

A New Proposal to Jefferson Lab PAC48

Measurement of the Two-Photon Exchange contribution to the electron-neutron elastic scattering cross section

S. Alsalmi (spokesperson)

King Saud University, Riyadh 11451, Saudi Arabia

E. Fuchey (spokesperson) and A.J.R. Puckett

University of Connecticut, Storrs, Connecticut 06269, USA

B. Wojtsekhowski (spokesperson), S. Barcus, A. Camsonne, D. Gaskell,
J.-O. Hansen, D. W. Higinbotham, M. Jones, C. Keppel, D. Mack,

D. Meekins, R. Michaels, B. Sawatzky, G. Smith, A. Tadepalli, and S. Wood

Thomas Jefferson National Accelerator Facility, Newport News, Virginia 23606, USA

K. Aniol

California State University, Los Angeles, CA 90032, USA

D. Armstrong, T. Averett, M. Satnik, Z. Wertz, and B. Yale

The College of William and Mary, Williamsburg, Virginia 23185, USA

J. Arrington and P. Reimer

Argonne National Laboratory, 9700 S Cass Ave, Lemont, Illinois 60439, USA

C. Ayerbe Gayoso, H. Bhatt, D. Bhetuwal, B. Devkota,

J. Dunne, D. Dutta, L. El-Fassi, and A. Karki

Mississippi State University, Mississippi State, MS 39762, USA

V. Bellini

Istituto Nazionale di Fisica Nucleare, I-95123 Catania, Italy

J. Bernauer

Stony Brook University, Stony Brook, NY 11794, US

Riken BNL Research Center, Upton, NY 11973, US

D. Biswas, M. E. Christy, B. Dongwi, I. Fernando, T. Gautam,
M. Kohl, A. Nadeeshani, J. Nazeer, T. Patel, and M. Rathnayake

Hampton University, Hampton, Virginia 23669, USA

W. Boeglin and P. Markowitz

Florida International University, Miami, FL 33199, USA

G. Cates, K. Gnanvo, N. Liyanage, and V. Nelyubin

University of Virginia, Charlottesville, Virginia 22904, USA

E. Cline

Stony Brook University, Stony Brook, NY 11794, US

E. Cisbani, F. Meddi, and G. Urciuoli

Istituto Nazionale di Fisica Nucleare - Sezione di Roma,

P.le Aldo Moro, 2 - 00185 Roma, Italy

J.C. Cornejo* and B. Quinn

Carnegie Mellon University, Pittsburgh, Pennsylvania 15213, USA

D. Hamilton and R. Montgomery

SUPA School of Physics and Astronomy,

University of Glasgow, Glasgow G12 8QQ, UK

F. Hauenstein

Old Dominion University, Norfolk, Virginia 23529, USA

T. Hobbs

Southern Methodist University, Dallas, TX 75205, USA

A. T. Katramatou and G.G. Petratos

Kent State University, Kent, OH 44242, USA

T. Kutz and A. Schmidt

The George Washington University, Washington, DC 20052, USA

D. Nguyen

Massachusetts Institute of Technology, Cambridge, MA 02139, USA

C. Petta and C. Sutera

Istituto Nazionale di Fisica Nucleare, Sezione di Catania, I-95123 Catania, Italy

A. Sarty

Saint Mary's University, Halifax, Nova Scotia B3H 3C3, Canada

K. Slifer

University of New Hampshire, Durham, NH 03824, USA

A. Shahinyan

AANL, 2 Alikhanian Brothers Street, 0036, Yerevan, Armenia

W. Tireman

Northern Michigan University, Marquette, Michigan 49855, USA

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(* - TBC)

Abstract

We propose to make a high precision measurement of the two-photon exchange contribution (TPE) in elastic electron-neutron scattering at a four-momentum transfer $Q^2 = 4.5$ $(\text{GeV}/c)^2$. While significant efforts to study the two-photon-exchange have focused around elastic electron-proton scattering, the impact of TPE on neutron form factors was never examined experimentally. The proposed experiment will provide the very first assessment of the two-photon exchange in electron-neutron scattering, which will be important for understanding the nucleon form factor physics.

The proposed experiment will be performed in Hall A using the BigBite (BB) spectrometer to detect the scattered electrons and the Super-BigBite (SBS) to detect the protons and neutrons. The experiment should run concurrently with the E12-09-019 G_M^n and E12-17-004 G_E^n -Recoil experiments, which are expected to run in 2021. The experimental setup of the proposed experiment will be identical to that of E12-09-019 experiment.

The “ratio” method will be used to extract the electric form factor of the neutron G_E^n by scattering unpolarized electrons from deuterium quasi-elastically at two beam energies 4.4 and 6.6 GeV and electron scattering angles 41.9 and 23.3 degrees respectively. In the proposed approach, systematic errors are greatly reduced compared to those in the traditional single electron arm configuration. Several experiments at Mainz and JLab have used the ratio method to measure the neutron magnetic form factor in the past years. The method can be extended to extract the neutron electric form factor even with less stringent requirements on the knowledge of the absolute neutron detection efficiency and experimental kinematics than required for neutron magnetic form factor measurements.

I. INTRODUCTION

In 1950s, a series of experiments performed by R. Hofstadter [?] revealed that nucleons have a substructure (which corresponds to our modern view in terms of quarks and gluons). The experiment confirmed M. Rosenbluth's theory of electron scattering [?] based on the one-photon exchange approximation. In this so-called Born approximation, where the interaction between the electron and the nucleon occurs *via* an exchange of one virtual photon (OPE), the unpolarized $e - N$ elastic cross section can be parameterized in terms of a nucleon magnetic, G_M , and electric, G_E , form factors. These form factors describe the deviation from a point-like scattering cross section, σ_{Mott} :

$$\left(\frac{d\sigma}{d\Omega} \right)_{eN \rightarrow eN} = \frac{\sigma_{Mott}}{\epsilon(1 + \tau)} [\tau \cdot G_M^2(Q^2) + \epsilon \cdot G_E^2(Q^2)], \quad (1)$$

where E and E' are the incident and scattered electron energies, respectively, θ is the electron scattering angle, $\tau \equiv -q^2/4M^2$, with $-q^2 \equiv Q^2 = 4EE' \sin(\theta/2)$ being the negative four momentum transfer squared, M is the nucleon mass, and $\epsilon = [1 + 2(1 + \tau) \tan^2(\theta/2)]^{-1}$ is the longitudinal polarization of the virtual photon. The reduced cross section is defined by:

$$\sigma_r \equiv \left(\frac{d\sigma}{d\Omega} \right) \cdot \frac{\epsilon(1 + \tau)}{\sigma_{Mott}} = \tau \cdot G_M^2(Q^2) + \epsilon \cdot G_E^2(Q^2) = \sigma_T + \epsilon \cdot \sigma_L, \quad (2)$$

where σ_L and σ_T are the cross sections for longitudinally and transversely polarized virtual photons, respectively.

The linear ϵ dependence of the cross section is due to the σ_L term. The ratio σ_L/σ_T is the so-called Rosenbluth slope related to G_E/G_M (in OPE), see Fig. ???. The data show that at Q^2 of 4-5 $(\text{GeV}/c)^2$ the Rosenbluth slope is three to four times larger than expected in OPE (shown as the dot-dashed line in Fig. ???) for the observed values of the G_E^p/G_M^p ratio.

The nucleon electromagnetic form factors can reveal a lot of information about the nucleon internal structure, as well as the quark distribution. The form factors depend only on one variable, the negative square of the four-momentum transfer carried by the photon, Q^2 . In

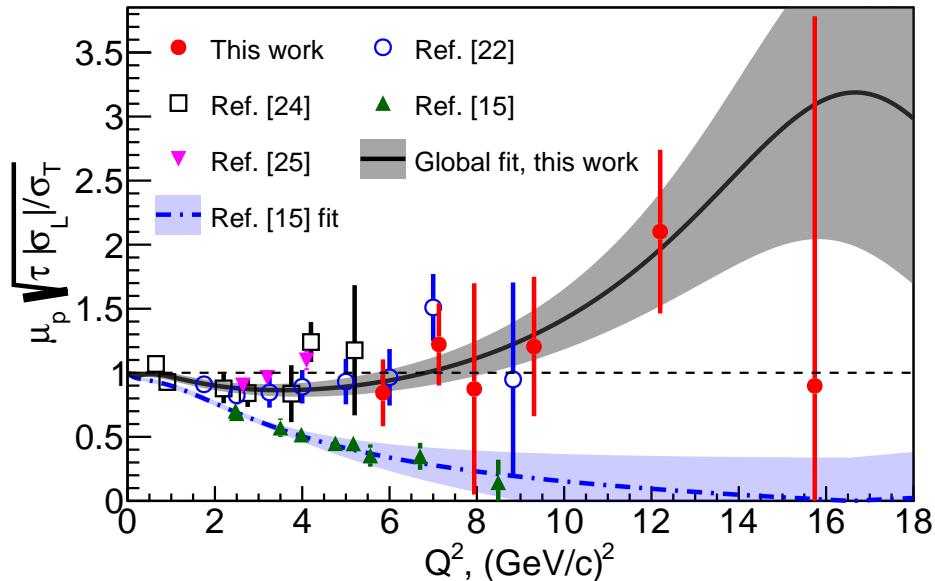


FIG. 1. The square root of Rosenbluth slope, corrected for kinematical factor $\sqrt{\tau}$ and μ_p , observed in elastic electron-proton scattering, adopted from Ref. [?]. References in the plot are also from Ref. [?]

²⁴ the limit of large Q^2 , perturbative QCD (pQCD) provides well-motivated predictions for the
²⁵ Q^2 -dependence of the form factors and their ratio. However, it was never predicted at what
²⁶ Q^2 range the pQCD prediction (scaling) will be valid. Studies show that pQCD validity
²⁷ will require a very large Q^2 of 100 (GeV/c)^2 . It was discovered at JLab, using the double
²⁸ polarization methods, that the proton electric and magnetic form factors behave differently
²⁹ starting at $Q^2 \approx 1 \text{ (GeV/c)}^2$.

³⁰ Experimentally, the nucleon form factors can be measured using one of two techniques:
³¹ the polarization transfer technique and the Rosenbluth technique. The polarization method
³² examines the polarization transfer from longitudinally polarized electron to the recoiling
³³ nucleon and determine the resulting azimuthal asymmetry distribution using a polarimeter.
³⁴ Alternatively, one can use a polarized electron beam and polarized target. In the Rosen-
³⁵ bluth method, the electric and magnetic from factors can be separated by making two or
³⁶ more measurements with different ϵ values (*i.e.* different beam energies and angles), but
³⁷ with same Q^2 value. The Rosenbluth technique requires an accurate measurement of the

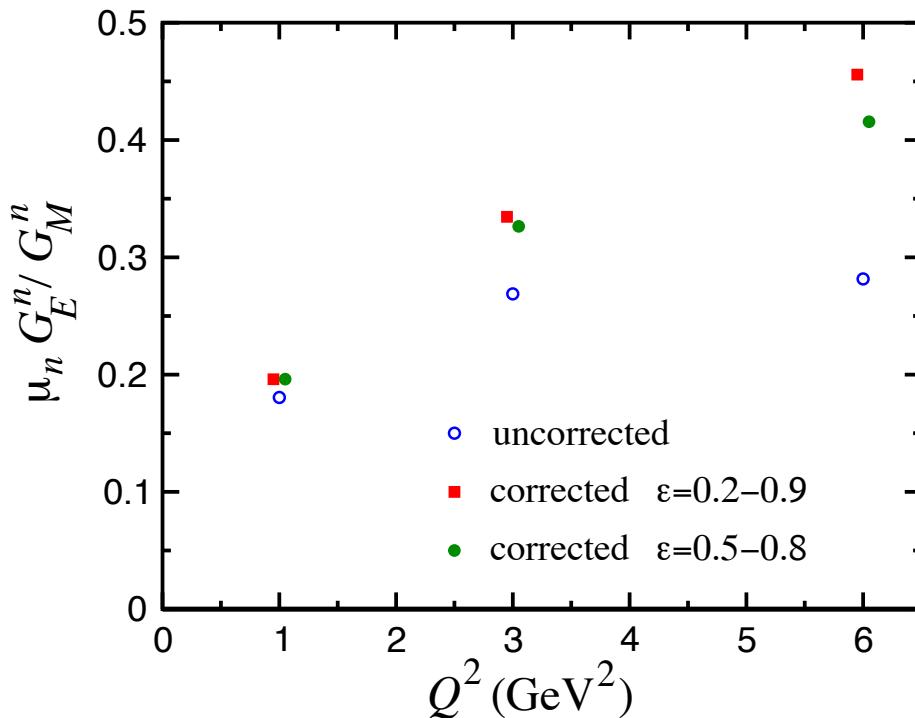


FIG. 2. Projected impact of TPE on G_E^n/G_M^n using LT separation, according to Ref. [?].

cross section and suffers from large systematic uncertainties arising from several factors, for instance the need for a precise determination of the scattering angle. Additionally, for a measurement of the neutron form factors, accurate knowledge of the neutron detector efficiency is required, which is particularly hard to achieve. These uncertainties can be greatly reduced by measuring the ratio of $e - n$ and $e - p$ quasi-elastic cross sections.

When comparing the values of G_E^n/G_M^n obtained from both techniques, a significant discrepancy was observed (see Fig. ??). Such a discrepancy implies a potential problem in our understanding of the nucleon substructure. Many efforts were made to explain this effect, and it is believed that the inconsistency is due to the contribution of two-photon exchange in $e - N$ elastic scattering process [? ?]. Predictions made for the neutron case are shown in Fig. 2, adopted from [?]. The contribution of TPE could reach about 30% of the Rosenbluth slope value at 5 (GeV/c) 2 .

50 In the following we propose to make a precision L/T separation of the elastic electron-
51 neutron cross section and first experimental assessment of the two-photon exchange contribu-
52 tion on the neutron magnetic form factor measurements (see also Ref. [?]). The result of
53 the nTPE experiment will likely add a new component to our understanding of the elastic
54 electron-nucleon process.

55

II. PHYSICS MOTIVATION

56 The nucleon plays the same central role in hadronic physics that the hydrogen atom does
 57 in atomic physics and the deuteron in the physics of nuclei. The structure of the nucleon
 58 and its specific properties, such as charge, magnetic moment, size, mass; the elastic electron
 59 scattering form factors, resonances; and structure functions in DIS, are of fundamental sci-
 60 entific interest. The isospin is a fundamental property of the nucleon, so both the proton
 61 and neutron investigations are important to do. By using data on the proton and neutron
 62 form factors the flavour structure could be explored [?]. It has already provided the most
 63 direct evidence for a diquark correlation in the nucleon [? ? ?].

64 Hadron structure, as seen in elastic electron scattering, in one-photon approximation, is
 65 defined by two functions of four momentum transfer square. They are: the helicity con-
 66 serving Dirac form factor, F_1 , which describes the distribution of the electric charge, and
 67 the helicity non-conserving Pauli form factor, F_2 , which describes the distribution of the
 68 magnetic moment. These two form factors are the ingredients of the hadronic current. They
 69 contain information on the transverse charge distribution for an unpolarized and transversely
 70 polarized nucleon, respectively, in the infinite momentum frame [? ?].

71 The Sachs form factors, G_E and G_M , the ratio of which will be extracted directly from
 72 the data, are related to F_1 and F_2 by

$$F_1 = \frac{G_E + \tau G_M}{1 + \tau} \text{ and } F_2 = \frac{G_M - G_E}{\kappa(1 + \tau)}, \quad (3)$$

73 where κ is the nucleon anomalous magnetic moment.

74 Already twenty-four years ago, an important development in QCD phenomenology has
 75 been the exploration of the generalized parton distribution (GPD) formalism [? ? ?],
 76 which provides relations between inclusive and exclusive observables. The nucleon elastic
 77 form factors F_1 and F_2 are given by the first moments of the GPDs

$$F_1(t) = \sum_q \int_0^1 H^q(x, \xi, t, \mu) dx \text{ and } F_2(t) = \sum_q \int_0^1 E^q(x, \xi, t, \mu) dx, \quad (4)$$

78 where H^q and E^q are two of the generalized parton distributions, x is the standard Bjorken
 79 x , ξ is the “skewness” of the reaction, t is the four-momentum transferred by the electron,

μ is a scale parameter necessary for the evolution over Q^2 , analogous to DIS parton distributions, and the sum is over all quarks and anti-quarks. GPDs may be accessed through processes such as deeply virtual Compton scattering, where the interaction is factorized into a hard part with the virtual photon/photon interactions with an individual quark and a soft part of the residual system where the GPD information is contained.

A fundamental nucleon feature, the spin, is related to GPDs, as shown by X. Ji [?]. The moments of GPDs can yield information, according to Ji's Angular Momentum Sum Rule, on the contribution to the nucleon spin from quarks and gluons, including both the quark spin and orbital angular momentum.

At present, experimental measurements of GPDs are still scarce. Until high Q^2 DVCS data becomes available, work has been done to attempt to parameterize these GPDs, which rely heavily on data from electromagnetic form factors and parton distributions from DIS as constraints [?]. Data at high Q^2 for G_E^n would contribute significantly in the development of these models.

As we presented above, nucleon elastic form factors provide important input for the modeling of GPDs. At the same time, the measured cross section of elastic $e - p$ scattering at high Q^2 is significantly larger than predicted by Born-approximation calculations [?], indicating that TPE effects play a critical role in the high- Q^2 region and therefore must be well understood before conclusions about GPDs can be drawn.

99

III. TECHNIQUE

100 This proposal is based on instrumentation, simulation, and analysis development made
 101 by the GMn/SBS collaboration for the GMn, E12-09-019, experiment [?]. The GMn
 102 experiment is one of several form factor experiments approved by JLab PAC. The SBS
 103 spectrometer was funded by DOE with large contributions provided by the collaborating
 104 institutions from USA, Italy, UK, and Canada. The apparatus and DAQ installation will
 105 start in 2020 and the data taking run is expected to be in summer-fall 2021.

106 The neutron form factors are challenging to be determine experimentally especially be-
 107 cause there is no free neutron target. However, since deuterium is a loosely coupled system,
 108 it can be viewed as the sum of a proton target and a neutron target. In fact, quasi-elastic
 109 scattering from deuterium has been used to extract the neutron magnetic form factor, G_M^n ,
 110 at modestly high Q^2 for decades [? ?] in the single arm (e, e') experiments. However, the
 111 proton cross section needs to be subtracted by applying a single-arm quasi-elastic electron-
 112 proton scattering. This “proton-subtraction” technique suffers from a number of systematic
 113 uncertainties e.g. contributions from inelastic and secondary scattering processes.

114 Many years ago, L. Durand [?] proposed the so-called “ratio-method” based on the
 115 measurement of both $D(e, e'n)$ and $D(e, e'p)$ reactions. In this method, many of the systematic
 116 errors are canceled out. Several experiments [? ? ?] have applied the ratio-method to
 117 determine the neutron magnetic form factor.

118 The GMn/SBS experiment [?] will take data for elastic $e - n$ scattering for several
 119 kinematics with Q^2 from 3.5 up to 13.5 $(\text{GeV}/c)^2$. We propose to use this method to measure
 120 the Rosenbluth slope and extract (in OPE approximation) the neutron electric form factor,
 121 G_E^n , at one value of momentum transfer. In fact, one of the required data points will be taken
 122 by the GMn experiment, so an additional measurement is needed only for one kinematics.

123 Data will be collected for quasi-elastic electron scattering from deuterium in the process
 124 $D(e, e'n)p$. Complementary $D(e, e'p)n$ data will be taken to calibrate the experiment appa-
 125 ratus. The current knowledge of the $e - p$ elastic scattering cross section (obtained in the
 126 single arm $H(e, e')p$ and $H(e, p)e'$ experiments) will be also used for precision determination
 127 the experiment kinematics.

128 Applying the Rosenbluth technique to measure G_E^n requires accurate measurement of the
 129 cross section and suffers from large uncertainties. To overcome this issue, we propose to
 130 extract the value of G_E^n from the ratio of quasi-elastic yields, $R_{n/p}$, in scattering from a
 131 deuteron target as follows:

$$R_{n/p} \equiv R_{observed} = \frac{N_{e,e'n}}{N_{e,e'p}} \quad (5)$$

132 $R_{observed}$ needs to be corrected to extract the ratio of e-n/e-p scattering from nucleons:

$$R_{corrected} = f_{corr} \times R_{observed} , \quad (6)$$

133 where the correction factor f_{corr} takes into account the variation in the hadron efficiencies
 134 due to changes of the $e - N$ Jacobian, the radiative corrections, and absorption in path from
 135 the target to the detector, and small re-scattering correction.

136 In one-photon approximation, $R_{corrected}$ can be presented as:

$$R_{corrected} = \frac{\sigma_{Mott}^n \cdot (1 + \tau_p)}{\sigma_{Mott}^p \cdot (1 + \tau_n)} \times \frac{\epsilon \sigma_L^n + \sigma_T^n}{\epsilon \sigma_L^p + \sigma_T^p} \quad (7)$$

It is important that the ratio $R_{Mott} = \frac{\sigma_{Mott}^n \cdot (1 + \tau_p)}{\sigma_{Mott}^p \cdot (1 + \tau_n)}$ could be determine with very high relative accuracy even with modest precision for the beam energy, electron scattering angle, and detector solid angle. Now, let us write the $R_{corrected}$ at two values of ϵ using $S_c^{n(p)} = \sigma_L^{n(p)} / \sigma_T^{n(p)}$ as:

$$R_{corrected,\epsilon_1} = R_{Mott,\epsilon_1} \times \frac{\epsilon_1 \sigma_L^n + \sigma_T^n}{\epsilon_1 \sigma_L^p + \sigma_T^p} \quad R_{corrected,\epsilon_2} = R_{Mott,\epsilon_2} \times \frac{\epsilon_2 \sigma_L^n + \sigma_T^n}{\epsilon_2 \sigma_L^p + \sigma_T^p}$$

In these two equations there are two unknown variables: σ_L^n and σ_T^n . We remind here that proton and neutron measurements are made simultaneously with the same apparatus. Thanks to this, the dominant contribution to the uncertainty of the Rosenbluth slope of the reduced cross section vs. ϵ , $S_c^n = \sigma_L^n / \sigma_T^n$, will come from the uncertainty of S_c^p . At $Q^2=4.5$ (GeV/c)², according to the global analysis of $e - p$ cross section [?], the value of S_c^p is close to $1/(\tau \mu_p^2) = 0.107$ with uncertainty of 0.01. The resulting equation for S_c^n is:

$$A = B \times \frac{1 + \epsilon_1 S_c^n}{1 + \epsilon_2 S_c^n} \approx B \times (1 + \Delta \epsilon \cdot S_c^n),$$

where the variable $A = R_{corrected,\epsilon_1}/R_{corrected,\epsilon_2}$ will be measured with statistical precision of 0.1%. Assuming, for this estimate, equal values of Q^2 for two kinematics, the τ and σ_T for two kinematics are canceled out, and the variable $B = R_{M,\epsilon_1}/R_{M,\epsilon_2} \times (1 + \epsilon_2 S_c^p)/(1 + \epsilon_1 S_c^p)$. For actual small range of ϵ and small value of the slope, the $B \approx (1 - \Delta\epsilon \cdot S_c^p)$. The value of B will be determined from global proton $e - p$ data to a precision of 0.25×0.01 .

At $Q^2=4.5$ (GeV/c) 2 the ratio $\mu_n G_E^n/G_M^n$ is 0.55 ± 0.05 based on polarization transfer data which is mostly insensitive to TPE, see review [?]. In the simplest model, the slope S_c^n is a sum of the slope due to G_E^n/G_M^n and the TPE contribution. If we use for TPE the prediction [?] which is reproduced on our Fig. 2, the TPE leads to increase of S_c^n by a factor of 2, so the result of this experiment for TPE will be $0.069 \pm 0.012 \pm 0.01$, where the first uncertainty is due to accuracy of G_E^n/G_M^n and the second one due to projected precision of this experiment. It would be a 4-4.5 sigma observation of the neutron TPE.

149

IV. PROPOSED MEASUREMENTS

We propose to use the same experimental setup of the E12-09-019 experiment. We will add a kinematic point at $Q^2 = 4.5 \text{ (GeV/c)}^2$, at a higher beam pass (6.6 GeV/3 pass instead of 4.4 GeV/2 pass), leading to a higher ϵ value. This additional point along with the data point of the E12-09-019 experiment will allow us to perform the standard Rosenbluth method to obtain (in one-photon approximation) the neutron electric and magnetic form factors. In addition, the ratio method (Sec.??), in which the systematic errors are greatly reduced, will be implemented to calculate the two photon exchange (TPE) contribution. The study of the ϵ dependence two photon exchange contribution to the neutron form factor ratio G_E^n/G_M^n . Table. I displays the kinematic settings of the proposed experiment.

Point	Q^2 (GeV/c) 2	E (GeV)	E' (GeV)	θ_{BB} degrees	θ_{SBS} degrees	ϵ
1	4.5	4.4	2.0	41.88	24.67	0.599
2	4.5	6.6	4.2	23.23	31.2	0.838

TABLE I. Kinematic settings of the proposed experiment. The kinematic point with the lowest ϵ value (blue row) is an existing measurement of the approved E12-09-019 experiment.

159

V. EXPERIMENTAL SETUP

160 As illustrated in Fig. ??, this experiment will study electron scattering from a 15 cm
 161 long liquid Deuterium target held in a vacuum. The scattered electron will be detected in
 162 the BigBite spectrometer with an upgraded electron detector stack. The neutron arm is
 163 arranged with a dipole magnet 48D48 (SBS) and a segmented hadron calorimeter HCAL.
 164 The whole detector package was designed and is being assembled for the GMn, E12-09-019,
 165 experiment.

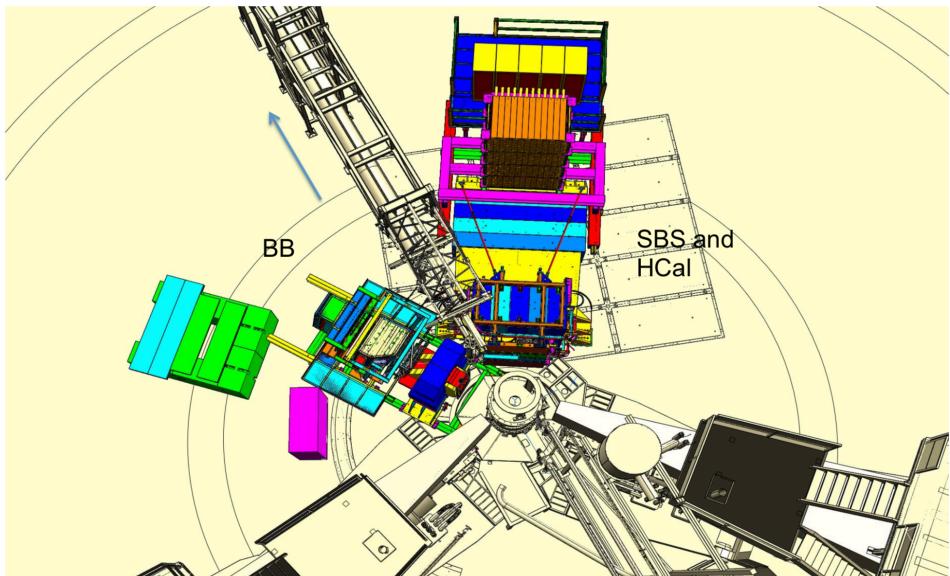


FIG. 3. Layout of the experimental setup in nTPE.

166

1. Parameters of the SBS

167 The 48D48 magnet from Brookhaven was acquired as part of the Super Bigbite project
 168 and will be available for this experiment. It consists of a large dipole magnet which provides
 169 a field integral of about $1.7 \text{ T} \cdot \text{m}$, allowing for quasielastic protons to be sufficiently deflected
 170 to allow clear differentiation from neutrons. The active field volume has an opening of $46 \times$
 171 $25 \text{ vertical} \times \text{horizontal}$), matching the aspect ratio of the neutron arm, and a depth of 48
 172 cm.

173 The placement of this magnet will be 1.6 m away from the target, which would normally
174 interfere with the beamline. To accommodate this, modifications were made to the iron yoke
175 such that the beamline will pass through the magnet yoke area.

176 The field configuration will be such that positively charged particles will be deflected
177 upwards away from the hall floor. For a field integral of 1.7 Tesla-m, protons of momentum
178 2.5 GeV/c will be deflected 250 mrad, which translates to a displacement of 1.29 m. Including
179 expected detector resolution, the $p_{miss,\perp}$ distribution will be similar to what was seen in
180 E02-013, so cuts of < 100 MeV/c will be appropriate. Monte Carlo simulations show a
181 contamination of charged quasielastics to be negligible.

182 The presence of the magnet also works to sweep low energy charged particles from the
183 target away from the neutron arm. Particles of momentum less than 1.3 GeV/c will be
184 entirely swept outside of the neutron arm acceptance. This greatly reduces the amount of
185 charged low energy background.

186

A. The BigBite Spectrometer

187 Scattered electrons will be detected in the BigBite spectrometer. The spectrometer con-
 188 sists of a single dipole magnet (with magnetic field approximately 1.2 T) and a detection
 189 system, see Fig. ??.

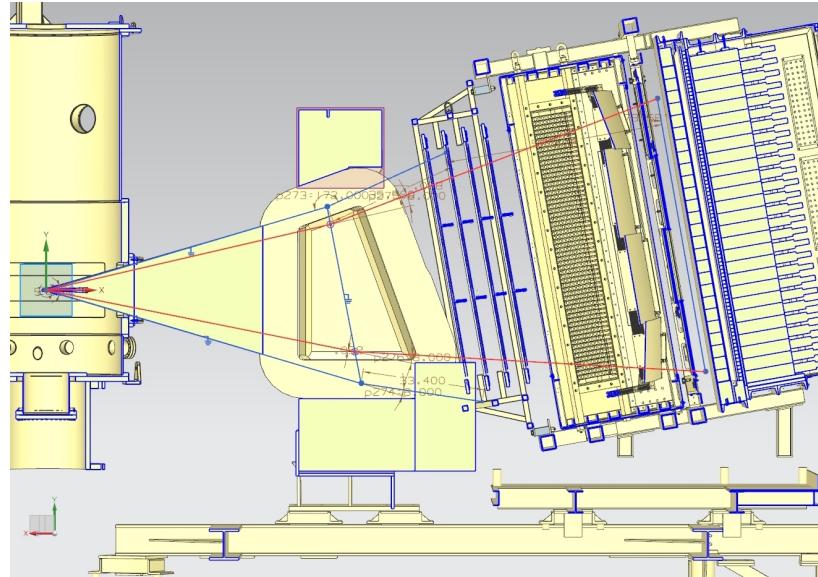


FIG. 4. The BigBite spectrometer with the upgraded detector stack.

190

1. GEM Chambers

191 To perform the tracking of charged particles under the high rates anticipated for this
 192 experiment, the drift chambers were replaced with gas electron multiplier (GEM) detectors.
 193 These detectors have proven to be capable of operating under luminosities of 25 kHz/mm^2
 194 for the COMPASS experiment at CERN and the spatial resolution of each of these chambers
 195 is anticipated to be about $70 \mu\text{m}$. There will be two sets of GEMs placed on each side of the
 196 GRINCH Cherenkov detector.

197 The set of GEMs in front of the GRINCH is composed of four layers of GEMs. Two of
 198 these layers have been built by the SBS collaborators from INFN. They are composed three

¹⁹⁹ modules each, measuring $40 \times 50 \text{ cm}^2$, such that each layer covers $40 \times 150 \text{ cm}^2$ (the
²⁰⁰ long dimension being vertical, along the dispersive direction). The readout of these modules
²⁰¹ are oriented in the x/y direction *i.e.* parallel and perpendicular to the dispersive direction
²⁰² (horizontal and vertical). The two other layers are being built by the SBS collaborators from
²⁰³ UVA. They are composed of a single module measuring $40 \times 150 \text{ cm}^2$, the long dimension
²⁰⁴ again being vertical and along the dispersive direction. The readout of these modules are
²⁰⁵ oriented in the u/v direction *i.e.* ± 30 degrees with respect to the horizontal direction.

²⁰⁶ The set of GEMs behind the GRINCH has been built by the SBS collaborators from
²⁰⁷ UVA. It is composed of a single layer composed of four modules measuring $50 \times 60 \text{ cm}^2$,
²⁰⁸ such that the layer covers $60 \times 200 \text{ cm}^2$ (the long dimension again being along the dispersive
²⁰⁹ direction). The readout of these modules are all oriented in the x/y direction.

²¹⁰ The background levels in the GEMs have been evaluated, with the help of the G4SBS
²¹¹ simulation package([?] and Sec. ??) for the G_M^n experimental readiness review. For the
²¹² G_M^n highest Q^2 point (which is the most constraining, since it combines mandatory maxi-
²¹³ mum luminosity and smaller BigBite angles), the rates in the front GEMs are of the order
²¹⁴ of 120 kHz/cm^2 for the front GEM layers, and below 50 kHz/cm^2 for the back GEM. To
²¹⁵ perform the GEM tracking within such a high-rate environment, we use the cluster recon-
²¹⁶ structed in the BigBite shower as a track seed to clean the large combinatorics that would
²¹⁷ otherwise be created by the large number of hits. After this, the main challenge is the
²¹⁸ separation by the clustering algorithm of the signal and background hits to minimize track
²¹⁹ smearing. At this level of background, a TreeSearch tracking algorithm combined with a
²²⁰ fairly simple cluster separation algorithm has already proven to achieve 70% efficiency at
²²¹ nominal luminosity. A better cluster separation algorithm is currently being developed and
²²² should allow to significantly improve this figure.

²²³

2. Shower/Preshower

²²⁴ The electromagnetic calorimeter configuration consists of two planes of lead glass blocks
²²⁵ which we call the preshower and shower. The preshower, located about 80 cm behind the
²²⁶ first GEM chamber, consists of a 2×26 plane of $37 \text{ cm} \times 9 \text{ cm}$ blocks. The shower, about

²²⁷ 1 m behind the first GEM chamber, consists of an 7×27 array of 8.5 cm \times 8.5 cm blocks.
²²⁸ Sums over these blocks form the physics event trigger for the experiment.

²²⁹ The preshower signal can be used to provide an additional method of pion rejection.
²³⁰ By selecting low preshower signals, a pion rejection factor of 1:50 can be achieved through
²³¹ optimization. Despite higher particle rates, pion rejection performance is anticipated to
²³² be similar to that achieved for Transversity, E06-010. By measuring the pedestal widths
²³³ and resolution for E06-010 and scaling to this proposal's conditions, overall relative energy
²³⁴ resolution for the detector is expected to become worse by a factor of 1.6, to about $\sigma_{\delta E/E} =$
²³⁵ 25%.

²³⁶ 3. Timing hodoscope

²³⁷ The BigBite timing hodoscope has been built by the SBS collaborators from Glasgow to
²³⁸ replace the BigBite scintillator plane. It will be composed of 90 bars stacked in a plane,
²³⁹ each with dimensions 1 in. \times 1 in. \times 60 cm. The paddle stack will be oriented such that
²⁴⁰ the long dimension of the bars is horizontal *i.e.* perpendicular to the dispersive direction.
²⁴¹ Each of these elements are read out by a PMT on each side, mostly to provide measurement
²⁴² redundancy.

²⁴³ This plane will primarily be used to provide a signal for nucleon time of flight reconstruc-
²⁴⁴ tion. A time resolution of 200 ps is anticipated. This fine segmentation is meant to lower the
²⁴⁵ rates in the detector. Background studies made for the G_M^n experimental readiness review
²⁴⁶ demonstrated that the rates experienced by each element was \leq 500 kHz at a luminosity of
²⁴⁷ 2.8×10^{38} cm $^{-2}$ s $^{-2}$. Signals from the PMTs are processed by NINO front-end cards which,
²⁴⁸ when the PMT pulse crosses the NINO threshold, will produce a digital signal to be read
²⁴⁹ out by CAEN 1190 TDCs which record a leading time and a trailing time.

²⁵⁰ 4. GRINCH cherenkov detector

²⁵¹ The main purpose of the GRINCH is to provide additional particle identification for offline
²⁵² pion rejection. The GRINCH consists of a tank with a maximum depth of 88.9 cm, with 4

253 cylindrical mirrors focussing the cherenkov light directly onto a 510 PMT array (60 lines of
254 PMTs, with lines of 9 PMTs alternating with lines of 8 PMTs) placed away from the beam.
255 The radiation gas will be C_4F_8 , which is by far the best compromise between light yield
256 for electrons and operating cost. With $n - 1 = 1.35 \times 10^{-3}$, the π threshold is only about
257 2.7 GeV, so the additional pion rejection will be most effective below this threshold.

258 Similar to the timing hodoscope, the signals from the GRINCH PMTs pulses are processed
259 by NINO front-end cards which, when the PMT pulse crosses the NINO threshold, will
260 produce a digital signal to be readout by VETROC TDCs, which for each PMT hit will
261 record a leading time and a trailing time. The analog signal will not be recorded however,
262 which means that for each PMT hit, the information of the number of photoelectrons is not
263 directly available (although it can in theory be deduced from the time over threshold).

264 All of this implies that the electron selection relies on the number of GRINCH PMT
265 firing, instead of relying on the signal amplitude.

266

B. Hadron Calorimeter (HCal)

267 The Hadron Calorimeter (HCal) has been designed specifically to measure the recoil
 268 nucleon for the SBS experiments. Specifically for this experiment (and for G_M^n), HCal
 269 combined with the SBS (48D48) magnet provides identification of the recoil nucleon, as
 270 well as additional kinematic constraint and possibly timing information on the measured
 271 interaction. Nucleon identification is illustrated on Fig. ???. This figure shows the compared
 272 proton and neutron position distribution in HCal at the same electron kinematics. The
 273 proton distribution is being shifted upwards by about 1 m compared to the neutron.

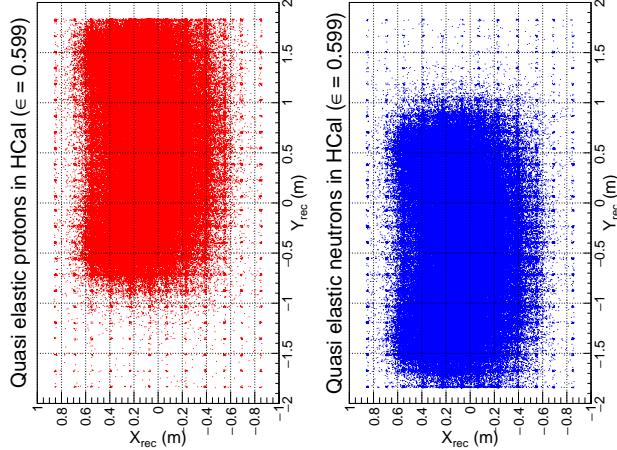


FIG. 5. Reconstructed HCal cluster from quasi-elastic events generated by G4SBS. The left distribution in red is for the proton, the right distribution in blue is for the neutron.

274 The HCal (a CAD model of which is shown in Fig. 6) is composed of 288 modules arranged
 275 in an array of 12×24 . In front of the full assembly is located a $3/4$ – inch steel plate which
 277 serves two purposes:

- 278 • initiate the hadronic shower to optimize the calorimeter response;
- 279 • shield the modules from a fraction of the low energy secondaries;

280 Each of these modules measures $6 \times 6 \text{ in}^2$ section, for 3 ft length. They are composed of
 281 alternating tiles of scintillators and iron around a central light guide which collects the light

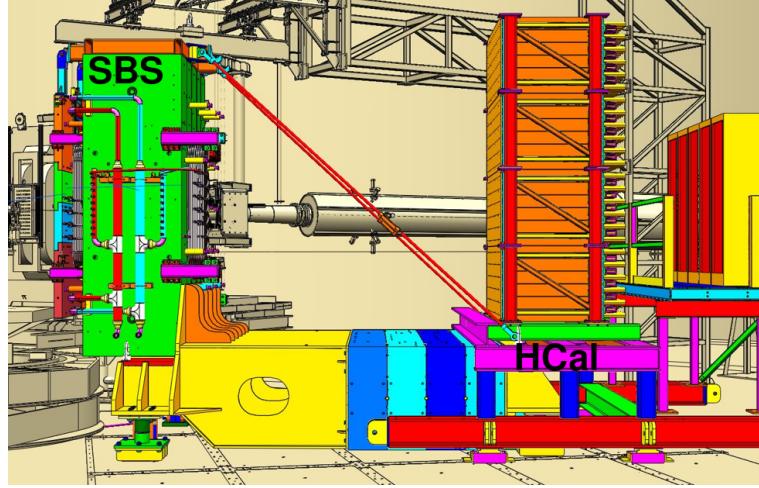


FIG. 6. CAD representation of HCal (right) with the SBS magnet (left)

generated in the scintillators by the hadronic shower, and guides it to the PMT at the end of the block. Cosmics tests have determined that the average light yield for the HCal modules is around 5 photoelectrons per MeV deposited in the scintillator tiles.

The PMTs are read out with FADC250 which sample the PMT signal every 4 ns and allow to reconstruct the PMT pulse shape, and hence its timing. They are also read out by TDCs which provide additional timing information. Thanks to this, the timing resolution can be better than 1 ns, which cosmics tests (in progress) seem to confirm.

The energy resolution is intrinsically broad (see Fig. ?? in Section ??), due mostly to the small fraction of energy from the hadronic shower actually measured by the scintillator tiles (≤ 0.1 - refer yet again to Fig. ??).

292 **VI. SIMULATIONS, ESTIMATIONS OF COUNTING RATES AND**
 293 **ACCIDENTALS**

294 The estimates of counting rates accidentals have been performed using G4SBS, the
 295 GEANT4-based simulation package developed for the SBS experiment [?]. This package
 296 includes a wide range of event generators, which allows us to evaluate the rates for both
 297 events of interest (signal) and background. The representation of the experiment apparatus
 298 in G4SBS is shown in the high ϵ configuration in Fig. ??.

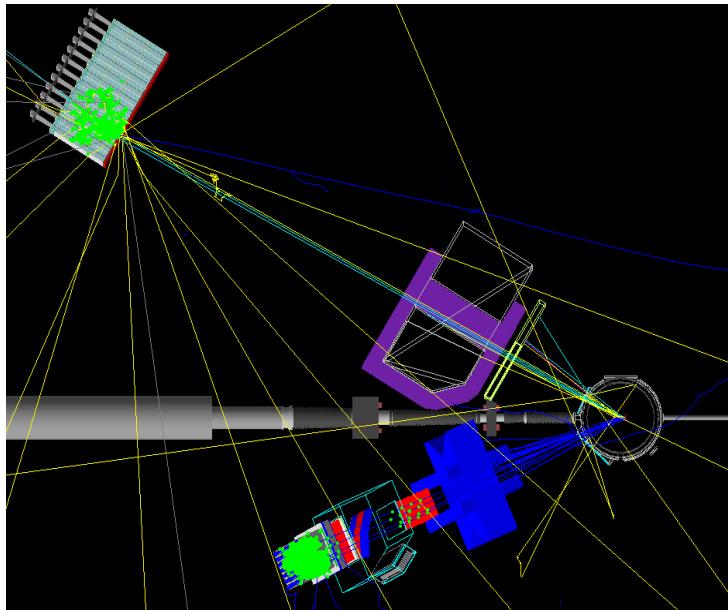


FIG. 7. Top view of the experimental apparatus model in G4SBS, shown in the high ϵ configuration. The beam direction is indicated, as well as the main elements (HCal, SBS magnet, BigBite spectrometer)

299 **A. Background and trigger rates**

300 The main processes expected to contribute to the trigger rates for the BigBite spectrom-
 301 eter are:

- 302 • the inelastic electron nucleon scattering process;

- 303 • photons from inclusive π^0 production;

- 304 • and to a lesser extent, charged pions.

305 Concerning HCal, various hadronic backgrounds are expected to contribute to the rates
 306 in HCal, the dominant ones being pions. Both the inelastic scattering and the inclusive
 307 neutral and charged pion production are implemented in G4SBS, the latter relying on the
 308 Wiser parametrization [?]. The minimum-bias “beam-on-target” generator (including all
 309 electromagnetic and hadronic processes) has also been considered for the HCal background.

310 The thresholds to apply to each arm are determined as a function of the elastic peak. For
 311 the electron arm, the threshold has been set at $\mu_E - 2.5\sigma_E$, μ_E and σ_E being respectively
 312 the position and width of the fitted elastic peak. Fig. ?? presents the distributions of rate
 313 of energy deposit for the different processes involved in the BigBite trigger rates.

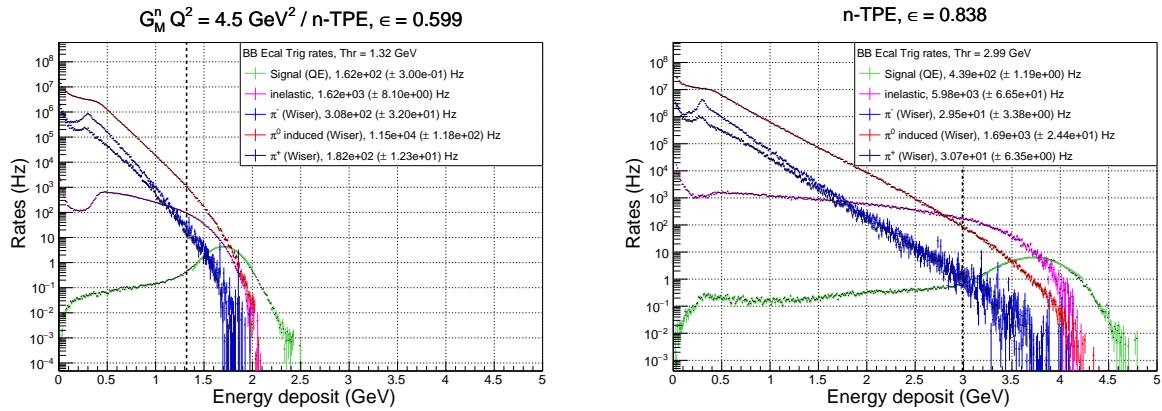


FIG. 8. Rates of the different process contributing to the BigBite electron arm trigger, for the low ϵ (left) and the high ϵ (right). Quasi-elastic is in green, inelastic in magenta, π^0 in red, π^- in blue, and π^+ in dark blue. Note the resolution for the elastic peak in the BigBite shower is ~ 0.3 GeV.

314 Since HCal is a sampling calorimeter (meaning that only a fraction of the shower energy
 315 is measured), its resolution is relatively wide (~ 0.7 GeV). Due to this, the threshold is at
 316 90% efficiency (which corresponds to ~ 0.1 GeV for both kinematics. Fig. ?? presents the
 317 distributions of rate of energy deposit for the different processes involved in the HCal trigger
 318 rates.

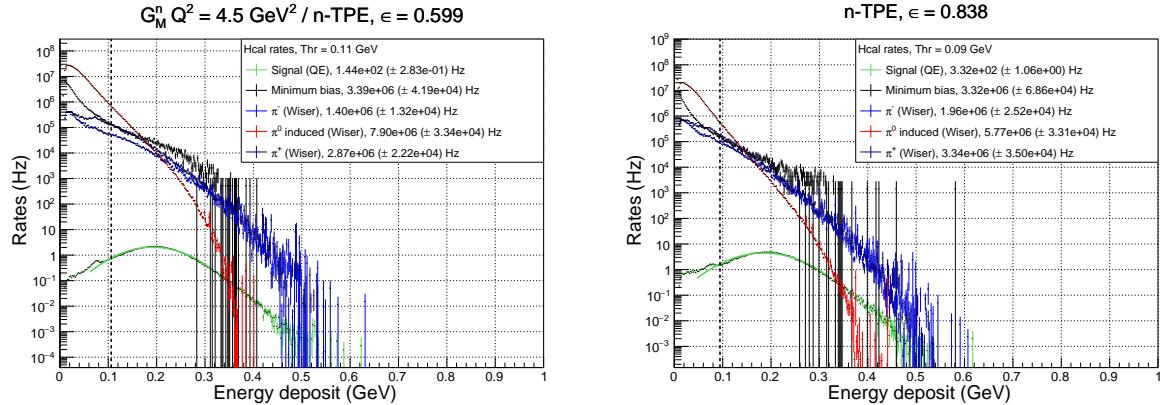


FIG. 9. Rates of the different process contributing to the HCal trigger, for the low ϵ (left) and the high ϵ (right). Quasi-elastic is in green, minimum bias in black, π^0 in red, π^- in blue, and π^+ in dark blue. Note the peak itself is around 0.2 GeV for 3.2 GeV nucleons.

320 The thresholds and trigger rates for each arm, as well as the coincidence rate (assuming
 321 30ns coincidence window), are summarized in Table. ???. Note that for HCal, the “total rates”
 322 is either the “minimum bias” beam on target, *or* the sum of inclusive charged and neutral
 323 pions evaluated with the Wiser cross sections. Comparisons between Wiser and minimum
 324 bias at very low energy shows that the Wiser code results dramatically overestimate the
 325 HCal rates, henceforth the HCal rates estimations using minimum bias are deemed more
 326 reliable (and emphasized in Table. ???. For the sake of thoroughness, we have checked the
 327 coincidence rates assuming the sum of the inclusive pions (evaluated with the Wiser cross
 328 sections) as the HCal rates.
 329

330 *Assuming this worst case scenario*, the coincidence rates could be as high as 5kHz, which
 331 might be at the limit of manageability for the DAQ. However, even if those rates were proven
 332 to be accurate, a slight increase on the HCal threshold (which would drop the efficiency from
 333 $\sim 90\%$ to $\sim 85\%$) would decrease the total HCal rates by $\sim 35\%$ to 40% in this worst case
 334 scenario, which would make the situation more manageable (3.3 kHz). In the more reasonable
 335 case where the HCal rates are more accurately described by the minimum bias prediction,
 336 the coincidence will be lower than 2kHz, rate at which the SBS DAQ should operate safely.

Point (ϵ)	1 (0.599)		2 (0.838)	
	BigBite rates (Hz)	HCal rates (Hz)	BigBite rates (Hz)	HCal rates (Hz)
threshold (GeV)	1.32	0.106	2.99	0.090
Quasi-elastic	1.62×10^2	1.44×10^2	4.39×10^2	3.48×10^2
Inelastic	1.62×10^3	-	5.98×10^3	-
π^- (Wiser)	3.08×10^2	1.40×10^6	2.95×10^2	1.96×10^6
π^0 (Wiser)	1.15×10^4	7.90×10^6	1.69×10^3	5.77×10^6
π^+ (Wiser)	1.82×10^2	2.87×10^6	3.07×10^2	3.34×10^6
Minimum bias	-	3.39×10^6	-	3.32×10^6 (*)
<i>Total</i>	1.37×10^4	3.39×10^6	8.17×10^3	3.32×10^6
$(\sum_{\pi(Wiser)} \text{for HCal})$		/ (1.22×10^7)		/ (1.11×10^7)
Coincidence rate	1.39×10^3		8.14×10^2	
$(\sum_{\pi(Wiser)} \text{for HCal})$	(5.01×10^3)		(2.72×10^3)	

TABLE II. Trigger rates for BigBite and HCal, with the different process contributions separated, and the sum. For HCal, the total rates is either estimated with the minimum bias generator or the sum of inclusive pions estimated with the Wiser cross section. The coincidence rates assume a 30 ns coincidence window.

337

B. Contamination from inelastic

338 The main source of contamination for the quasi-elastic comes from the inelastic electron-
 339 nucleon scattering. Most of this contamination can be cleaned out thanks to a selection on
 340 the center of mass energy

$$W^2 = M_N^2 + 2M_N^2(E - E') - Q^2, \quad (8)$$

341 and the missing transverse momentum of the nucleon

$$p_{\perp miss} = \sqrt{(q_x - p'_x)^2 + (q_y - p'_y)^2}, \quad (9)$$

where M_N is the mass of the nucleon, E and E' the initial and final energy of the electron, and $q_{x,y}$, $p'_{x,y}$ are the projections on x , y of the vectors of the virtual photon and final nucleon. The distributions of these quantities (weighted with cross section and including detector resolutions) are displayed for quasi-elastic and inelastic scattering, and for proton and nucleon, on Fig. ?? for the low ϵ kinematic, and on Fig. ?? for the high ϵ kinematic.

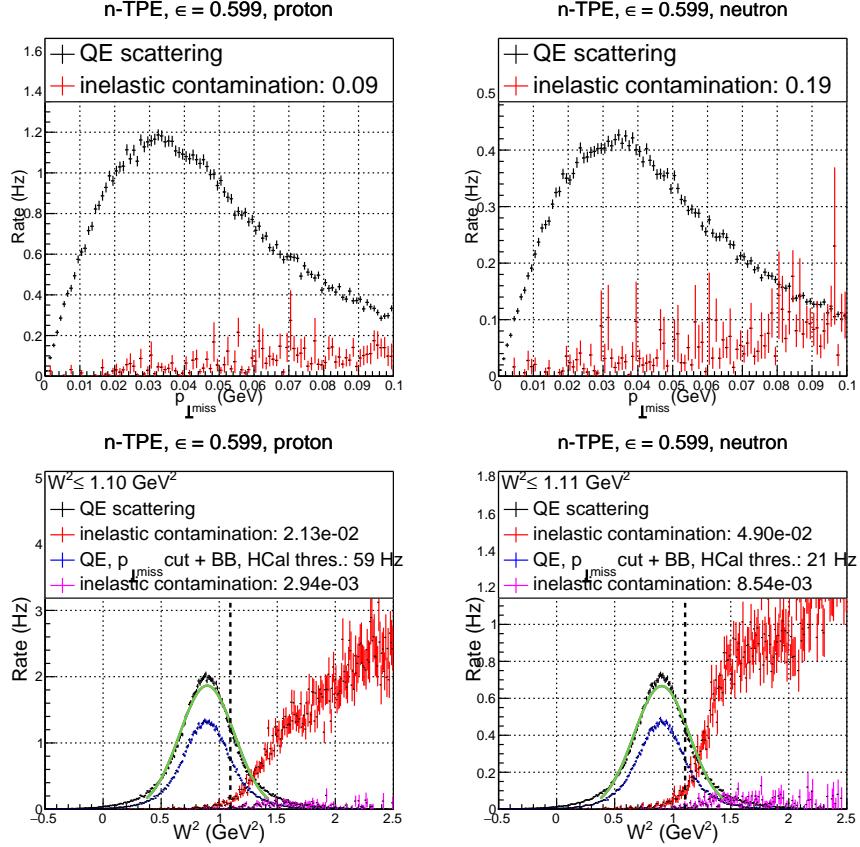


FIG. 10. Compared quasi-elastic and inelastic distributions (including detectors resolutions) for $p_{\perp miss}$ (top) and W^2 (bottom), for the low ϵ kinematic. Comparison for protons is on the left, and comparison for neutrons is on the right. On the bottom panel, black and red are before the $p_{\perp miss} \leq 0.1$ GeV selection, while blue and magenta are after $p_{\perp miss} \leq 0.1$ GeV selection and application of BigBite shower and HCal thresholds.

Provided that we are not limited by statistics and we prioritize sample purity is capital for our experiment, we set the selection criteria on W^2 and $p_{\perp miss}$ to minimize inelastic

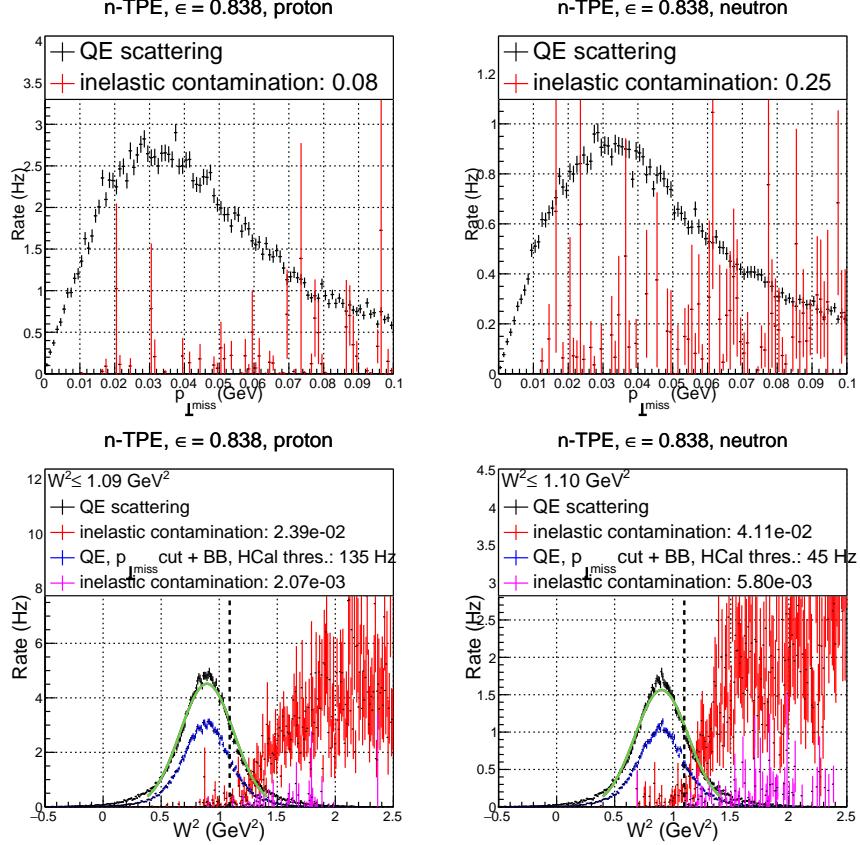


FIG. 11. Compared quasi-elastic and inelastic distributions (including detectors resolutions) for $p_{\perp miss}$ (top) and W^2 (bottom), for the high ϵ kinematic. Comparison for protons is on the left, and comparison for neutrons is on the right. On the bottom panel, black and red are before the $p_{\perp miss} \leq 0.1$ GeV selection, while blue and magenta are after $p_{\perp miss} \leq 0.1$ GeV selection and application of BigBite shower and HCal thresholds.

contamination (ideally below 1 %). Setting $p_{\perp miss} \leq 0.1$ GeV and $W^2 \leq 1.1$ GeV 2 , the inelastic contamination of the elastic sample ranges from 0.2 % to 0.9 %, while retaining ≥ 60 % of the quasi-elastic events properly recorded in the BigBite-SBS pair. Table. ?? summarizes the quasi-elastic selection cuts, and inelastic contamination δ_{inel} .

Point (ϵ)	N	W^2 cut	$p_{\perp miss}$ cut	δ_{inel}
1 (0.599)	n	1.10	0.10	2.94×10^{-3}
	p	1.11	0.10	8.54×10^{-3}
2 (0.838)	n	1.09	0.10	2.07×10^{-3}
	p	1.10	0.10	5.80×10^{-3}

TABLE III. Summary of cuts for quasi-elastic selection and resulting inelastic contamination δ_{inel} .

353

C. Quasi-elastic counting rates

354 The signals for this experiment have been generated using the G4SBS elastic/quasi-elastic
 355 generator. We generated a reasonably large sample of quasi-elastic events N_{Gen} for each
 356 kinematics, within a solid angle $\Delta\Omega_{Gen}$ that was larger than the detector acceptance. To
 357 evaluate the detector solid angle, we define simple criteria that each event has to pass, defined
 358 as follows:

- 359 • require a primary track, going through all 5 GEM layers (electron arm);
 360 • require non-zero energy deposit in both the preshower and shower (electron arm);
 361 • require non-zero energy deposit in HCal (hadron arm).

362 The detector solid angle, for both proton and neutron, are defined in Table. ???. We also
 363 define there the p - n acceptance asymmetry $A_{\Delta\Omega}$ such as:

$$A_{\Delta\Omega} = \frac{(\Delta\Omega_e \otimes \Delta\Omega_n) - (\Delta\Omega_e \otimes \Delta\Omega_p)}{(\Delta\Omega_e \otimes \Delta\Omega_n) + (\Delta\Omega_e \otimes \Delta\Omega_p)} \quad (10)$$

364 Then, we evaluate the detection efficiency. For the electron, we require the energy recon-
 365 structed in the BigBite calorimeter to be above a threshold defined as $thr = \mu_E - 2.5 * \sigma_E$, as
 366 well as a minimum number of GRINCH PMTs fired due to the primary electron; For HCal,
 367 we select a threshold that yields 90% efficiency. These values are summarized in Table. ???.
 368 Quasi-elastic selection efficiency η_{sel} are also provided.

369 The counting rates are evaluated using among the N_{Gen} events generated the events that
 370 have passed the selection described below, and weighting those events with the cross section

Point (ϵ)	$\Delta\Omega_e$ (msr)	$\Delta\Omega_e \otimes \Delta\Omega_n$ (msr)	$\Delta\Omega_e \otimes \Delta\Omega_p$ (msr)	$A_{\Delta\Omega}$ (%)
1 (0.599)	52.4	46.7	47.2	0.5
2 (0.838)	32.7	20.8	22.2	3.0

TABLE IV. Kinematics electron solid angle, and convoluted electron/hadron solid angle, and acceptance asymmetry.

Point (ϵ)	BB thr. (GeV)	HCal thr. (GeV)	$\eta_{det\ e}$	$\eta_{det\ n}$	$\eta_{det\ p}$	$\eta_{sel\ n}$	$\eta_{sel\ p}$
1 (0.599)	1.32	0.11	0.902	0.904	0.892	0.589	0.605
2 (0.838)	2.99	0.09	0.808	0.889	0.882	0.617	0.647

TABLE V. Kinematics electron thresholds, particle detection efficiencies (η_{det}), and efficiency of quasi-elastic selection η_{sel} separated for the proton and the neutron.

³⁷¹ $d\sigma/d\Omega|_i$ calculated by G4SBS, multiplied by the generation solid angle $\Delta\Omega_{Gen}$, using the
³⁷² formula:

$$N_{est} = \frac{\mathcal{L}_{exp}\Delta t}{N_{Gen}} \times \sum_{i \in \text{accepted evts}} \left(\frac{d\sigma}{d\Omega} \Big|_i \times \Delta\Omega_{Gen} \right) , \quad (11)$$

³⁷³ where Δt the running time and \mathcal{L}_{exp} the experimental luminosity. \mathcal{L}_{exp} can be calculated as
³⁷⁴ follows:

$$\mathcal{L}_{exp} = \frac{I_{exp}}{q_e} \cdot L_{tgt} \cdot d_{tgt} \frac{N_A}{m_D} , \quad (12)$$

³⁷⁵ where I_{exp} is the beam current, q_e is the electron charge, L_{tgt} and d_{tgt} are the target length
³⁷⁶ and density respectively, N_A is Avogadro's number, and m_D is the deuterium mass number.

³⁷⁷ Events are “accepted” if they meet the following criteria:

³⁷⁸ • the electron is in the BigBite acceptance;

³⁷⁹ • the electron passes the BigBite threshold defined in Table ?? and gives signal in the
³⁸⁰ GRINCH;

- 381 • the nucleon is in the HCal acceptance and passes the HCal threshold defined in Ta-
 382 ble ??;
- 383 • the event passes the quasi-elastic selection defined in the previous section *i.e.* $W^2 \leq 1.1 \text{ GeV}^2$
 384 and $p_{\perp miss} \leq 0.10 \text{ GeV}$.

385 The total quasi-elastic statistics N_{QE} , as well as the total form factor, F^2 :

$$F^2 = \frac{N_{QE}}{\mathcal{L}_{exp} \cdot \Delta t \cdot d\sigma_{Mott}/d\Omega \cdot \Delta\Omega \cdot \eta} \quad (13)$$

386 and its statistical error $\Delta F^2 = F^2 / \sqrt{N_{QE}}$ are compiled for both kinematics in Table. VI,
 387 assuming a running time $\Delta t = 12$ hours of running at a beam intensity of $I_{exp} = 30 \mu\text{A}$ on
 388 a liquid deuterium target with length $l_{tgt} = 15 \text{ cm}$ and density $d_{tgt} = 0.169 \text{ g.cm}^{-3}$. In
 389 Eq. 13, $\Delta\Omega$ is the convoluted BigBite-HCal solid angle, and η is the product of all efficiencies
 390 (detection efficiencies $\eta_{det} \times$ selection efficiency η_{sel}).

Point (ϵ)	N_{QE} (e-n)	N_{QE} (e-p)	F_n^2 ($\times 10^{-3}$)	ΔF_n^2 ($\times 10^{-6}$)	F_p^2 ($\times 10^{-3}$)	ΔF_p^2 ($\times 10^{-6}$)
1 (0.599)	9.07×10^5	2.55×10^6	0.99	1.04	2.73	1.70
2 (0.838)	1.94×10^6	5.83×10^6	0.72	0.52	1.93	0.80

TABLE VI. Quasi-elastic counting rates, and total form factor (defined in Eq. 11).

391 The calculation of the F_2 term requires the evaluation of the Mott cross section:

$$\sigma_{Mott} \equiv \frac{d\sigma_{Mott}}{d\Omega} = (\hbar c \alpha_{EM})^2 \frac{1}{4E^2} \left(\frac{\cos \theta_e/2}{\sin^2 \theta_e/2} \right)^2 \frac{E'}{E} \quad (14)$$

392 The Mott cross section has been calculated with the weighted average of the electron variables
 393 (momentum and polar angle).

Point (ϵ)	$\langle \theta_e \rangle$	$\langle k' \rangle$	$\langle Q^2 \rangle$	σ_{Mott}
	(deg)	(GeV)	(GeV 2)	(nb sr $^{-1}$)
1 (0.599)	41.88	2.0	4.5	6.62
2 (0.838)	23.23	4.2	4.5	44.2

TABLE VII. The Mott cross section weighted average of kinematic variables over the BigBite acceptance.

394

VII. SYSTEMATIC ERRORS

In this section we will estimate (or set upper limits on) the contributions to the systematic uncertainty for this experiment. The sources of systematic uncertainties from the experimental setup (target, acceptance, inelastic contamination) were already estimated for the SBS G_M^n experiment proposal [?]. Note that a majority of the potential sources of systematic uncertainties (nuclear corrections, accidentals, radiative corrections, target density, etc) cancel in the ratio $R = f_{corr} \times N_{e,e'n}/N_{e,e'p}$, which is one of the strengths of this experimental method. The sources of uncertainties as well as their estimation for each kinematic is provided in Table. ???. Since the experimental setup has evolved since then, some of these uncertainties have been reevaluated, namely the acceptance loss and inelastic contamination.

Table. IX lists the estimated contributions to systematic errors on the two-photon-exchange

TABLE VIII. Estimated contributions (in percent) to the systematic error on $R = f_{corr} \times N_{e,e'n}/N_{e,e'p}$. Quantities marked with * are taken from the SBS G_M^n experiment proposal [?].

The total systematic errors on R is the quadratic sum of all other errors.

Kinematic (ϵ)	(1) 0.599	(2) 0.838
Acceptance losses	0.5 %	3.0 %
Inelastic contamination	0.9 %	0.6 %
Nucleon mis-identification*	0.6 %	
Syst. error on $R = f_{corr} \times N_{e,e'n}/N_{e,e'p}$ (Quadratic sum of the errors above)	1.3 %	3.1 %

405

406

contribution (TPE). The systematics for S_c^p and $\mu_n G_E^n/G_M^n$ have already been explicated in Sec. ??, and are the leading contributions to the total uncertainty.

Inelastic contamination has been reevaluated in Sec. ???. To evaluate the upper limit on our uncertainty, we added quadratically the inelastic contamination evaluated for the proton and the neutron for each kinematics. This would be the error that we make on R if we ignore

TABLE IX. Estimated contributions to systematic error on the Rosenbluth slope.

Syst. error on p cross section ($S_c^p = \sigma_L^p / \sigma_T^p$)	0.01
Syst. error on n form factor ($\mu_n G_E^n / G_M^n$)	0.05
Syst. error on Rosenbluth slope (TPE)	0.012

⁴¹³ the inelastic contamination in the quasi-elastic $e - n$ and $e - p$ samples. Even in this case, we
⁴¹⁴ expect less than 1% systematic errors. Of course, we do plan to reevaluate and subtract the
⁴¹⁵ inelastic contamination from our actual data sample, so the quoted systematic uncertainty
⁴¹⁶ coming from inelastic contamination should be a upper limit.

⁴¹⁷ The acceptance loss in SBS (*i.e.* the proportion of non-detected nucleons for each detected
⁴¹⁸ electron) have been evaluated for both kinematics. They are about 10% for the $\epsilon = 0.60$
⁴¹⁹ kinematic (meaning that for every good electron measured, we will not measure the recoil
⁴²⁰ nucleon 10% of the times), but they are over 30 % for the $\epsilon = 0.84$ kinematics, which is due to
⁴²¹ a larger spread of the nucleon imprint. The systematic uncertainty on the acceptance loss for
⁴²² the ratio $R = f_{corr} \times N_{e,e'n} / N_{e,e'p}$ is maximized by the proton-neutron solid angle asymmetry
⁴²³ $A_{\Delta\Omega} = \Delta\Omega_n - \Delta\Omega_p / \Delta\Omega_n + \Delta\Omega_p$. This asymmetry is about 0.5% for the $\epsilon = 0.60$ kinematic
⁴²⁴ (consistent with the G_M^n proposal), but goes up to 3% for the $\epsilon = 0.84$ kinematics.

425

VIII. BEAM TIME REQUEST

426 We request 48 hours total time (32 PAC hours of beam-on target) to measure
 427 the two-photon effect (and G_E^n in one-photon approximation) at $Q^2 = 4.5$ (GeV/c)² through
 428 a measurement of the cross sections of the reaction D(e,e'N) at a large value of the virtual
 429 photon polarization $\epsilon=0.84$. *The measurement at $Q^2 = 4.5$ (GeV/c)², $\epsilon=0.60$ is already*
 430 *scheduled as part of the SBS G_M^n experiment E12-09-019 [?].*

431 We plan to take 12 hours of data at a full luminosity of $2.86 \times 10^{38} \text{ cm}^{-2}\text{s}^{-1}$, which
 432 corresponds to a beam intensity of $I_{exp} = 30 \mu\text{A}$ on a liquid deuterium target with length
 433 $l_{tgt} = 15 \text{ cm}$ and density $d_{tgt} = 0.169 \text{ g.cm}^{-3}$. To have a better handle on our backgrounds,
 434 we also plan to take 12 hours of data at half luminosity (basically by lowering the beam
 435 intensity by a factor 2). In each of these configurations, we also need to take data on a
 436 “dummy” target (*i.e.* on a target cell identical to the one used for production, but empty)
 437 to understand the contamination of our data from the target walls.

438 In addition to this beam time, we also require 16 hours (two shifts) to change the exper-
 439 imental configuration. This configuration change means:

- 440 • BigBite spectrometer angle and distance change;
 - 441 • Beam pass change (from 4.4 GeV/2 pass to 6.6 GeV/3 pass);
- 442 If this experiment is approved, we plan to insert this experiment in the GMn E12-09-019
 443 run plan in such a way that we can avoid a change in configuration for the SBS magnet
 444 and the HCal, which is very time consuming. Table. ?? displays an excerpt of the GMn run
 445 plan, and points out where the nTPE measurement inserts. The beam pass change and the
 446 BigBite move may be done in parallel, and should take one shift (eight hours). We require
 447 an additional shift (eight hours) for beam tuning after beam pass change. The projected use
 448 of this time is summarized in Table. XI.

451 This experiment will take place in Hall A, along the already scheduled SBS G_M^n experiment
 452 E12-09-019, utilizing the BigBite spectrometer to detect electrons scattered off the liquid
 453 deuterium target, and HCal calorimeter to detect the recoiling neutron and proton.

TABLE X. Excerpt of GMn E12-09-019 run plan table, showing where the $\epsilon = 0.84$ measurement would be inserted in our run plan. The $\epsilon = 0.60$ measurement is also emphasized in blue.

Step #	task	Q^2 (GeV/c) ²	$\theta_{BB} / \theta_{SBS}$ degrees	Beam GeV	Time hours	Tech work time (h)
4b (install GEn-RP)	GEn-RP		41.9 / 24.7	-	4	4
4c (GEn-RP)	Production	4.5	41.9 / 24.7	4.4	104 (calendar) (52 PAC hours)	
4d (remove GEn-RP)	GEn-RP		41.9 / 24.7	-	56	24
4e (GMn/nTPE low ϵ)	Production	4.5	41.9 / 24.7	4.4	64 (calendar) (32 PAC hours)	
5a (conf. change)	BB/SBS/HCal		32.5 / 31.1	-	32	16
5b (beam tune)	beam		32.5 / 31.1	4.4	4	
5c (GMn)	Production	3.5	32.5 / 31.1	4.4	64 (calender) (32 PAC hours)	
6a (pass change)	beam/BB		23.2 / 31.1	6.6	8	4
6b (beam tune)	beam		23.2 / 31.1	6.6	8	
6c see Table. X	Production	4.5	23.2 / 31.1	6.6	64 (calendar) (32 PAC hours)	
7a (conf. change)	BB/SBS/HCal		58.4 / 17.5		32	16
+ (pass change)	beam		58.4 / 17.5	4.4	during SBS move	
7b (beam tune)	beam	-	58.4 / 17.5	4.4	4	
7c	Production	5.7	58.4 / 17.5	4.4	50 (calendar) (25 PAC hours)	

⁴⁵⁴ Data taking (if approved by PAC48) will take place in summer 2021 during the approved
⁴⁵⁵ and scheduled run of the GMn, E12-09-019, experiment, which is going to measure the $e - n$
⁴⁵⁶ elastic scattering cross section at $Q^2 = 4.5$ (GeV/c)² at $\epsilon=0.60$.

⁴⁵⁷ The set of instrumentation and required beam current for proposed measurement is iden-

TABLE XI. Summary table for the beam time request. Setting changes include SBS and BigBite angles change, as well as a beam pass change from 4.4 GeV (2 pass) to 6.6 GeV (3 pass). This beam pass change can mostly be done in parallel to the SBS

Task	Target	I_{exp}	time requested
Data taking (Prod.)	15 cm LD ₂	30 μ A	12 hours
Data taking (Syst.)	15 cm “Dummy”	30 μ A	4 hours
Data taking (Prod.)	15 cm LD ₂	15 μ A	12 hours
Data taking (Syst.)	15 cm “Dummy”	15 μ A	4 hours
Setting changes (BigBite move, beam pass change)			8 hours
Beam tune after beam pass change			8 hours
Total			48 hours

458 tical to one in the GMn experiment. The beam energy of 6.6 GeV will be used. One of two
 459 data points required for the cross section LT separation is already in the data taking plan of
 460 GMn.

461 There are no other measurements of TPE in the $e - n$ elastic scattering and knowledge
 462 of the TPE is essential for the understanding of the elastic electron scattering from neutron
 463 (and proton) and hadron structure. Furthermore, it is a necessary input in the analysis and
 464 interpretation of a wide range of electron scattering processes.

465 The kinematics of our measurements emphasize the same Q^2 range where TPE in $e - p$
 466 elastic scattering was observed to dominate in Rosenbluth slope. Measuring at this high
 467 momentum transfers will provide unique input for testing TPE calculations [?].

468 We propose to measure the Rosenbluth slope and extract (in one-photon approximation)
 469 $\delta G_E^n/G_M^n$ to an accuracy of 0.15, which would bring its precision to a level comparable with
 470 that of the double polarization experiments GEN-RP and GEN-He3 at such value of Q^2 .
 471 Such precision should be sufficient to detect the TPE contribution to the $e - n$ Rosenbluth
 472 slope on the three sigma level.

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