PROJECTING DATA ONTO ROAD NETWORK: MAP MATCHING

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HONR 39900: Foundations of Geospatial Analytics

Fall 2021



Topics

- Collecting GPS Data
 - Dirty Map Data
 - What is Map Matching?
- How to Map Match Raw GPS Data
 - Case Study: Uber and Hidden Markov Models
 - Solution via PostGIS
- A Brief Introduction to Hidden Markov Models:
 - Context: What are Markov Chains and Transition States?
 - Hidden Markov Models
- NEXT WEEK: PostGIS implementation



Collecting GPS Data

- Sometimes GPS data are not as accurate as we would like:
 - Low sampling rate
 - Noise
 - Lack of granularity

WHAT THE NUMBER OF DIGITS IN YOUR COORDINATES MEANS LAT/LON PRECISION MEANING

CHITCON FINECISION	MEANING
28°N, 80°W	YOU'RE PROBABLY DOING SOMETHING SPACE-RELATED
28.5°N, 80.6°W	YOU'RE POINTING OUT A SPECIFIC CITY
28.52°N, 80.68°W	YOU'RE POINTING OUT A NEIGHBORHOOD
28.523°N, 80.683°W	YOU'RE POINTING OUT A SPECIFIC SUBURBAN CUL-DE-SAC
28.5234°N, 80.6830°W	YOU'RE POINTING TO A PARTICULAR CORNER OF A HOUSE
28.52345°N, 80.68309°W	YOU'RE POINTING TO A SPECIFIC PERSON IN A ROOM, BUT SINCE YOU DIDN'T INCLUDE DATUM INFORMATION, WE CAN'T TELL WHO
28.5234571°N, 80.6830941°W	YOU'RE POINTING TO WALDO ON A PAGE
28.523457182°N, 80.683094159°W	"HEY, CHECK OUT THIS SPECIFIC SAND GRAIN!"
28.523457182818284°N, 80.683094159265358°W	EITHER YOU'RE HANDING OUT RAW FLOATING POINT VARIABLES, OR YOU'VE BUILT A DATABASE TO TRACK INDIVIDUAL ATOMS. IN EITHER CASE, PLEASE STOP.



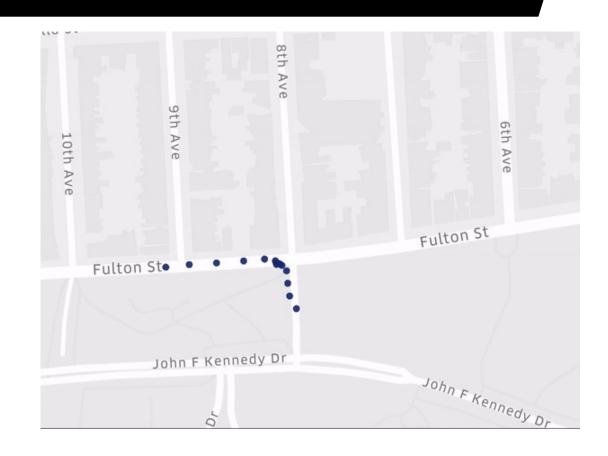
Is there anything Wrong with these Data?





Dirty Map Data

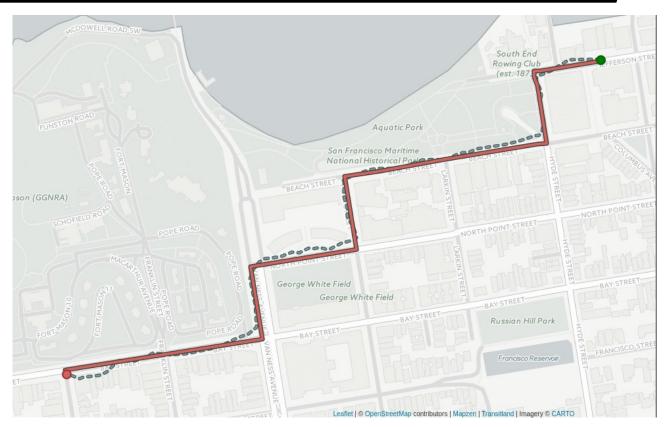
- Are GPS points clearly on the road network?
- Do GPS points stay on a single road/accurately depict where someone was driving?





Dirty Map Data

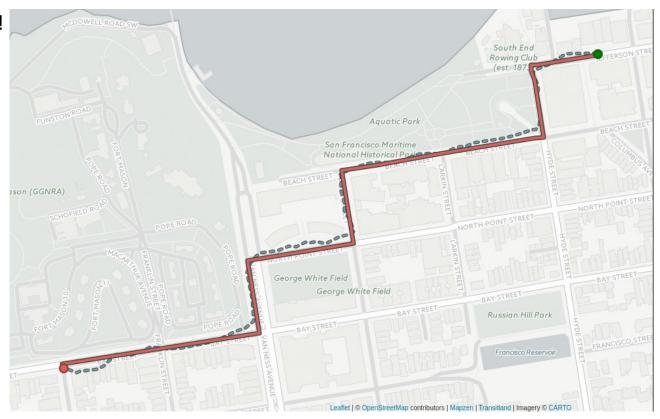
We need to project our GPS traces to a given road network, as depicted right.





What is Map Matching?

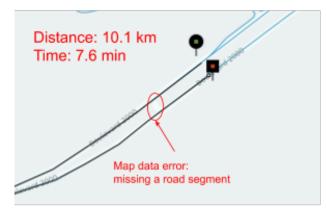
- This leads us to Map Matching!
 - The process taking input as raw GPS data and giving output as the actual position of road network.





Why is Map Matching Important?

- Let's look at a ride-hailing example (e.g., Uber).
- When generating routes, Uber wants to minimize the distance and time to reach a destination:
 - Distance: Decreased wear on drivers' vehicles and reduction in fuel required to execute a trip.
 - Time: A driver can accomplish more rides in a shift and the customer gets to their destination faster.



(a) Suboptimal navigation instruction due to map data error.



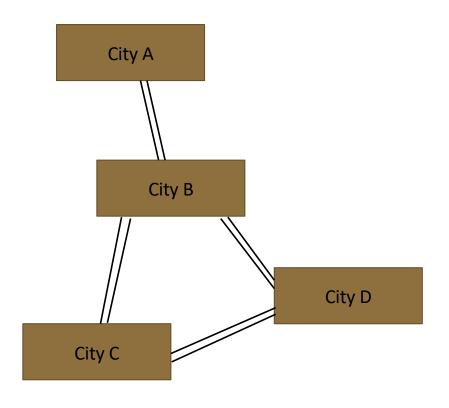
(b) Optimal navigation instruction as a result of fixing the map data error.



How to Map Match Raw GPS Data

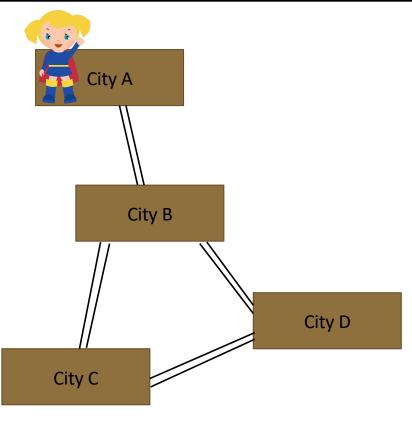
- In this class, we will learn of two approaches to map matching:
 - 1. Hidden Markov Models
 - 2. PostGIS implementation
- Uber uses Hidden Markov Models as their map matching tool





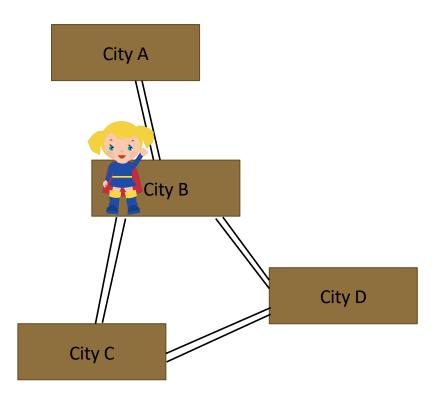
- We have 4 cities, each with a rail connection
- However, not every city has a direct connection to the others
- Unfortunately, these cities have a lot of crime...
 - But, we have a Markovian Superhero who can save us!
 - She has some limitations, though:
 - 1. Can only travel by rail
 - 2. She is a forgetful superhero, and doesn't know where she has been. Thus, to get between cities, she randomly chooses the next city to go to.



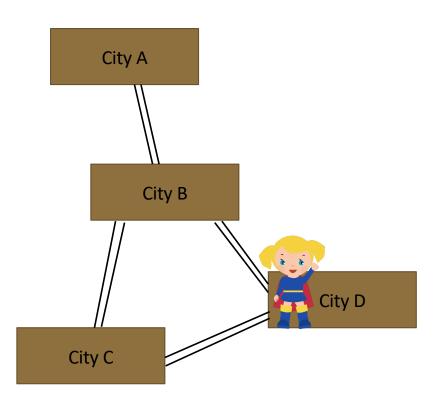


 Our superhero is at City A...there is only 1 option as to where she can travel: to City B



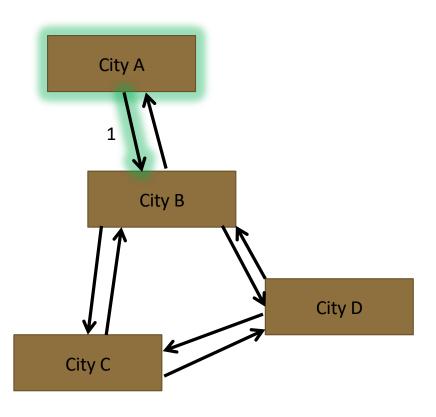


- Now, our Markovian Superhero is in City B. Remember, she has no memory of being in City A to fight crime. All she knows is that she is in City B.
- There are 2 options as to where she can go: City D or City C. She will randomly choose 1 of them.

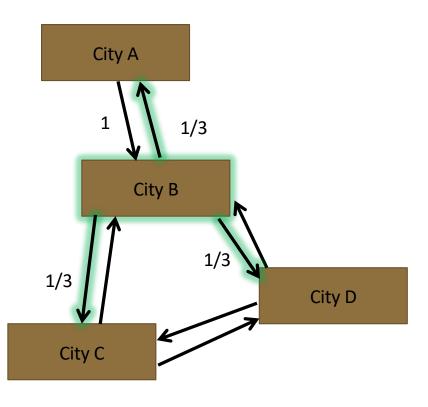


- In City D, the superhero faces the same problem...randomly choose to go to City B or City C.
- This is a Markovian example in which our superhero is always deciding the next step is just a random choice in where she currently is...
- A Markov Chain is a sequence of events such that the probabilities of the future depend ONLY on the present.

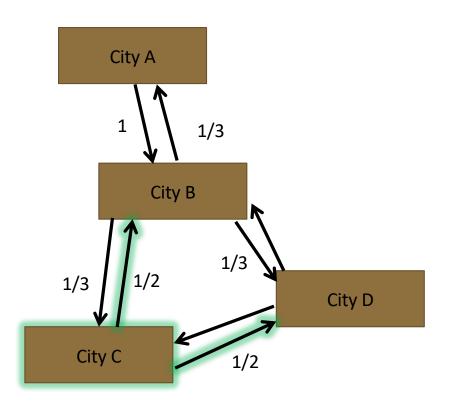




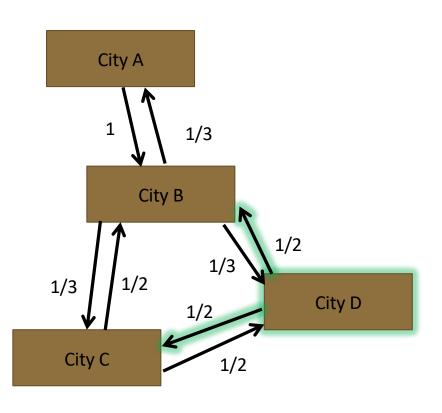
What are the probabilities of traveling from one city to another?



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- What are the probabilities of traveling from one city to another?
- A Transition Diagram lists all the possible states and then lists the probability for every connection between possible states.

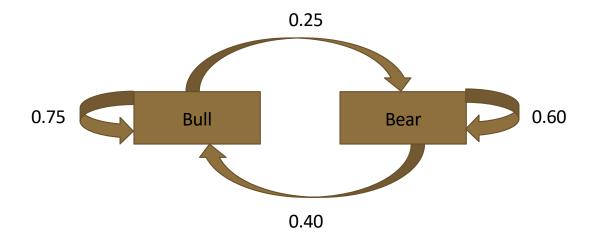
- Example: Stock Market
 - 75% a bull market followed by a bull market (going up)
 - 60% a bear market followed by a bear market (going down)

Bull

Bear

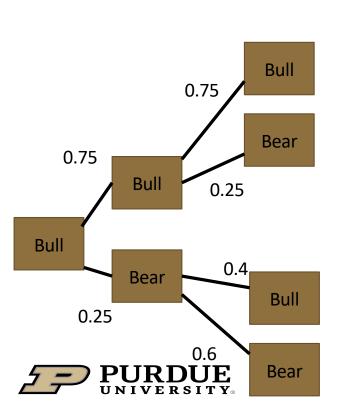


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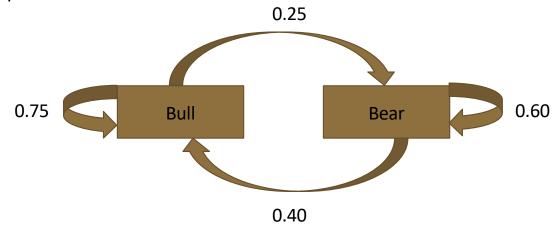




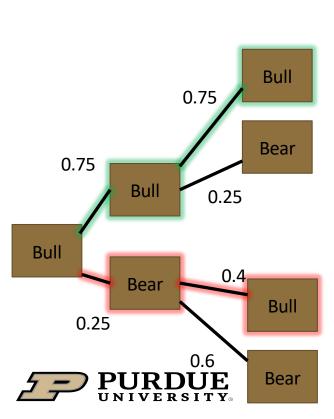
• If there is a bull market this week, what are the probabilities in TWO weeks?



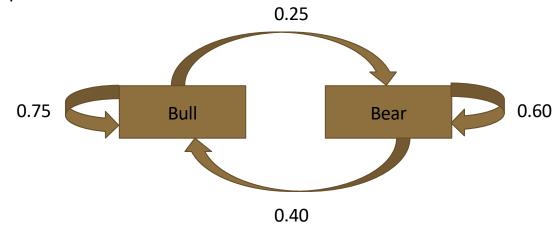
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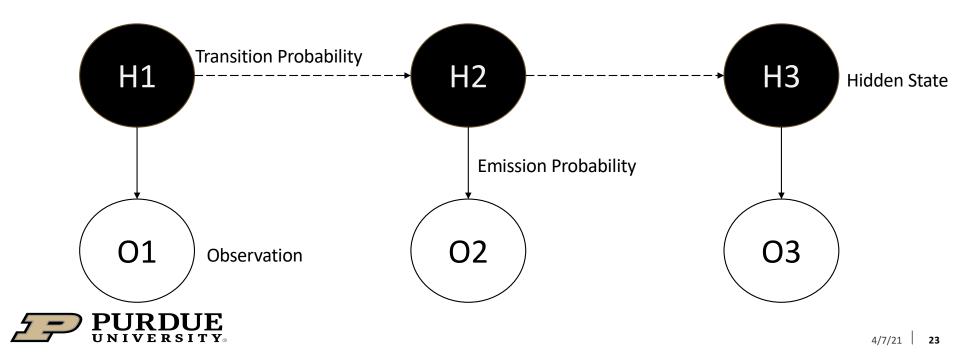


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- Markov process + unobservable state
- Observations, which depend only on the current state, are visible



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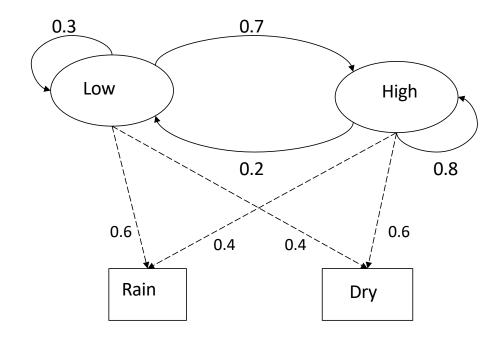
- Set of states: $\{S_1,S_2,\ldots,S_N\}$ Process moves from one state to another generating a $S_{i1},S_{i2},\ldots,S_{ik},\ldots$ sequence of states:
- Markov chain property: probability of each subsequent state depends only on what was the previous state:

$$P(s_{ik} \mid s_{i1}, s_{i2}, ..., s_{ik-1}) = P(s_{ik} \mid s_{ik-1})$$

- States are not visible, but each state randomly generates one of M observations (or visible states) $\{v_1, v_2, ..., v_M\}$
- To define hidden Markov model, the following probabilities have to be specified: matrix of transition probabilities $A=(a_{ii})$, $a_{ii}=P(s_i\mid s_i)$, matrix of observation probabilities $B=(b_i(v_m)), b_i(v_m)=P(v_m \mid s_i)$ and a vector of initial probabilities $\pi = (\pi_i)$, $\pi_i = P(s_i)$. Model is represented by M = (A, A)B, π).



Example



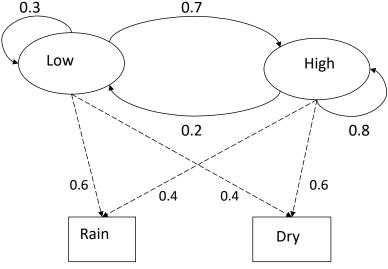


- Two states: 'Low' and 'High' atmospheric pressure.
- Two observations: 'Rain' and 'Dry'.
- Transition probabilities: P('Low'|'Low')=0.3, P('High'|'Low')=0.7, P('Low'|'High')=0.2, P('High'|'High')=0.8

• Observation probabilities : P('Rain'|'Low')=0.6, P('Dry'|'Low')=0.4, P('Rain'|'High')=0.4,

P('Dry'|'High')=0.3.

• Initial probabilities: say P('Low')=0.4, P('High')=0.6



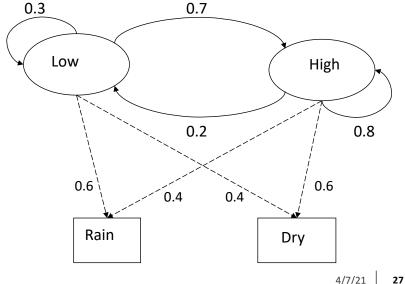


- Calculation of Observation Sequence Probability
- Suppose we want to calculate a probability of a sequence of observations in our example, {'Dry','Rain'}.
- Consider all possible hidden state sequences:

$$P(\{\text{'Dry','Rain'}\}) = P(\{\text{'Dry','Rain'}\}, \{\text{'Low','Low'}\}) + P(\{\text{'Dry','Rain'}\}, \{\text{'Low','High'}\}) + P(\{\text{'Dry','Rain'}\}, \{\text{'High','Low'}\}) + P(\{\text{'Dry','Rain'}\}, \{\text{'High','High'}\})$$

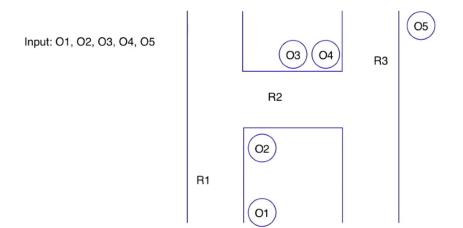
where first term is :

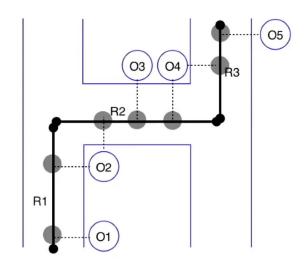
$$\begin{split} &P(\{\text{'Dry','Rain'}\}, \{\text{'Low','Low'}\}) = \\ &P(\{\text{'Dry','Rain'}\} \mid \{\text{'Low','Low'}\}) \mid P(\{\text{'Low','Low'}\}) = \\ &P(\text{'Dry'} \mid \text{'Low'}) P(\text{'Rain'} \mid \text{'Low'}) \mid P(\text{'Low'}) P(\text{'Low'} \mid \text{'Low}) \\ &= 0.4*0.4*0.6*0.4*0.3 \end{split}$$





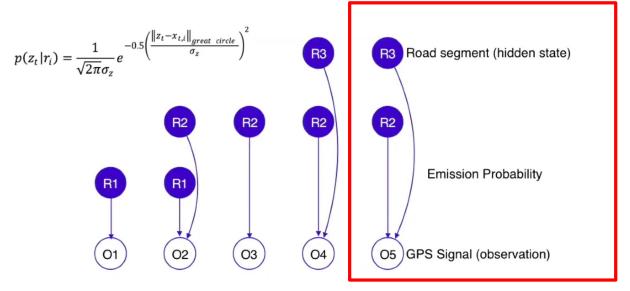






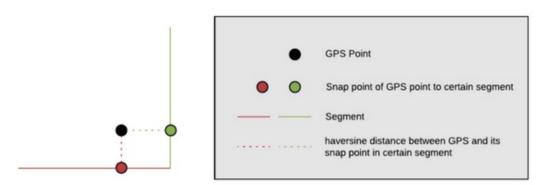


 Emission probability represents the likelihood of a vehicle present on certain road segments at certain moments





- For one GPS point with *m* number of road segments nearby, there will be *m* emission probabilities representing the likelihood of this GPS trace on each road segment.
- For GPS points G1, which have *m* nearby segments, and G2, which has *n* nearby segments, there are *m* * *n* transition probabilities. These probabilities are in HMM... pick up a sequence of states with maximum probabilities that are most likely to represent road segments on which the vehicle was moving.



$$P(GPS \mid Segment) = \frac{1}{\sigma\sqrt{2\pi}}e^{-0.5(\frac{Distance(GPS \mid Snap)}{\sigma})^2}$$

Figure 4: By calculating the haversine distance, we can determine the emission probability of a GPS point, the black point in this illustration, to different road segments, the red and green segments in this illustration.



 calculating transition probability regarding one GPS point on a certain segment to another GPS point on a certain segment, calculated using the following formula

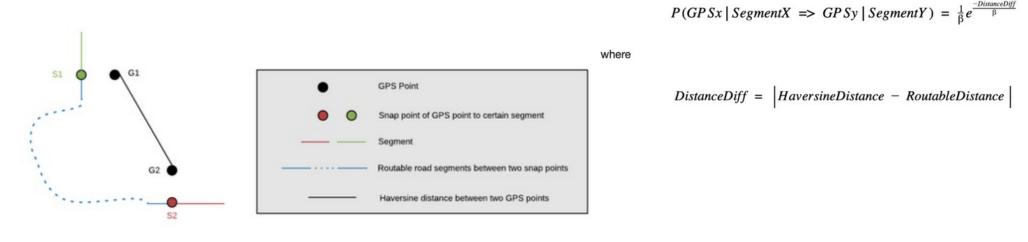


Figure 5: The transition probability from G1 to G2 is calculated by creating a route between their snap points, S1 to S2, and measuring the distance of that route.



 Transition probability represents the likelihood of a vehicle moving from one road segment to another road segment over a certain duration

