

# CPSC-354 Report

Emma Garofalo  
Chapman University

September 28, 2024

## Abstract

This document outlines what has been learned week by week through this class. For now, it only contains the information learned for week one.

## Contents

<b>1</b>	<b>Introduction</b>	<b>1</b>
<b>2</b>	<b>Week by Week</b>	<b>1</b>
2.1	Week 1 . . . . .	1
2.2	Week 2: Recursion . . . . .	3
2.3	Week 3: Programming with LLMs . . . . .	6
2.4	Week 4: Parsing and Context-Free Grammars . . . . .	6
2.5	Week 5: Propositions as Types, Dependent Types . . . . .	8
2.6	... . . . .	10

## 1 Introduction

Welcome to my class report! As the class progresses, I will add my learning from each week. For now, it only has week one.

## 2 Week by Week

### 2.1 Week 1

#### Notes

This week we discussed the foundation of what the class is about. The main idea was that this class is largely about the intersection of math and programming, beginning with revisiting the principles we learned in discrete mathematics. We also learned about LaTeX, which we will be using throughout the semester to edit documents like this one. The general idea of the week was setting all of us students up for what to expect throughout the semester.

We also covered the topics of Formal Systems, which are explained in more detail in the below section. And how to determine the relations between a Lean proof and a Math proof.

## Homework

The reading that we had to cover for homework discussed the MUI problem, which helps us break down what a formal system is, and how these attributes can be seen in mathematics like discrete math. A formal system carries the requirement of formality, which states that you must not do anything outside of the set rules. Theorems, axioms, rules of production, and the decision procedure are all key parts of a formal system.

We also had to complete the tutorial world of the natural number game. Here are the solutions for levels 5-8.

### Level 5

Goal:  $a + (b + 0) + (c + 0) = a + b + c$

Solution:

---

```
rw[add_zero]
rfl
```

---

### Level 6

Goal:  $a + (b + 0) + (c + 0) = a + b + c$

Solution:

---

```
rw[add_zero c]
rw[add_zero]
rfl
```

---

### Level 7

Goal:  $\text{succ } n = n + 1$

Solution:

---

```
rw[one_eq_succ_zero]
rw[add_succ]
rw[add_zero]
rfl
```

---

### How is this lean proof related to mathematics proofs?:

The definition of Natural Numbers. 1. "There is a special natural number, called zero, denoted by 0." 2. "For any natural number  $n$ , there is a unique next natural number, called the successor of  $n$ ."

$\text{succ } n = n + 1$		(1)
$\text{succ } n = n + \text{succ}(0)$	definition of natural numbers	(2)
$\text{succ } n = \text{succ}(n + 0)$	prop. of $+$ for successors	(3)
$\text{succ } n = \text{succ } n$	additive identity property	(4)
		(5)

## Level 8

Goal:  $2 + 2 = 4$

Solution:

---

```
nth_rewrite 2[two_eq_succ_one]
rw[one_eq_succ_zero]
rw[four_eq_succ_three]
rw[three_eq_succ_two]
nth_rewrite 2[two_eq_succ_one]
rw[one_eq_succ_zero]
rw[two_eq_succ_one]
rw[one_eq_succ_zero]
rw[add_succ]
rw[add_succ]
rw[add_zero]
rfl
```

---

I learned a lot from this homework. It basically acted as a refresher for discrete mathematics, and how what seems like such a simple solution is much more complicated than you think it is. It also shows the various ways that you can derive the same solutions.

## Comments and Questions

This week provided me with a good refresher of the discrete mathematics class that I took a while ago. It brought to my attention how much there is a crossover between math and code, and I am so excited to explore that in this class.

My question for the week relates to the foundation of mathematics, and where it has all evolved from there. We refreshed on discrete math, which shows us why even the simplest mathematic proofs are valid. And it makes me wonder how mathematics has evolved so much since then. We have such calculated math that has all built off of these proofs. Seeing how much math has evolved since then, does that mean that math will continue to evolve in complexity forever? As we create new technologies and understand our world better, will more complicated relationships continue to be found?

## 2.2 Week 2: Recursion

### Notes

The main topic of this week was recursion, and how it can be visualized with the "Tower of Hanoi" exercise. We learned that the definition of recursion is nesting, and variations on nesting. Recursive definitions are defined in simpler terms of itself, but they never lead to infinite regress or paradox. The "Tower of Hanoi" showed us this well by demonstrating that once you find a base case (a simpler way to break the problem down), then you can use that and the successor of that to solve recursively. We considered the problem from the bottom disk up, and observed how both a stack machine and a rewriting machine can find the efficient recursive solutions.

### Homework

The reading that we had for homework was about the "Little Harmonic Labyrinth". This story was a complex example of how recursion is nesting, and variations on nesting. Another real life example that this reading provided was postponing the completion of a task in favor of completing a simpler task, which I think is something that humans naturally do all the time.

We also completed the addition world of the Natural Number Game, and some solutions are outlined below.

### Level 1

Goal:  $0 + n = n$

Solution:

---

```
induction n with d hd
rw[add_zero]
rfl

rw[add_succ]
rw[hd]
rfl
```

---

### Level 2

Goal:  $\text{succ } a + b = \text{succ } (a + b)$

Solution:

---

```
induction b with n hn
rw[add_zero]
rw[add_zero]
rfl

rw[add_succ]
rw[hn]
rw[add_succ]
rfl
```

---

### Level 3

Goal:  $a + b = b + a$

Solution:

---

```
induction b with d hd
rw[add_zero]
rw[zero_add]
rfl

rw[add_succ]
rw[hd]
rw[succ_add]
rfl
```

---

### Level 4

Goal:  $a + b + c = a + (b + c)$

Solution:

---

```

induction c with d hd
rw[add_zero]
rw[add_zero]
rfl

rw[add_succ]
rw[hd]
rw[add_succ]
rw[add_succ]
rfl

```

---

**How is this lean proof related to mathematics proofs?:**

$a + b + c = a + (b + c)$	proof by induction on c	(6)
$a + b + 0 = a + (b + 0)$	base case	(7)
$a + b = a + b$	additive identity	(8)
$\text{succ}(a + b + d) = a + (b + \text{succ}d)$	inductive step	(9)
$\text{succ}(a + (b + d)) = a + (b + \text{succ}d)$	substitution with inductive hypothesis	(10)
$\text{succ}(a + (b + d)) = \text{succ}(a + (b + d))$	prop. of + for successors	(11)
		(12)

Then the identity property for addition is performed, showing that  $a + 0 = a$ . Once the base case is proven, the successor must be proven as well. The property of addition for successors simplifies the goal so that the inductive hypothesis can be substituted. With another simplification from the addition of successors, both sides of the equation are shown to be equivalent.

## Level 5

Goal:  $a + b + c = a + c + b$

Solution:

---

```

induction c with d hd
rw[add_zero]
rw[add_zero]
rfl

rw[add_succ]
rw[add_succ]
rw[hd]
rw[succ_add]
rfl

```

---

This homework was all about recursion. It refreshed my knowledge on how to apply induction to reach the goal.

## Comments and Questions

The "Tower of Hanoi" problem reminded me the give and take when it comes to finding recursive solutions. Oftentimes, a recursive solution is a more efficient one, but the time it takes to think up this solution and the possible complexity of it needs to be taken into consideration.

My question of the week relates to this. Is there a key way to always identify that the most efficient solution to a particular problem is recursion? I feel like when a problem becomes more complicated, I struggle to identify if it can be solved recursively, and because of this, I try multiple other solutions before and waste a lot of time coming to a recursive solution.

## 2.3 Week 3: Programming with LLMs

### Notes

LLMs for literature reviews

Start discussing creating a calculator in python

### Homework

The homework for this week had us focus on how to use LLMs effectively. We had to have a conversation with an LLM of our choice, and use it to create a literature review on a topic of our choosing related to programming languages.

[My literature review](#): I covered the topic of programming languages in video game design. The README is linked in the title above. I also wrote a more detailed summary in my discord posting [here](#), under the name MagicTurtle. These documents follow the general trajectory that programming languages have taken over time, and how they have been used and improved. It also covers the general strengths of the common programming languages used today, and why they are better for particular types of games than others.

### Other Literature Reviews That I Found Interesting:

#### [Programming Languages and Art](#)

Author: Keira Ryan As someone who is not as familiar with art, this literature review was very interesting to me. I think that it took a very good stance on the hot topic of AI art and whether or not it is "real". It explains that AI can be used as a tool in the art world, and a way to experiment with new processes.

#### [Exploring Garbage Collection Across Programming Languages](#)

Author: Chris Joo I found this interesting because it is an aspect of programming that is often overlooked. It is an extremely important part of programming, but when it is taken care of, I often do not think twice about how it is accomplished.

### Comments and Questions

This week provided me with a good refresher of the discrete mathematics class that I took a while ago. It brought to my attention how much there is a crossover between math and code, and I am so excited to explore that in this class.

My question for the week relates to the foundation of mathematics, and where it has all evolved from there. We refreshed on discrete math, which shows us why even the simplest mathematic proofs are valid. And it makes me wonder how mathematics has evolved so much since then. We have such calculated math that has all built off of these proofs. Seeing how much math has evolved since then, does that mean that math will continue to evolve in complexity forever? As we create new technologies and understand our world better, will more complicated relationships continue to be found?

## 2.4 Week 4: Parsing and Context-Free Grammars

### Notes

Concrete syntax vs. abstract syntax

Parsing

Context-Free Grammar

Calculator with parser generator

## Homework

We did various different assignments for homework this week. The first is shown below. Using this context-free grammar

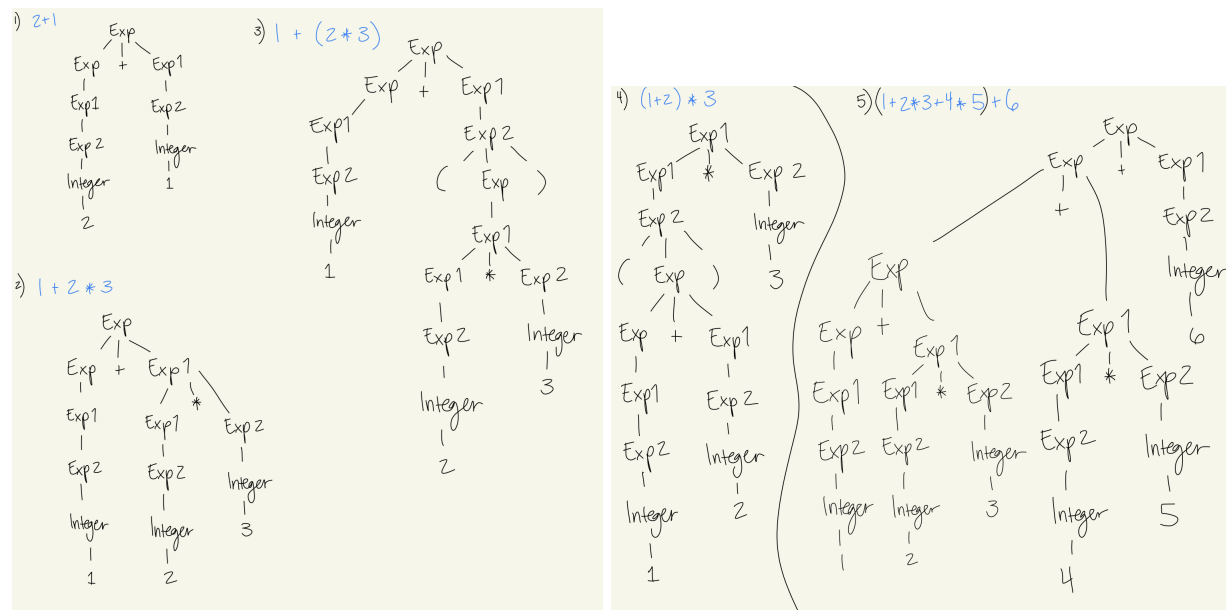
---

```
Exp -> Exp '+' Exp1
Exp1 -> Exp1 '*' Exp2
Exp2 -> Integer
Exp2 -> '(' Exp ')'
Exp -> Exp1
Exp1 -> Exp2
```

---

write out derivation/parse trees for each string:

1.  $2+1$
2.  $1+2*3$
3.  $1+(2*3)$
4.  $(1+2)*3$
5.  $1+2*3+4*5+6$



We also worked on creating a calculator in python that completes basic math operations (parentheses, exponents, multiplication, subtraction, and addition). We did this our own way, but we discussed that a great way to complete this project would be by creating a parser generator in a software like Lark.

The reading this week went into detail on the topic of parsing and context free grammars. These context free grammars are basically sets of rules that are created to define a language. They must be grammatically

defined by four components: a finite set of symbols, finite set of variables, a start symbol, and a finite set of productions. From these, you can perform either recursive inferences or derivations.

### Comments and Questions

This week focused a lot on breaking down what defines a context free grammar and all of the very complicated details that make up a CFG. The topic puts a lot of focus on what is allowed in a context free grammar, so I wanted to instead focus on the exclusions from these languages and how they are identified. When a CFG is used for a programming language syntax, how is it able to give meaningful error messages? Is it able to identify what part of the language that a string would not be valid for and then give an error message in relation to that? I am just unsure overall of how meaningful error messages are given when a CFG is used because it is something I have never really thought about until now.

## 2.5 Week 5: Propositions as Types, Dependent Types

### Notes

This week we discussed a LARL (look-ahead, left to right, rightmost derivation parser). This kind of parser moves all the way to the right when performing a derivation in order to perform the rightmost derivation first. In its derivation, it can only perform two actions: shift or reduce. Sometimes this creates shift-reduce conflicts.

### Homework

For homework we worked on programming assignment 2, which started with the base of a python calculator script and lark parsing grammar. Our goal was to add operations to this base while being sure that the order of operations was respected, even for long mathematical expressions. For each added expression, we went through the steps of adding the operation to the grammar (in the correct order), adding that operation to the python transformer function, then adding it to the evaluator. Each new operation needed to be tested both on its own and with other operations in order to ensure that they functioned correctly and respected the order of operations.

We also completed the tutorial world of the Lean Logic Game. This showed how to solve problems in a language that operates only with variables and functions. No data types or memory exist. The solutions to the tutorial world are shown below:

#### Level 1

---

```
(P : Prop)(todo_list : P) : P := by
```

---

Solution:

---

```
exact todo_list
```

---

#### Level 2

---

```
(P S : Prop)(p: P)(s : S) : P /\ S := by
```

---

Solution:

---

```
exact <p,s>
```

---



### Level 3

---

```
(A I O U : Prop)(a : A)(i : I)(o : O)(u : U) : (A /\ I) /\ O /\ U := by
```

---

Solution:

---

```
exact <<a,i> , o, u>
```

---

### Level 4

---

```
(P S : Prop)(vm: P /\ S) : P := by
```

---

Solution:

---

```
exact vm.left : p
```

---

### Level 5

---

```
(P Q : Prop)(h: P /\ Q) : Q := by
```

---

Solution:

---

```
exact h.right
```

---

### Level 6

---

```
(A I O U : Prop)(h1 : A /\ I)(h2 : O /\ U) : A /\ U := by
```

---

Solution:

---

```
exact <h1.left, h2.right>
```

---

### Level 7

---

```
(C L : Prop)(h: (L /\ (((L /\ C) /\ L) /\ L /\ L /\ L)) /\ (L /\ L) /\ L) : C := by
```

---

Solution:

---

```
have h1 := h.left
have h2 := h.right
have h4 := h1.right
have h5 := h4.left
have h6 := h5.left
exact h6.right
```

---

### Level 8

---

```
(A C I O P S U : Prop)(h: ((P /\ S) /\ A) /\ -I /\ (C /\ -O) /\ -U) : A /\ C /\ P /\ S := by
```

---

Solution:

---

```
have h1 := h.left
have h2 := h1.left
have h3 := h1.right
have h4 := h.right
have h5 := h4.right
have h6 := h5.left
have h7 := h6.left
exact <h3, h7, h2>
```

---

How is this lean proof related to mathematics proofs?:

<i>haveh1 := h.left</i>	isolate (P AND S) AND A	(13)
<i>haveh2 := h1.left</i>	isolate P AND S	(14)
<i>haveh3 := h1.right</i>	isolate A	(15)
<i>haveh4 := h.right</i>	isolate I AND (C AND ¬O) AND ¬U	(16)
<i>haveh5 := h4.right</i>	isolate (C AND ¬O) AND ¬U	(17)
<i>haveh6 := h5.left</i>	isolate C AND ¬O	(18)
<i>haveh7 := h6.left</i>	isolate C	(19)
<i>exact &lt; h3, h7, h2 &gt;</i>	and intro	(20)
		(21)

The goal of this problem is to break down the hypothesis into smaller chunks that are already known in order to prove that it is true. Once we get to the digestable values of P AND S, C, and A. We are then able to show that if these are each true individually, then they can be combined to also all be true.

### Comments and Questions

This week we went into parsing trees a bit more in our lecture, and one of the things that we talked about were LARLs, or look ahead/rightmost derivation trees. It is one of the kinds of predictive parsing, but it made me wonder what situations this type of parsing is actually used, and how it could possibly be flexible in any way. Does relying on rightmost derivation limit it's efficiency to very particular problems? Or is there a way to make it more flexible so that it can handle left-recursive grammars just as well?

## 2.6 ...

...