Touronouespurence press Pyre

$$f(x) \in L_R(-1, 1)$$
 u un nepuog 21

 $L_R - ode$ . uniesp.,  $\tau \cdot e \cdot \int_{-1}^{1} f(x) dx$  ate.

$$cl_n = \frac{1}{1} \int_{-1}^{1} f(t) \cos \frac{\pi nt}{1} dt , n = 1, 2, \dots$$

$$b_n = \frac{1}{1} \int_{-1}^{1} f(t) \sin \frac{\pi nt}{1} dt , n = 1, 2, \dots$$

Lerna Prinana

$$f(x) \in L_{R}(I) = 3 \int f(t) \cos t x dt \rightarrow 0 \quad \text{npm} \quad x \rightarrow \infty$$

$$I - \text{npower}.$$

$$\int_{I} f(t) \sin t x dt \rightarrow 0 \quad x \rightarrow \infty$$

Cregardine: 
$$f(x) \in L_n(-1; 1) = 3a_n$$
,  $b_n \to 0$   
 $f_{nm}$ ,  $p_{ng} = \frac{d_0}{2} + \sum_{n=1}^{\infty} f_{nn} \cos \frac{\pi n \times 1}{4} + b_n \sin \frac{\pi n \times 1}{4} - p_{ng} + c_n \cos \frac{\pi n \times 1}{4}$ 

Charleska

2. f(x) -reproguens > uniegas nomes desir no rodony ornezny gumon 21

Daraiernoe yerobre perguonumoin le p. Pype (cregation my mp. lubumya)

1. 
$$f(x) \in h_R(-1; 1)$$
, un reprog 21

B T. Xo uneer konernue agnocropo nume rpange  $f'_+(x_0) = f'_-(x_0)$ .

Forgo pay  $P$ .  $f(x)$  b T. Xo exagures  $x$   $f(x_0)$ .

2. Myore 
$$f(x) \in L_R(-1; 1)$$
, un reprog 2 l

 $X_0 = 7$ . Parpula 1 pages,  $\exists$  nonembre nodo Injernou' ognocio ponnue reposso ognose;

lim  $\frac{f(x_0 + u) - f(x_0 + o)}{u}$ ,  $\lim_{n \to +\infty} \frac{f(x_0 - u) - f(x_0 - o)}{-u}$ 

Torga pay opypue 
$$B_1$$
, to exequite  $\kappa$  up, aprepu.  $\frac{f(x_0+0)+f(x_0-0)}{2}$ 

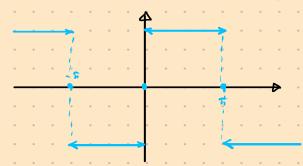


Vacso 
$$l=\bar{n}$$
, regge  $a_n = \frac{1}{\pi} \int_{-\pi}^{\pi} f(t) \cos nt \, dt$ ,  $b_n = \frac{1}{\pi} \int_{-\pi}^{\pi} f(t) \sin nt \, dt$ 

$$\frac{a_0}{2} + \sum_{n=1}^{\infty} \left[ a_n \cos nx + b_n \sin nx \right]$$

#### Bagora 1

Parsonning & p. Pype f(x) = sign x, - si exe si fp. cymm paga esponses grazy.



$$g_{-u}$$
 never =>  $a_n = 0$ 

$$g_n = \frac{2}{l} \int_0^{l} f(t) \sin \frac{h}{l} dt - gu never, gr-un$$

$$g_n = \frac{2}{h} \int_0^{l} signt \sin nt dt =$$

$$= \frac{2}{\pi} \int_{0}^{\pi} \sin nt \, dt = \frac{2}{\sin} \left( -\cos nt \right) \int_{0}^{\pi} dt$$

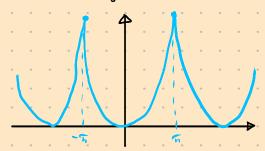
$$= \frac{2}{\pi} \left( 1 - \left( -1 \right)^{\eta} \right)$$

$$\operatorname{Sign} X = \sum_{n=1}^{\infty} \frac{2}{\pi_n} \left( 1 - \left( -1 \right)^n \right) \operatorname{Sin} X , \quad -\widehat{n} < x < \overline{n}$$

#### Bagara 2

$$\beta(x) = x^{2} \quad \text{na} \quad -\pi < x < \pi$$

$$\alpha_{n} = \frac{2}{\pi} \int x^{2} \cos nx \, dx \quad , \quad \delta_{n} = 0$$



$$\hat{y}^{2} = \frac{y^{2}}{3} + \sum_{n=1}^{\infty} \frac{4}{n^{2}} \left(-1\right)^{n} \left(-1\right)^{n}$$

$$\sum_{n=1}^{\infty} \frac{1}{n^{2}} = \frac{R^{2}}{6}$$

$$0 = \frac{7i^2}{3} + \sum_{n=1}^{\infty} \frac{4}{n^2} \left(-1\right)^n \qquad \sum_{n=1}^{\infty} \frac{\left(-1\right)^n}{n^2} = -\frac{7i^2}{12}$$

Does. yee plu cx. p. Pypel.

f(x) & ha [-1;1], repring 21, u agramo - waginar nu [-1;17.

(fk) nenp. na L-l, l], f'lx) xyeorno-nenp. na L-l; l], τ.l. ein zonemel rizero
τ. pozpula I poque). Forge p-Pyne f(x) ex. p/n na lien remolent aparron

Uzlevino: eem f'(x) omp. berogy na monem, no y née ne monet dois perzonales A page. Postary B reopene o palm. Cx, p. Prypre B  $\sigma$ . puzzula f'(x) ne onp. Cx, p. A Cx, P Cx

YEL 22-110

Prysie spur pay (gua moirera (= 5)

 $\frac{a_0}{2} + \sum_{n=1}^{\infty} (a_n \cos nx + b_n \sin nx)$  (i)  $\cos p/n$  ha  $(-\omega) + \omega$ ). Donga ero cyana f(x) - resp. 25 - represent op-u2, <math>n (i) - p. Pryme cheen cyana.

 $\Box f(x) = \frac{a_0}{2} + \sum_{n=1}^{\infty} (a_n \omega_{S} n_x + b_n \sin n_x) - \rho f_n c_x, \\
Cyuna \rho f_n c_x, paya uz neny, q_-un-henp, q_-un.$ Uneet reprog 2i- oneb.

P/n cx. pag uz reng quin na konernan aspezze nomno nomenno unsegupolasse.

 $\int_{-\overline{h}}^{\overline{h}} f(t)dt = \frac{\alpha_0}{2} \cdot 2\overline{h} + \sum_{n=1}^{\infty} (a_n \int_{-\overline{h}}^{\overline{h}} \cos nt \, dt + b_n \int_{-\overline{h}}^{\overline{h}} S_{n}^{(n)} nt \, dt) => a_0 = \frac{1}{\pi} \int_{-\overline{h}}^{\overline{h}} f(t) dt$ 

Eun p/n cx. pay yenomine ra orp-q-uo, on ocranetes p/n cx.

F(x) cos  $mx = \frac{\alpha_0}{2}$  cos  $mx + \sum_{n=1}^{\infty} (\alpha_n \cos nx \cos mx + \beta_n \sin nx \cos mx)$ , m gruse.

 $\int_{-\pi}^{\pi} f(t) \cos mt \, dt = \frac{a_0}{2} \int_{-\pi}^{\pi} \cos mt \, dt + \sum_{n=1}^{\infty} \left( a_n \int_{-\pi}^{\pi} \cos nt \, dt + b_n \int_{-\pi}^{\pi} \sin nt \, \cos mt \, dt \right) =$ 

Optiononaumocino cuestand {1, cost, sint, ..., cosne, sinnt, ...} renp qu'un na orip. [-ti; ti] co coarponen monge [flt)g(t) de an = in if f(t) cas me de

Sagara 22-111

Al 
$$\tau_2$$
 in payarin Pryper?

1.  $\sum_{n=1}^{\infty} \frac{\cos nx}{n^2}$  - pay  $\cos nx$  ph in  $R \Rightarrow pay Pryper or chair eyend$ 

#### Bogora 4

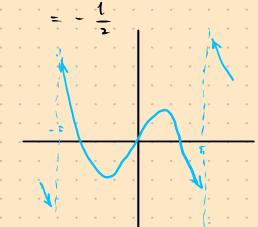
$$f(x) = x \cos x$$
,  $-5 \le x \le 5$  - novernal,  $\alpha_n \ge 0$ 

$$\delta_n = \frac{2}{\pi} \int_{0}^{\pi} t \cos t \cdot \sin nt dt = \frac{2}{\pi} \int_{0}^{\pi} t \cdot (\sin(n\tau)) + \sin(n\tau) dt = \frac{2}{\pi} \int_{0}^{\pi} t \cos t \cdot \sin(n\tau) dt$$

$$= \frac{1}{n} \left[ \left( \frac{t \cos(n+i)t}{n+i} - \frac{t \cos(n-i)t}{n-i} \right) \right]_{0}^{n} + \int_{0}^{\infty} \frac{\cos(n+i)t}{n+i} dt + \int_{0}^{\infty} \frac{\cos(n-i)t}{n-i} dt \right] =$$

$$= \left(-1\right)^{n+1} \left(\frac{1}{n+1} + \frac{1}{n-1}\right) = \left(-1\right)^{n+1} \frac{2n}{n^2-1} - 6n \quad n_{\text{pin}} \quad n \ge 2$$

$$N_{pn} = 1 \quad \theta_{n} = \frac{2}{2\pi} \int_{0}^{\pi} t \sin 2t \, dt = \frac{1}{\pi} \left[ -\frac{1}{2} t \cos 2t \right]_{0}^{\pi} + \int_{0}^{\pi} \frac{\cos 2t}{2} \, dt = \frac{1}{2\pi} \left[ -\frac{1}{2} t \cos 2t \right]_{0}^{\pi}$$



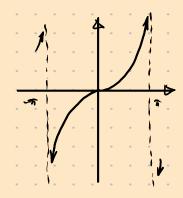
$$x \cos x = -\frac{1}{2} \sin x + \sum_{n=2}^{\infty} \frac{(-1)^{n} 2n}{n^{2}-1} \sin nx$$

Payromenne no cos u no sin

Eun le mogramuis no reinner 
$$\rightarrow f(x) \in L_n(-l;1)$$

## Bagara 1

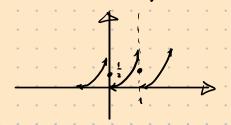
$$P(x) = x^2$$
 ocx  $4\pi$  no sin



$$a_n = 0$$

$$b_n = \frac{2}{\pi} \int_0^{\pi} t^2 \sin nt \, dt$$

Payeomin 1 pay Pype



$$F(x) = x^{2} \quad \text{net} \quad (0; 1) \quad \text{conspring an } 1$$

$$2l = 1 \Rightarrow l = \frac{1}{2}$$

$$a_{n} = 2 \int t^{2} \cos 2\pi n t \, dt \quad n = 0, 1, 2...$$

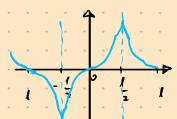
$$b_{n} = 2 \int t^{2} \sin 2\pi n t \, dt$$

$$x^{2} = \frac{do}{2} + \sum_{n=1}^{\infty} (a_{n} \cos z \cos x + b_{n} \sin z \cos x) \quad \text{nea} \quad 0 < x < 1$$

Pag cx-co nepabnomeno na (-0) 100) 1-4. cyenna pozporbana

#### Porgramenue no sin um cos resnus hu neresnus kpasnus que

1 P(x) & Le (0; 1/2)



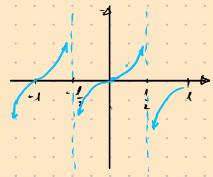
$$f(x) = f(1-x)$$
,  $o(x) = \frac{1}{2}$  - connerpre orner  $x = \frac{1}{2}$   
Dance no never main, game enemogen 21

B stan cyrue 
$$a_n = b_{in} = 0$$

$$b_{2n+1} = \frac{4}{1} \int_{0}^{\infty} P(t) \sin \frac{\pi(2n+1)t}{t} dt$$
  $n = 0, 1, 2, ...$ 

$$(3) \quad f(x) \in L_{R}(s; \frac{1}{2})$$

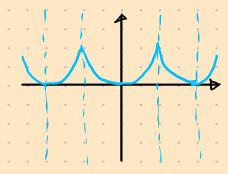
$$f(x) = -f(1-x), \quad o < x < \frac{1}{2} - cunusyms \quad oin. \quad i. \quad (\frac{1}{2}; s)$$



$$a_{n}=0$$
,  $b_{n+1}=0$ ,  $b_{2n}=\frac{4}{1}\int_{0}^{1}f(t)$   $sin\frac{2\pi nt}{1}dt$ 

$$\sum_{n=0}^{\infty} \alpha_{2n+1} \cos \frac{\pi(2n+1)}{l} x$$

(4) 
$$f(x) = f(l-x)$$
  $oexel - comm. or x = 1$ 

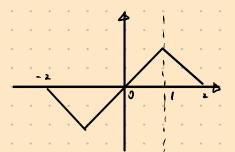


$$\int_{n=0}^{\infty} Q_{2n+1} = 0$$

$$\int_{k}^{\infty} \int_{n=0}^{\infty} f(k) \cos \frac{n \cdot 2n \cdot 4}{n} dk$$

$$\frac{\text{Segond 1}}{f(x) = \begin{cases} x, & 0 \le x \le 1 \\ 2 - x, & 1 \le x \le 2 \end{cases}}$$

Payromuss no [0)2]



Presegue cuma sin. x=1 f(x) = f(2x), 0 = x=1

Rougeaice no sin nerienne en gye Banti = 4 1 t sin Tr (en+i)t de

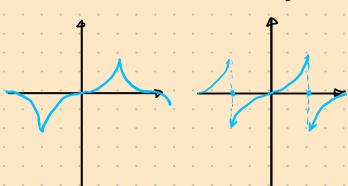
$$F(x) = \sum_{n=0}^{\infty} \frac{\theta(-1)^n}{\pi^2 (2n+1)^2} \sin \pi \left(n+\frac{1}{2}\right) x$$

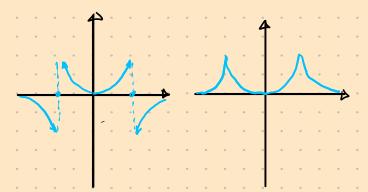
Roy 0x-4 p/n na (-co; +co) Tin, f(x) mult nemoy 4 u na [-4; 4]

#### Bugara z

Novipour op. yenne pegol ies, a neres apointex que Cxogeres in our p/n?

f(x) = sh x



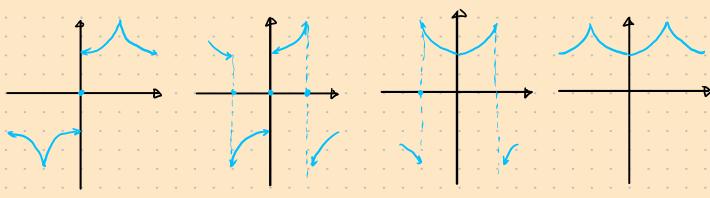


anyer ner. 4p. gyi cx. p/n s.u. um. nepung zā n uayen magnera ne Lingtil

Cumpus res. up. gy co. me p/n r. u. ruspula

kournyer never, 4p. gy ex. ne p/n

koringen res, ap. gy ox. P/n



amyen ner. ep. cro. ne p/n

cumpus ser up gy cx ne p/n

konnysi neres, 4. gy cy ne 1/4

koringin ies; op. gy. cr. ph

## Novemor gruppepennyapolame pagal Pypel

I flx) um nemoy 21 u rye na 1-1;1], Ronga:

1. Pag 9. cx. p/n nor (-co, +co)

2 Long 9. homno novenno guysqo:

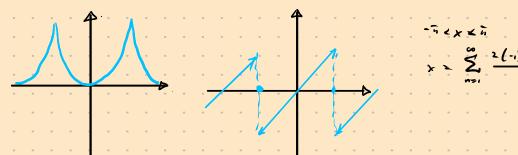
Eum  $f(x) = \frac{a_0}{2} + \sum_{n=1}^{\infty} \left[ a_n \cos \frac{\hat{n}_{n,x}}{\ell} + l_n \sin \frac{\hat{n}_{n,x}}{\ell} \right]$ 

To pag 9. f'(x) (x-par kye nemp nu l. l; 11) rays, gapmanimin graper paga Pyra f:

 $f'(x) \sim \sum_{n=1}^{\infty} \left(-a_n \cdot \frac{\bar{n}n}{1} \sin \frac{\bar{n}nx}{1} + l_n \frac{\bar{n}n}{1} \cos \frac{\bar{n}nx}{1}\right) - ne odorgon exorposece!$ 

$$\chi^{2} = \frac{\pi^{2}}{3} + \sum_{n=1}^{\infty} \frac{4(-1)^{n}}{n^{2}} \cos n\chi \qquad -6 \le \chi \in \mathbb{R}$$

 $2x \sim \sum_{n=1}^{\infty} \frac{4(-1)^{n+1}}{n} \sin nx$ cyema porza polone 2x nel (-5; 5) a. 1 mp. hubenning



$$x = \sum_{n=1}^{\infty} \frac{2(-1)^{n+1} \sin nx}{n}$$

### Palenisto Mapcebar

$$\frac{d^2}{2} + \sum_{n=1}^{\infty} a_n^2 + \ell_n^2 = \frac{1}{\ell} \int_{-\ell}^{\ell} (f(x))^2 dx$$

### Rynnep

$$\sum_{n=1}^{\infty} \frac{4}{n^2} = \frac{1}{\pi} \int_{0}^{\pi} x^2 dx = \frac{2\pi^2}{\pi} \int_{0}^{\pi} x^2 dx = \frac{2\pi^2}{3}$$

$$\sum_{n=1}^{\infty} \frac{1}{h^2} = \frac{\pi^2}{6}$$

$$f(x) = x^2$$
:

$$\frac{2}{9}\pi^{4} + \sum_{n=1}^{\infty} \frac{15}{n^{n}} = \frac{1}{\pi} \int_{-\pi}^{\pi} x^{n} dx = \frac{2}{\pi} \int_{3}^{\pi} x^{n} dx = \frac{2\pi^{4}}{5}$$

$$\sum_{n=1}^{\infty} \frac{1}{n^n} = \frac{\overline{n}^n}{90}$$

# Kepoleniska Psystemepu

$$\int_{a}^{b} f(x)^{2} dx \leq C \int_{a}^{b} f'(x)^{2} dx$$

### Bayora 2

flx) up. no. no. [a, b], 
$$f(a) = f(b) = 0$$
  
Foreyor  $\int_{a}^{b} f(x)^{2} dx \leq \frac{(b-a)^{2}}{n^{2}} \int_{a}^{b} f'(x)^{2} dx$ 

$$\varphi(b-a)=f(b)=0$$

Mayor no névérocin, zerenc neprogon  $2 \cdot (b-a)$  (l=b-a)The one ryeth, p Myre  $c_{R}$ , p/n (b-a) (b-a)

Nyers f(x) eye. -nem na E-l; l7, un. nep. 21

$$f(x) \sim \frac{a_0}{2} + \sum_{n=1}^{\infty} \left( a_n \cos \frac{\pi n x}{\ell} + b_n \sin \frac{\pi n x}{\ell} \right)$$

Ohyper

Forga 
$$f(x) = \int_{k_0}^{x} f(t) dt - \frac{a_0 x}{2} - xy_1 ... no. L(1) f(-1) = f(1)$$

$$F(x) = \frac{C}{z} + \sum_{n=1}^{\infty} \left( \frac{8}{n} a_n \sin \frac{n n x}{l} - \frac{8}{n n} \ln \cos \frac{n n x}{l} \right) - cynne pho cx, p. Type$$

$$C = \frac{1}{4} \int_{-1}^{1} F(t) dt$$

