

CPSC-354 Report

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November 3, 2024

Abstract

This document outlines what has been learned week by week through this class. For now, it only contains the information learned for week one.

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1 Introduction

Welcome to my class report! As the class progresses, I will add my learning from each week. For now, it only has week one.

2 Week by Week

2.1 Week 1

Notes

This week we discussed the foundation of what the class is about. The main idea was that this class is largely about the intersection of math and programming, beginning with revisiting the principles we learned in discrete mathematics. We also learned about LaTeX, which we will be using throughout the semester to edit documents like this one. The general idea of the week was setting all of us students up for what to expect throughout the semester.

We also covered the topics of Formal Systems, which are explained in more detail in the below section. And how to determine the relations between a Lean proof and a Math proof.

Homework

The reading that we had to cover for homework discussed the MUI problem, which helps us break down what a formal system is, and how these attributes can be seen in mathematics like discrete math. A formal system carries the requirement of formality, which states that you must not do anything outside of the set rules. Theorems, axioms, rules of production, and the decision procedure are all key parts of a formal system.

We also had to complete the tutorial world of the natural number game. Here are the solutions for levels 5-8.

Level 5

Goal: $a + (b + 0) + (c + 0) = a + b + c$

Solution:

```
rw[add_zero]
rfl
```

Level 6

Goal: $a + (b + 0) + (c + 0) = a + b + c$

Solution:

```
rw[add_zero c]
rw[add_zero]
rfl
```

Level 7

Goal: $\text{succ } n = n + 1$

Solution:

```
rw[one_eq_succ_zero]
rw[add_succ]
rw[add_zero]
rfl
```

How is this lean proof related to mathematics proofs?:

The definition of Natural Numbers. 1. "There is a special natural number, called zero, denoted by 0." 2. "For any natural number n , there is a unique next natural number, called the successor of n ."

$\text{succ } n = n + 1$		(1)
$\text{succ } n = n + \text{succ}(0)$	definition of natural numbers	(2)
$\text{succ } n = \text{succ}(n + 0)$	prop. of $+$ for successors	(3)
$\text{succ } n = \text{succ } n$	additive identity property	(4)
		(5)

Level 8

Goal: $2 + 2 = 4$

Solution:

```
nth_rewrite 2[two_eq_succ_one]
rw[one_eq_succ_zero]
rw[four_eq_succ_three]
rw[three_eq_succ_two]
nth_rewrite 2[two_eq_succ_one]
rw[one_eq_succ_zero]
rw[two_eq_succ_one]
rw[one_eq_succ_zero]
rw[add_succ]
rw[add_succ]
rw[add_zero]
rfl
```

I learned a lot from this homework. It basically acted as a refresher for discrete mathematics, and how what seems like such a simple solution is much more complicated than you think it is. It also shows the various ways that you can derive the same solutions.

Comments and Questions

This week provided me with a good refresher of the discrete mathematics class that I took a while ago. It brought to my attention how much there is a crossover between math and code, and I am so excited to explore that in this class.

My question for the week relates to the foundation of mathematics, and where it has all evolved from there. We refreshed on discrete math, which shows us why even the simplest mathematic proofs are valid. And it makes me wonder how mathematics has evolved so much since then. We have such calculated math that has all built off of these proofs. Seeing how much math has evolved since then, does that mean that math will continue to evolve in complexity forever? As we create new technologies and understand our world better, will more complicated relationships continue to be found?

2.2 Week 2: Recursion

Notes

The main topic of this week was recursion, and how it can be visualized with the "Tower of Hanoi" exercise. We learned that the definition of recursion is nesting, and variations on nesting. Recursive definitions are defined in simpler terms of itself, but they never lead to infinite regress or paradox. The "Tower of Hanoi" showed us this well by demonstrating that once you find a base case (a simpler way to break the problem down), then you can use that and the successor of that to solve recursively. We considered the problem from the bottom disk up, and observed how both a stack machine and a rewriting machine can find the efficient recursive solutions.

Homework

The reading that we had for homework was about the "Little Harmonic Labyrinth". This story was a complex example of how recursion is nesting, and variations on nesting. Another real life example that this reading provided was postponing the completion of a task in favor of completing a simpler task, which I think is something that humans naturally do all the time.

We also completed the addition world of the Natural Number Game, and some solutions are outlined below.

Level 1

Goal: $0 + n = n$

Solution:

```
induction n with d hd
rw[add_zero]
rfl

rw[add_succ]
rw[hd]
rfl
```

Level 2

Goal: $\text{succ } a + b = \text{succ } (a + b)$

Solution:

```
induction b with n hn
rw[add_zero]
rw[add_zero]
rfl

rw[add_succ]
rw[hn]
rw[add_succ]
rfl
```

Level 3

Goal: $a + b = b + a$

Solution:

```
induction b with d hd
rw[add_zero]
rw[zero_add]
rfl

rw[add_succ]
rw[hd]
rw[succ_add]
rfl
```

Level 4

Goal: $a + b + c = a + (b + c)$

Solution:

```

induction c with d hd
rw[add_zero]
rw[add_zero]
rfl

rw[add_succ]
rw[hd]
rw[add_succ]
rw[add_succ]
rfl

```

How is this lean proof related to mathematics proofs?:

$a + b + c = a + (b + c)$	proof by induction on c	(6)
$a + b + 0 = a + (b + 0)$	base case	(7)
$a + b = a + b$	additive identity	(8)
$\text{succ}(a + b + d) = a + (b + \text{succ}d)$	inductive step	(9)
$\text{succ}(a + (b + d)) = a + (b + \text{succ}d)$	substitution with inductive hypothesis	(10)
$\text{succ}(a + (b + d)) = \text{succ}(a + (b + d))$	prop. of + for successors	(11)
		(12)

Then the identity property for addition is performed, showing that $a + 0 = a$. Once the base case is proven, the successor must be proven as well. The property of addition for successors simplifies the goal so that the inductive hypothesis can be substituted. With another simplification from the addition of successors, both sides of the equation are shown to be equivalent.

Level 5

Goal: $a + b + c = a + c + b$

Solution:

```

induction c with d hd
rw[add_zero]
rw[add_zero]
rfl

rw[add_succ]
rw[add_succ]
rw[hd]
rw[succ_add]
rfl

```

This homework was all about recursion. It refreshed my knowledge on how to apply induction to reach the goal.

Comments and Questions

The "Tower of Hanoi" problem reminded me the give and take when it comes to finding recursive solutions. Oftentimes, a recursive solution is a more efficient one, but the time it takes to think up this solution and the possible complexity of it needs to be taken into consideration.

My question of the week relates to this. Is there a key way to always identify that the most efficient solution to a particular problem is recursion? I feel like when a problem becomes more complicated, I struggle to identify if it can be solved recursively, and because of this, I try multiple other solutions before and waste a lot of time coming to a recursive solution.

2.3 Week 3: Programming with LLMs

Notes

LLMs for literature reviews

Start discussing creating a calculator in python

Homework

The homework for this week had us focus on how to use LLMs effectively. We had to have a conversation with an LLM of our choice, and use it to create a literature review on a topic of our choosing related to programming languages.

[My literature review](#): I covered the topic of programming languages in video game design. The README is linked in the title above. I also wrote a more detailed summary in my discord posting [here](#), under the name MagicTurtle. These documents follow the general trajectory that programming languages have taken over time, and how they have been used and improved. It also covers the general strengths of the common programming languages used today, and why they are better for particular types of games than others.

Other Literature Reviews That I Found Interesting:

[Programming Languages and Art](#)

Author: Keira Ryan As someone who is not as familiar with art, this literature review was very interesting to me. I think that it took a very good stance on the hot topic of AI art and whether or not it is "real". It explains that AI can be used as a tool in the art world, and a way to experiment with new processes.

[Exploring Garbage Collection Across Programming Languages](#)

Author: Chris Joo I found this interesting because it is an aspect of programming that is often overlooked. It is an extremely important part of programming, but when it is taken care of, I often do not think twice about how it is accomplished.

Comments and Questions

This week provided me with a good refresher of the discrete mathematics class that I took a while ago. It brought to my attention how much there is a crossover between math and code, and I am so excited to explore that in this class.

My question for the week relates to the foundation of mathematics, and where it has all evolved from there. We refreshed on discrete math, which shows us why even the simplest mathematic proofs are valid. And it makes me wonder how mathematics has evolved so much since then. We have such calculated math that has all built off of these proofs. Seeing how much math has evolved since then, does that mean that math will continue to evolve in complexity forever? As we create new technologies and understand our world better, will more complicated relationships continue to be found?

2.4 Week 4: Parsing and Context-Free Grammars

Notes

Concrete syntax vs. abstract syntax

Parsing

Context-Free Grammar

Calculator with parser generator

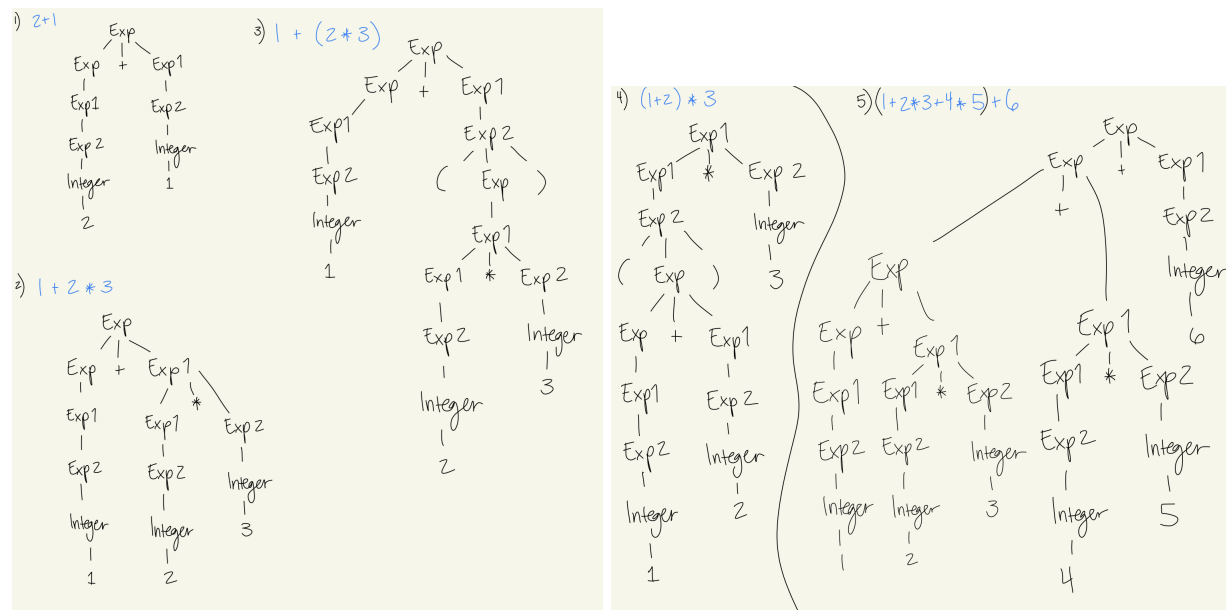
Homework

We did various different assignments for homework this week. The first is shown below. Using this context-free grammar

```
Exp -> Exp '+' Exp1
Exp1 -> Exp1 '*' Exp2
Exp2 -> Integer
Exp2 -> '(' Exp ')',
Exp -> Exp1
Exp1 -> Exp2
```

write out derivation/parse trees for each string:

1. $2+1$
2. $1+2*3$
3. $1+(2*3)$
4. $(1+2)*3$
5. $1+2*3+4*5+6$



We also worked on creating a calculator in python that completes basic math operations (parentheses, exponents, multiplication, subtraction, and addition). We did this our own way, but we discussed that a great way to complete this project would be by creating a parser generator in a software like Lark.

The reading this week went into detail on the topic of parsing and context free grammars. These context free grammars are basically sets of rules that are created to define a language. They must be grammatically

defined by four components: a finite set of symbols, finite set of variables, a start symbol, and a finite set of productions. From these, you can perform either recursive inferences or derivations.

Comments and Questions

This week focused a lot on breaking down what defines a context free grammar and all of the very complicated details that make up a CFG. The topic puts a lot of focus on what is allowed in a context free grammar, so I wanted to instead focus on the exclusions from these languages and how they are identified. When a CFG is used for a programming language syntax, how is it able to give meaningful error messages? Is it able to identify what part of the language that a string would not be valid for and then give an error message in relation to that? I am just unsure overall of how meaningful error messages are given when a CFG is used because it is something I have never really thought about until now.

2.5 Week 5: Propositions as Types, Dependent Types

Notes

This week we discussed a LARL (look-ahead, left to right, rightmost derivation parser). This kind of parser moves all the way to the right when performing a derivation in order to perform the rightmost derivation first. In its derivation, it can only perform two actions: shift or reduce. Sometimes this creates shift-reduce conflicts.

Homework

For homework we worked on programming assignment 2, which started with the base of a python calculator script and lark parsing grammar. Our goal was to add operations to this base while being sure that the order of operations was respected, even for long mathematical expressions. For each added expression, we went through the steps of adding the operation to the grammar (in the correct order), adding that operation to the python transformer function, then adding it to the evaluator. Each new operation needed to be tested both on its own and with other operations in order to ensure that they functioned correctly and respected the order of operations.

We also completed the tutorial world of the Lean Logic Game. This showed how to solve problems in a language that operates only with variables and functions. No data types or memory exist. The solutions to the tutorial world are shown below:

Level 1

```
(P : Prop)(todo_list : P) : P := by
```

Solution:

```
exact todo_list
```

Level 2

```
(P S : Prop)(p: P)(s : S) : P /\ S := by
```

Solution:

```
exact <p,s>
```

Level 3

```
(A I O U : Prop)(a : A)(i : I)(o : O)(u : U) : (A /\ I) /\ O /\ U := by
```

Solution:

```
exact <<a,i> , o, u>
```

Level 4

```
(P S : Prop)(vm: P /\ S) : P := by
```

Solution:

```
exact vm.left : p
```

Level 5

```
(P Q : Prop)(h: P /\ Q) : Q := by
```

Solution:

```
exact h.right
```

Level 6

```
(A I O U : Prop)(h1 : A /\ I)(h2 : O /\ U) : A /\ U := by
```

Solution:

```
exact <h1.left, h2.right>
```

Level 7

```
(C L : Prop)(h: (L /\ (((L /\ C) /\ L) /\ L /\ L /\ L)) /\ (L /\ L) /\ L) : C := by
```

Solution:

```
have h1 := h.left
have h2 := h.right
have h4 := h1.right
have h5 := h4.left
have h6 := h5.left
exact h6.right
```

Level 8

```
(A C I O P S U : Prop)(h: ((P /\ S) /\ A) /\ -I /\ (C /\ -O) /\ -U) : A /\ C /\ P /\ S := by
```

Solution:

```
have h1 := h.left
have h2 := h1.left
have h3 := h1.right
have h4 := h.right
have h5 := h4.right
have h6 := h5.left
have h7 := h6.left
exact <h3, h7, h2>
```

How is this lean proof related to mathematics proofs?:

<i>haveh1 := h.left</i>	isolate (P AND S) AND A	(13)
<i>haveh2 := h1.left</i>	isolate P AND S	(14)
<i>haveh3 := h1.right</i>	isolate A	(15)
<i>haveh4 := h.right</i>	isolate I AND (C AND ¬O) AND ¬U	(16)
<i>haveh5 := h4.right</i>	isolate (C AND ¬O) AND ¬U	(17)
<i>haveh6 := h5.left</i>	isolate C AND ¬O	(18)
<i>haveh7 := h6.left</i>	isolate C	(19)
<i>exact < h3, h7, h2 ></i>	and intro	(20)
		(21)

The goal of this problem is to break down the hypothesis into smaller chunks that are already known in order to prove that it is true. Once we get to the digestable values of P AND S, C, and A. We are then able to show that if these are each true individually, then they can be combined to also all be true.

Comments and Questions

This week we went into parsing trees a bit more in our lecture, and one of the things that we talked about were LARs, or look ahead/rightmost derivation trees. It is one of the kinds of predictive parsing, but it made me wonder what situations this type of parsing is actually used, and how it could possibly be flexible in any way. Does relying on rightmost derivation limit it's efficiency to very particular problems? Or is there a way to make it more flexible so that it can handle left-recursive grammars just as well?

2.6 Week 6: Higher Order Functions

Notes

The topics of this week mostly included currying and lambda calculus. In class, we discussed that currying is like creating a chain of functions in order to solve a particular problem. This is done because in the scenarios that it is used, each function only takes in one argument.

We also focused a lot of lambda calculus, which as we previously discussed, is made up of only variables and functions. In order to dive deeper into the topic, we broke it down into syntax and semantics. The syntax of lambda calculus is what I have below. The bottom two being abstraction and application, respectively.

```
exp -> var
exp -> 'lambda' var '.' exp
exp -> exp exp
```

The operational semantics of lambda calculus, otherwise known as how programs will run, was broken down when observing the proof of an identity function. We stressed that each function is only able to take one input, and observing parenthesis properly while using substitution with capture avoiding is necessary in lambda calculus.

Homework

This week's homework was the "Party Snacks" level of the lean logic world, focusing on lambda calculus. We pushed ourselves to solve each problem in a single line. The solutions to problems 1-9 are shown below: ('lambda' and 'maps to' symbols are represented in text because of latex restrictions)

Level 1

```
(P C: Prop) (p: P) (bakery_service : P -> C) : C := by
```

Solution:

```
exact bakery_service p
```

Level 2

```
(C: Prop) : C -> C
```

Solution:

```
exact 'lambda' c 'maps to' c
```

Level 3

```
(I S: Prop) : I /\ S -> S /\ I
```

Solution:

```
exact 'lambda' <I, S> 'maps to' <S, I>
```

Level 4

```
(C A S: Prop) (h1 : C -> A) (h2 : A -> S) : C -> S
```

Solution:

```
exact 'lambda' c 'maps to' h2 (h1 c)
```

Level 5

```
(P Q R S T U: Prop) (p : P) (h1 : P -> Q) (h2 : Q -> R) (h3 : Q -> T) (h4 : S -> T) (h5 : T -> U)
: U
```

Solution:

```
exact h5 (h3 (h1 p))
```

Level 6

```
(C D S: Prop) (h : C /\ D -> S) : C -> D -> S
```

Solution:

```
exact 'lambda' c d 'maps to' h <c, d>
```

Level 7

```
(C D S: Prop) (h : C -> D -> S) : C /\ D -> S
```

Solution:

```
exact 'lambda' <c, d> 'maps to' h c d
```

Level 8

```
(C D S : Prop) (h : (S -> C) /\ (S -> D)) : S -> C /\ D
```

Solution:

```
exact 'lambda' s 'maps to' <h.left s, h.right s>
```

Level 9

```
(R S : Prop) : R -> (S -> R) /\ (-S -> R)
```

Solution:

```
exact 'lambda' r 'maps to' <'lambda' s 'maps to' r, 'lambda' ns 'maps to' r>
```

Comments and Questions

One of the topics generally mentioned this week was the Curry-Howard correspondence. It demonstrates a connection between formal systems of logic and programming languages, stating that a propositions correspond to types, proofs correspond to programs, and proof reductions correspond to program evaluation. It

is able to show the direct connections between mathematics and programming. My question for the week is how can this understanding improve our approach to programming?

2.7 Week 7

Notes

This week we covered why lambda calculus is turing complete. We wanted to show how to represent numbers, operations, conditionals, memory, and loops. We also observed recursion in lambda calculus.

Homework

For homework, we had to practice capture avoiding substitution. We were tasked with this problem:

1. Reduce the following lambda term:

```
((\m. \n. m n) (\f. \x. f (f x))) (\f. \x. f (f (f x)))
```

Here is my step by step solution to this problem, all using beta reduction:

```
((\m. \n. m n) (\f. \x. f (f x))) (\f. \x. f (f (f x))) -> left-most beta reduction
(\n. (\f. \x. f (f x)) n) (\f. \x. f (f (f x))) -> left-most beta reduction
(\f. \x. f (f x)) (\f. \x. f (f (f x))) -> left-most beta reduction
\x. (\f. \x. f (f (f x))) ((\f. \x. f (f (f x))) x) -> right-most beta reduction
\x. (\f. \x1. f (f (f x1))) (\f. \x2. f (f (f x2)))x -> alpha reduction of x
\x. (\f. \x1. f (f (f x1))) (\x2. x (x (x x2)))x -> right-most beta reduction
\x. (\x1. (\x2. x (x (x x2))) ((\x2. x (x (x x2)))x ((\x2. x (x (x x2)))x x1))) -> right-most
beta reduction
\x. (\x1. (\x2. x (x (x x2))) ((\x2. x (x (x x2)))x ((x (x (x x1)))))) -> right-most beta
reduction
\x. (\x1. (\x2. x (x (x x2))) ((x(x(x(x(x x1))))))) -> right-most beta reduction
\x. (\x1. (x(x(x(x(x(x(x x1)))))))) -> right-most beta reduction
```

2. Explain what function on natural numbers

```
(\m. \n. m n)
```

implements:

First we need to discuss what church numerals are. In lambda calculus, natural numbers are represented as functions because the only two things that exist in lambda calculus are functions and variables. A church numeral (n) takes two arguments, a function (f) and a value (x), and applies f to x n times.

In this question, m and n are church numerals. The expression takes two church numerals, m and n, as input and returns m n. So overall, this function takes two church numerals, and applies the first church numeral (function) to the second church numeral (argument), applying the function to the argument.

Comments and Questions

When thinking about church numerals, it adds another layer to lambda calculus that I didn't really remember needed to be represented. It challenges our understanding of the difference between computation and representation in a system that is only able to use variables and functions for operations. So, my question for this week is : In what ways do church encodings in lambda calculus illustrate the relationship between data representation and function application, and how might this influence our understanding of computational efficiency and expressiveness in modern programming languages?

2.8 Week 8 and 9

Notes

The focus of week 8 and 9 was on programming assignment 3. The goal was to understand how capture avoiding substitution can be implemented into a python script lambda calculus calculator. It also gave us the opportunity to learn or refresh on how to use the vscode python debugger with breakpoints and our own traces to determine where bugs exist within a script.

Homework

As we completed assignment 3, we were told to answer the guiding questions below to help assist us in understanding the lambda calculus calculator:

1. Add new test cases to each of the functions.
2. Explain why `abcd` reduces to `((a b) c) d` and why `(a)` reduces to `a`.
 - The first expression is returned with parenthesis that demonstrate the "order of operations". This program evaluates the expressions through leftmost reductions, so `abcd` is reduced to `((a b) c) d` showing that `(a b)` is first evaluated, then the result is evaluated with `c`, and then with `d`. That is why providing the program with `abcd` returns the corresponding answer. `(a)` reduces to `a` because there are no further simplifications for the given expression.
3. How does capture avoiding substitution work? How is it implemented?
 - Capture avoiding substitution changes the names of variables in an expression with alpha substitutions in order to avoid changing nested variables of the same name that are not in the same scope. This is done by renaming variables of the current scope to `Var(x)`, `x` being the count of substitutions. Doing this maintains proper reductions of the lambda calculus calculator.
4. Do you always get the expected result? Do all computations reduce to normal form?
 - When testing the original program, you do not always get the expected result. Any computation that requires rightmost substitution to be completely reduced is not returned with the proper value.
5. What is the smallest lambda expression you can find that does not reduce to normal form?

```
(\f. \x. f (f x)) (\x. x)
```

6. Use the python debugger to step through the interpreter (nothing to report for this question)
7. How does the interpreter evaluate

```
((\m.\n. m n) (\f.\x. f (f x))) (\f.\x. f (f (f x)))
```

Write a new line for each substitution.

```
((\m.\n. m n) (\f.\x. f (f x))) (\f.\x. f (f (f x)))  
((\Var1. (\f.\x. f (f x)) Var1) ) (\f.\x. f (f (f x)))  
(\Var1. ((\f. (\x. (f (f x)))) Var1))  
((\Var2. (\Var4. (Var2 (Var2 Var4)))) (\f. (\x. (f (f (f x))))))  
(\Var5. ((\f. (\x. (f (f (f x))))) ((\f. (\x. (f (f (f x))))) Var5)))
```

8. Write out the trace in the format that we used for the towers of hanoi for the same example as above.

```

12: eval (((\m.(\n.(m n))) (\f.(\x.(f (f x)))) (\f.(\x.(f x))))
39: eval ((\m.(\n.(m n))) (\f.(\x.(f (f x))))
39: eval (\m.(\n.(m n)))
44: substitute ((\n.(m n)), 'm', (\f.(\x.(f (f x))))
89: substitute (substitute((m n), 'n', 'Var1'), 'm', (\f.(\x.(f (f x))))
92: substitute ('m', 'n', 'Var1')
92: substitute ('n', 'n', 'n')
92: sub substitute ('m', 'm', 'm')
92: sub substitute ('Var1', 'm', (\f.(\x.(f (f x))))
45: eval (\Var1.((\f.(\x.(f (f x)))) Var1))
44: substitute (((\f.(\x.(f (f x)))) Var1), 'Var1', (\f.(\x.(f (f (f x)))) )
92: substitute ((\f.(\x.(f (f x)))), 'Var1', (\f.(\x.(f (f (f x))))))
92: substitute ('Var1', 'Var1', 'Var1')
89: substitute (substitute((\x.(f (f x))), 'f', 'Var2'),
'Var1', (\f.(\x.(f (f (f x))))))
89: substitute (substitute ((f (f x)), 'x', 'Var3'), 'f', 'Var2')
92: substitute ('f', 'x', 'Var3')
92: substitute ((f x), 'x', 'Var3')
92: substitute ('f', 'x', 'Var3')
92: substitute ('x', 'x', 'Var3')
92: substitute ('f', 'f', 'Var2')
92: substitute ((f Var3), 'f', 'Var2')
92: substitute ('f', 'f', 'Var2')
92: substitute ('Var3', 'f', 'Var2')
89: substitute (substitute((Var2 (Var2 Var3)),
'Var3', 'Var4'), 'Var1', (\f.(\x.(f (f (f x))))))
92: substitute ('Var2', 'Var3', 'Var4')
92: substitute ((Var2 Var3), 'Var3', 'Var4')
92: substitute ('Var2', 'Var3', 'Var4')
92: substitute ('Var3', 'Var3', 'Var4')
92: substitute ('Var2', 'Var1',
(\f.(\x.(f (f (f x))))))
92: substitute ((Var2 Var4), 'Var1',
(\f.(\x.(f (f (f x))))))
92: substitute ('Var2', 'Var1',
(\f.(\x.(f (f (f x))))))
92: substitute ('Var4', 'Var1',
(\f.(\x.(f (f (f x))))))
45: eval ((\Var2.(\Var4.(Var2 (Var2 Var4)))) (\f.(\x.(f (f (f x))))))
39: eval (\Var2.(\Var4.(Var2 (Var2 Var4))))\
44: substitute ((\Var4.(Var2 (Var2 Var4))), 'Var2', (\f.(\x.(f (f (f x))))))
89: substitute (substitute((Var2 (Var2 Var4)), 'Var4', 'Var5'), 'Var2',
(\f.(\x.(f (f (f x))))))
92: substitute ('Var2', 'Var4', 'Var5')
92: substitute ((Var2 Var4), 'Var4', 'Var5')
92: substitute ('Var2', 'Var4', 'Var5')
92: substitute ('Var2', 'Var4', 'Var5')
92: substitute ('Var2', 'Var2', (\f.(\x.(f (f (f x))))))
92: substitute ((Var2 Var5), 'Var2', (\f.(\x.(f (f (f x))))))
92: substitute ('Var2', 'Var2', (\f.(\x.(f (f (f x))))))
92: substitute ('Var5', 'Var2', (\f.(\x.(f (f (f x))))))

```

```
45: eval (\Var5.((\f.(\x.(f (f (f x)))) (\f.(\x.(f (f (f x)))) Var5)))
```

(we later realized that we did not have to keep a portion of this trace that we accidentally kept but we already went through all of it so we decided we might as well leave it in the report.)

Comments and Questions

Week 8 Question: What are the pros and cons of using the Python debugger tool through vscode versus print statement debugging?

Week 9 Question: How does the design of Python as a language affect the debugging process of Python scripts?

2.9 Week 10

Notes

This week we began discussing the topic of rewriting. We previously defined rewriting as a finite number of rules to create finite expressions using pattern matching. We now abstract it even more by removing the pattern matching and considering the possibility of an infinite set of rules. We covered directed graphs, and how they can be used to represent abstract reduction systems (ARSs). We defined confluence to be the ability to rejoin in rewriting after a divergence, and termination as the ability for the ARS to not admit an infinite computation. This information was used to set us up for the homework that we have for week 11.

Homework

For this homework, we were told to reflect on Assignment 3. Below are the questions we were instructed to answer:

1. What did you find most challenging when working through Homework 8/9 and Assignment 3?
 - I think the most difficult thing to do was understand the code that already existed for Assignment 3. Taking someone else's code and interpreting it can already be hard, but on top of that we were analyzing code for a topic that I am not sure I fully grasped just yet (lambda calculus). I think it was easy for me to understand what the program was doing incorrectly, but using that knowledge to find the part of the program that was causing the incorrect operation was really difficult for me. This was remedied by what I will discuss in the next question.
2. How did you come up with the key insight for Assignment 3?
 - Once my group talked to Professor Kurz about the issue we were coming across, he gave great insight on a solution to help us target the mistake in the program that we needed to fix. He told us to find the smallest example we could that was returning an incorrect result. This minimal example was what we really needed to understand what was going on. From there, we used the breakpoints that we already established in the code and the python debugger to finally target where we needed to put in the missing code and make the program run as intended.
3. What is your most interesting takeaway from Homework 8/9 and Assignment 3?
 - I actually had never used the python debugger before, so understanding that tool was the most interesting thing that I will be able to takeaway from this experience. It will definitely be something that I use in the future to help solve coding bugs that I may come across.

Comments and Questions

My question for the week relates to the topic of termination in abstract reduction systems. When evaluating if an ARS is terminating, is there really any way to determine with absolute certainty that it is? Or are there situations where it is impossible to identify?

2.10 ...

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