$$x(t) = \begin{cases} 2At, & 0 \le t \le T/2 \\ -2A(t-T), & T/2 \le t \le T \end{cases}$$

$$\alpha_0 = \frac{1}{T} \int_0^T x(t) dt = \frac{2A}{T} \left[\int_0^{T/2} t dt - \int_{T/2}^T (t - T) dt \right] = \frac{AT}{2}$$

$$\alpha_{n} = \frac{1}{T} \int_{0}^{T} x(t) e^{jn2\pi t/T} dt = \frac{2A}{T} \left[\int_{0}^{T/2} t e^{jn2\pi t/T} dt - \int_{T/2}^{T} (t-T) e^{jn2\pi t/T} dt \right] = \begin{cases} -2AT/n^{2}\pi^{2}, & n \text{ odd} \\ 0, & n \text{ even, } n \neq 0 \end{cases}$$

(A lot of combinations and cancellations occur in this one.)

$$x(t) = \begin{cases} A\sin(2\pi t/T), & 0 \le t \le T/2 \\ 0, & T/2 \le t \le T \end{cases}$$

$$\alpha_0 = \frac{1}{T} \int_0^T x(t) dt = \frac{A}{T} \int_0^{T/2} \sin(2\pi t/T) dt = \frac{A}{\pi}$$

$$\alpha_{n} = \frac{1}{T} \int_{0}^{T} x(t) e^{jn2\pi/T} dt = \frac{A}{T} \int_{0}^{T/2} \sin(2\pi t/T) e^{jn2\pi/T} dt = \frac{A}{j2T} \int_{0}^{T/2} \left[e^{j2\pi/T} - e^{-j2\pi/T} \right] e^{jn2\pi/T} dt$$

$$= \begin{cases} -A/\pi (n^{2} - 1), & n \text{ even} \\ 0, & n \text{ odd} \end{cases}$$

(Again, some convenient combinations occur.)

$$x_{5}(t) = \frac{4}{\pi} \sum_{n=1}^{5} \frac{1}{2n-1} \sin(2\pi(2n-1)t)$$

$$x_{10}(t) = \frac{4}{\pi} \sum_{n=1}^{10} \frac{1}{2n-1} \sin(2\pi(2n-1)t)$$

$$x_{15}(t) = \frac{4}{\pi} \sum_{n=1}^{10} \frac{1}{2n-1} \sin(2\pi(2n-1)t)$$

$$x_{15}(t) = \frac{4}{\pi} \sum_{n=1}^{15} \frac{1}{2n-1} \sin(2\pi(2n-1)t)$$

$$x(t) = \sum_{\substack{n=-\infty\\n\neq 0}}^{\infty} \frac{(-1)^n}{jn} e^{jn2\pi/T}$$

$$= \sum_{n=1}^{\infty} \frac{(-1)^n}{jn} \left[e^{jn2\pi/T} - e^{-jn2\pi/T} \right]$$

$$= \sum_{n=1}^{\infty} \frac{2(-1)^n}{n} \sin(n2\pi t/T)$$
Fourier Series Partial Sum

$$\begin{bmatrix} \frac{1}{n} & \frac{1}{n} & \frac{1}{n} \\ \frac{1}{n} & \frac{1}{n} \end{bmatrix}$$

$$x(t) = \sum_{\substack{n = -\infty \\ n \neq 0}}^{\infty} \frac{(-1)^n}{n^2} e^{jn2\pi t/T}$$
$$= \sum_{n=1}^{\infty} \frac{(-1)^n}{n^2} \left[e^{jn2\pi t/T} + e^{-jn2\pi t/T} \right]$$
$$= \sum_{n=1}^{\infty} \frac{2(-1)^n}{n^2} \cos(n2\pi t/T)$$

