BB503/BB602 - R Training - Week XI

Ege Ulgen

Power Analysis/Sample Size Calculation

```
# install.packages("pwr")
library(pwr)
### Effect size: magnitude of the effect under the alternative hypothesis
# The larger the effect size, the easier it is to detect an effect and require fewer samples
### Power: probability of correctly rejecting the null hypothesis if it is false
# The higher the power, the more likely it is to detect an effect if it is present and the more samples
# Standard setting for power is 0.80
### Significance level (alpha): probability of falsely rejecting the null hypothesis even though it is
# The lower the significance level, the more likely it is to avoid a false positive and
# the more samples needed
# Standard setting for alpha is 0.05
### Correlation
?pwr.r.test
# r=correlation
# sig.level=significant level
# power=power of test
# effect size >>> 0.1=small, 0.3=medium, and 0.5 large
# Is there a correlation between hours studied and test score?
# assuming large correlation
pwr.r.test(r=0.5, sig.level=0.05, power=0.80)
##
##
        approximate correlation power calculation (arctangh transformation)
##
##
                 n = 28.248
##
                 r = 0.5
##
         sig.level = 0.05
##
             power = 0.8
       alternative = two.sided
# calculating power
pwr.r.test(n = 50, r=0.5, sig.level=0.05)
##
##
        approximate correlation power calculation (arctangh transformation)
##
##
                 n = 50
##
                 r = 0.5
```

```
##
         sig.level = 0.05
##
             power = 0.96698
##
       alternative = two.sided
pwr.r.test(n = 10, r=0.5, sig.level=0.05)
##
##
        approximate correlation power calculation (arctangh transformation)
##
##
                 n = 10
                 r = 0.5
##
##
         sig.level = 0.05
##
             power = 0.32907
##
       alternative = two.sided
### Two-sample t-test
?pwr.t.test
# d=effect size
# siq.level=siqnificant level
# power=power of test
# type=type of test
# effect size >>> 0.2=small, 0.5=medium, and 0.8 large
# effect size calculation >>> Cohen's D
# Are the average body temperatures of women and men different?
# assuming medium effect size
pwr.t.test(d=0.5, sig.level=0.05, power=0.80, type="two.sample", alternative="two.sided")
##
        Two-sample t test power calculation
##
##
                 n = 63.766
##
                 d = 0.5
##
##
         sig.level = 0.05
##
             power = 0.8
##
       alternative = two.sided
##
## NOTE: n is number in *each* group
# small effect size
pwr.t.test(d=0.2, sig.level=0.05, power=0.80, type="two.sample", alternative="two.sided")
##
##
        Two-sample t test power calculation
##
##
                 n = 393.41
##
                 d = 0.2
##
         sig.level = 0.05
##
             power = 0.8
##
       alternative = two.sided
## NOTE: n is number in *each* group
# large effect size
pwr.t.test(d=0.8, sig.level=0.05, power=0.80, type="two.sample", alternative="two.sided")
```

```
##
##
        Two-sample t test power calculation
##
##
                 n = 25.525
##
                 d = 0.8
##
         sig.level = 0.05
##
             power = 0.8
##
       alternative = two.sided
## NOTE: n is number in *each* group
# Is the average body temperature higher in women than in men?
pwr.t.test(d=0.5, sig.level=0.05, power=0.80, type="two.sample", alternative="greater")
##
##
        Two-sample t test power calculation
##
##
                 n = 50.151
##
                 d = 0.5
##
         sig.level = 0.05
##
             power = 0.8
##
       alternative = greater
##
## NOTE: n is number in *each* group
### One-way ANOVA
?pwr.anova.test
# k=number of groups
# f=effect size
# sig.level=significant level
# power=power of test
# effect size >>> 0.1=small, 0.25=medium, and 0.4 large
# Is there a difference in disease incidence across 6 different cities?
# assuming small effect size
pwr.anova.test(k = 6, f = 0.1, sig.level = 0.05, power = 0.80)
##
##
        Balanced one-way analysis of variance power calculation
##
##
                 k = 6
##
                 n = 214.72
                 f = 0.1
##
##
         sig.level = 0.05
##
             power = 0.8
##
## NOTE: n is number in each group
### Chi-squared test
?pwr.chisq.test
# w=effect size
# df=degrees of freedom
# sig.level=significant level
# power=power of test
```

```
# effect size >>> 0.1=small, 0.3=medium, and 0.5 large
# Does the observed proportions of phenotypes from a genetics experiment different from the expected 9:
# aassuming medium effect
# df = 4 (phenotypes) - 1 = 3
pwr.chisq.test(w=0.3, df=3, sig.level=0.05, power=0.80)
##
##
        Chi squared power calculation
##
                 w = 0.3
##
##
                 N = 121.14
##
                df = 3
##
         sig.level = 0.05
##
             power = 0.8
##
## NOTE: N is the number of observations
### Linear Regression
?pwr.f2.test
# u=numerator degrees of freedom
# v=denominator degrees of freedom
# f2=effect size
# sig.level=significant level
# power=power of test
# effect size >>> 0.02=small, 0.15=medium, and 0.35 large
# Can height, age, and time spent at the gym, predict weight in adult males?
# assuming medium effect size
(res \leftarrow pwr.f2.test(u = 3, f2 = 0.15, sig.level = 0.05, power = 0.8))
##
##
        Multiple regression power calculation
##
##
                 u = 3
##
                 v = 72.706
##
                f2 = 0.15
##
         sig.level = 0.05
             power = 0.8
##
res$v + 4 #(tot. num. of variables) ### Correlation
## [1] 76.706
?pwr.r.test
# r=correlation
# siq.level=siqnificant level
# power=power of test
# effect size >>> 0.1=small, 0.3=medium, and 0.5 large
```

```
# Is there a correlation between hours studied and test score?
# assuming large correlation
pwr.r.test(r=0.5, sig.level=0.05, power=0.80)
##
##
        approximate correlation power calculation (arctangh transformation)
##
##
                 n = 28.248
##
                 r = 0.5
##
         sig.level = 0.05
##
             power = 0.8
##
       alternative = two.sided
# calculating power
pwr.r.test(n = 50, r=0.5, sig.level=0.05)
##
##
        approximate correlation power calculation (arctangh transformation)
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                 n = 50
##
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##
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pwr.r.test(n = 10, r=0.5, sig.level=0.05)
##
##
        approximate correlation power calculation (arctangh transformation)
##
##
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##
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# effect size >>> 0.2=small, 0.5=medium, and 0.8 large
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##
##
        Two-sample t test power calculation
##
##
                 n = 63.766
                 d = 0.5
##
##
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```

```
##
             power = 0.8
##
       alternative = two.sided
##
## NOTE: n is number in *each* group
# small effect size
pwr.t.test(d=0.2, sig.level=0.05, power=0.80, type="two.sample", alternative="two.sided")
##
        Two-sample t test power calculation
##
##
##
                 n = 393.41
                 d = 0.2
##
##
         sig.level = 0.05
##
             power = 0.8
##
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##
## NOTE: n is number in *each* group
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pwr.t.test(d=0.8, sig.level=0.05, power=0.80, type="two.sample", alternative="two.sided")
##
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## NOTE: n is number in *each* group
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# Is there a difference in disease incidence across 6 different cities?
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pwr.anova.test(k = 6, f = 0.1, sig.level = 0.05, power = 0.80)
##
##
        Balanced one-way analysis of variance power calculation
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##
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##
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##
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### Chi-squared test
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# w=effect size
# df=degrees of freedom
# sig.level=significant level
# power=power of test
# effect size >>> 0.1=small, 0.3=medium, and 0.5 large
# Does the observed proportions of phenotypes from a genetics experiment different from the expected 9:
# aassuming medium effect
# df = 4 (phenotypes) - 1 = 3
pwr.chisq.test(w=0.3, df=3, sig.level=0.05, power=0.80)
##
##
        Chi squared power calculation
##
##
                 w = 0.3
##
                 N = 121.14
##
                df = 3
         sig.level = 0.05
##
##
             power = 0.8
## NOTE: N is the number of observations
### Linear Regression
?pwr.f2.test
# u=numerator degrees of freedom
# v=denominator degrees of freedom
# f2=effect size
# siq.level=siqnificant level
# power=power of test
\# effect size >>> 0.02=small, 0.15=medium, and 0.35 large
# Can height, age, and time spent at the gym, predict weight in adult males?
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```

```
(res \leftarrow pwr.f2.test(u = 3, f2 = 0.15, sig.level = 0.05, power = 0.8))
##
##
        Multiple regression power calculation
##
##
                  u = 3
##
                  v = 72.706
##
                 f2 = 0.15
##
         sig.level = 0.05
             power = 0.8
##
res$v + 4 #(tot. num. of variables)
## [1] 76.706
```

Linear Regression

Rationale

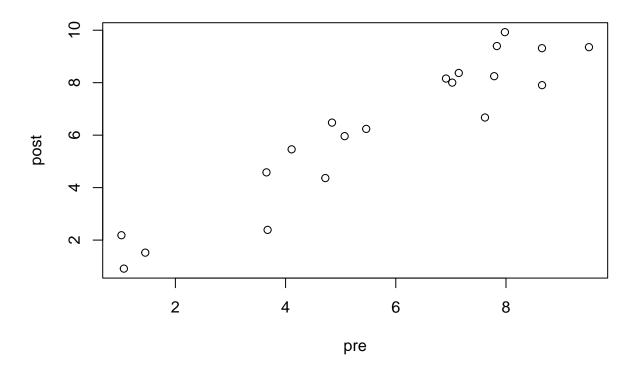
We'll use the pre/post dataset for this exercise. This dataset contains simulated data for pre-intervention measurements (pre) for 20 individuals together with their post-intervention measurements (post).

```
pre_post_df <- read.csv(".../data/pre_post_data.csv")
dim(pre_post_df)

## [1] 20 2
head(pre_post_df, 3)

## pre post
## 1 7.7858 8.2474
## 2 7.6186 6.6725
## 3 8.6532 9.3145

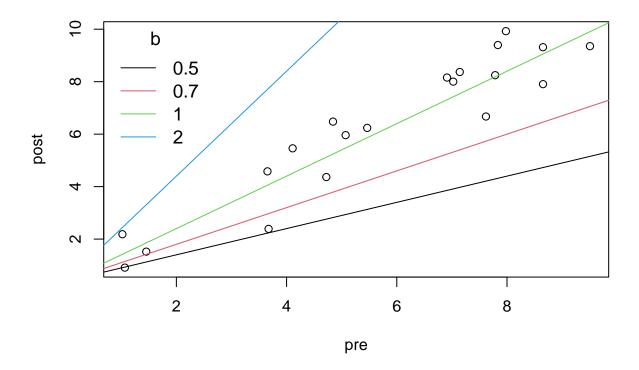
Let's visualize the scatter plot to investigate any relationship between pre and post measurements:
plot(post~pre, data = pre_post_df)</pre>
```



Using the function abline(), we can add different lines, where the argument b is the slope and a is the intercept

```
plot(post~pre, data = pre_post_df)
# y = bx + a
abline(a = .4, b = .5, col = 1)
abline(a = .4, b = .7, col = 2)
abline(a = .4, b = 1, col = 3)
abline(a = .4, b = 2, col = 4)

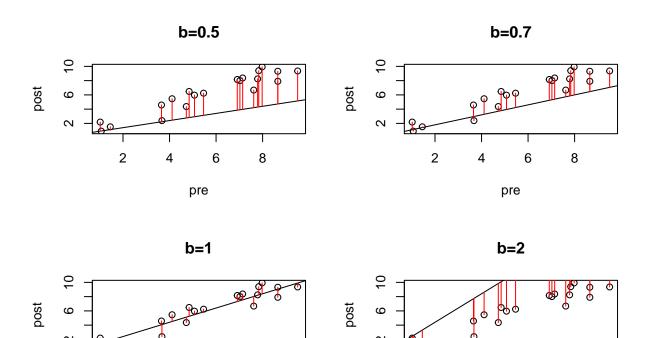
legend("topleft", legend = c(.5, .7, 1, 2), title = "b", col = 1:4, cex = 1.2, bty = "n", lty = 1)
```



Our aim is to minimize the distance to the line (residuals = errors):

```
plot_residual_dist <- function(df, b, a = .4, col = 1) {
    plot(post~pre, data = df, main = pasteO("b=", b))
    abline(a = a, b = b, col = col)
    segments(x0 = df$pre, y0 = df$post, x1 = df$pre, y1 = b * df$pre + a, col = "red")
}

par(mfrow = c(2, 2))
plot_residual_dist(pre_post_df, .5)
plot_residual_dist(pre_post_df, .7)
plot_residual_dist(pre_post_df, 1)
plot_residual_dist(pre_post_df, 2)</pre>
```



```
par(mfrow = c(1, 1))
```

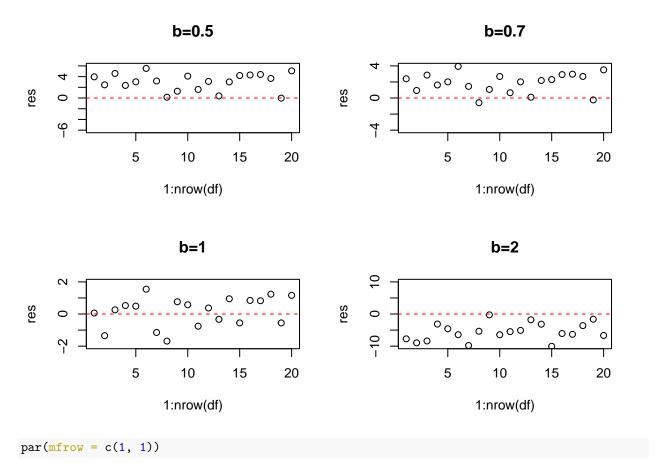
pre

The residuals should be around 0:

pre

```
plot_residual_vals <- function(df, b, a = .4) {
    preds <- b * df$pre + a
    res <- df$post - preds
    tmp <- round(max(abs(res)))
    plot(1:nrow(df), res, ylim = c(-tmp, tmp), main = paste0("b=", b))
    abline(h = 0, col = "red", lty = 2)
}

par(mfrow = c(2, 2))
plot_residual_vals(pre_post_df, 0.5)
plot_residual_vals(pre_post_df, 0.7)
plot_residual_vals(pre_post_df, 1)
plot_residual_vals(pre_post_df, 2)</pre>
```



Examples

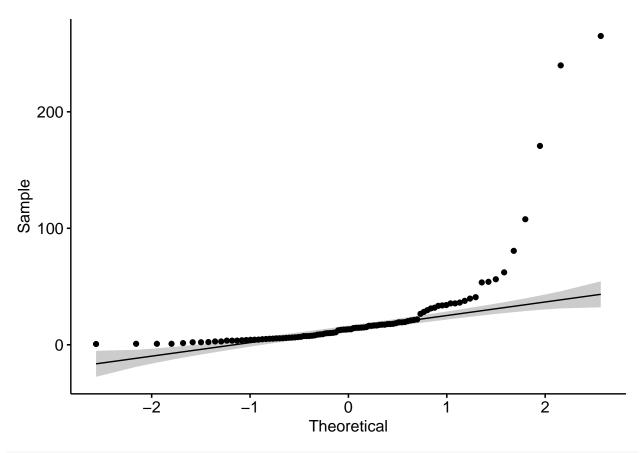
Simple Linear Regression

```
fit_simple <- lm(post~pre, pre_post_df)</pre>
summary(fit_simple)
##
## Call:
## lm(formula = post ~ pre, data = pre_post_df)
##
## Residuals:
##
      Min
              1Q Median
                            ЗQ
                                  Max
  -1.811 -0.670 0.278 0.668
##
                                1.342
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 0.4616
                            0.5165
                                       0.89
                                                0.38
                            0.0826
                                      12.32 3.3e-10 ***
## pre
                 1.0177
##
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.94 on 18 degrees of freedom
## Multiple R-squared: 0.894, Adjusted R-squared: 0.888
```

```
## F-statistic: 152 on 1 and 18 DF, p-value: 3.32e-10
# prediction
new data \leftarrow data.frame(pre = c(3.2, 1.8, 8.2))
predict(fit_simple, new_data)
        1
                2
## 3.7182 2.2935 8.8067
Multiple Linear Regression
We'll use the prostate cancer dataset for this exercise. The main aim of collecting this data set was to inspect
the associations between prostate-specific antigen (PSA) and prognostic clinical measurements in men with
advanced prostate cancer. Data were collected on 97 men who were about to undergo radical prostectomies.
prca_df <- read.csv("../data/prostate_cancer.csv")</pre>
dim(prca_df)
## [1] 97 8
head(prca_df, 3)
##
       PSA
               vol
                       wt age BPH invasion penetration Gleason
## 1 0.651 0.5599 15.959
                           50
                                 0
                                           0
                                                        0
                                                                 6
                                                                 7
## 2 0.852 0.3716 27.660
                           58
                                 0
                                           0
                                                        0
                                                                 7
## 3 0.852 0.6005 14.732
                           74
                                           0
                                                        0
# turn categorical variables into factors
prca_df$invasion <- as.factor(prca_df$invasion)</pre>
prca_df$Gleason <- as.factor(prca_df$Gleason)</pre>
summary(prca_df)
##
         PSA
                             vol
                                                                 age
##
    Min.
           : 0.651
                       Min.
                               : 0.259
                                          Min.
                                                 : 10.7
                                                           Min.
                                                                   :41.0
    1st Qu.: 5.641
                       1st Qu.: 1.665
                                          1st Qu.: 29.4
                                                           1st Qu.:60.0
##
    Median : 13.330
                       Median : 4.263
                                          Median: 37.3
                                                           Median:65.0
##
##
    Mean
           : 23.730
                       Mean
                               : 6.999
                                          Mean
                                                 : 45.5
                                                           Mean
                                                                   :63.9
##
    3rd Qu.: 21.328
                       3rd Qu.: 8.415
                                          3rd Qu.: 48.4
                                                           3rd Qu.:68.0
##
    Max.
           :265.072
                       Max.
                               :45.604
                                          Max.
                                                  :450.3
                                                           Max.
                                                                   :79.0
##
         BPH
                     invasion penetration
                                                 Gleason
##
                                                 6:33
   Min.
           : 0.00
                     0:76
                               Min.
                                      : 0.000
   1st Qu.: 0.00
                     1:21
                               1st Qu.: 0.000
                                                 7:43
                                                 8:21
## Median : 1.35
                               Median : 0.449
## Mean
           : 2.53
                                      : 2.245
                               Mean
##
    3rd Qu.: 4.76
                               3rd Qu.: 3.254
## Max.
           :10.28
                               Max.
                                       :18.174
## check normality of dependent variable
library(ggpubr)
```

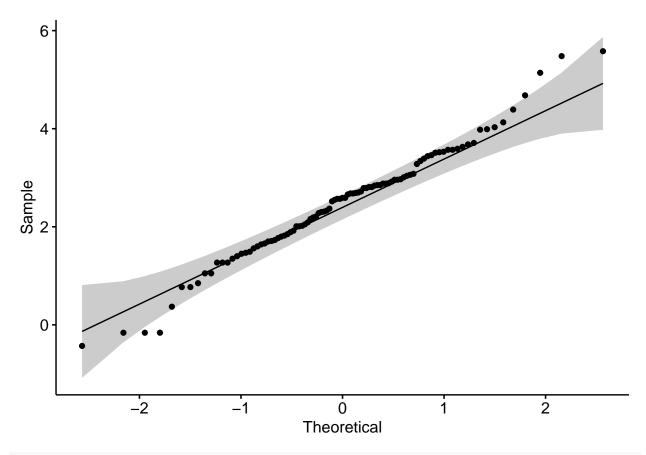
Loading required package: ggplot2

ggqqplot(prca_df\$PSA)



the data quantiles deviates from the normal distribution quantiles shapiro.test(prca_df\$PSA)

```
##
## Shapiro-Wilk normality test
##
## data: prca_df$PSA
## W = 0.479, p-value <2e-16
# For this reason, take the natural log values of the PSA levels, and again test for normality
prca_df$log_PSA <- log(prca_df$PSA)
ggqqplot(prca_df$log_PSA)</pre>
```



```
shapiro.test(prca_df$log_PSA)
```

```
##
##
    Shapiro-Wilk normality test
##
## data: prca_df$log_PSA
## W = 0.984, p-value = 0.31
Let's check the effect of Gleason score on log(PSA) levels:
fit_gleason <- lm(log_PSA~Gleason, data = prca_df)</pre>
summary(fit_gleason)
##
## Call:
## lm(formula = log_PSA ~ Gleason, data = prca_df)
##
## Residuals:
##
       Min
                1Q Median
                                 ЗQ
                                        Max
   -2.5462 -0.6000 0.0052 0.5840
                                     2.1600
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  1.870
                             0.168
                                      11.13 < 2e-16 ***
                              0.223
                                               0.023 *
## Gleason7
                  0.516
                                       2.31
## Gleason8
                  1.755
                             0.269
                                       6.51 3.6e-09 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 0.965 on 94 degrees of freedom
## Multiple R-squared: 0.314, Adjusted R-squared:
## F-statistic: 21.6 on 2 and 94 DF, p-value: 1.97e-08
# change reference level
?relevel()
prca_df$Gleason
## Levels: 6 7 8
prca_df$Gleason <- relevel(prca_df$Gleason, ref = "7")</pre>
prca_df$Gleason
## [1] 6 7 7 6 6 6 6 6 7 6 6 6 7 7 7 6 7 6 6 7 6 7 6 7 6 6 7 7 7 6 6 6 6 6 6 7 8 7
## Levels: 7 6 8
fit_gleason2 <- lm(log_PSA~Gleason, data = prca_df)</pre>
summary(fit_gleason2)
##
## Call:
## lm(formula = log_PSA ~ Gleason, data = prca_df)
##
## Residuals:
##
     Min
            1Q Median
                         3Q
                               Max
## -2.5462 -0.6000 0.0052 0.5840
##
## Coefficients:
           Estimate Std. Error t value Pr(>|t|)
##
              2.386
                       0.147
                              16.21 < 2e-16 ***
## (Intercept)
             -0.516
                       0.223
                              -2.31
                                     0.023 *
## Gleason6
## Gleason8
              1.239
                       0.257
                              4.82 5.5e-06 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.965 on 94 degrees of freedom
## Multiple R-squared: 0.314, Adjusted R-squared:
## F-statistic: 21.6 on 2 and 94 DF, p-value: 1.97e-08
prca_df$Gleason <- relevel(prca_df$Gleason, ref = "6")</pre>
Let's adjust for age:
fit_gleason3 <- lm(log_PSA~Gleason + age, data = prca_df)</pre>
summary(fit_gleason3)
##
## Call:
## lm(formula = log_PSA ~ Gleason + age, data = prca_df)
## Residuals:
##
     Min
            1Q Median
                         3Q
                               Max
```

```
## -2.6336 -0.6132 0.0181 0.5386 2.1002
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                1.2972
                            0.8569
                                      1.51
                                              0.133
                 0.4878
                            0.2278
                                      2.14
                                              0.035 *
## Gleason7
## Gleason8
                 1.7140
                                      6.19 1.6e-08 ***
                            0.2767
                 0.0093
## age
                            0.0137
                                      0.68
                                              0.497
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.968 on 93 degrees of freedom
## Multiple R-squared: 0.318, Adjusted R-squared: 0.296
## F-statistic: 14.4 on 3 and 93 DF, p-value: 8.42e-08
fit_gleason4 <- lm(log_PSA~Gleason + I(age - min(age)), data = prca_df)</pre>
summary(fit_gleason4)
##
## Call:
## lm(formula = log_PSA ~ Gleason + I(age - min(age)), data = prca_df)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
## -2.6336 -0.6132 0.0181 0.5386 2.1002
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
                                  0.3275
                                            5.13 1.6e-06 ***
## (Intercept)
                       1.6786
## Gleason7
                       0.4878
                                  0.2278
                                            2.14
                                                    0.035 *
## Gleason8
                       1.7140
                                  0.2767
                                            6.19 1.6e-08 ***
## I(age - min(age))
                       0.0093
                                  0.0137
                                            0.68
                                                    0.497
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.968 on 93 degrees of freedom
## Multiple R-squared: 0.318, Adjusted R-squared: 0.296
## F-statistic: 14.4 on 3 and 93 DF, p-value: 8.42e-08
fit_gleason5 <- lm(log_PSA~Gleason * age, data = prca_df)</pre>
summary(fit_gleason5)
##
## Call:
## lm(formula = log_PSA ~ Gleason * age, data = prca_df)
## Residuals:
                1Q Median
                                3Q
## -2.7096 -0.6077 0.0198 0.4919 2.0275
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
                                    -0.22
                -0.2895
                            1.3455
                                              0.8301
## (Intercept)
## Gleason7
                  1.5521
                             2.0264
                                       0.77
                                              0.4457
## Gleason8
                  6.2421
                                       2.90
                                              0.0047 **
                             2.1540
```

```
0.0351
                             0.0217
                                      1.62
                                              0.1093
                             0.0319
## Gleason7:age -0.0177
                                      -0.55
                                              0.5803
## Gleason8:age -0.0704
                             0.0333
                                      -2.11
                                              0.0375 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.955 on 91 degrees of freedom
## Multiple R-squared: 0.351, Adjusted R-squared: 0.315
## F-statistic: 9.84 on 5 and 91 DF, p-value: 1.53e-07
  • the effect of age when (Gleason score = 6) = 0.0351
  • the effect of age when (Gleason score = 7) = 0.0351 + (-0.0177)
  • the effect of age when (Gleason score = 8) = 0.0351 + (-0.0704)
What are important factors that have an effect on PSA levels?
fit0 <- lm(log_PSA~vol + wt + age + BPH + invasion + penetration + Gleason, data = prca_df)
summary(fit0)
##
## Call:
## lm(formula = log_PSA ~ vol + wt + age + BPH + invasion + penetration +
##
       Gleason, data = prca_df)
##
## Residuals:
      Min
                1Q Median
                                30
                                       Max
## -1.8512 -0.4541 0.0702 0.4555 1.5093
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 1.49646
                          0.72260
                                      2.07
                                           0.0413 *
                           0.01537
                                      4.39 3.1e-05 ***
## vol
               0.06745
## wt
               0.00127
                           0.00185
                                      0.69
                                           0.4942
              -0.00280
                           0.01178
                                    -0.24
## age
                                           0.8127
## BPH
               0.08911
                          0.02997
                                      2.97
                                            0.0038 **
                          0.27061
## invasion1
               0.79318
                                      2.93 0.0043 **
## penetration -0.02653
                          0.03301
                                     -0.80 0.4238
                                     1.57
## Gleason7
               0.29677
                           0.18891
                                             0.1198
## Gleason8
               0.74661
                                      2.81
                                             0.0062 **
                           0.26604
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.771 on 88 degrees of freedom
## Multiple R-squared: 0.59, Adjusted R-squared: 0.553
## F-statistic: 15.8 on 8 and 88 DF, p-value: 3.14e-14
# equivalently
prca_df2 <- prca_df</pre>
prca df2$PSA <- NULL</pre>
fit0 <- lm(log_PSA~., data = prca_df2)
summary(fit0)
##
## Call:
## lm(formula = log_PSA ~ ., data = prca_df2)
##
```

```
## Residuals:
##
      Min
               1Q Median
                               30
                                      Max
## -1.8512 -0.4541 0.0702 0.4555 1.5093
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
                          0.72260
                                   2.07
## (Intercept) 1.49646
                                            0.0413 *
                                     4.39 3.1e-05 ***
## vol
               0.06745
                          0.01537
## wt
               0.00127
                          0.00185
                                     0.69
                                            0.4942
                                    -0.24
## age
              -0.00280
                          0.01178
                                            0.8127
## BPH
               0.08911
                          0.02997
                                     2.97
                                            0.0038 **
## invasion1
                                     2.93
                                           0.0043 **
               0.79318
                          0.27061
## penetration -0.02653
                          0.03301
                                    -0.80
                                            0.4238
## Gleason7
                                     1.57
                                            0.1198
               0.29677
                          0.18891
## Gleason8
               0.74661
                          0.26604
                                     2.81
                                            0.0062 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.771 on 88 degrees of freedom
## Multiple R-squared: 0.59, Adjusted R-squared: 0.553
## F-statistic: 15.8 on 8 and 88 DF, p-value: 3.14e-14
## keeping only significant variables, fit final model
fit1 <- lm(log_PSA~vol + BPH + invasion + Gleason, data = prca_df)
summary(fit1)
##
## Call:
## lm(formula = log_PSA ~ vol + BPH + invasion + Gleason, data = prca_df)
##
## Residuals:
##
      Min
                1Q Median
                               3Q
                                      Max
## -1.8524 -0.4578 0.0674 0.5165 1.5320
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                1.3882
                           0.1561
                                     8.89 5.3e-14 ***
                                     4.57 1.6e-05 ***
## vol
                0.0624
                           0.0137
## BPH
                0.0927
                           0.0263
                                     3.53 0.00066 ***
## invasion1
                0.6965
                           0.2384
                                     2.92 0.00439 **
## Gleason7
                0.2603
                                     1.42 0.15790
                           0.1828
## Gleason8
                0.7055
                           0.2571
                                     2.74 0.00732 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.764 on 91 degrees of freedom
## Multiple R-squared: 0.585, Adjusted R-squared: 0.562
## F-statistic: 25.6 on 5 and 91 DF, p-value: 4.72e-16
# prediction
new_data <- data.frame(vol = 0.42, BPH = 1.8, invasion = "1", Gleason = "6")
predict(fit1, new_data)
##
```

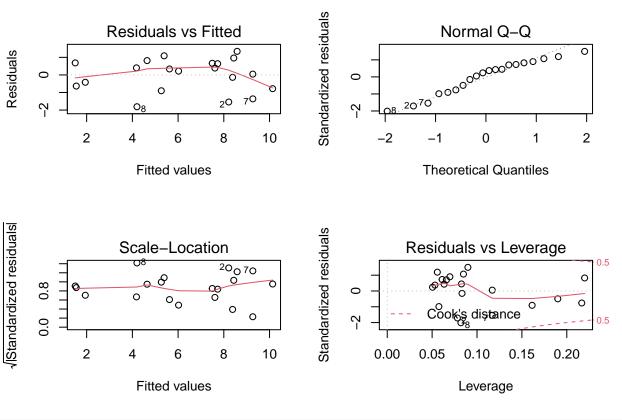
2.2776

Model Diagnostics

For detailed information, read this article on STHDA: http://sthda.com/english/articles/39-regression-model-diagnostics/161-linear-regression-assumptions-and-diagnostics-in-r-essentials/

Let's evaluate the diagnostic plots for the initial simple linear regression model fit_simple:

```
par(mfrow = c(2, 2))
plot(fit_simple)
```



par(mfrow = c(1, 1))

Residuals vs Fitted

Used to check the linear relationship assumptions. A horizontal line, without distinct patterns is an indication for a linear relationship. In this case, there is a slight deviation, which is an issue.

Normal Q-Q

Used to examine whether the residuals are normally distributed.

Scale-Location (or Spread-Location)

Used to check the homogeneity of variance of the residuals (homoscedasticity). Horizontal line with equally spread points is a good indication of homoscedasticity. In this case, there seems to be a heteroscedasticity issue.

Residuals vs. Leverage

Used to identify influential cases, that is extreme values that might influence the regression results when included or excluded from the analysis

- Standardized residual: the residual divided by its estimated standard error. Standardized residuals can be interpreted as the number of standard errors away from the regression line. Observations whose standardized residuals are greater than 3 in absolute value are possible outliers
- Leverage: A data point has high leverage, if it has extreme predictor x values

Outlying values are generally located at the upper right corner or at the lower right corner. Those spots are the places where data points can be influential against a regression line.

Cook's Distance

This metric defines influence as a combination of leverage and residual size .

plot(fit_simple, 4)

