# Injection, dissipation, efficiency of motor activity in a living cell

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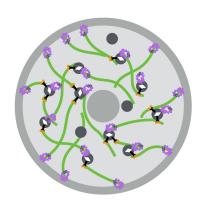


Statphys26 – Biological physics

#### Living mouse oocytes

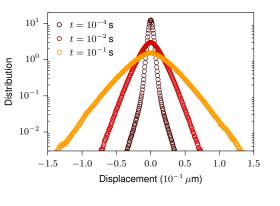


W. W. Ahmed, M. Bussonnier, T. Betz (Curie Institute) M. Almonacid, M.-H. Verlhac (Collège de France) N. S. Gov (Weizmann Institute of Science)

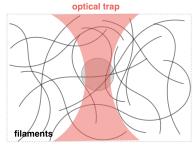




#### Statistics of tracer displacement



#### Measuring the mechanics



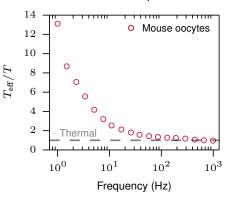
$$\langle \delta r(t) \rangle = \int_0^t \underbrace{R(t-s)}_{\text{Response}} F(s) ds$$

Trademark of equilibrium

$$R(t) = -\frac{1}{T} \frac{d}{dt} \underbrace{\langle x(t)x(0)\rangle}_{C(t)} \rightarrow T = \frac{\omega C(\omega)}{2R''(\omega)}$$

Fluctuation-dissipation theorem





Violation of FDT

$$T_{\text{eff}}(\omega) = \frac{\omega C(\omega)}{2R''(\omega)}$$

- D. Mizuno et al., Science 315, 370 (2007)
- C. Wilhelm, Phys. Rev. Lett. 101, 028101 (2008)
  - F. Gallet et al., Soft Matter 5, 2947 (2009)
  - H. Turlier et al., Nat. Phys. 12, 512 (2016)

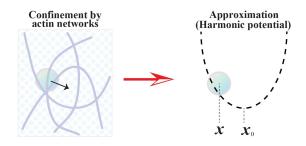
Bridging departure from equilibrium to the microscopics

Tracer dynamics: phenomenological model

Tracer dynamics: phenomenological model

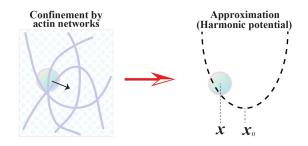
Energy transfers: stochastic energetics

Tracer dynamics: phenomenological model



$$0 = -k(x - x_0) - \gamma \frac{\mathrm{d}x}{\mathrm{d}t} + \xi$$

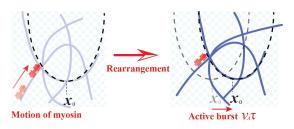
 $\xi$  Gaussian white noise



$$0 = -k(x - x_0) - \gamma * \frac{\mathrm{d}x}{\mathrm{d}t} + \xi$$

 $\xi$  Gaussian colored noise

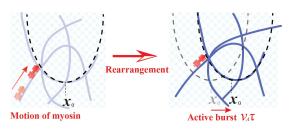
#### Active motion of local minimum



$$\gamma * \frac{dx}{dt} = -k(x - x_0) + \xi, \quad \gamma * \frac{dx_0}{dt} = F_M$$

 $F_{\rm M}$  colored noise: persistence time  $\tau$ 

#### Active motion of local minimum



$$\gamma * \frac{\mathrm{d}x}{\mathrm{d}t} = -kx + \underbrace{F_{\mathrm{A}}}_{kx_{\mathrm{N}}} + \xi, \quad \gamma * \frac{\mathrm{d}x_{\mathrm{0}}}{\mathrm{d}t} = F_{\mathrm{M}}$$

 $F_{\rm M}$  colored noise: persistence time au

1 Tracer dynamics: phenomenological model

2 Energy transfers: stochastic energetics

#### Active force power

$$J_{\text{tracer}} = \left\langle F_{\text{A}} \frac{\mathrm{d}x}{\mathrm{d}t} \right
angle$$

#### Stochastic energetics

$$J_{\text{tracer}} = \left\langle \left( \gamma * \frac{dx}{dt} - \xi \right) \frac{dx}{dt} \right\rangle + \left\langle kx \frac{dx}{dt} \right\rangle$$

#### Active force power

$$J_{\text{tracer}} = \left\langle F_{\text{A}} \frac{\text{d}x}{\text{d}t} \right\rangle$$

#### Stochastic energetics

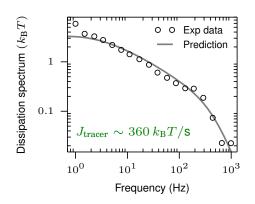
$$J_{\text{tracer}} = \underbrace{\left\langle \left( \gamma * \frac{\mathrm{d}x}{\mathrm{d}t} - \xi \right) \frac{\mathrm{d}x}{\mathrm{d}t} \right\rangle}_{\text{Dissipated power}} + \underbrace{\left\langle \left( \gamma * \frac{\mathrm{d}x}{\mathrm{d}t} - \xi \right) \frac{\mathrm{d}x}{\mathrm{d}t} \right\rangle}_{\text{Dissipated power}}$$

Spectral decomposition

$$J_{\text{tracer}} = \int I(\omega) \frac{\mathsf{d}\omega}{2\pi}$$

Spectrum of dissipated power

$$I(\omega) = rac{2 igl[ T_{
m eff}(\omega) - T igr]}{1 - igl[ R''(\omega)/R'(\omega) igr]^2}$$



Persistence time  $\tau \sim 0.3 \, \text{ms}$ 

Myosin-V power stroke  $\sim 0.5 \, \text{ms}$ 

G. Cappello et al., PNAS 104, 15328 (2007)

#### Tracer dynamics

$$\gamma*rac{\mathrm{d}x}{\mathrm{d}t} = -k\mathbf{x} + F_{\mathrm{A}} + \xi, \quad \gamma*rac{\mathrm{d}x_{\mathrm{0}}}{\mathrm{d}t} = F_{\mathrm{M}}$$

Power injected by motors into cage

$$J_{\mathsf{cage}} = \left\langle F_{\mathsf{M}} \frac{\mathsf{d} x_0}{\mathsf{d} t} \right
angle \sim 2 \cdot 10^5 \, k_{\mathsf{B}} \, T/s$$

Power injected by one myosin-V  $\sim 10^4 \, k_{\rm B} \, T/{\rm s}$ K. Fujita *et al.*, Nat. Com. **3**, 956 (2012)

Efficiency of power transduction

$$\frac{\mathsf{cage} \to \mathsf{tracer}}{\mathsf{motors} \to \mathsf{cage}} = \frac{J_{\mathsf{tracer}}}{J_{\mathsf{cage}}} \sim 10^{-3}$$

Main energy injection goes to network remodeling

### Conclusion

Energetics in living cells

What have we learned?

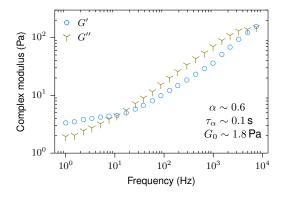
- Kinetics of fluctuations
- Separating injection and dissipation
- Efficiency of energy transfers

References | arXiv:1510.08299, arXiv:1511.00921

## Microrheology

Complex modulus

$$G^*(\omega) = rac{1}{6\pi a R(\omega)}$$



$$G^* = \underbrace{G'}_{\text{Elastic mod}} + \underbrace{\mathsf{i}G''}_{\text{Viscous mod}}$$

$$G^*(\omega) = G_0 [1 + (\mathrm{i}\omega au_lpha)^lpha]$$

Visco-elastic material

### Force spectrum

#### Spectrum of stochastic forces

$$S_{\text{cell}}(\omega) = \mathcal{F} \left\langle (\xi + F_{A})(t)(\xi + F_{A})(0) \right\rangle$$

$$= \underbrace{S_{\text{th}}(\omega)}_{\text{mechanics (FDT)}} + S_{A}(\omega)$$

