

Homework 2 (70pts)

For full credit, show your work.

Formatting (6pts)

Single file, in pdf format.

Definitions (8pts)

- a. Informed Player
- b. Mixed Strategy
- c. Strictly Dominated Strategy
- d. Explain why you wouldn't want to include a strictly dominated strategy in a mixed strategy.

Problem #1 Graphing Payouts When Strategies are Mixed (12 pts)

For each of the following game tables,

- I. Eliminate any strictly dominated strategies. Also, state which strategy is dominated and by what.
- II. Graph player 1's pure strategy payouts if player 2 uses a mixed strategy.

a)

		Player 2	
		S	T
Player 1	F	7, 3	2, 4
	G	5, 2	6, 1
	H	6, 1	5, 4

b)

		Player 2	
		X	Y
Player 1	A	2, 3	6, 1
	B	4, 2	1, 3
	C	3, 1	2, 4

c)

		Player 2		
		Left	Center	Right
Player 1	Top	3, 1	3, 1	0, 2
	Middle	1, 2	2, 1	1, 2
	Bottom	0, 2	3, 0	3, 1

Problem #2 Mixed-Strategy Nash Equilibrium (16 points)

For each of the following game tables, find all Nash equilibria.

a)

		Daffy	
		Duck	Rabbit
Bugs	Duck	-2, 1	0, 0
	Rabbit	0, 0	1, -2

b)

		Buzz	
		Bail	Drive
Jim	Bail	0, 0	-1, 1
	Drive	1, -1	-10, -10

Problem #3: States of nature (12 points)

Consider the following variant of the Prisoner's Dilemma: Guido and Luca work for a mob boss named Vito, who is unpredictable. Vito is not a player in this game, but when Guido and Luca are arrested, Vito may be Nice, with probability p , or Nasty, with probability $1 - p$. Game tables for the two states are shown below:

Vito is Nice (p)				Vito is Nasty ($1 - p$)			
		Luca				Luca	
		Testify	Quiet			Testify	Quiet
Guido	Testify	-10, -10	0, -20	Guido	Testify	-40, -40	-20, -20
	Quiet	-20, 0	-1, -1		Quiet	-20, -20	-1, -1

- a) First, assume that $p = 0.5$, so that Vito is equally likely to be Nice or Nasty. Combine these two game tables into one table containing Guido and Luca's expected payoffs, then find all of the pure-strategy Nash equilibria in this game.

- b) Now, assume that p is unknown. Once again, combine the two game tables into one table containing Guido and Luca's expected payoffs. **(Hint: These expected payoffs will have to be written in terms of p .)**

- c) Based on your answer to b), for what values of p is (Quiet, Quiet) a Nash equilibrium?

Problem #4 Pure Strategy Bayesian Nash Equilibrium (16pts)

Suppose player 1 knows there exists a probability distribution over states with some unknown value p , and player 2 knows which state is going to be realized.

What are the possible pure strategy BNEs? Dr. Wu (University at Oregon)

		Good (p)				Bad (1-p)		
		player 2				player 2		
		C	D			C	D	
player 1	A	(2,2)	(0,0)			A	(2,2)	(4,0)
	B	(0,0)	(3,3)			B	(0,4)	(3,3)