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The gcdlike function is similar to the Euclidean algorithm for computing the greatest common divisor (GCD) of two integers p and q. However, it has a slightly different purpose. Here is the function for reference:

```
public static boolean gcdlike(int p, int q) {
   if (q == 0) return (p == 1);
   return gcdlike(q, p % q);
}
```

Understanding the Function

This function checks whether the GCD of two integers $\,p\,$ and $\,q\,$ is $\,1\,$. In other words, it checks if $\,p\,$ and $\,q\,$ are **coprime** (i.e., they have no common divisors other than $\,1\,$). Let's break down the logic:

1. Base Case:

- if (q == 0) return (p == 1);
- When q becomes 0, the function returns whether p is 1. If p is 1, it returns true; otherwise, it returns false.

2. Recursive Case:

- return gcdlike(q, p % q);
- The function recursively calls itself with $\,q\,$ and $\,p\,$ % $\,q\,$, continuing the Euclidean algorithm process.

How It Works

The Euclidean algorithm repeatedly replaces the larger number by its remainder when divided by the smaller number, until one of the numbers becomes 0. The last non-zero remainder is the GCD of the original two numbers. In this function:

- If p % q is calculated and the function continues with the new pair (q, p % q).
- Eventually, q becomes 0, and the function checks if the current value of p is 1.

Effect of the Function

The function gcdlike(p, q) returns true if and only if the GCD of p and q is 1, meaning p and q are coprime. Here's what it means in terms of integers and divisors:

1. When gcdlike(p, q) Returns true:

- p and q have no common divisors other than 1.
- There are no integers greater than $\,1\,$ that divide both $\,p\,$ and $\,q\,$.

2. When gcdlike(p, q) Returns false:

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- p and q have a common divisor greater than 1.
- There exists at least one integer greater than 1 that divides both p and q.

Example Walkthrough

```
Let's consider an example with p = 14 and q = 9:
```

```
    gcdlike(14, 9):

            q is not 0, so call gcdlike(9, 14 % 9) which is gcdlike(9, 5).

    gcdlike(9, 5):

            q is not 0, so call gcdlike(5, 9 % 5) which is gcdlike(5, 4).

    gcdlike(5, 4):

            q is not 0, so call gcdlike(4, 5 % 4) which is gcdlike(4, 1).

    gcdlike(4, 1):

            q is not 0, so call gcdlike(1, 4 % 1) which is gcdlike(1, 0).

    gcdlike(1, 0):

            q is 0, so check if p is 1. Since p is 1, return true.
```

Thus, gcdlike(14, 9) returns true, indicating that 14 and 9 are coprime.

Summary

The gcdlike function effectively determines whether two integers p and q are coprime. If the function returns true, the integers share no common divisors other than 1, meaning they are coprime. If the function returns false, they share at least one common divisor greater than 1.