Natural Language Processing - Ex1

Due: Sunday 12.11.17 23:55

- 1. (10 pts) Given a bigram language model for sentences of the form START $w_1 \ w_2 \ w_3 \ \cdots \ w_n$ STOP (where w_i for $1 \le w \le n$ is a word), show that if the transition probabilities are well-defined (i.e., sum up to 1) and have some non-zero probability for generating STOP, then the probability over finite sequences is well-defined as well.
- 2. (20 pts) We want to build a spelling corrector, focusing on the distinction between "where" and "were". Given a sentence as input, the corrector should predict the true spelling for each instance of "where" or "were" and correct the spelling in the case of mistake.

For example, given the sentence "He went where there where more opportunities", the corrector should predict "where" for the first instance and "were" for the second one. It should also correct the word in the second case.

Suppose we use a language model for this task. Given a language model $p(w_1w_2\cdots w_n)$ where n is the length of the sentence, the corrector returns the spelling that gives the highest probability.

In our example, the spelling corrector will output "were" for the second instance if:

p(He went where there were more opportunities) > p(He went where there where more opportunities)

- (a) Describe formally a unigram language model for the spelling corrector. Assume that the probability of a word is given by its proportion in the corpus (the training set) and that the number of instances in the corpus of each word in the vocabulary is strictly bigger than 0. Given the sentence "He went where there where more opportunities", under which conditions will the spelling corrector give a right answer for the first instance of "where"? for the second instance of "where"? for both instances?
- (b) Describe formally a bigram language model for the spelling corrector. Assume again that we estimate the parameters of the model using relative frequency and that the number of instances in the corpus of each word in the vocabulary is strictly bigger than 0. Why might this model be better that the model in (a)? Can a sentence in this model get a zero-probability? Would it be a problem for the model?
- 3. (20 pts) Consider the following toy example. Training data:

START John likes NLP STOP START He likes Mary STOP START He is John STOP START John she likes STOP START John NLP is STOP START Mary likes NLP STOP

In the following questions include START and STOP in your counts just like any other token.

- (a) We use a bigram language model based on the above training data. Complete the following sentence with the most probable word predicted by the model: "He likes ...".
- (b) Assuming the same model as is (a) and the above training data, compute the probability and the perplexity of the following two sentences.
 - i. START John likes Mary STOP
 - ii. START Mary likes John STOP
- (c) Now we use linear interpolation smoothing between a maximum-likelihood bigram model and a maximum-likelihood unigram model with $\lambda_1 = 2/3$ and $\lambda_2 = 1/3$, using the same training data. Given this new model, compute the probability and the perplexity of the sentences (i) and (ii) written above.
- 4. (20 pts) Consider the advanced smoothing method called Good-Turing smoothing. Let N_c be the number of word types (unique words) which appeared exactly c times in the training corpus (e.g., N_1 is the number of unique words that appeared one time in the training corpus). N denotes the total number of word instances in the training corpus. An estimate of the total probability of all unseen words (i.e., words that do not appear in the training corpus) is given by $p_{unseen} = \frac{N_1}{N}$.

The smoothed Good-Turing estimate of a frequency of a word that appears c times in the training corpus is $\frac{(c+1)N_{c+1}}{N_c \cdot N}$.

- (a) Show that the sum over all word types in the training corpus of their smoothed Good-Turing frequency estimates is $1 p_{unseen}$.
- (b) Write down the equation for the smoothed Add-One estimate of a frequency of a word that appears c times in the training corpus. Show that there is a threshold μ , such that for all words of frequency less than μ , their smoothed estimate is higher than the MLE, and for all words of frequency more than μ , their smoothed estimate is lower than the MLE.
- (c) Show that the property in (b) does not necessarily hold for the smoothed Good-Turing estimate.

5. (20 pts)

- (a) Write down the equation for a trigram language model (without detailing the probability estimations). Which (conditional) independence assumption is made in the model?
- (b) Give an example of an English sentence and a Hebrew sentence where the phenomenon of verbsubject agreement (see below) is captured by the model in (a). That is, give an example where the model in (a) is likely to predict the correct inflection of the verb, given the subject.
- (c) Give an example of an English sentence and a Hebrew sentence where subject-verb agreement is not captured. Which n (for an n-gram model) is necessary for capturing this phenomenon in your example?

Note: Subject-verb agreement is the correspondence between the morphological inflection of the verb and the type of the subject. For instance, in English where the subject is singular, verbs in present tense end with an 's', while the base form is used for plural subjects. (e.g., "a dog barks", "dogs bark")

6. (10 pts) Give an example of a sentence (in Hebrew or in English), where each consecutive pair of words is grammatically valid, but the sentence is not grammatically valid. Do the same with consecutive triplets and consecutive 4-tuples. You will note that doing this exercises for 4-tuples is considerably more difficult than for pairs. What does that indicate, in terms of the suitability of Markov models (of various orders) to be language models?

Note: A sequence of words is said to be *grammatically valid* in a language, if there is a grammatical sentence in that language that contains the sequence as a sub-string.