Penenne unemors ypobneme 2 regorges

P-ra lugbur - Ociparpognes:
$$W(y_i, y) = Ce^{-\sum_{x_i} \frac{a_i(t)}{a_i(t)} dt} = C_i(x)$$

$$\left|\begin{array}{ccc} y', & y', \\ y', & y' \end{array}\right| = Cu(x) \qquad \frac{y \cdot y' - y \cdot y'}{y^2} = \frac{Cu(x)}{y^2}$$

$$\left(\frac{y}{y}\right)' = \frac{C\varphi(x)}{y^2}$$

OPMY: bagnanges normoni:
$$y = (, (x)y, (x) + (, (x)y, (x))$$

$$C_{1}^{2}(x)y_{1}+C_{1}^{2}(x)y_{2}=0$$

$$C'(x) y'_{1} + C'_{2}(x) y'_{2} = \frac{b(x)}{a}$$

$$\Delta = W(y_1, y_2) \neq 0$$

$$C_{1}(x) = ...$$
 $C_{2}(x) = ...$

Bagara 1

$$2xy'' + (4x+1)y' + (2x+1)y = e^{-x}$$
, $x>0$

$$y - mough.$$
, $y - y - g - mx + 1$
 $W(y_1, y) = Ce^{-\int_{x_0}^{x} \frac{nx+1}{2x} dx} = Ce^{-(2x + \frac{1}{2} \ln x)} = Ce^{-2x} x^{-\frac{1}{2}}$

$$\int_{x_{2}}^{x} \frac{u_{X+1}}{z_{X}} dx = 2x + \frac{1}{z} \int_{x_{2}}^{x} \frac{1}{z} dx = 2x + \frac{1}{z} \ln x + C,$$

$$W(y,y) = \begin{vmatrix} e^{-x} & y \\ -e^{-x} & y \end{vmatrix} = y'e^{-x} + ye^{-x}$$

Drum no
$$e^{-2x}$$
:

 $\frac{y' e^{-x} + y e^{-x}}{e^{-2x}} = Cx^{-1/2}$
 $(x-x)' = Cx^{-1/2}$

$$\begin{cases} (', x) e^{-x} + C_{2}(x) e^{-x} \int_{x}^{x} = 0 \\ -C_{1}(x) e^{-x} - C_{2}(x) e^{-x} \int_{x}^{x} + C_{1}(x) \frac{e^{-x}}{2\sqrt{x}} = \frac{e^{-x}}{2x} \end{cases}$$

$$C_{2}(l_{x}) = \frac{l}{\sqrt{x}}$$

$$C_{1}(k) = -1$$

$$C_{2}(k) = 2 \sqrt{k} + C_{2}$$

$$C_{1}(k) = -x + C_{1}$$

Orber:
$$y = (-x+C_1) e^{-x} + (2\int_X + C_2) e^{-x} \int_X = C_1 e^{-x} + C_2 e^{-x} + x e^{-x}$$

$$(x^{2}(\ln x - 1)y^{2} - xy^{2} + y = x(\ln x - 1)^{2}, x > e)$$

UPOY 1 $y_{1} = x$

$$y_i = x$$

$$\begin{vmatrix} y_1 & y_2 \\ y_1 & y_2 \end{vmatrix} = Ce^{\int \frac{dx}{x(\ln x - 1)}} = C(\ln x - 1)$$

$$\int \frac{dx}{x(\ln x - i)} = \int \frac{d(\ln x - i)}{(\ln x - i)} = \ln(\ln x - i) + C$$

$$\frac{y_1y'-y_1y}{y_1^2}=\frac{C(\ln x\cdot 1)}{x^2} \qquad \left(\frac{\ln x}{x}\right)'=\frac{1-\ln x}{x^2}$$

$$\left(\frac{y}{y_{i}}\right)^{1} = \frac{C(\ln x - 1)}{x^{2}}$$

$$\frac{x}{y} = c \frac{\ln x}{x} + C$$

$$\begin{cases} C_1'(x) \times + C_2'(x) \ln x = 0 \\ C_1'(x) + C_2'(x) \frac{1}{x} = \frac{\ln x - 1}{x} \quad | \cdot x \rangle \\ C_1'(x) \times + C_2'(x) \ln x = 0 \\ C_1'(x) \times + C_2'(x) = \ln x - 1 \\ C_2'(x) = -1 \qquad C_1'(x) = \frac{\ln x}{x} \\ C_1(x) = -x + C_2 \qquad C_1(x) = \frac{\ln^2 x}{2} + C_1 \end{cases}$$

Orber:
$$y = \frac{\ln^2 x}{2} + C_1 \times + \frac{(C_2 - x) \ln x}{2}$$

 $y = C_1 x + (2 \ln x + \frac{x \ln^2 x}{2} - x \ln x)$

Bogora 3

$$(2x+3) y'' - 2y' - \frac{6}{\lambda^2} y = 3(2x+3)^2$$
Wherem 4POY B large x^{k} :
$$K(k-1) \cdot (2x+3) x^{k-2} - 2Kx^{k-1} - 6x^{k-2} = 0$$

$$(2x+3) k(x-1) - 2Kx - 6 = 0$$

$$(2x+3) k(k-1) - 6 = 0$$

$$K=2 \Rightarrow y = x^2$$

$$\begin{vmatrix} y_1 & y_2 \\ y_1 & y_2 \end{vmatrix} = Ce^{\int \frac{2}{2\lambda + 3}} dx$$

$$\left(\frac{y}{y}\right)^{2} = \frac{2C}{x^{3}} + \frac{3C}{x^{3}} \Rightarrow \frac{y}{y} = C\left(\frac{1}{x^{2}} + \frac{1}{x^{3}}\right) + C$$

$$OP OY \quad y = C, \quad x^{2} + C_{2}\left(\frac{1}{x} + 1\right)$$

Opny:
$$y = (1/x)x^2 + C_1(x)(\frac{1}{x}+1)$$

$$C_1(x)x^2 + C_2(x)(\frac{1}{x}+1) = 0 \quad | \quad 1 \leq C_1(x) \quad 2x - C_2(x)(\frac{1}{x}) = 0 \quad | \quad 1 \leq x + 0$$

$$- \begin{cases} 2C_1 \times^2 + 2C_2 \cdot \left(\frac{1}{x} + 1\right) = 0 \\ 2C_1 \times^2 - C_2 \cdot \frac{1}{x} = 6x^2 + 9x \end{cases}$$

$$3C_{1}^{2}\frac{1}{x}+2C_{1}^{2}=-6x^{2}-9x$$

$$C_{1}^{1} = -3x^{2}$$

$$C_{1}^{2} = 3 + \frac{3}{x}$$

$$C_{2} = -x^{3} + C_{1}$$

$$C_{1} = 3x + 3 \ln x + C_{1}$$

$$y = (3x + 3 \ln x + C_{1})x^{2} + (-x^{3} + C_{2})(\frac{1}{x} + 1)$$

$$y = C_{1}x^{2} + C_{1}(\frac{1}{x} + 1) + 3x^{2} \ln x + 2x^{3} - x^{2}$$

$$y = C_{1}x^{2} + C_{2}(\frac{1}{x} + 1) + 2x^{3} + 3x^{2} \ln x$$

Ypabneme Beccess

$$x^{2}y'' + xy' + (x^{2} \cdot y^{2}) y = 0, y = const$$

D-96, zie yp-e ne nomei uneio zi um nezab. pem-un, ay. l'agn-in O brace. Le c spouzbogovern.

$$W(y_1,y) = \begin{vmatrix} y_1 & y_2 \\ y_1' & y_2' \end{vmatrix} = Ce^{-\int_{x_0}^{x_0} \frac{dx}{x}} = \frac{C}{x}, C \neq 0 \text{ i.e., } y_1 = y_2 \text{ i.m., negal.}$$

$$y, y, -y, y_2 = \frac{C}{x}$$
 $corp. 8 oxp-in 0$ selono neoxp.

Viz.

Apribegeme un yp-ni 20 rapagna k bugy, ne cog-y

$$a_0(x)y' + a_1(x)y' + a_2(x)y = 0$$

$$-\frac{1}{2} + a_1(x)z = 0$$

$$Z'' + a_1(x)z = 0$$

$$-\frac{1}{2} + a_2(x)y' + a_2(x)y = 0$$

$$-\frac{1}{2} + a_1(x)y' + a_2(x)y = 0$$

$$y = 2 \cdot erp\left(-\frac{1}{2}\int_{\lambda_0}^{\lambda} \frac{a_1(t)}{a_0(t)} dt\right)$$

By yp-m Secreta:
$$y = z x^{-1/2}$$

$$y' = z'x^{-1/2} - \frac{1}{2}z x^{-3/2}$$

$$y'' = z''x^{-1/2} - \frac{1}{2}z'x^{-1/2} - \frac{1}{2}z'x^{-1/2} + \frac{3}{4}z x^{-5/2}$$

Manyreen
$$z'' x''^2 - z' x'' + \frac{3}{4} z x^{-1/2} + \frac{1}{2} x''^2 - \frac{1}{2} z x''^4 + (x^2 - V^2) z x''^2 = 0$$

$$z'' x''^2 + \frac{1}{4} z x^{-1/2} + z x''^2 - V^2 z x''^2 = 0 \quad | : x''^2$$

$$z'' + \frac{1}{4} x^{-2} + z - V^2 z x'^2 = 0$$

$$Z'' + 2\left(1 + \frac{\frac{1}{4} - J^2}{\chi^2}\right) = 0$$

$$Illy J = \pm \frac{1}{2} \rightarrow 0 \text{ spacely per } 2'' + 2 = 0 \Rightarrow Z = C_1 \cos x + C_2 \sin x$$

$$Illy m \text{ or } J \text{ per - } x \text{ rel} \text{ } xD - \text{in } y \text{ rem}. \text{ } qp - \text{warm}.$$

Bagan Kom gil um yp i n-20 napogra

X o E E

Rene z komm 3! na Belin nponemytre I

Bone of Trob obosen your, see one I! & oup in to.

$$a_0(x)$$
 $y'' + a_1(x)y' + a_2(x)y = 0 \longrightarrow z'' + Q(x)z = 0$
 $y = z e^{-\frac{1}{2} \int \frac{a_1(x)}{a_0(x)} dx}$ - speodp-e Agubuur

Apre Becces:
$$x^2y'' + xy' + (x^2 - y^2)y = 0$$

$$y = 2x^{-1/2}$$

$$z'' + \left(1 + \frac{h^2 - y^2}{x^2}\right)z = 0$$

Banerdule! you raxen zamene kon lo kyier pen 1 yp 1 ne ulnseid.

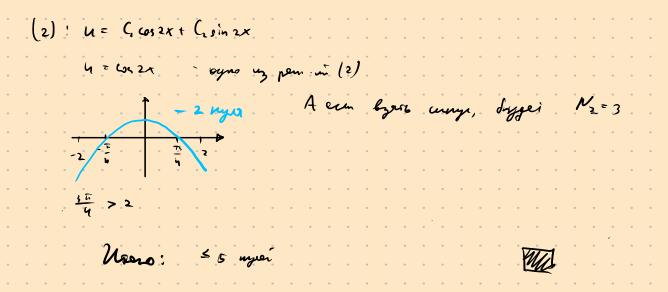
Vil hadd neight pen e yp. a beccer her co mare hyren na La; +co),

$$\square Q(x) = 1 + \frac{\frac{1}{4} - v^2}{x^2} \Big|_{x \to rco} 1$$

$$\exists C: \forall x > C \to Q(x) > \frac{1}{2} ; \text{ non original Lass CI remains mus nyells.}$$
Eun korq-7 b saven yn m nn, norm, kerep-5, 40 no 7. Wayyour 4TA

- Oyemboen

$$D-is$$
, vio $N, \leq 3$ => $N_2 \leq 2$, repure korop. $b(z)$ beneure corq. $A b(\cdot)$ $(u > \frac{x}{u})$ and N_2 washim some for L per $-e(z)$ former, vio $N_2 \leq 2$ $(-2, 2b)$



Tercrobas

Drug 200 V neigned, pen yp. 9 y' + (2 + 6532) y = 5 (2) m osp. 1-1; 67 } server 5,

rge y'(3)=0. (govai. nex. 86, 200 eets 32 mgs, uno 5. Pour dypet U(4))

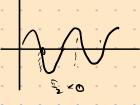
2+0057x > 1 Nr neu-be mujer nermb, pen. (2), N. - ons me ques (1) Grubmuberen c yp. 2"+2 = 0 (1)

N. : N2+1 = 1 N2>, N;-1, roys N2= 3 - myone naise weight pen (1) y K-pars >3 nyen men [-1; 6].

Z= Cousx + Casinx

E= cos x ne [-1; 6]

Bieró horegni N:=2-neus



Unger pen e b grapue Z = sin (x-y)

D-20, 200 ecm $g(x) \le 0$, 200 bee peur y = 0

De repositiones myrite $\exists x_i$: $y(x_i) \leq 0$. Example oux $\exists z \in (x_i, x_i)$: y(z) = 0. $y'(x_i) = \lim_{t \to 0} \frac{y(x_0 + t) - y(x_0)}{t}$

] 8 >0, Vx & (no) xo +6 | - y (x) > y (xo)

Consider, rise 3 - herrer, my i., rge y (x)=0.

Mu los region respects perm un conservant obje venerno => ne nomes uneix

konernoux gregeroroux $T_i => inf journ x, rise y(y)=0$, when C whin,

=> y(x) renormin. nd $(x_0; 3)$. y'+q(x)y'=0 y(x)=0 y(x)=0

 $g(k) \leq 0$ $y \geq 0$ => $y \approx 0$ me (x_0, z) => y = 0 me (x_0, z) => y = 0 me (x_0, z) => y = 0 me (x_0, z) => $(x_0, z) = 0$ $(x_0, z) = 0$ $(x_0, z) = 0$ me $(x_0, z) = 0$ me $(x_0, z) = 0$ me memor odp. $(x_0, z) = 0$ memor od

Pazobil mælkenn abienommer meier

$$\bar{\chi}(t) = \begin{pmatrix} \chi_1(t) \\ \chi_n(t) \end{pmatrix}$$

Moranamai unemai ognopognes curieme: = A(x) (abieno mocre - b
nezabucunerin or t)

 $\lambda = A(\bar{x}), \quad t > t$ $\bar{x} = A(\bar{x}), \quad t > t$

Pen-e 3. Kom 3! na (tojso) erm A(x) nenge leasop gr-us

Reme east yoular ((n+1) - nogran up be.

n-neproe y 60 - quezobel y be

Meenen penens in R" & R" - grazabar maentopus.

One zagoceses sem me yp. sum, no man negramaspur. zergement symbal b

Charletha

peu. e

- q mainispui

- cipiere cooil.

- () Ecn x (4)-pen-e, 50 x (++C) pan-e C sen me mælsiernen.
 - 3 2 paznez spolkagum ne urenot Obryux forex.
 - Troumsepono Torrey (no someme pubnoberus)

Kaz ux visate (n = 2)

$$\frac{1}{f(x,y)} = f(x,y)$$

$$\frac{dy}{dx} = \frac{f(x,y)}{f(x,y)}$$

Immer per - 1 Hero yugup. you l buye F(t,y)=C.

9 - us Fly), now ne reamyon perm con - un 12 roci, ne noclon

Fredericam my -co replace unsequen cuesem

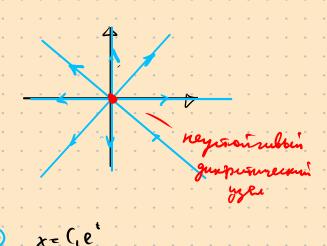
Trockhapun - mum ypobus replace unterpara.

3 moiso permes un my

Nymes

$$d(\frac{\chi}{x})=0 \Rightarrow \frac{\chi}{x}=C$$
 - replan unerpor $f(x,y)=\frac{\chi}{x}$.

humm ynobus neplose unserpare - menure. No èquerciepur - eyou, regrynne



hymne hari - use menn ynder replace uni. u oz odnym coods. pazdres un na maeniapum.

Brownseym; 1. Noromenne publisher.
2. Nym, burneyengue uz romm. publisher.

Kracciepieragus nacementin palnobecus que uneinoux cueren

$$\begin{cases} \dot{x} = a_1 x + a_2 y \\ \dot{y} = b_1 x + b_2 y \end{cases}$$

Prymer n. p. net L=3 | d. d. | + 0 um l=0 ne st-ce cochit. zon.

