

Investigating how the formation process of Cu nanoparticles can affect their CO₂RR activity

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We propose a multiscale numerical model to estimate how the formation process to produce Cu nanoparticles affect their catalytic activity for CO₂ reduction. Although this reaction can lead to multiple hydrocarbon products, we focus our attention on the hydrogenation to methane for which the protonation of CO to CHO is the rate-limiting step. Using classical molecular dynamics, we model three formation processes, namely the annealing from a liquid droplet; the solid growth proceeding via the addition of single atoms; and the coalescence of two nanoparticles. We explore the size range between 1.5-2.5 nm. Our model analyses the evolution of the generalised coordination number during the formation process and employs an available structure-energy relationship to estimate the specific and the mass activities. We show that each formation process leads to a different size-behaviour for the activity. The obtained mass activities range between 5.2-11.2 mA/mg. There is a clear evidence that surface roughness and defects improve catalytic performance of Cu nanoparticles for the CO protonation. Quite surprisingly, the activity has a different size-trend depending on the formation process. While the annealing has a monotonic decrease with the nanoparticle size, larger and more defected nanoparticles obtained via the one-by-one growth - although depending on the shape of the initial seed - are the most active. Coalescence has a non-monotonic behaviour with size strongly depending on how fast necks and interfaces of the individual nanoparticles rearrange.

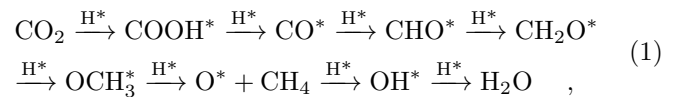
I. INTRODUCTION

Electroreduction of CO₂ represents a promising approach toward artificial carbon recycling for addressing global challenges in energy and sustainability. As CO₂ is thermodynamically stable and kinetically inert^{1,2}, its efficient conversion requires the use of catalysts capable of selectively reducing CO₂ to valuable (oxygenated) hydrocarbon products at low overpotential. In recent years, CO₂ conversion using electrochemical catalysis approaches has attracted great attention for its several advantages: (1) the process is controllable by electrode potentials and reaction temperature; (2) the supporting electrolytes can be fully recycled so that the overall chemical consumption can be minimized to water only; (3) the electricity used to drive the process can be obtained by employing renewable energies; and (4) the electrochemical reaction systems are compact, modular, on-demand, and easy for scale-up applications³⁻⁶. Metallic nanoparticles (NPs) are deemed to be likely candidates for the purpose of heterogeneous catalysis in electrochemical fuel cells⁷⁻⁹. To propose robust design-rules for nanocatalysts (their size, shape, chemical composition and ordering) avoiding a costly and ineffective trial-and-error procedure, two factors should be simultaneously taken into account: (i) the variety of adsorption sites per each isomer¹⁰, which influences both activity and selectivity, and (ii) the coexistence of different geometries, eventually related to their formation process¹¹. Out of the polycrystalline metals, copper (Cu) is the only heterogeneous catalyst that has shown a propensity to produce valuable hydrocarbons, aldehydes and alcohols from electrochemical CO₂ Reduction Reaction (CO₂RR)¹. Even if copper has already largely been used as a catalyst to reduce the CO₂^{1,2,5,6,12-20,22-24,26,27,29,51}, it is still a challenge to reach higher efficiencies³⁹. Here for the first time, we adopt our recently proposed nanoCHE model^{45,68} to the protonation of CO into CHO. The catalytic performance of Cu is closely associated with the electronic structure of the active site^{40,42}. The prediction of the catalytic activity of Cu by means of the atop generalised coordination number, a suitable geometrical descriptor to classify every adsorption sites, provides a robust structure-energy relationship, to be combined with the nanoCHE

model^{22,43,47}. Furthermore we demonstrate that the formation process can significantly affect the Cu activity. We model freezing, growth atom-by-atom and coalescence. The mass activity of structures resulting from freezing decreases with the increase in size. Growth from the subsequent addition of atoms improves NP activity while coalescence does not show any particular size-behaviour. We anticipate that our results may be of interest to the experimental communities - who could use our findings to engineer tailored experiments.

II. METHODOLOGY

The reaction pathways from CO₂ to CH₄ on Cu have been established by Peterson et al.^{20,21} as :



where * stands for adsorbed molecules. For CH₄, the rate limiting step is considered to be the the protonation of adsorbed CO to make adsorbed CHO²³. The binding energy difference between the two adsorbates will dictate the relative activity of each NP facet. The activity of a NP is the rate of a specific reaction happening on its surface; it can be normalised to the real NP's area (leading to the specific activity, SA), or to the NP's mass (leading to the mass activity, MA). The SA determines how much current is achieved at a certain applied overpotential¹².

For the case of the electrochemical reduction of carbon dioxide to CH₄, which involves the atop adsorption of CO, the atop Generalized Coordination Number, aGCN, , as demonstrated by Zhao et al.²². The core assumption of this model is that the reaction free energy ΔG of the rate limiting step of the reaction can be written as a function of the generalized coordination number.

To monitor the evolution of the mass activity for various nanoparticle shapes, we employ the NanoCHE model. This is an extension of the CHE model pioneered by Norskov and co-workers⁷¹. It allows to translate changes in the coordination of active sites - because of the intrinsic structural

fluxionality of nanoparticles^{59–61} into potential changes of their activity. This approach also enables to simulate a linear sweep voltammetry experiment upon metallic nanosystems with a wide variety of non equivalent adsorption sites.

The atop generalised coordination number (aGCN) - which has been proven to be a robust activity descriptor⁴⁷ - is introduced and its relation to the reaction free energy ΔG for CHO formation is taken from Zhao et al.²², and reported in the turquoise box in Figure 1. At a certain time t of the evolution, at a temperature T , and at an applied voltage U , the current density is⁷⁰

$$j_{NP}(t, T, U) = \sum_{i \in \{aGCN\}} C \frac{\Omega(i)}{N_{sites}} i e^{\beta(\Delta G(i) - neU)} \quad , \quad (2)$$

where $aGCN_i$ equals $\sum_j \frac{CN_j}{CN_{max}}$. CN_j is the nominal coordination number of the j -neighbouring atoms of i calculated within a cut-off distance r_{cut} , defined as the first minimum in the pair-distance distribution function (PDDF) and CN_{max} is set to 12. T is kept at 300 K, since catalysis occurs usually at room temperature. The temperature used in the CMD simulations should be considered as a tool to accelerate rate events. N_{sites} corresponds to the number of surface sites. The pre-factor C is fitted to reproduce the specific activity of low-Miller index surfaces⁷⁰ and by combining the experimental value of the IV-curve of a 24 nm cube.⁴⁶ We fix C to $-3.01 \cdot 10^{14}$ mA/cm².

The mass activity (MA) at a certain applied potential U^* , here 1.1 V, is

$$MA = \frac{j_{NP}^* \cdot A_{surf}}{M} \quad , \quad (3)$$

where the mass is the number of atoms N in the NP multiplied by their atomic mass, i.e. 63.546 a.u. for Cu. The surface area A_{surf} is quantifiable as a function of the aGCN too, $A_{surf} = \sum_i^N 4\pi r_{atomic}^2 \left(1 - \frac{aGCN(i)}{12}\right)$, where the sum is over all atoms i in the nanoparticle, and r_{atomic} is the atomic radius of the particle, namely 0.128 nm for Cu.

We model different formation processes, namely freezing, growth, coalescence, through classical molecular dynamics (CMD) simulations as available in the LoDiS package⁵⁷ and we use a common neighbour analysis (CNA)^{49,50} to classify Cu-NPs into geometrical families, namely FCC, Icosahedra (Ih) and Decahedra (Dh), as well as defects formation, i.e. re-entrances and elongated concavities, and the formation of twin planes, grain boundaries, and five-fold axes. A velocity-Verlet algorithm⁵⁶ is exploited to evolve Newton's Equation of motion with a time step of 5 fs and the atomic interaction is described by the Rosato-Guillopie-Legrand (RGL) potential⁵⁷, with parameters for Cu from⁵⁷. An Andersen thermostat is used to control the temperature. Per each system we accumulate four independent simulations and average them. The NPs vary from a size of 110 to 976 atoms, i.e. 1.5-2.5 nm. The geometries used are FCC polyhedra, namely Octahedra (Oh) and their regular truncation (To), Marks-Decahedra (MDh), Icosahedra (Ih) and defected Icosahedra (dIh) resulting from a basin-hopping algorithm at not-magic sizes⁶².

The annealing of a liquid droplet at 147, 250, 561, 585, 586, 891, and 976 atoms follows the iterative Molecular Dynamics (itMD) algorithm⁵⁷. This is various and concatenated canonical NVT runs, where the temperature is lowered from 1200 K to 400 K at a rate of 5 K/ns. We model the atom-by-atom growth as described in detailed

in⁶², starting from three seed of similar size as Cu₁₄₆ (Oh), Cu₁₄₇ (Ih) and Cu₂₀₁ (To) up to 996 atoms, where atoms are deposited every 4 ns at 600 K. Coalescence is the process by which two clusters are made colliding along the z axis. Each nanoparticle is free to move at 600 K, and we analyse the first 0.05 ns of their dynamics.

The workflow of the proposed multiscale numerical strategy is visually represented in Figure 1.

III. RESULTS AND DISCUSSION

Surface atoms are believed to correspond to a coordination between 2 and 9 are considered: only such atoms are considered, in order to be consistent with Zhao et al.²². The aGCN distribution is more widely spread for liquid structures, since they are disordered and low-coordinated; it narrows down to specific signatures when the temperature is decreased. NPs resulting from growth are highly under-coordinated, and are thus expected to produce a higher current density. The Ih evolution produces more under-coordinated sites than the Oh or the To evolution. Coalescence leads to defected or amorphous elongated structures. The aGCN distributions at different sizes produced by the three processes can be seen in Figure 2.

Small NPs (1.5 nm) produced by growth are low-coordinated, presenting aGCN values of around 2. This will increase their current density. Frozen droplets of sizes between 490 and 850 atoms are more highly coordinated than collided and grown ones at the same sizes. Coalescence of a system composed of 581 atoms leads to a NP which is less coordinated than one resulting from growth.

Some NP snapshots of structures at various sizes are displayed in Figure 3.16 to perform useful comparisons.

Cu₁₄₇ is expected to be highly active, being its surface extraordinarily low-coordinated. It is surprising how the simulation time is sufficient to bring it to a perfectly ordered Ih. Frozen NPs become defected Ih, Dh and FCC structures, preserving their initial spherical shape. On the contrary, the growth of both Oh and To presents structures with many (111), (100) and (211) facets. The Oh exhibits triangular facets, while the To hexagonal ones. The Ih evolution proceeds with a layer-by-layer deposition, maintaining its Ih resemblance. Collided NPs' final geometries are elongated and, in most cases, amorphous. The neck formation leads to a peak in highly-coordinated sites.

The NP coordination is employed to obtain IV curves for the protonation of CO to CHO. The current density results range from -0.12 mA/cm² (frozen Cu₅₆₁) to -0.69 mA/cm² (liquid Cu₁₄₇) at an applied potential of -1.11 V, and they are displayed in Figure 4.

It can be seen how in the coalescence process the size does not influence the current density evolution. The collision of a mDh with Ih and dIh (sizes of 581 and 719 atoms) lead to NPs carrying more current density than other collided structures. Such high j s are only achieved at liquid small NPs. The case of liquid small NPs is extraordinary; liquid Cu₁₄₇, due to its small size and high number of low-coordinated sites carries an extremely high current density. Some quantum effects are not to be excluded in this case. Frozen NPs carry a low current density; the only ones that can be compared to other results are Cu₂₅₀ and Cu₅₈₆, which are disordered enough to exhibit low-coordinated sites: the first produces a current density equivalent to an FCC grown to 250 atoms, while the latter

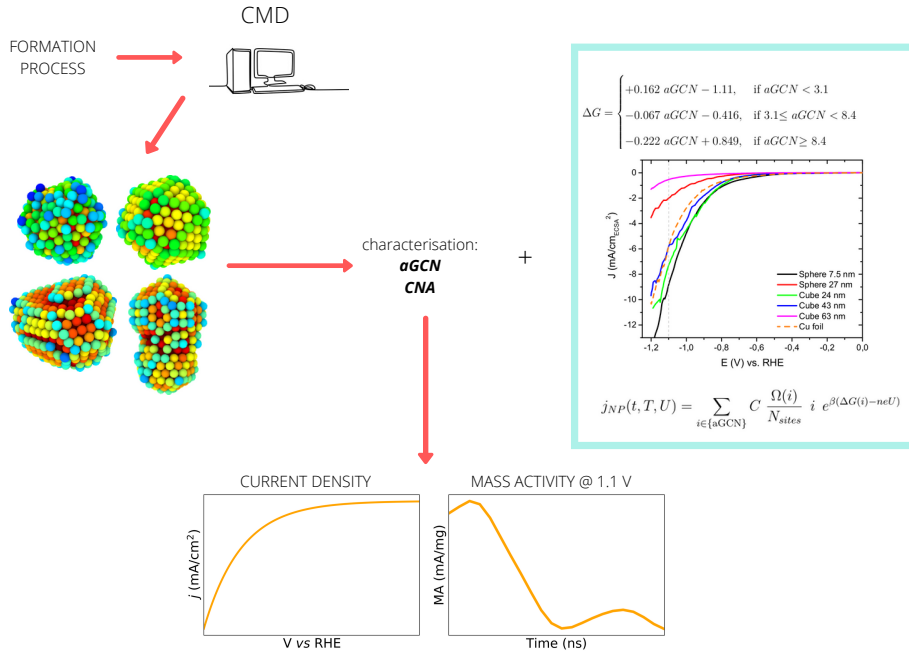


FIG. 1: Workflow. The formation process (freezing, growth, coalescence) is investigated by means of classical molecular dynamics (CMD). Various shapes and sizes are produced. They are geometrically characterized through a CNA and by analysing their aGCN distribution. By combining our data with other studies^{22,46} (reported in the box) the current density j produced by the NP is calculated, to then measure the cluster’s mass activity and quantify their catalytic properties.

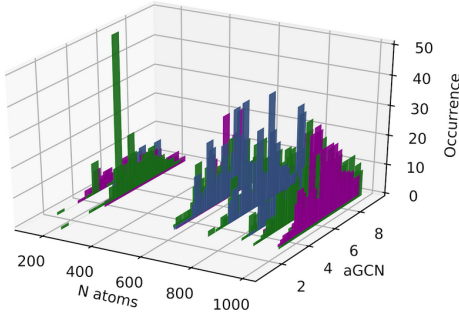


FIG. 2: aGCN occurrence at 600K for different processes and different cluster dimensions. ■ represents freezing, ■ growth and ■ coalescence.

to an Oh grown to 976 atoms. Liquid structures are better than frozen ones at equivalent sizes, apart the case of Cu_{250} , since it is the only one starting from a non-magical size. Within the grown structures, the Ih evolution leads to less current density at every size considered. At very small (250 atoms) and very big (976 atoms) sizes the FCC evolution produces more current density, while at intermediate sizes the Oh seems to be more favourable for the CO_2 activity.

To obtain the mass activity of the cluster, surface area calculations are performed. The surface area noticeably decreases throughout the freezing process, dropping from values of $1.2-5.4 \cdot 10^{-15} \text{ cm}^2$ (the highest achieved) to $1-3.8 \cdot 10^{-15} \text{ cm}^2$. The surface area of grown structures increases monotonically with size, leading to values between $1-3.5 \cdot 10^{-15} \text{ cm}^2$. Coalescence leads to structures with a surface area of $1.4-3.6 \cdot 10^{-15} \text{ cm}^2$.

The MAs calculated through Equation 3 are reported in Figure 5.

The liquid droplet of Cu_{147} is extremely active, as expected from its high current density. The results prove that small NPs with low-coordinated surface atoms are more favorable for CO_2 dissociation than larger particles²⁴. Liq-

SIZE	LIQUID (1200 K)	FROZEN (400 K)	GROWN (Oh)	GROWN (Ih)	GROWN (FCC)	COLLIDED
240	x	x				
250						x
520	x	x				
561						x
585						
719	x	x				
839	x	x				
891						x
976						x

FIG. 3: Pictorial representation of common snapshots found listed per each formation processes for Cu-nanoparticles. Atoms are coloured accordingly to their atop GCN (red 2 and blue 9) following the color gradient

uid NPs are more active than solid ones due their lower-coordination: the only exception is, again, given by the freezing of a non-magical size, Cu_{250} . The low current density produced by large NPs and their larger mass result in a restricted mass activity of large structures produced by freezing, compared to smaller ones resulting from the same formation process. Small grown NPs made of around 250 atoms report a MA between 6.5 mA/mg and 7.5 mA/mg, noticeably lower than the activity of a frozen NP at the same size, which is about 4.6 mA/mg. There are, however,

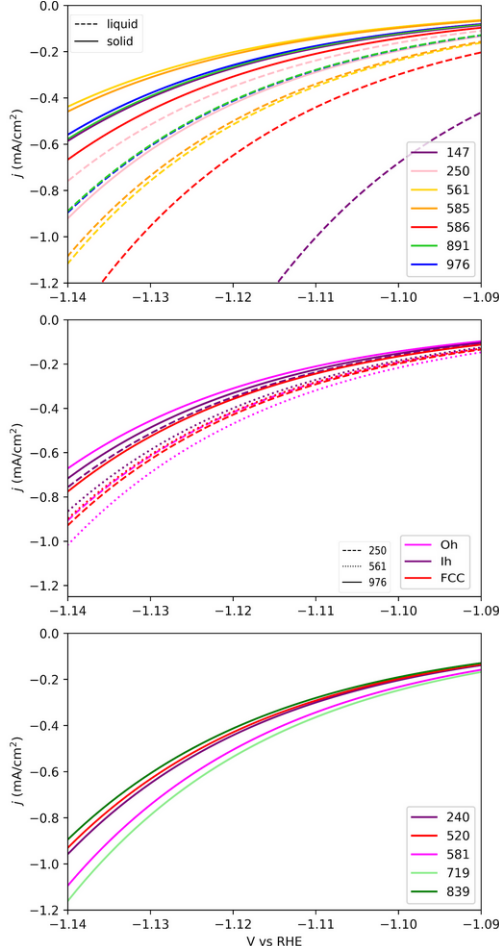


FIG. 4: IV curves for $\text{CO} \rightarrow \text{CH}$. (top) freezing process, dashed line refers to the melted phase and solid-line for the frozen object; (middle) growth one-by-one, different colours refers to different initial seed; (bottom) coalescence after 0.05 ns.

a few exceptions to the monotonically increasing mass activity with the decrease of NP's size in freezing processes, due to the free energy dependence on structure's coordination (Cu_{585} is less active than Cu_{561} , for instance). The increase in surface area with the increase in size for one-by-one growth processes leads to a monotonically increasing relationship between activity and NP's size. From sizes of 550 to 650 atoms the Oh evolution seems the most promising one, with a MA of around 8.5 mA/mg, high compared to the value of 7.5 mA/mg produced by frozen Cu_{561} . At this stage (2 nm) already, grown NPs appear to be more active than frozen ones.

The collisions between a mDh (Cu_{434}) and an Ih (Cu_{147}) produces 10.3 mA/mg, being more active than the collision of a mDh with a dIh or a To. Collided Ih appear to be better catalysts than other collided shapes.

IV. CONCLUSIONS

The Cu catalytic activity for protonation of CO to CHO for CO_2RR to CH_4 is successfully investigated through the NanoCHE model, and is found to follow a different size-trend depending on the CMD formation process. Small liquid droplets reach the highest results achieved, with a mass

activity equivalent to 29.4 mA/mg. Freezing processes are characterised by a monotonically increase in mass activity with the decrease of NP's size, while the opposite behaviour

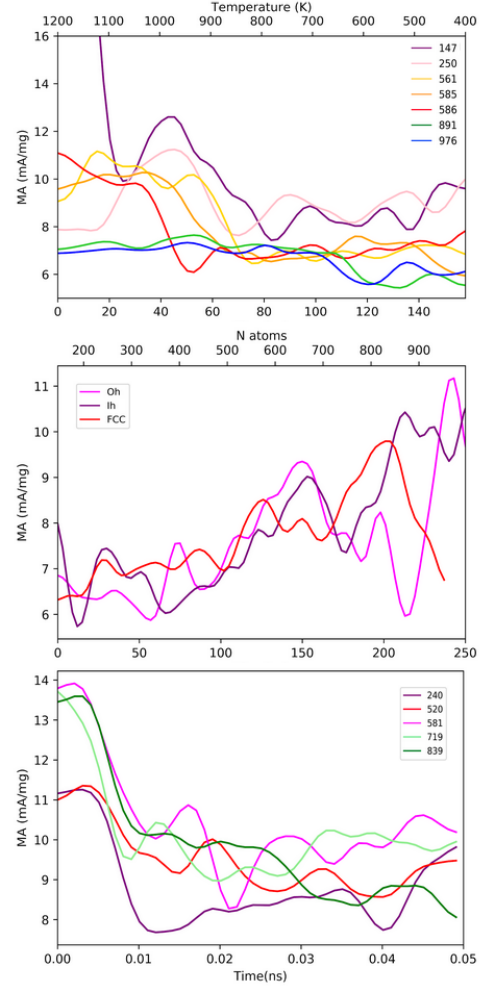


FIG. 5: Mass activity evolution in mA/mg. The lines have been smoothed using a Gaussian fit to make them more readable. The plots refer to (top) freezing process, (middle) growth one-by-one and (bottom) coalescence. The legends for freezing and coalescence represent the number of Cu atoms.

is observed in one-by-one growth processes, where larger and more defected NPs are the most active. At sizes of 1.6 nm the mass activity is equivalent to 9.6 mA/mg and 7 mA/mg for frozen droplets and deposited NPs respectively, while at larger sizes of 2.5 nm grown structures produce 11.2 mA/mg, and frozen ones 5.2 mA/mg. NPs produced by collision report an activity which is dependent on how fast necks and interfaces of the individual nanoparticles rearrange, rather than on their sizes.

V. ACKNOWLEDGEMENTS

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