CAP-372 / 2019 - QUARTA LISTA DE EXERCÍCIOS

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Exercício de integração numérica. Função escolhida:

$$\int x^n dx = \frac{1}{n+1} x^{n+1}$$

Intervalo = [a,b] = [-100, 900]

O resultado $\acute{e} = 164.000.000.000$

Programa:

```
! $ gfortran -o intetrap intetrap.f90
! $ ./intetrap
PROGRAM intetrap
     IMPLICIT NONE
    DOUBLE PRECISION, PARAMETER :: a = -100D0, b = 900D0

CALL CalcInterv(a, b, 2**10)

CALL CalcInterv(a, b, 2**20)

CALL CalcInterv(a, b, 2**30)
CONTAINS
    FUNCTION F(x)
         IMPLICIT NONE
         DOUBLE PRECISION :: F
DOUBLE PRECISION, INTENT(IN) :: x
F = (x**3) ! function x<sup>3</sup>
     \textbf{END FUNCTION} \ \ \mathbb{F}
     FUNCTION TRAP(local_a, local_b, local_n)
          IMPLICIT NONE
         DOUBLE PRECISION :: TRAP
DOUBLE PRECISION, INTENT(IN) :: local_a, local_b
          INTEGER, INTENT(IN) :: local_n
INTEGER :: i
DOUBLE PRECISION :: integral, x, h
          integral = (F(local_a) + F(local_b))/2.0

x = local_a

h = (local_b - local_a)/local_n
          DO i = 1, local_n - 1
x = x + h
              integral = integral + F(x)
         ENDDO
TRAP = integral*h
     END FUNCTION TRAP
SUBROUTINE CalcInterv(a, b, n)
         IMPLICIT NONE
          DOUBLE PRECISION, INTENT(IN) :: a, b
          INTEGER, INTENT(IN) :: n
DOUBLE PRECISION :: r
         REAL :: t1, t2
CALL CPU_TIME(t1)
          CALL CFO_TARD(CF, r = TRAP(a, b, n)

CALL CPU_TIME(t2)

PRINT *, "Result=", r, "for", n, "partitions in", t2-t1, "s"
    END SUBROUTINE CalcInterv
END PROGRAM intetrap
```

Teste no PC local (Intel i7):

```
$ gfortran -o intetrap intetrap.f90
$ ./intetrap
Result= 164000190734.86325 for 1024 partitions in 3.89998313E-05 s
Result= 164000000000.18250 for 1048576 partitions in 2.44660005E-02 s
Result= 164000000000.00443 for 1073741824 partitions in 4.90481424 s
```

Usando MPI:

```
! CAP372 exercise 4 - trapezoidal rule - 2019-09-01 ! function: y = x³; integral: x⁴ / 4 ! range a = -100 and b = 900, result = 164.000.000.000 ! cat /proc/cpuinfo | grep proc --> 4 ! $ mpif90 -o intetrapprl intetrapprl.f90 ! $ mpirun -n 4 ./intetrapprl
PROGRAM intetrapprl
   USE MPT
   IMPLICIT NONE
   INTEGER :: n !
INTEGER :: ierror
                           ! qty of partitions; should be multiple of p
   DOUBLE PRECISION, PARAMETER :: a = -100D0, b = 900D0 ! interval
   CALL MPI_Init(ierror)
   n = 2**10
  CALL CalcInterv(a, b, n)

n = 2**20
   CALL CalcInterv(a, b, n)
   CALL CalcInterv(a, b, n)
  CALL MPI_Finalize(ierror)
CONTAINS
   FUNCTION f(x)
     IMPLICIT NONE
      DOUBLE PRECISION :: f
     DOUBLE PRECISION, INTENT(IN) :: x
      f = (x**3)
                          ! function x3
   END FUNCTION F
   FUNCTION Trap(local_a, local_b, local_n)
     IMPLICIT NONE
     DOUBLE PRECISION :: Trap
DOUBLE PRECISION, INTENT(IN) :: local_a, local_b
INTEGER, INTENT(IN) :: local_n
INTEGER :: i
     DOUBLE PRECISION :: integral, x, local_h
     integral = (f(local_a) + f(local_b))/2.0
     x = local_a
     local_h = (local_b - local_a)/local_n
DO i = 1, local_n - 1
x = x + local_h
         integral = integral + f(x)
     ENDDO
Trap = integral * local_h
   END FUNCTION Trap
   SUBROUTINE CalcInterv(a, b, n)
      IMPLICIT NONE
      DOUBLE PRECISION, INTENT(IN) :: a, b ! interval INTEGER, INTENT(IN) :: n ! qty of p
                                                                ! qty of partitions
      INTEGER :: my_rank
                                                               ! rank
     INTEGER :: p ! qty o
INTEGER :: source, dest, ierror, part_n
INTEGER, PARAMETER :: tag = 0
INTEGER, DIMENSION(MPI_STATUS_SIZE) :: status
                                                               ! qty of processes
      DOUBLE PRECISION :: r, tot, h, hn, part_a, part_b
     REAL :: ta, tb, tc
     CALL MPI_Comm_rank(MPI_COMM_WORLD, my_rank, ierror)
CALL MPI_Comm_size(MPI_COMM_WORLD, p, ierror)
CALL MPI_Barrier(MPI_COMM_WORLD, ierror)
      CALL CPU_TIME(ta)
     h = (b - a) / n
part_n = n / p
hn = h * part_n
                                                               partition size
                                                            ! partitions per process
                                                            ! process size
```

Teste no PC local (Intel i7):

```
$ mpif90 -o intetrapprl intetrapprl.f90

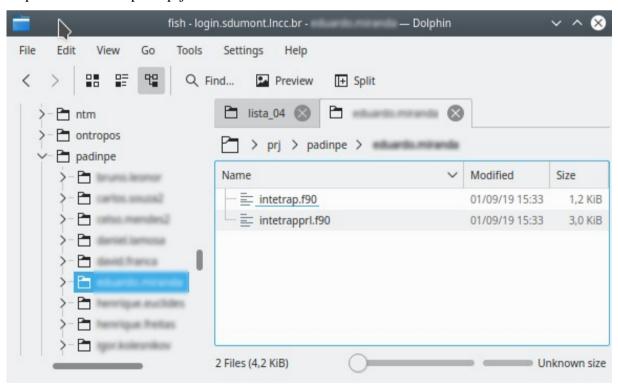
$ mpirun -n 4 ./intetrapprl

Result= 164000190734.86325 for 1024 partitions in 5.50001860E-05 s

Result= 164000000000.18051 for 1048576 partitions in 7.85399973E-03 s

Result= 164000000000.00674 for 1073741824 partitions in 2.58868909 s
```

Copiando os fontes para /prj

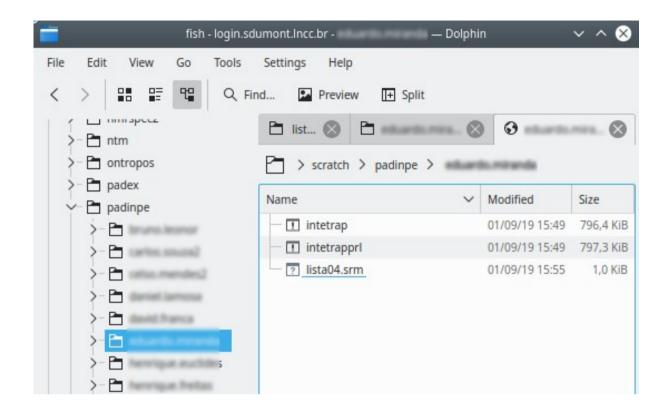


Compilando em /prj

Execução para testes em /prj

```
[xxxxxxx.xxxxxxe@sdumont11 ~]$ ./intetrap
Result= 16400190734.863 for 1024 partitions in 3.0000228E-06 s
Result= 16400000000.182 for 1048576 partitions in 5.9999991E-04 s
Result= 16400000000.014 for 1073741824 partitions in 0.5608560 s
[xxxxxxx.xxxxxxe@sdumont11 ~]$ ./intetrapprl
Result= 164000190734.863 for 1024 partitions in 3.9972365E-06 s
Result= 16400000000.182 for 1048576 partitions in 6.5699965E-04 s
Result= 16400000000.014 for 1073741824 partitions in 0.6175130 s
[xxxxxxx.xxxxxxxe@sdumont11 ~]$
```

Copiando os executáveis para /scratch



Rodando em /scratch

```
[xxxxxxx.xxxxxx@sdumont11 ~]$ cd /scratch/padinpe/xxxxxx.xxxxxxxxxxxx
[xxxxxxx.xxxxxx@sdumont11 xxxxxxx.xxxxxxx]$ sbatch lista04.srm
Submitted batch job 395819
[xxxxxxx.xxxxxxx@sdumont11 xxxxxxx.xxxxxxx]$ ls
intetrap intetrappr1 lista04.srm slurm-395819.out
[xxxxxxx.xxxxxx@sdumont11 xxxxxxx.xxxxxxx]$
```

SAÍDA

```
$ cat. slurm-395819.out.
sdumont1391
sdumont1391
            164000190734.863
                                                  1024 partitions in
                                                                        4.0000305E-06 s
 Result=
                                     for
 Result=
            164000190734.863
                                     for
                                                  1024 partitions in
                                                                         4.9998052E-06 s
            164000190734.863
164000190734.863
 Result=
                                     for
                                                  1024 partitions in
                                                                        1.1000317E-05 s
                                                       partitions in
                                                                         1.2999866E-05 s
 Result=
                                     for
                                                  1024
                                                                        4.0000305E-06 s
5.0002709E-06 s
            164000190734.863
                                                  1024 partitions in 1024 partitions in
 Result=
                                     for
            164000190734.863
 Result=
                                     for
            164000190734.863
                                                  1024 partitions in
 Result=
                                     for
            164000190734.863
                                                  1024 partitions in
                                                                         3.9995648E-06 s
 Result=
                                     for
                                              1048576 partitions in
 Result=
            16400000000.182
                                     for
                                                                         6.0799997E-04 s
                                              1048576 partitions in
1048576 partitions in
1048576 partitions in
                                                                         6.0799997E-04 s
 Result=
            164000000000.182
                                     for
            16400000000.182
                                                                         6.0700066E-04 s
 Result=
                                     for
            164000000000.182
                                                                         6.0500018E-04 s
 Result=
                                     for
            16400000000.182
                                              1048576 partitions in
                                                                         5.7100039E-04 s
 Result=
                                     for
            16400000000.182
                                              1048576 partitions in
 Result=
                                     for
                                                                         5.7100039E-04 s
 Result=
            16400000000.182
                                              1048576 partitions in
                                     for
                                                                         6.2000006E-04
 Result=
            164000000000.182
                                     for
                                              1048576
                                                       partitions in
 Result=
            16400000000.014
                                     for
                                           1073741824 partitions in 1073741824 partitions in
                                                                         0.6153200
            164000000000.014
                                                                         0.6169440
 Result=
                                     for
                                                                                         S
            164000000000.014
                                           1073741824 partitions in
                                                                         0.6181700
 Result=
                                     for
                                                                                         S
 Result=
            164000000000.014
                                           1073741824 partitions in
                                                                         0.6196440
                                     for
                                                                                         S
            164000000000.014
                                           1073741824 partitions in
                                                                         0.6197030
 Result=
                                     for
                                                                                         S
 Result=
            16400000000.014
                                     for
                                           1073741824 partitions in
                                                                         0.6206610
                                                                                         S
 Result=
            16400000000.014
                                           1073741824 partitions in
                                                                         0.6207520
                                     for
 Result=
            164000000000.014
                                     for
                                           1073741824 partitions in
                                                                        0.6231370 s
3.4260005E-03 s
            164000190734.863
                                                  1024 partitions in
 Result=
                                     for
```

```
Result= 164000000000.182 for 1048576 partitions in 1.0200590E-04 s
Result= 16399999999.998 for 1073741824 partitions in 8.8807002E-02 s
```

A saída não foi o esperado, ficou diferente dos demais testes realizados no pc local e em /prj . Porém é possível utilizar os tempos medidos.

RESULTADO

O Speedup é o tempo de um programa serial dividido pelo tempo do programa paralelo:

Para 2^{10} partições S1 = 3.4260005E-03 / 5.0002709E-06 = 685

Para 2^{20} particões S2 = 1.0200590E-04 / 6.6399947E-04 = 0.15

Para 2^{30} partições S3 = 8.8807002E-02 / 0.6231370 = 0.14

A Eficiência é o Speedup dividido pelo nro. de processadores:

E1 = 685 / 8 = 85

E2 = 0.019

E3 = 0.018

CONCLUSÃO

Foi possível rodar conforme descrito na lista de exercícios, e os resultados mostraram que para um grande número de partições (áreas) o resultado em /scratch foi pior do que rodando em /prj . É necessário investigar mais para ter certeza, porém aparentemente isso mostra que existe uma parte não paralelizável que está influenciando no resultado. Também é necessário investigar por que a tela de saída ficou diferente em /scratch quando comparado com a execução em /prj e no pc local.

REFERÊNCIAS

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