A função "cpu_time()" não é adequada para o nosso objetivo:

"cpu_time adds up the time spent by all the threads" https://software.intel.com/en-us/forums/intel-fortran-compiler/topic/281897

"cpu_time() is not suitable to measure the performance of multi-threaded code. cpu_time() will add the total time of all the threads which is likely to increase with increasing number of threads." https://stackoverflow.com/questions/15362966/fortran-openmp-more-slow-that-sequential

Usando a função "omp_get_wtime()":

VERSÃO PARALELA

```
program list06p
  CAP372 - exercise 06 - parallel version - 2019-09-21 integration of pi : 4.0/(1+x*) dx, interval: 0 to hs gfortran -Og -Wall -fcheck=all -fopenmp -o list06p list06p.f90 gfortran -fopenmp -o list06p list06p.f90
   ./list06p
   use omp_lib
   implicit none
  integer :: n, t
n=2**26
   call calc(n, t)
   call calc(n, t)
   call calc(n, t)
   n=2**28
   call calc(n, t)
   call calc(n, t)
   call calc(n, t)
   n=2**30
   call calc(n, t)
   call calc(n, t)
   call calc(n, t)
contains
  subroutine calc(n, t)
  integer, intent(in) :: n, t
  double precision, parameter :: a=0.0, b=1.0
  double precision :: pi, t1, t2, x, h, integral=0.0
      integer :: i
      t1 = omp_get_wtime()
      integral = ( ( 4.0 / ( 1.0 + a * a ) ) + & ( 4.0 / ( 1.0 + b * b ) ) ) / 2.0
h = ( b - a ) / n
!$omp parallel do private(x) reduction(+:integral) num_threads(t)
       do i = 1, n - 1
 x = a + h * i
          integral = integral + 4.0 / (1.0 + x * x)
      end do
!$omp end parallel do
     mp end parallel do
pi = integral * h
t2 = omp_get_wtime()
print*, "Partitions:", n," Threads:", t
print*, "Result:", pi, " Error:", dacos(-1.d0) - pi
print*, "Elapsed time:", t2 - t1
print*, ""
end program list06p
```

RESULTADO

```
$ gfortran -fopenmp -o list06p list06p.f90
$ ./list06p
Partitions: 67108864 Threads: 2
Result: 3.1415926535892620 Error: 5.3113069498067489E-013
Elapsed time: 0.42782379799973569

Partitions: 67108864 Threads: 3
Result: 3.1415926535899472 Error: -1.5409895581797173E-013
Elapsed time: 0.28681157699975302

Partitions: 67108864 Threads: 4
Result: 3.1415926535894423 Error: 3.5083047578154947E-013
Elapsed time: 0.22577948499747436
```

```
Partitions: 268435456 Threads: Result: 3.1415926535900667
                                                 Error: -2.7355895326763857E-013
Elapsed time: 1.6969807259993104
Partitions: 268435456 Threads: Result: 3.1415926535899752 Elapsed time: 1.1460634920003940
                                                 Error: -1.8207657603852567E-013
Partitions:
                 268435456
                                    Threads:
             3.1415926535901377
                                                 Error: -3.4461322684364859E-013
Result:
Elapsed time: 0.89091836199804675
Partitions: 1073741824 Threads
Result: 3.1415926535899747
Elapsed time: 6.7740604739992705
                                    Threads:
                                                 Error: -1.8163248682867561E-013
Partitions: 1073741824
Pasult: 3.1415926535897745
                                    Threads:
                                                 Error:
                                                            1.8651746813702630E-014
Elapsed time: 4.6008846500008076
                1073741824
Partitions: 1073741824 Result: 3.1415926535898269
                                    Threads:
                                                 Error: -3.3750779948604759E-014
Elapsed time: 3.6927661669978988
```

VERSÃO SÉRIE

```
Program list06s
! CAP372 - exercise 06 - serial version - 2019-09-21
! integration of pi : 4.0/(1+x*) dx, interval: 0 to hs
! gfortran -Og -Wall -fcheck=all -fopenmp -o list06p list06p.f90
! gfortran -fopenmp -o list06s list06s.f90
    ./list06s
   use omp_lib
implicit none
    integer :: n
   call calc(n)
n=2**28
   call calc(n)
   n=2**30
   call calc(n)
contains
   subroutine calc(n)
       integer, intent(in) :: n
       double precision, parameter :: a=0.0, b=1.0
double precision :: pi, t1, t2, x, h, integral=0.0
integer :: i
       t1 = omp_get_wtime()
       integral = ( (4.0 / (1.0 + a * a ) ) + & (4.0 / (1.0 + b * b ) ) ) / 2.0
       x = a
h = (b - a) / n
do i = 1, n - 1
x = a + h * i
           integral = integral + 4.0 / (1.0 + x * x)
       end do
       pi = integral * h
t2 = omp_get_wtime()
print*, "Partitions:", n
print*, "Result:", pi, " Error:", dacos(-1.d0) - pi
print*, "Elapsed time:", t2 - t1
print*, ""
   end subroutine
end program list06s
```

RESULTADO

```
$ gfortran -fopenmp -o list06s list06s.f90

$ ./list06s

Partitions: 67108864

Result: 3.1415926535890550 Error: 7.3807626677080407E-013

Elapsed time: 0.85066184799870825

Partitions: 268435456

Result: 3.1415926535898735 Error: -8.0380146982861334E-014

Elapsed time: 3.3845648820024508

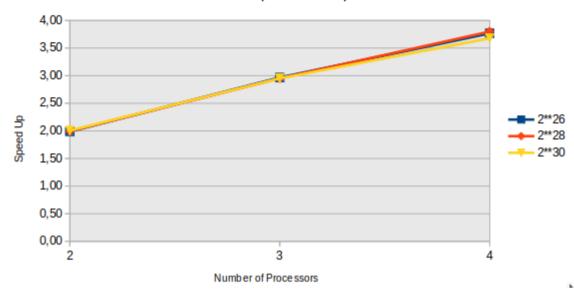
Partitions: 1073741824

Result: 3.1415926535901244 Error: -3.3129055054814671E-013

Elapsed time: 13.583390687999781
```

Partitions	Serial Algorithm	2			3			4		
			Spee	Efficie		Spee	Efficie		Spee	Efficie
	Algorithm	Time	d Up	ncy	Time	d Up	ncy	Time	d Up	ncy
2**26	0,8506618	4,28E-01	1,99	0,99	0,2868116	2,97	0,99	0,2257795	3,77	0,94
2**28	3,3845649	1,6969807	1,99	1,00	1,1460635	2,95	0,98	0,8909184	3,80	0,95
2**30	13,583391	6,7740605	2,01	1,00	4,6008847	2,95	0,98	3,6927662	3,68	0,92

Results of computational experiments



CAT /PROC/CPUINFO (processador de 2 núcleos)

```
$ cat /proc/cpuinfo
processor
vendor_id
                           : GenuineIntel
cpu family
                           : 6
                           : 142
model
                              Intel(R) Core(TM) i7-7500U CPU @ 2.70GHz
model name
stepping
microcode
                           : 0xb4
                              600.047
cpu MHz
cache size
                              4096 KB
physical id
siblings
                              0
core id
cpu cores
                              2
apicid
                              0
initial apicid
                              0
                           : yes
                           : yes
fpu_exception
cpuid level
                           : ves
flags : fpu vme de pse tsc msr pae mce cx8 apic sep mtrr pge mca cmov pat pse36 clflush dts acpi mmx fxsr sse sse2 ss ht tm pbe syscall nx pdpe1gb rdtscp lm constant_tsc art arch_perfmon pebs bts
rep_good nopl xtopology nonstop_tsc cpuid aperfmperf tsc_known_freq pni pclmulqdq dtes64 monitor ds_cpl vmx est tm2 ssse3 sdbg fma cx16 xtpr pdcm pcid sse4_1 sse4_2 x2apic movbe popcnt tsc_deadline_timer aes xsave avx f16c rdrand lahf_lm abm 3dnowprefetch cpuid_fault epb invpcid_single pti ssbd ibrs ibpb stibp tpr_shadow vnmi flexpriority ept vpid ept_ad fsgsbase tsc_adjust bmi1 avx2 smep bmi2 erms invpcid mpx rdseed adx smap clflushopt intel_pt xsaveopt xsavec xgetbv1 xsaves dtherm ida arat pln pts hwp
hwp_notify hwp_act_window hwp_epp md_clear flush_l1d
                           : cpu_meltdown spectre_v1 spectre_v2 spec_store_bypass l1tf mds swapgs
bogomips
                           : 5808.00
clflush size
                           : 64
cache_alignment: 64
address sizes
                           : 39 bits physical, 48 bits virtual
power management:
```

RODANDO EM UM PROCESSADOR DE 4 NÚCLEOS

```
ef@TOPS:~$ cat /proc/cpuinfo
processor
vendor_id
                                  : GenuineIntel
cpu family
model
                                 : 42
                                 : Intel(R) Core(TM) i7-2630QM CPU @ 2.00GHz : 7
model name
stepping
                                 : 0x2f
microcode
                                 : 798.191
cpu MHz
 cache size
                                  : 6144 KB
physical id
                                 : 0
siblings
                                  : 8
core id
                                  : 0
cpu cores
                                  : 0
apicid
initial apicid : 0
fpu
                                  : yes
fpu_exception
: yes
flags : fpu vme de pse tsc msr pae mce cx8 apic sep mtrr pge mca cmov pat pse36 clflush dts
acpi mmx fxsr sse sse2 ss ht tm pbe syscall nx rdtscp lm constant_tsc arch_perfmon pebs bts nopl
xtopology nonstop_tsc cpuid aperfmperf pni pclmulqdq dtes64 monitor ds_cpl vmx est tm2 ssse3 cx16 xtpr
pdcm pcid sse4_1 sse4_2 x2apic popcnt tsc_deadline_timer aes xsave avx lahf_lm epb pti ssbd ibrs ibpb
stibp tpr_shadow vnmi flexpriority ept vpid xsaveopt dtherm ida arat pln pts md_clear flush_l1d
bugs : cpu_meltdown spectre_v1 spectre_v2 spec_store_bypass l1tf mds swapgs
bogomips : 3990.95
clflush size : 64
cpuid level
bogomips
clflush size
                                 : 64
cache_alignment : 64
address sizes : 36 bits physical, 48 bits virtual
power management:
```

PARALELO

```
ef@TOPS:~$ gfortran -fopenmp list06p.f90 ef@TOPS:~$ ./a.out
Partitions: 67108864
Result: 3.1415926535892620
                                 Threads:
                                                        5.3113069498067489E-013
                                             Error:
 Elapsed time: 0.63812972799996714
 Result: 3.1415926535894432
                                             Error:
                                                        3.4994229736184934E-013
 Elapsed time: 0.34222608099997842
                  67108864
 Partitions:
                                 Threads:
            3.1415926535898167
                                             Error:
                                                       -2.3536728122053319E-014
 Result:
 Elapsed time: 0.17422291200000473
 Partitions: 268435456 Threads: Result: 3.1415926535900667 Elapsed time: 2.5080567939999696
                                             Error: -2.7355895326763857E-013
                268435456
 Partitions:
                                 Threads:
 Result: 3.1415926535901377
                                             Error: -3.4461322684364859E-013
 Elapsed time: 1.3487727319999863
 Partitions: 268435456
Result: 3.1415926535898744
                268435456
                                 Threads:
                                             Error: -8.1268325402561459E-014
 Elapsed time: 0.71615645599996469
 Partitions: 1073741824
Result: 3.1415926535899747
                                 Threads:
                                             Error: -1.8163248682867561E-013
 Elapsed time: 10.058801081000013
 Partitions: 1073741824
Result: 3.1415926535898269
                                 Threads:
                                                       -3.3750779948604759E-014
                                             Error:
 Elapsed time: 5.3947735290000196
               1073741824
 Partitions:
Result: 3.1415926535897096
Elapsed time: 2.8449099649999994
                                             Error:
                                                        8.3488771451811772E-014
```

SÉRIE

```
## SINTE

## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ## 1875  ##
```

SPEED UP

Partitions	Serial Algorithm	2			4			8		
			Spee	Efficie		Spee	Efficie		Spee	Efficie
	Algorithm	Time	d Up	ncy	Time	d Up	ncy	Time	d Up	ncy
2**26	1,2188645	6,38E-01	1,91	0,96	0,3422261	3,56	0,89	0,1742229	7,00	0,87
2**28	4,8607448	2,5080568	1,94	0,97	1,3487727	3,60	0,90	0,7161565	6,79	0,85
2**30	19,422819	10,058801	1,93	0,97	5,3947735	3,60	0,90	2,84491	6,83	0,85

Results of computational experiments

