

### Homework Assignment #6

1. Find the  $z$  transform of each of the following sequences.

$$(a) \quad f(k) = 2\delta(k) - \delta(k-2) = \begin{cases} 2, & k = 0 \\ -1, & k = 2 \\ 0 & \text{otherwise} \end{cases}$$

$$(b) \quad f(k) = \begin{cases} 0, & k < 0 \\ 1, & 0 \leq k \leq 5. \\ 2^{k-5}, & k \geq 5 \end{cases}$$

$$(c) \quad f(k) = \{2, 2, 0, -1, -1, -1, 2, 2, 0, -1, -1, -1, 2, 2, 0, -1, -1, -1, \dots\}.$$

[Hint: Express  $f(k)$  as the sum of shifted, identical, finite sequences.]

$$(d) \quad f(k) = \begin{cases} 2, & k \text{ odd} \\ 0, & k \text{ even.} \\ 0, & k \leq 0 \end{cases}$$

$$(e) \quad f(k) = a^{k-1}u_s(k-1) + \frac{1}{a}\delta(k)$$

2. Find the  $z$  transform of each of the following sequences.

$$(a) \quad f(k) = (0.5)^k \cos(k \frac{\pi}{4})u_s(k).$$

$$(b) \quad f(k) = (0.5)^{(k-2)} \cos((k-2) \frac{\pi}{4})u_s(k-2).$$

$$(c) \quad f(k) = (0.5)^k \cos(k \frac{\pi}{4})u_s(k-2).$$

$$(d) \quad f(k) = [(0.2)^k + (-2)^{k-1}]u_s(k).$$

$$(e) \quad f(k) = (0.2)^k u_s(k) + (-2)^{k-1} u_s(k-1).$$