

Let's analyze the `mystery` function and determine what it computes. Here is the function for reference:

```
public static int mystery(int a, int b) {
    if (b == 0) return 0;
    if (b % 2 == 0) return mystery(a + a, b / 2);
    return mystery(a + a, b / 2) + a;
}
```

Analyzing the Function

To understand the function, let's go through the steps for `mystery(2, 25)` and `mystery(3, 11)`.

`mystery(2, 25)`

- Initial call: `mystery(2, 25)`
 - `b` is not 0 and `b % 2` is 1 (odd), so it returns `mystery(4, 12) + 2`
 - `mystery(4, 12)`
 - `b` is not 0 and `b % 2` is 0 (even), so it returns `mystery(8, 6)`
 - `mystery(8, 6)`
 - `b` is not 0 and `b % 2` is 0 (even), so it returns `mystery(16, 3)` - `mystery(16, 3)` - `b` is not 0 and `b % 2` is 1 (odd), so it returns `mystery(32, 1) + 16` - `mystery(32, 1)` - `b` is not 0 and `b % 2` is 1 (odd), so it returns `mystery(64, 0) + 32` - `mystery(64, 0)` returns 0 - Result: $32 + 0 = 32$ - Result: $32 + 16 = 48$
 - Result: 48
 - Result: 48
 - Result: $48 + 2 = 50$

`mystery(3, 11)`

- Initial call: `mystery(3, 11)`
 - `b` is not 0 and `b % 2` is 1 (odd), so it returns `mystery(6, 5) + 3`
 - `mystery(6, 5)`
 - `b` is not 0 and `b % 2` is 1 (odd), so it returns `mystery(12, 2) + 6`
 - `mystery(12, 2)`
 - `b` is not 0 and `b % 2` is 0 (even), so it returns `mystery(24, 1)` - `mystery(24, 1)` - `b` is not 0 and `b % 2` is 1 (odd), so it returns `mystery(48, 0) + 24` - `mystery(48, 0)` returns 0 - Result: $24 + 0 = 24$
 - Result: 24

- Result: $24 + 6 = 30$
- Result: $30 + 3 = 33$

Explanation of the Function

The function `mystery(a, b)` actually performs the multiplication $a * b$ using a recursive method similar to the ancient Egyptian multiplication method, also known as peasant multiplication. Here's how it works:

- If `b` is `0`, the result is `0` (base case).
- If `b` is even, it calls itself with `a` doubled and `b` halved.
- If `b` is odd, it adds `a` to the result of the recursive call with `a` doubled and `b` halved.

This is equivalent to decomposing the multiplication into additions.

Modified Function with `+` Replaced by `*`

Let's modify the function:

```
public static int mystery(int a, int b) {
    if (b == 0) return 1;
    if (b % 2 == 0) return mystery(a * a, b / 2);
    return mystery(a * a, b / 2) * a;
}
```

Analyzing the Modified Function

This modified function now performs exponentiation instead of multiplication.

`mystery(2, 25)`

- Initial call: `mystery(2, 25)`
 - `b` is not `0` and `b % 2` is `1` (odd), so it returns `mystery(4, 12) * 2`
 - `mystery(4, 12)`
 - `b` is not `0` and `b % 2` is `0` (even), so it returns `mystery(16, 6)`
 - `mystery(16, 6)`
 - `b` is not `0` and `b % 2` is `0` (even), so it returns `mystery(256, 3)` - `mystery(256, 3)` - `b` is not `0` and `b % 2` is `1` (odd), so it returns `mystery(65536, 1) * 256` - `mystery(65536, 1)` - `b` is not `0` and `b % 2` is `1` (odd), so it returns `mystery(4294967296, 0) * 65536` - `mystery(4294967296, 0)` returns `1` - Result: `65536 * 1 = 65536` - Result: `65536 * 256 = 16777216`
 - Result: `16777216`
 - Result: `16777216`

- Result: $16777216 * 2 = 33554432$

`mystery(3, 11)`

- Initial call: `mystery(3, 11)`
 - `b` is not `0` and `b % 2` is `1` (odd), so it returns `mystery(9, 5) * 3`
 - `mystery(9, 5)`
 - `b` is not `0` and `b % 2` is `1` (odd), so it returns `mystery(81, 2) * 9`
 - `mystery(81, 2)`
 - `b` is not `0` and `b % 2` is `0` (even), so it returns `mystery(6561, 1) - mystery(6561, 1) - b` is not `0` and `b % 2` is `1` (odd), so it returns `mystery(43046721, 0) * 6561 - mystery(43046721, 0)` returns `1` - Result: $6561 * 1 = 6561$
 - Result: `6561`
 - Result: $6561 * 9 = 59049$
 - Result: $59049 * 3 = 177147$

Summary

- The original function `mystery(a, b)` computes the product $a * b$ using a recursive algorithm.
- The modified function with `+` replaced by `*` and `return 0` replaced by `return 1` computes a raised to the power of b (i.e., a^b).