |  |
| 18     | 107.24                                | 18 | <.0001     | -0.343           | -0.358 | -0.170 | -0.100 | -0.026 | -0.012 |  |  |
| 24     | 127.51                                | 24 | <.0001     | -0.042           | -0.085 | -0.205 | -0.270 | -0.153 | -0.083 |  |  |





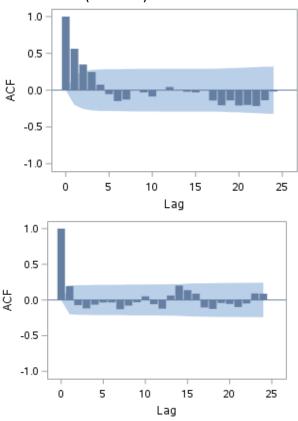
This series was generated by a **MA(2)** because the ACF has a cutoff at lag 2 and the PACF seems decay exponentially to zero alternating between positive and negative numbers

## PROBLEM 7)



ACF for first half of the observations(1-100) observations(101-200)

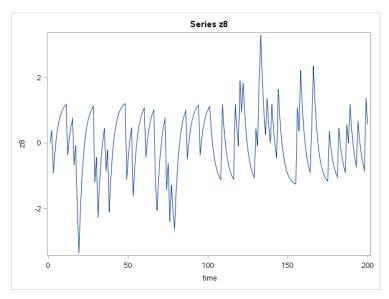
ACF for second half of the



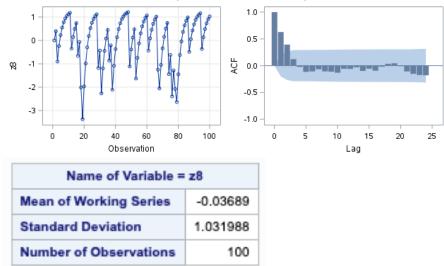
(d) Does not have a constant ACF.

The graph seems to indicate a constant mean and variance but we can observe that the ACF for the first half of the series(observations 1-100) is different from the ACF from the other half of the series(observations101-200 indicating the ACF is not constant throughout this series

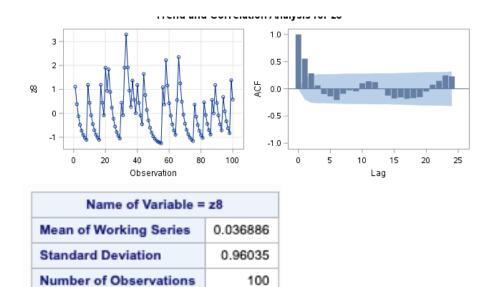
### PROBLEM 8)



First half of times series z8(observations 1-100):



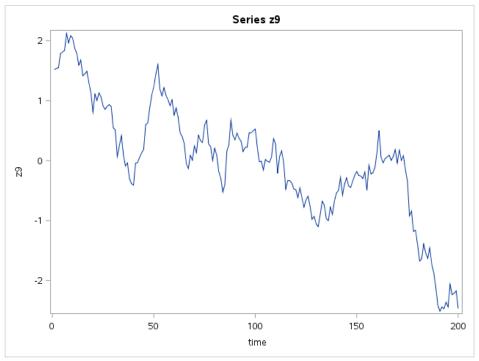
Second half of times series z8(observations 101-200):



#### (e) Is weakly stationary, but not strictly stationary

We can observe that this graph seems to have a constant variance, mean and ACF in both halves of the series but the behavior seems different on both halves so it is weakly stationary.

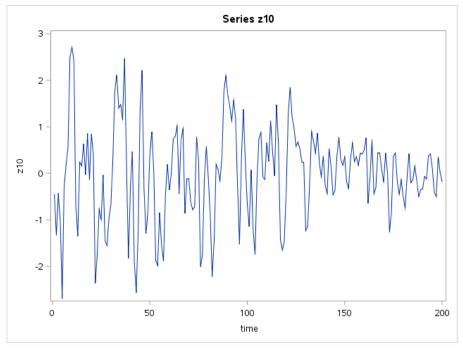
### PROBLEM 9)



(b)Does not have a constant mean.

The graph does not seem to have a spread around 0 with values decreasing over time meaning the mean is not constant throughout the series.

#### PROBLEM 10)

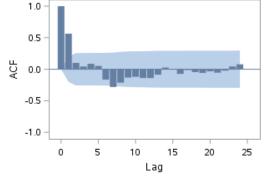


First half of series (observations 1 to 100):



#### The ARIMA Procedure

| Name of Variable =     | z10      |
|------------------------|----------|
| Mean of Working Series | -0.05642 |
| Standard Deviation     | 1.244017 |
| Number of Observations | 100      |

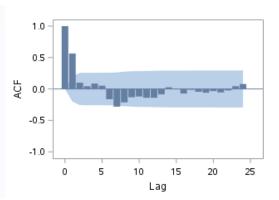


Second half of series (observations 101 to 200):

#### Series z10, observations 101 to 200

#### The ARIMA Procedure

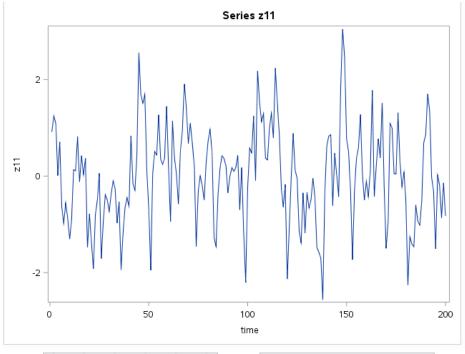
| Name of Variable =     | z10      |
|------------------------|----------|
| Mean of Working Series | 0.056416 |
| Standard Deviation     | 0.660357 |
| Number of Observations | 100      |

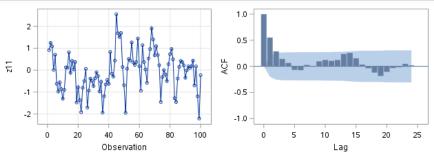


(c) Does not have a constant variance.

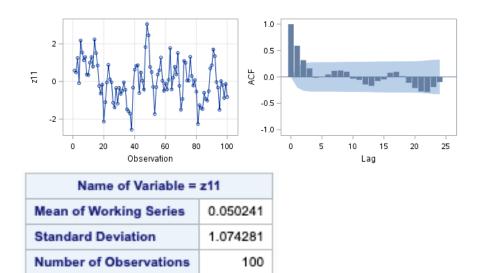
The mean and ACF seems to be constant and the time series graph display a spread around 0 throughout the entire series. However, the trend indicates that the variance gets smaller over time. Using the standard deviation from both halves, we can observe that the second half has a variance ½ times smaller than the first half which is in accordance with what the graph displays therefore the variance is not constant.

# PROBLEM 11)





| Name of Variable = z11          |          |  |  |  |  |
|---------------------------------|----------|--|--|--|--|
| Mean of Working Series -0.05025 |          |  |  |  |  |
| Standard Deviation              | 0.911515 |  |  |  |  |
| Number of Observations          | 100      |  |  |  |  |



#### (a) Stationary

The mean, ACF and variance are constant and the behavior seems to be the same on throughout all the so this series is stationary.

#### SAS Code

```
/* Problems 1-6 */
filename what "/home/eff100/my_courses/huffer/hw2p1_data.txt";
data hw2p1;
infile what;
input z1-z6;
run;
/* The following code will produce the usual items
 used to "identify" an ARMA model for a time series.
 This will be done for each of the series z1 to z6. */
proc arima data=hw2p1;
identify var=z1; /* Problem 1 */
identify var=z2; /* Problem 2 */
identify var=z3; /* Problem 3 */
identify var=z4; /* Problem 4 */
identify var=z5; /* Problem 5 */
identify var=z6; /* Problem 6 */
run;
/* Problems 7-11 */
filename what "/home/eff100/my_courses/huffer/hw2p2_data.txt";
data look;
infile what;
time= n;
input z7-z11;
run;
/* Problem 7 */
/* Creating time series plots for z7 to z11. */
title "Series z7";
proc sgplot data=look;
series x=time y=z7;
run;
/* Splitting series z7 into half */
title "Series z7, observations 1 to 100";
proc arima data=look(firstobs=1 obs=100);
identify var=z7;
run;
title "Series z7, observations 101 to 200";
proc arima data=look(firstobs=101 obs=200);
identify var=z7;
run;
/* Problem 8 */
title "Series z8";
proc sgplot data=look;
series x=time y=z8;
/* Splitting series z8 into half */
title "Series z8, observations 1 to 100";
proc arima data=look(firstobs=1 obs=100);
identify var=z8;
run;
```

```
title "Series z8, observations 101 to 200";
proc arima data=look(firstobs=101 obs=200);
identify var=z8;
run;
/* Problem 9 */
title "Series z9";
proc sgplot data=look;
series x=time y=z9;
run;
/* Problem 10 */
title "Series z10";
proc sgplot data=look;
series x=time y=z10;
run;
/* Splitting series z10 into half */
title "Series z10, observations 1 to 100";
proc arima data=look(firstobs=1 obs=100);
identify var=z10;
run;
title "Series z10, observations 101 to 200";
proc arima data=look(firstobs=101 obs=200);
identify var=z10;
run;
/* Problem 11 */
title "Series z11";
proc sgplot data=look;
series x=time y=z11;
run;
/* Splitting series z11 into half */
title "Series z11, observations 1 to 100";
proc arima data=look(firstobs=1 obs=100);
identify var=z11;
run;
title "Series z11, observations 101 to 200";
proc arima data=look(firstobs=101 obs=200);
identify var=z11;
run;
```