

To estimate the memory usage of the `CompareDocuments` class as a function of the number of documents n and the dimension d , we need to consider the primary data structures and their sizes:

```
public class CompareDocuments {
    public static void main(String[] args) {
        int k = Integer.parseInt(args[0]);
        int d = Integer.parseInt(args[1]);
        String[] filenames = StdIn.readAllStrings();
        int n = filenames.length;

        // create document sketches
        Sketch[] sketches = new Sketch[n];
        for (int i = 0; i < n; i++) {
            In in = new In(filenames[i]);
            String text = in.readAll();
            sketches[i] = new Sketch(text, k, d);
        }

        // print header
        StdOut.print(" ");
        for (int i = 0; i < n; i++) {
            StdOut.printf("%8.4s", filenames[i]);
        }
        StdOut.println();

        // print n-by-n table
        for (int i = 0; i < n; i++) {
            StdOut.printf("%.4s", filenames[i]);
            for (int j = 0; j < n; j++) {
                StdOut.printf("%8.2f",
                    sketches[i].similarTo(sketches[j]));
            }
            StdOut.println();
        }
    }
}
```

1. Array of filenames:

- **Memory Usage:** This array will hold references to the filenames.
- **Size:** n references.

2. Array of `Sketch` objects:

- **Memory Usage:** This array will hold references to the `Sketch` objects.
- **Size:** n references.

3. `Sketch` Objects:

- The `Sketch` class is initialized with the text of the document, and the parameters k and d . Assuming the `Sketch` class processes the text and stores information in an array of size d , the memory usage will depend on the implementation of `Sketch`.

Assuming each `Sketch` object contains:

- A reference to the original document text.
- A data structure (e.g., an array) of size d to store the sketch.

Let's assume each element in the sketch array is a double (8 bytes).

- **Memory Usage per `Sketch` object:**
 - Reference to text: typically 8 bytes (on a 64-bit JVM).
 - Sketch array of size d : $d \times 8$ bytes.

4. Auxiliary Data Structures:

- The `String` text data and its internal representation.
- Temporary variables, loop counters, etc.

To sum up, the memory usage can be approximated as follows:

1. Array of filenames: $n \times \text{reference_size}$

- On a 64-bit JVM, reference size is 8 bytes.
- Memory: $n \times 8$ bytes.

2. Array of `Sketch` objects: $n \times \text{reference_size}$

- Memory: $n \times 8$ bytes.

3. Each `Sketch` object:

- Reference to the document text: 8 bytes.
- Sketch array: $d \times 8$ bytes.
- Total per `Sketch`: $8 + d \times 8$ bytes.
- For n sketches: $n \times (8 + d \times 8)$.

Combining these components:

- Array of filenames: $n \times 8$ bytes.
- Array of `Sketch` objects: $n \times 8$ bytes.
- Total for `Sketch` objects: $n \times (8 + d \times 8)$ bytes.

Thus, the total memory usage M as a function of n and d is:

$$M(n, d) = n \times 8 + n \times 8 + n \times (8 + d \times 8) \quad M(n, d) = n \times (8 + 8 + 8 + d \times 8)$$

$$M(n, d) = n \times (24 + 8d)$$

So, the estimated memory usage is $M(n, d) = n \times (24 + 8d)$ bytes.