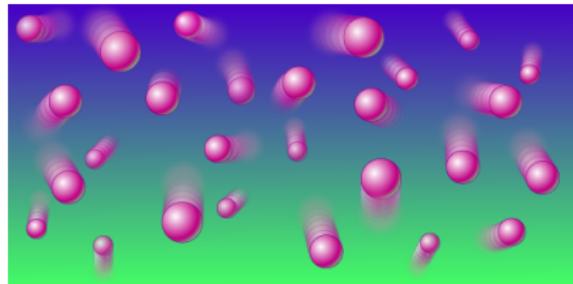


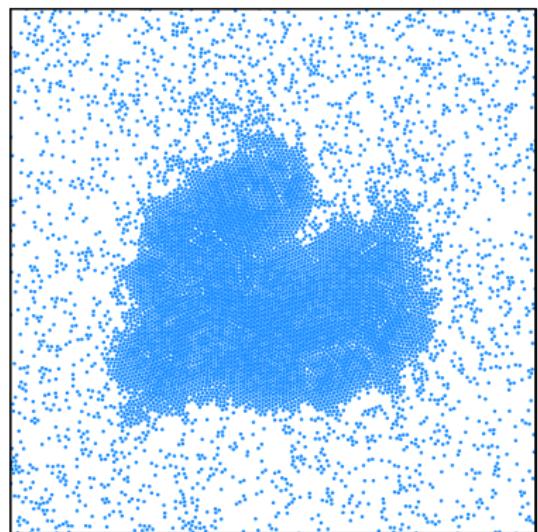
Nonequilibrium soft and active matter

Dpt of Physics and Materials Science

University of Luxembourg



"In, Yet Out of Equilibrium" Physics (2016)



Soft condensed matter

From passive to biological materials

Structure at mesoscale

Sensitivity to thermal energy

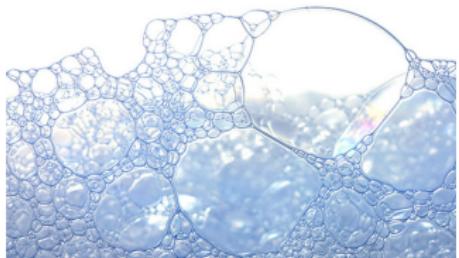
Colloids and Liquid Crystals

Prof Scalia, Winter Sem

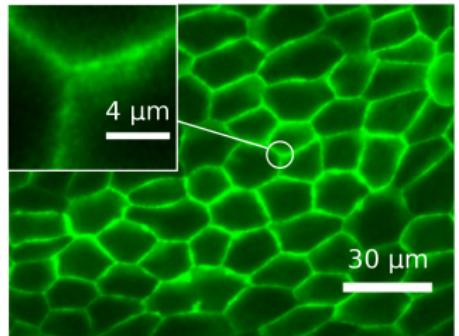
Physics of Living Matter

Prof Sengupta, Summer Sem

Bubble foam



Cell tissue

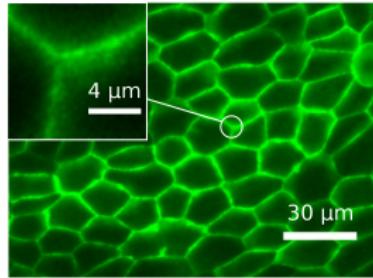


Active matter across scales

Consume energy to produce nonequilibrium forces

Cell assemblies

ÉF et al, Biophys J 114, 939 (2018)



Animal groups

Bialek et al, PNAS 109, 4786 (2012)



Human crowds

Bain et al, Science 363, 6422 (2019)



→ Scale

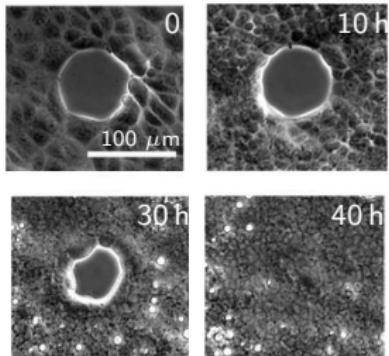
Active matter across domains

From biological and social applications

... to synthetic systems

Wound healing

Niera *et al*, PNAS 112, 9546 (2015)



How to improve
wound recovery?

Crowd management

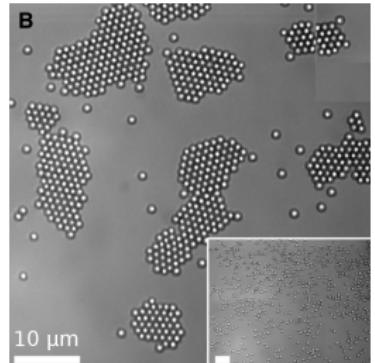
Bottinelli *et al*, PRL 117, 228301 (2016)



How to prevent
crowd disaster?

Colloidal self-assembly

Palacci *et al*, Science 339, 936 (2013)



How to assemble
synthetic colloids?

Statistical mechanics of active matter

How to control the emerging collective behavior?

- ▶ Transition in passive matter: Assembly of water molecules



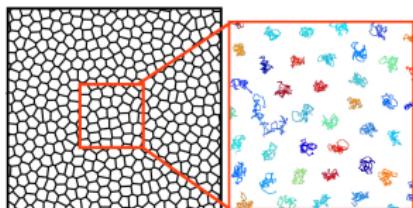
Solid



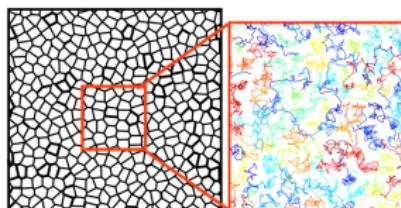
Liquid

→ Temperature

- ▶ Transition in active matter: Assembly of cells [Bi *et al*, PRX 6, 021011 (2016)]



Solid



Liquid

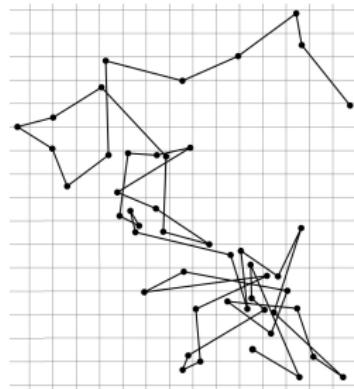
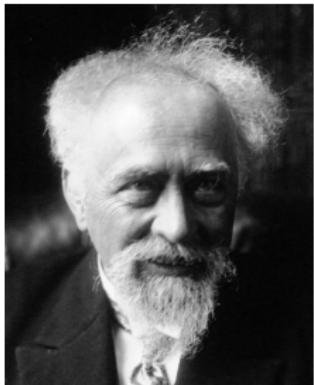
→ Energy fuel

Experiments on fluctuating systems

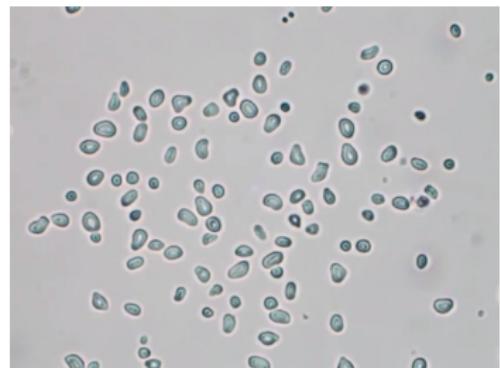
Passive systems: Equilibrium dynamics

Tracers in a viscous solvent

Jean Perrin (Nobel Prize, 1926)



Pollen grains in water

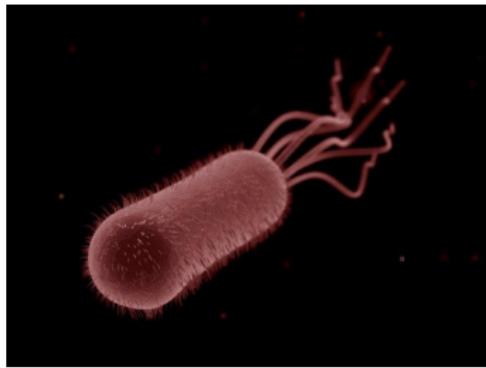


Experiments on fluctuating systems

Active systems: Nonequilibrium dynamics

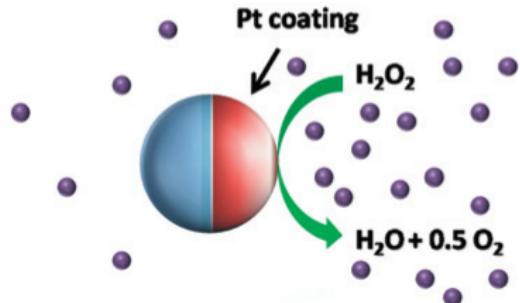
Extract energy to produce directed motion

Biological swimmers



Turner, Ryu, Berg,
J Bacteriol 182, 2793 (2000)

Synthetic active colloids

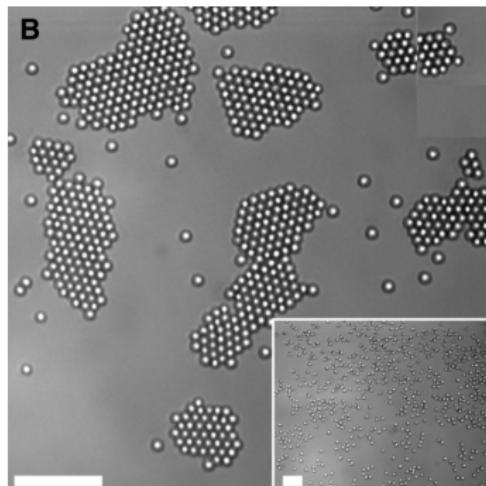


Walther, Müller,
Soft Matter Review 4, 663 (2008)

Experiments on fluctuating systems

Collective dynamics of active particles

Clustering of colloids



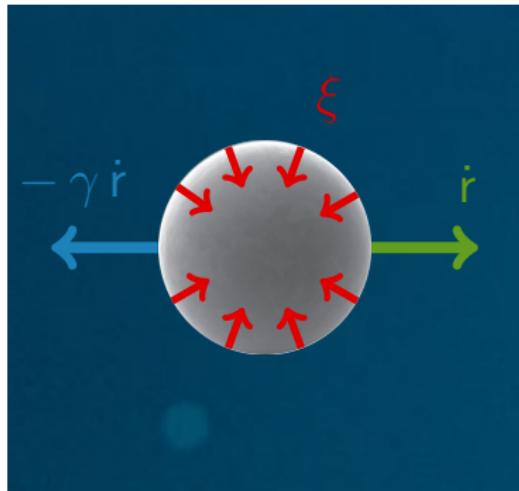
Palacci, Sacanna, Steinberg, Pine, Chaikin,
Science **339**, 936 (2013)

Flocking of birds



Bialek, Cavagna, Giardina, Mora, Silvestri,
Viale, Walczak, PNAS **109**, 4786 (2012)

Modelling passive fluctuations



Langevin equation

Effective tracer dynamics

$$m \ddot{\vec{r}} = -\nabla U - \gamma \dot{\vec{r}} + \xi$$

Equilibrium fluctuations

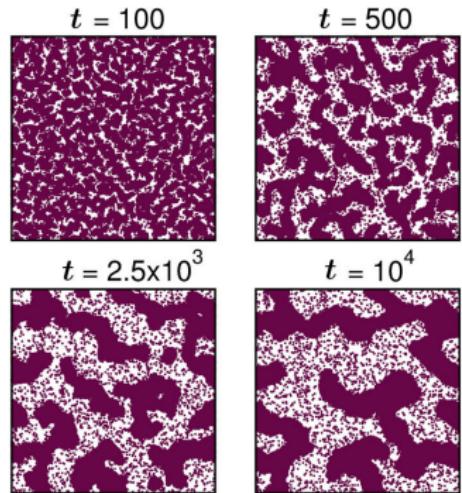
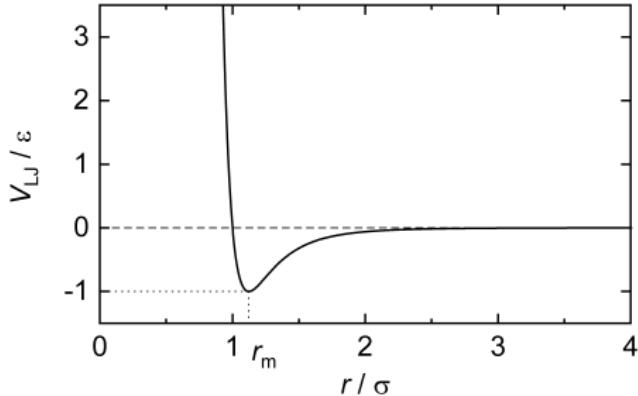
$$\langle \xi(t) \xi(0) \rangle = 2 \gamma T \delta(t)$$

Fluctuating energy $E = U + m \dot{\vec{r}}^2 / 2$

Boltzmann distribution $P_s \sim e^{-E/T}$

Modelling passive fluctuations

Repulsion and attraction



Equation of state: Connecting thermodynamic observables

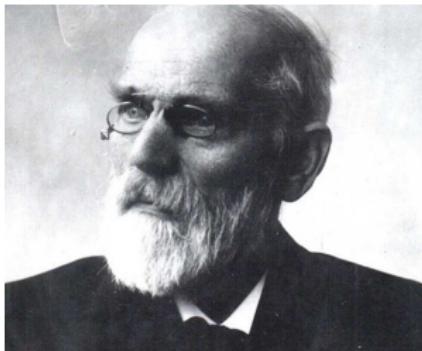
pressure P , temperature T , density ρ

e.g. law of ideal gas $P = \rho T$

Modelling passive fluctuations

Equilibrium phase transitions

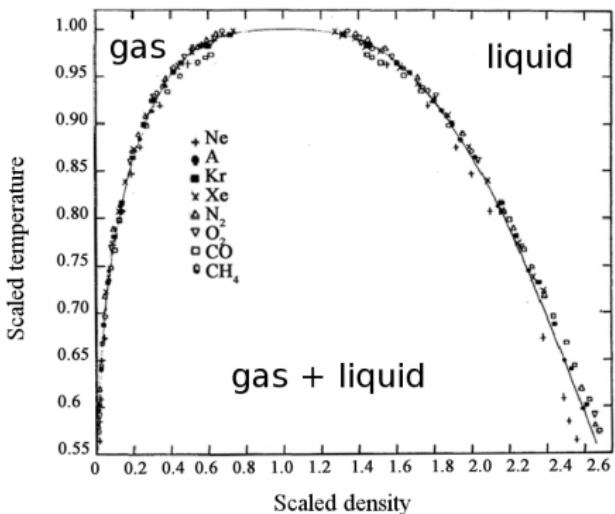
Johannes van der Waals
(Nobel Prize, 1910)



Equation of state

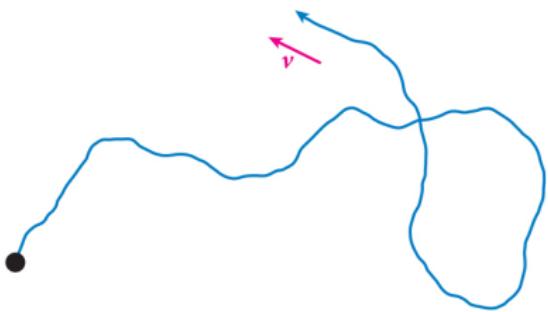
$$(P + a\rho^2)(1 - b\rho) = \rho T$$

Law of corresponding state



Guggenheim, J Chem Phys 13, 253 (1945)

Modelling active fluctuations



Langevin equation

$$m \ddot{r} = -\nabla U - \gamma \dot{r} + \xi + f_a$$

Non-equilibrium fluctuations

$$\langle f_a(t) f_a(0) \rangle = \frac{\gamma T_a}{\tau} e^{-|t|/\tau}$$

Persistence time τ

(a)



(b)



(c)



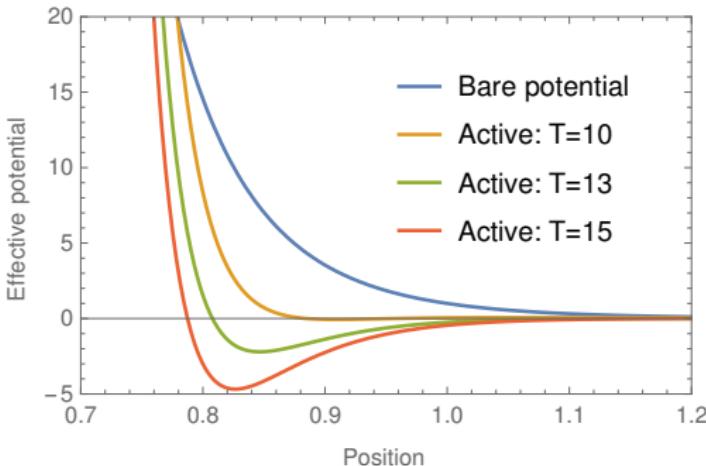
(d)



Modelling active fluctuations

Effective potential $U_{\text{eff}} = -T_A \ln P_S$

$$U_{\text{eff}} = U + \frac{\tau}{\gamma} \left[\frac{(\nabla U)^2}{2} - T_A \nabla^2 U \right]$$



Repulsive bare potential

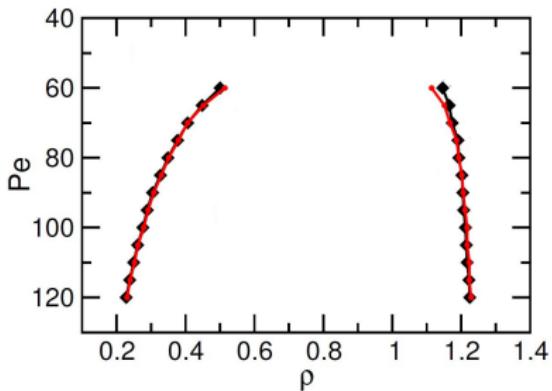
$$U \sim 1/r^{12}$$

Effective attraction in U_{eff}
due to persistence

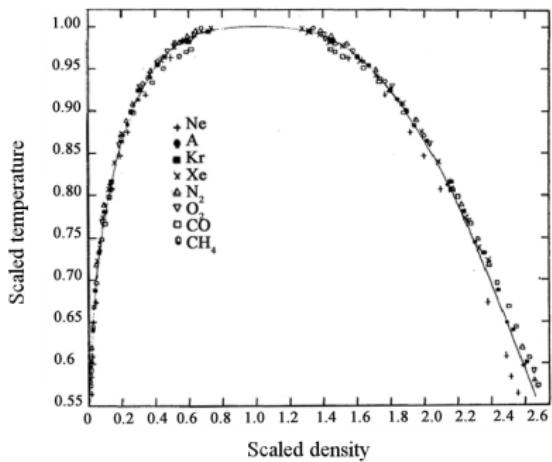
Modelling active fluctuations

Phase diagram: Persistence (Pe) vs density (ρ)

Active particles



Equilibrium analogue



Solon, Stenhammar, Cates, Kafri,

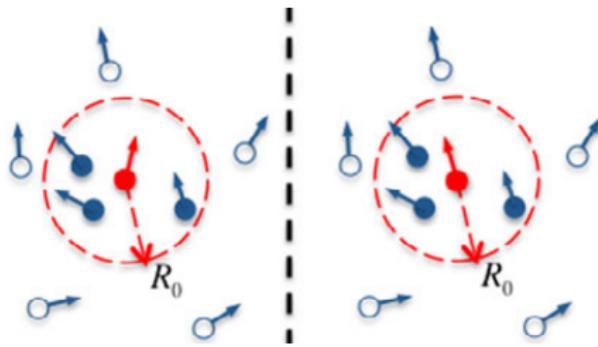
Tailleur, PRE **97**, 020602(R) (2018)

Guggenheim, J Chem Phys **13**, 253 (1945)

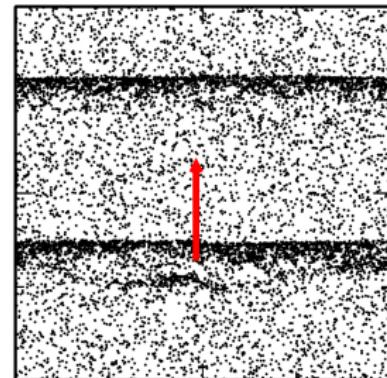
Modelling active fluctuations

Flocking transition towards collective motion

Vicsek model of aligning active particles



Ginelli, Eur Phys J **225**, 2099 (2016)

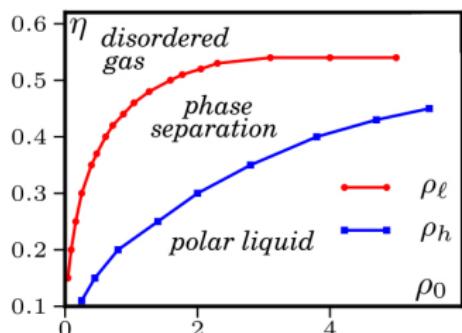


Chaté *et al*, PRE **77**, 046113 (2008)

Modelling active fluctuations

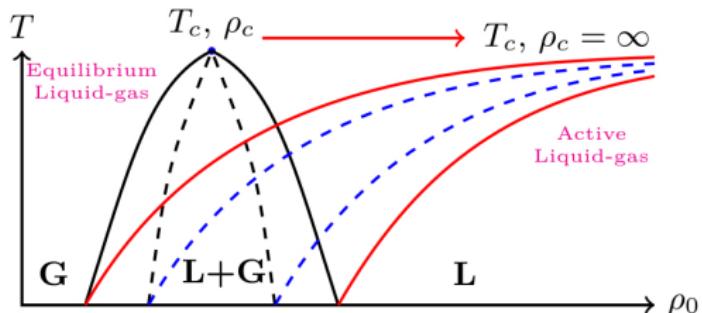
Phase diagram: Persistence ($1/\eta$) vs density (ρ)

Active particles



Solon *et al*, PRL 114, 068101 (2015)

Equilibrium analogue

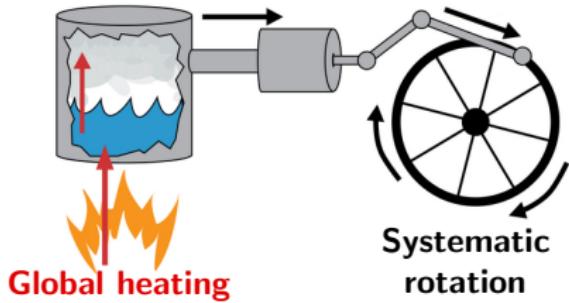


Solon *et al*, PRE 92, 042119 (2015)

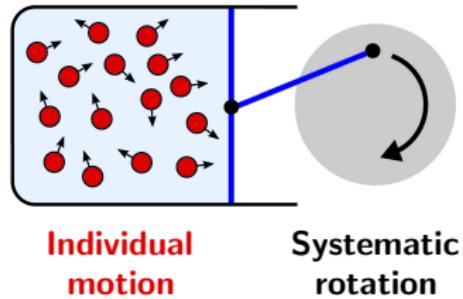
Statistical mechanics of fluctuating systems

How to extract energy from perturbation?

► Passive engine



► Active engine



19th century Physics

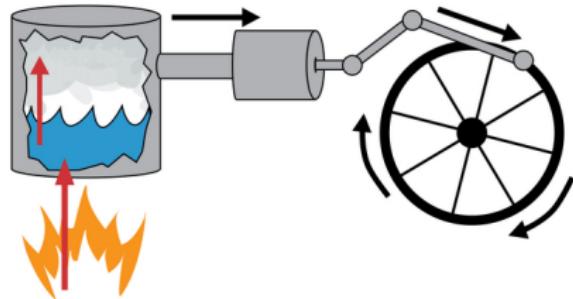
Passive thermodynamics

21st century Physics

Active thermodynamics

Foundations of thermodynamics

Designing and optimizing thermal engines



Sadi Carnot



Robert Stirling

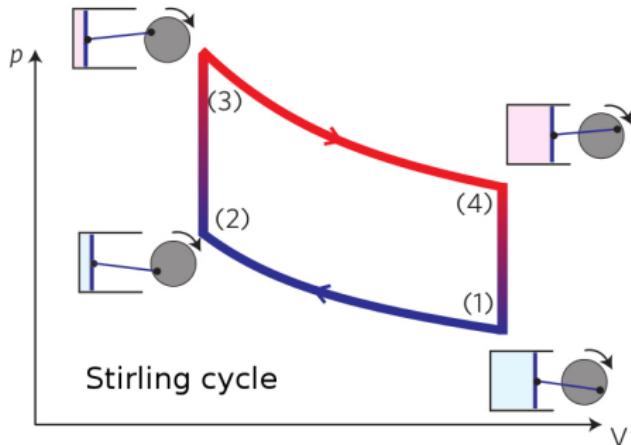


“Science owes more to the steam engine than the steam engine owes to Science”

Lawrence J. Henderson

Foundations of thermodynamics

Designing and optimizing thermal engines



Sadi Carnot



Robert Stirling



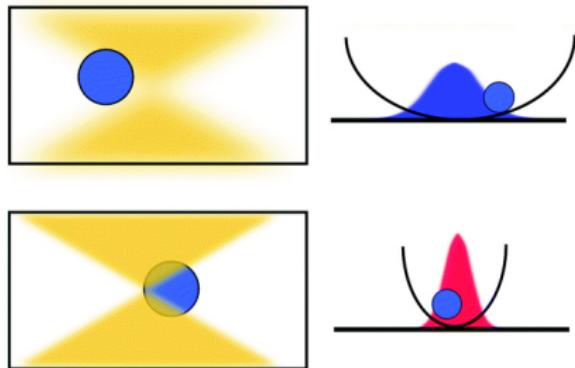
Blickle, Bechinger, Nat Phys 8, 143 (2011)

Compress at low pressure and expand at high pressure

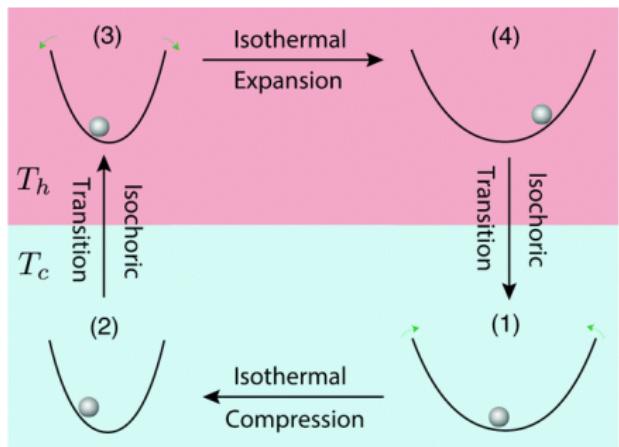
Foundations of thermodynamics

Colloid confined in harmonic trap

Optical tweezers



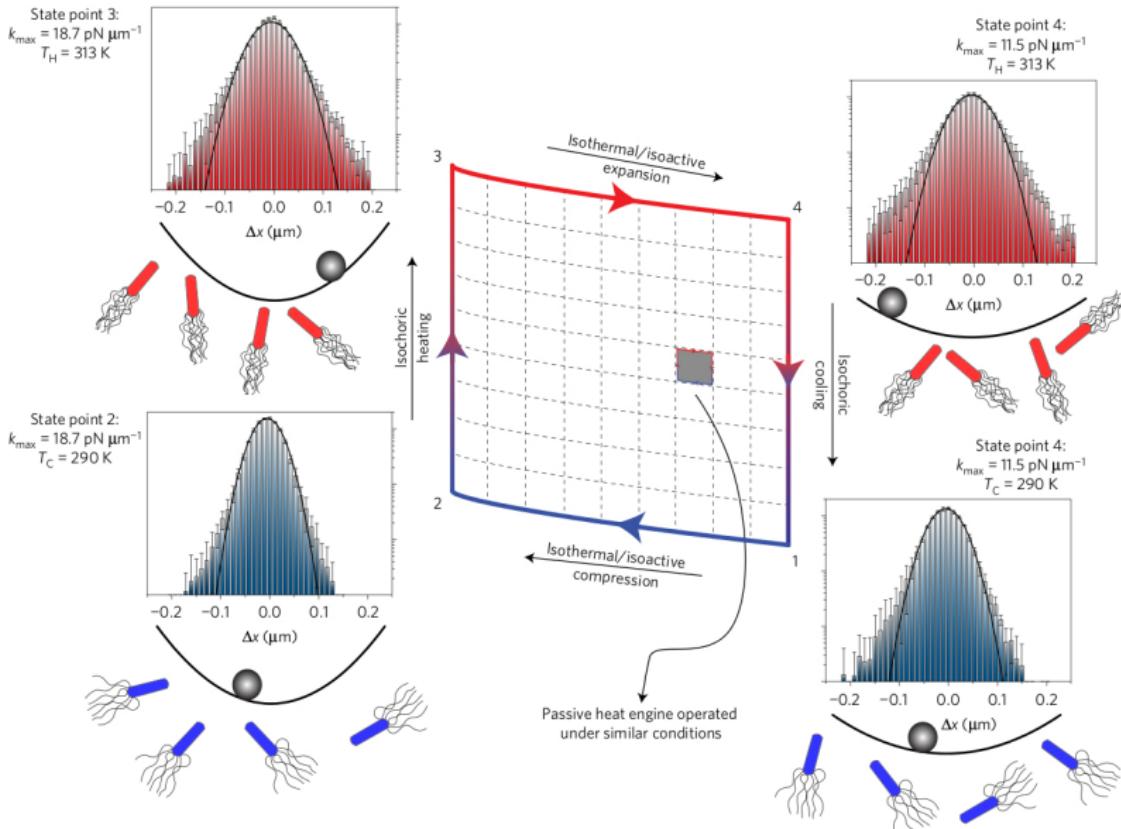
Colloidal engine



Martínez, Roldán, Dinis, Rica,
Soft Matter **13**, 22 (2017)

Blickle, Bechinger, Nat Phys **8**, 143 (2011)

Foundations of thermodynamics



Overview of the course

From equilibrium to nonequilibrium systems

- ▶ What are the main features of equilibrium?

[Week 1 to Week 7](#)

Role of dynamical reversibility

Thermodynamics at small scales

- ▶ What are the consequences of irreversibility?

[Week 8 to Week 14](#)

Nonequilibrium properties of active matter

From single particle to collective effects