

Biostatistics Week I

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ACIBADEM
MEHMET ALİ AYDINLAR
ÜNİVERSİTESİ

Statistics

- A discipline concerned with
 - **Collecting data** for a certain purpose
 - **Analysis** of the collected data
 - **Reaching conclusions** based on the analysis

Statistics

Collection

Organization

Analysis

Interpretation

Presentation

Biotatistics

- Does a novel drug affect survival in pancreatic cancer?
- Which mutation is most likely the cause of an inherited disease?
- Can health status of advanced AIDS patients be improved by a novel treatment?

Descriptive/Inferential Statistics

- Descriptive Statistics
 - Organization of collected data, calculation of mean and dispersion, presentation as tables, graphics, etc.
- Inferential Statistics
 - Building hypothesis concerning the population based on sample findings, hypothesis testing, interpretation.

Population vs. Sample

- Population

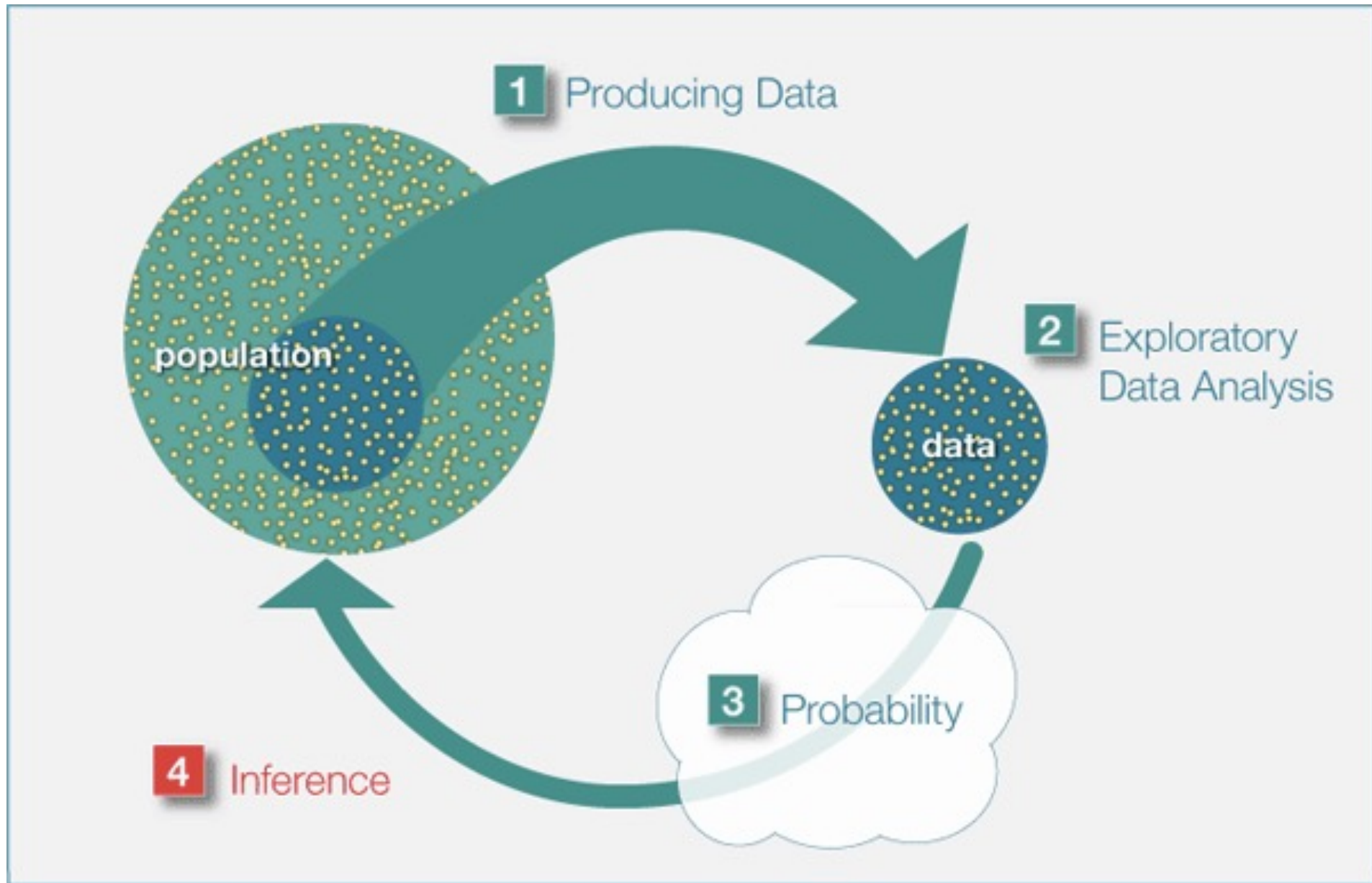
- All subjects under consideration that have the same properties
 - E.g., everyone living in Istanbul
- N** = 15.52 million (as of 31 Dec 2019)

- Sample

- A proportion of the population (ideally randomly selected)
 - E.g., **n** = 500, 1000, 5000, ...
- (n might be decided based on sample size calculations)

Terminology/Notation

	Sample Statistic	Population Parameter
Size	n	N
Mean	$\bar{x} = \frac{\sum x}{n}$	$\mu = \frac{\sum X}{N}$
Variance	$s^2 = \frac{\sum (x - \bar{x})^2}{n-1}$	$\sigma^2 = \frac{\sum (X - \mu)^2}{N}$
Standard Deviation	$s = \sqrt{s^2}$	$\sigma = \sqrt{\sigma^2}$
Proportion	$\hat{p} = \frac{n \text{ of successes}}{n \text{ of trials}}$	$p = \frac{N \text{ of successes}}{N \text{ of trials}}$



Data/Variable

- Items of information, often numeric, that are collected through observation
 - Age
 - Gender
 - Ethnicity
 - Systolic blood pressure
 - Treatment type
 - ...

Example Study

- Main question
 - Can the health status of advanced AIDS patients be improved by a novel drug treatment?
- Sub-questions
 - Are there differences between treatments in terms of health benefits?
 - Do health benefits differ with respect to gender?
 - Do health benefits differ with respect to age?

Example Study (cont.)

- Randomized clinical trial
- 1178 patients
 - 289, 288, 293, and 308 patients per treatment arm
- Data collection at baseline (week = 0)
- 5 more follow-ups with 8-week intervals

Example Study (cont.)

- Variables
 - Identification number
 - Treatment arm
 - Age
 - Gender
 - CD4 cell count at each follow-up
 - Time of follow-up (in weeks since baseline)

Example Study (cont.)

First 5 patients' data, out of 1,178 (only for the first two weeks)

id	treatment	age	gender	week_1	cd4_1	week_2	cd4_2
1	trt2	36.43	male	0	22	7.57	20
2	trt4	47.85	male	0	21	8.00	48
4	trt3	36.60	male	0	61	7.14	60
5	trt1	35.95	male	0	35	8.00	30
6	trt2	38.40	male	0	10	7.29	10

«Clean» Data

country	year	cases	population
Afghanistan	1999	7745	19987071
Afghanistan	2000	8666	20595360
Brazil	1999	37737	172006362
Brazil	2000	80488	174504898
China	1999	212258	1272915272
China	2000	213766	1280425583

variables

country	year	cases	population
Afghanistan	1999	7745	19987071
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Brazil	1999	37737	172006362
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observations

country	year	cases	population
Afghanistan	99	7745	19987071
Afghanistan	00	8666	20595360
Brazil	99	37737	172006362
Brazil	00	80488	174504898
China	99	212258	1272915272
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values

Variable Types

- **Discrete/Categorical/Qualitative**
 - Measured in a discrete manner
 - **Nominal**: no natural ordering. E.g., eye color, zip-code
 - **Dichotomous/binary**: only takes two values. E.g., dead/alive, female/male
 - **Ordinal**: natural ordering. E.g., agree/neutral/disagree, bad/fair/good
 - **Count**: counted values. E.g., number of tumor occurrences in one month

Variable Types

- **Continuous/Quantitative**
 - Measured in a continuous manner
 - **Interval:** real number (+/- including 0). E.g., temperature, location
 - **Ratio:** positive values (**0 indicates none**). E.g., height, age, daily calcium consumption (mg).

Example Study (cont.)

id	treatment	age	gender	week_1	cd4_1	week_2	cd4_2
1	trt2	36.43	male	0	22	7.57	20
2	trt4	47.85	male	0	21	8.00	48
4	trt3	36.60	male	0	61	7.14	60
5	trt1	35.95	male	0	35	8.00	30
6	trt2	38.40	male	0	10	7.29	10

Discrete - nominal

Contin.-
ratio

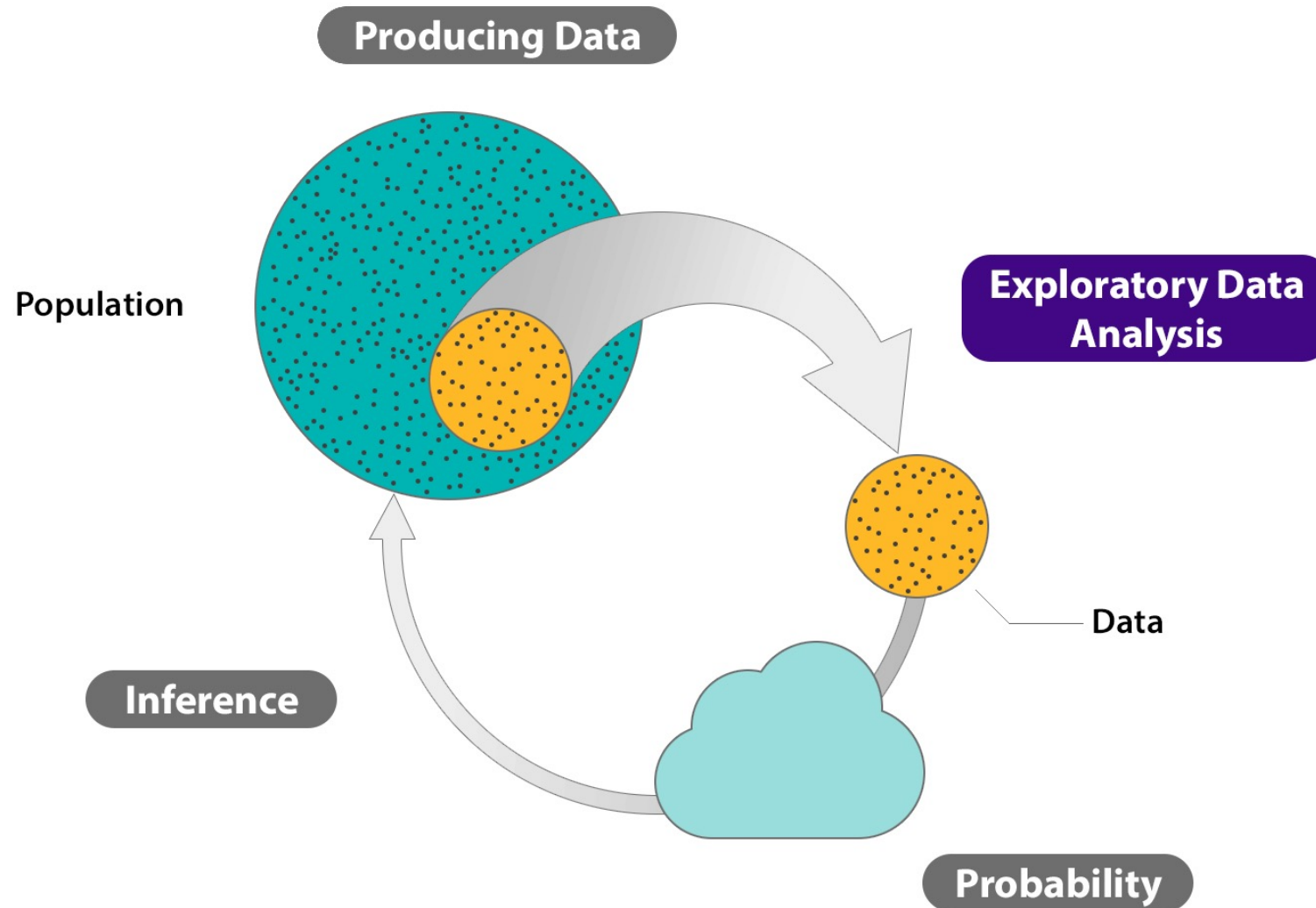
Discrete –
nominal
/binary

Discrete - count
Contin. - ratio

Same variable – different classifications

1. Time after study entry
0, 1.2, 2.5, 3.1, 4.6, 5.2, 6.6, 7.1, 8 weeks
Continuous - ratio
2. Time after study entry
< 4 weeks, ≥ 4 weeks
Categorical - binary
3. Time after study entry
< 2 weeks, ≥ 2 and < 4 weeks, ≥ 4 weeks
Categorical - ordinal
4. Time after study entry
-4.6, -3.4, -2.1, -1.5, 0, 0.6, 2, 2.5, 3.4 weeks
Continuous - interval

The Big Picture



Exploratory Data Analysis (EDA)

- Examining Distributions — exploring data **one variable at a time**.
- Examining Relationships — exploring data **two variables at a time**.

Frequency Tables – Categorical Variable

- Eye colors of 10 individuals:
blue, green, brown, blue, brown, blue, blue, green, brown, brown

Frequency Tables – Categorical Variable

- Eye colors of 10 individuals:
blue, green, brown, blue, brown, blue, blue, green, brown, brown

Eye Color	Frequency
Blue	4
Brown	4
Green	2

Frequency Tables – Categorical Variable

- Eye colors of 10 individuals:
blue, green, brown, blue, brown, blue, blue, green, brown, brown

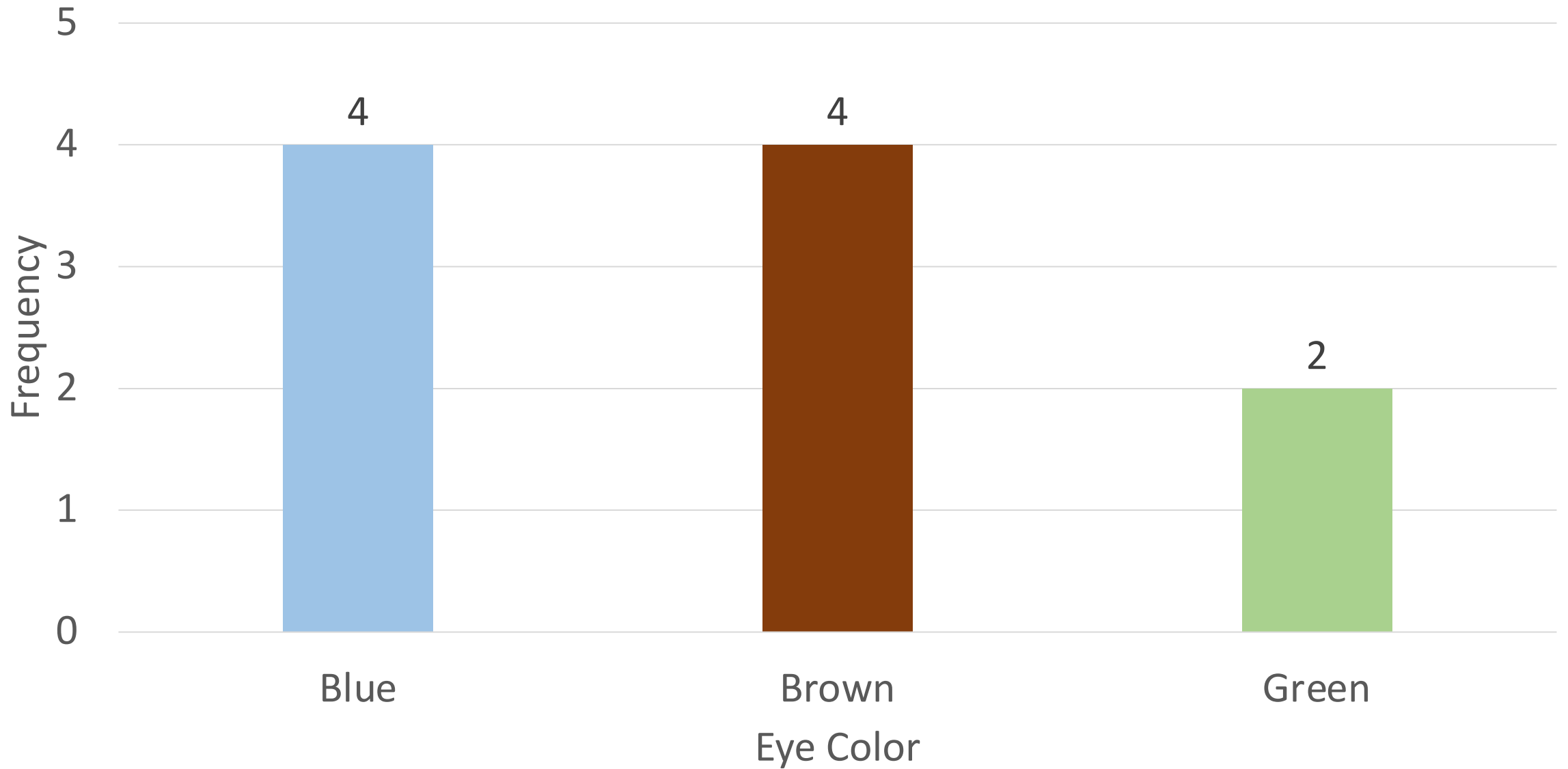
Eye Color	Frequency	Relative Freq.
Blue	4	$4/10 = 0.4$
Brown	4	$4/10 = 0.4$
Green	2	$2/10 = 0.2$

Frequency Tables – Categorical Variable

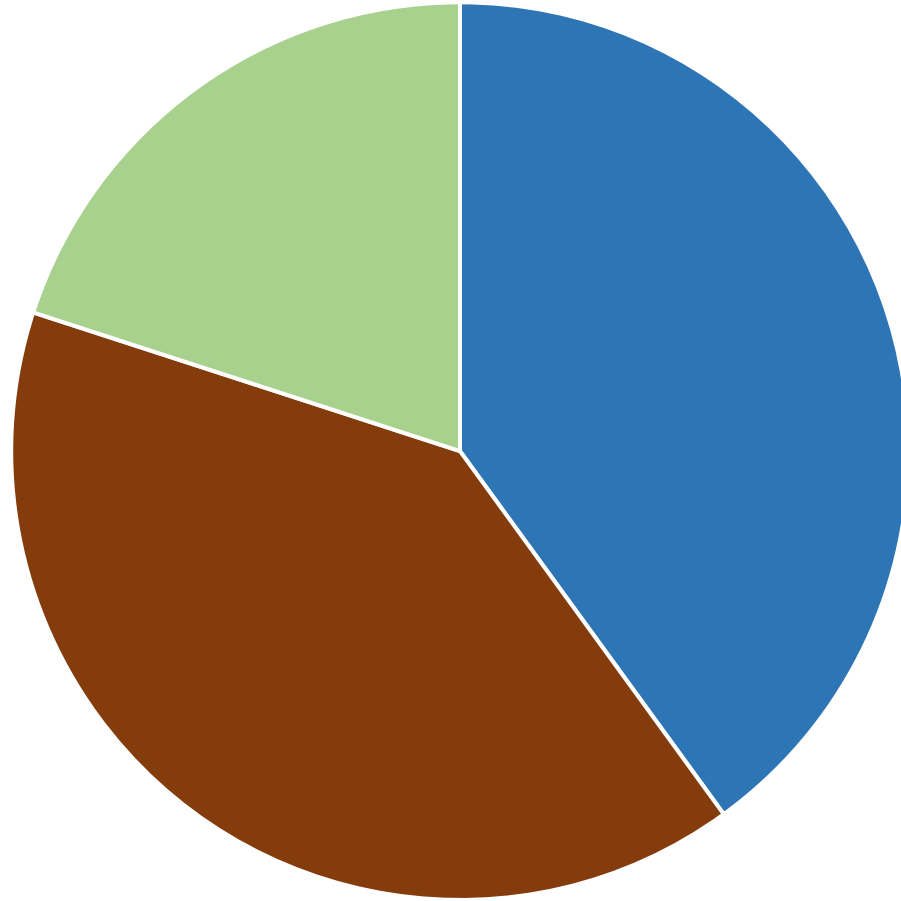
- Eye colors of 10 individuals:
blue, green, brown, blue, brown, blue, blue, green, brown, brown

Eye Color	Frequency	Relative Freq.	%
Blue	4	$4/10 = 0.4$	40
Brown	4	$4/10 = 0.4$	40
Green	2	$2/10 = 0.2$	20

Bar Chart of Eye Color Frequencies



Do not use pie charts!



Contingency table/Cross tabulation/Crosstab

- Tables in which two categorical variables are investigated together

	Male	Female
No education	4	10
Primary school	3	5
High school	2	8
Bachelor's degree	7	9

Frequency Tables – Continuous Variable

Cholesterol levels of 40 patients:

Original data

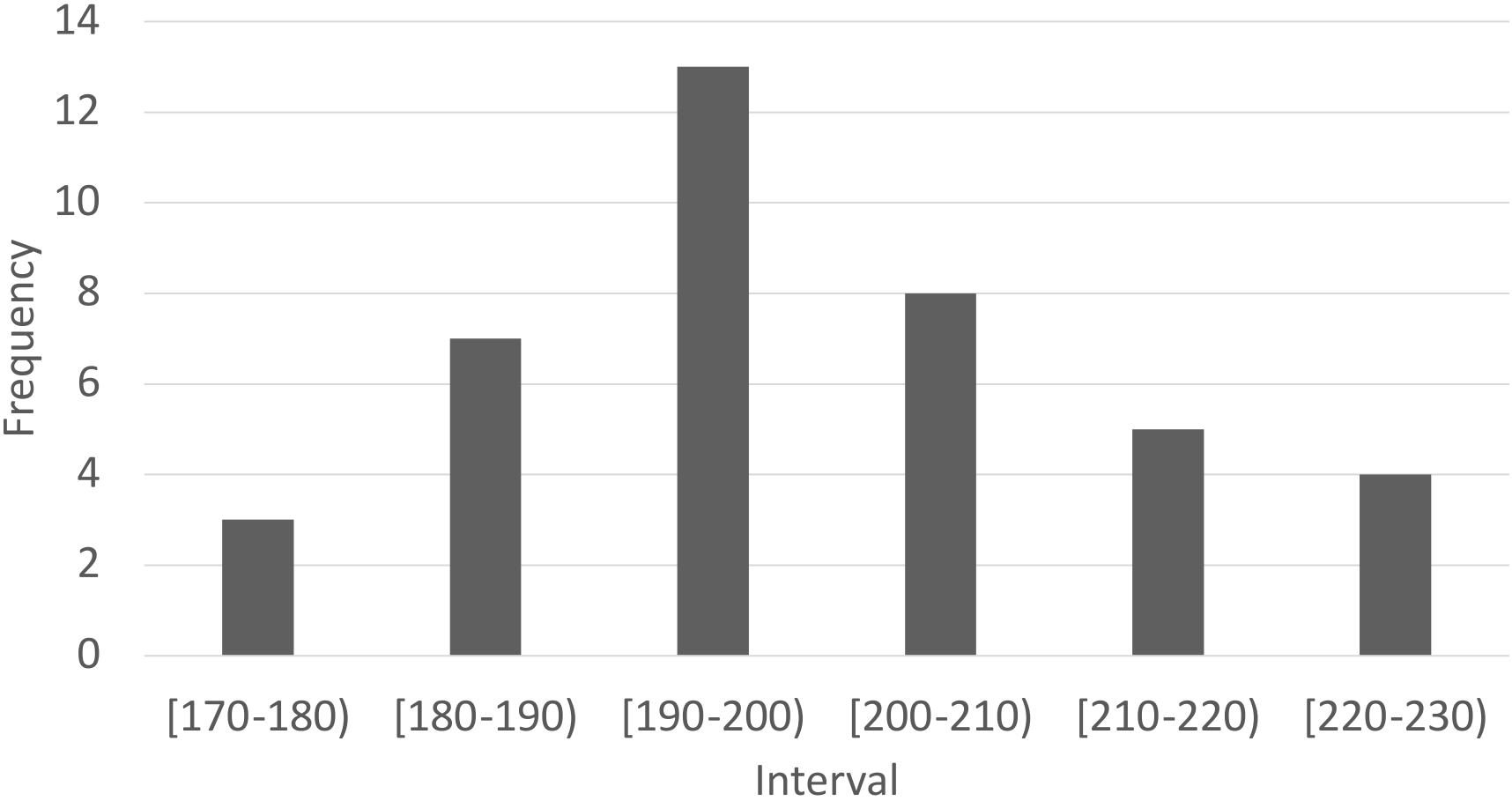
213, 174, 193, 196, 220, 183, 194, 200, 192, 200, 200, 199, 178, 183, 188, 193,
187, 181, 193, 205, 196, 211, 202, 213, 216, 206, 195, 191, 171, 194, 184, 191,
221, 212, 221, 204, 204, 191, 183, 227

Sorted data

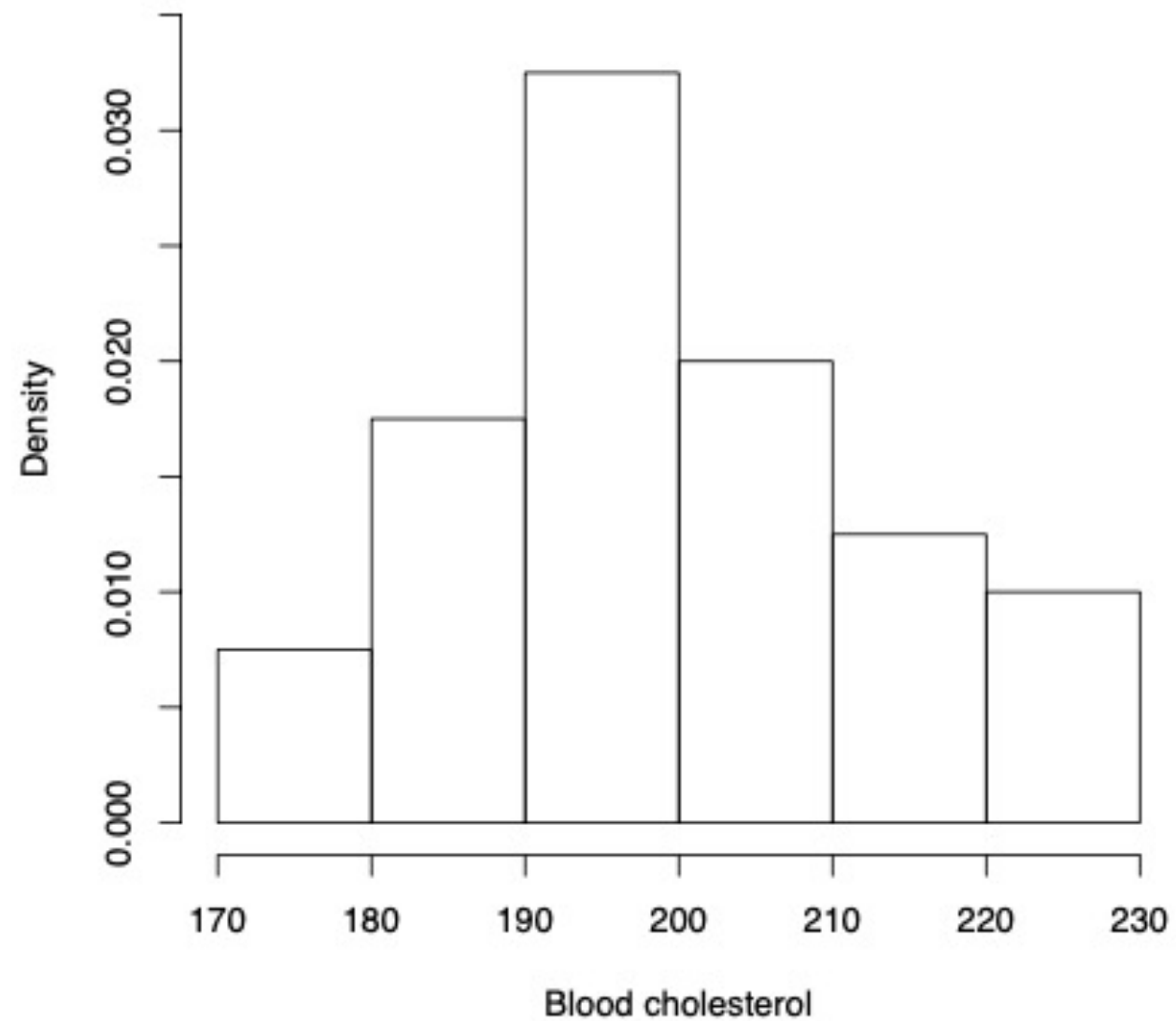
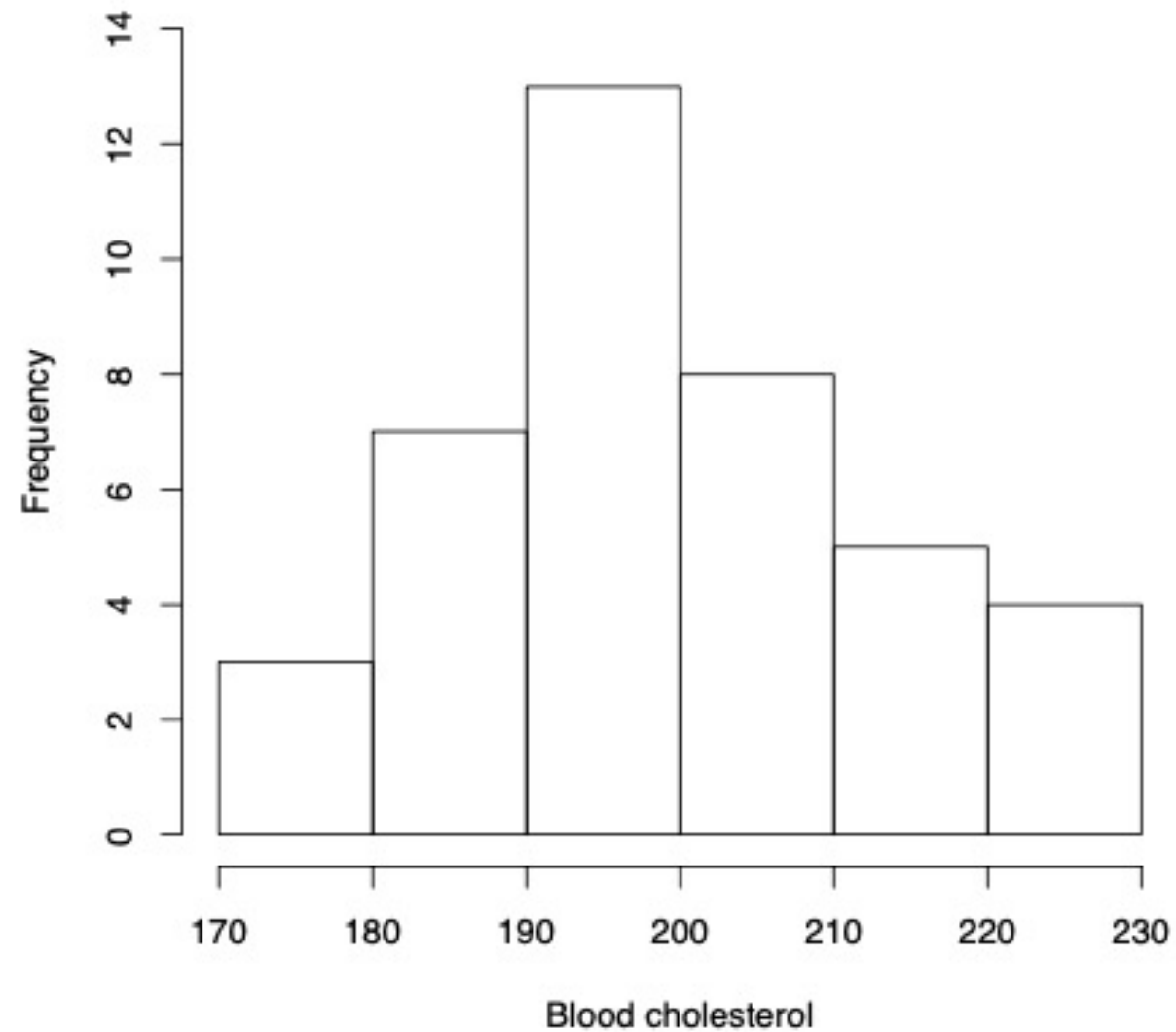
171, 174, 178, 181, 183, 183, 183, 184, 187, 188, 191, 191, 191, 192, 193, 193,
193, 194, 194, 195, 196, 196, 199, 200, 200, 200, 202, 204, 204, 205, 206, 211,
212, 213, 213, 216, 220, 221, 221, 227

Interval	Frequency	Relative Freq.	%
[170-180)	3	$3/40 = 0.075$	7.5
[180-190)	7	$7/40 = 0.175$	17.5
[190-200)	13	$13/40 = 0.325$	32.5
[200-210)	8	$8/40 = 0.200$	20.0
[210-220)	5	$5/40 = 0.125$	12.5
[220-230)	4	$4/40 = 0.100$	10.0

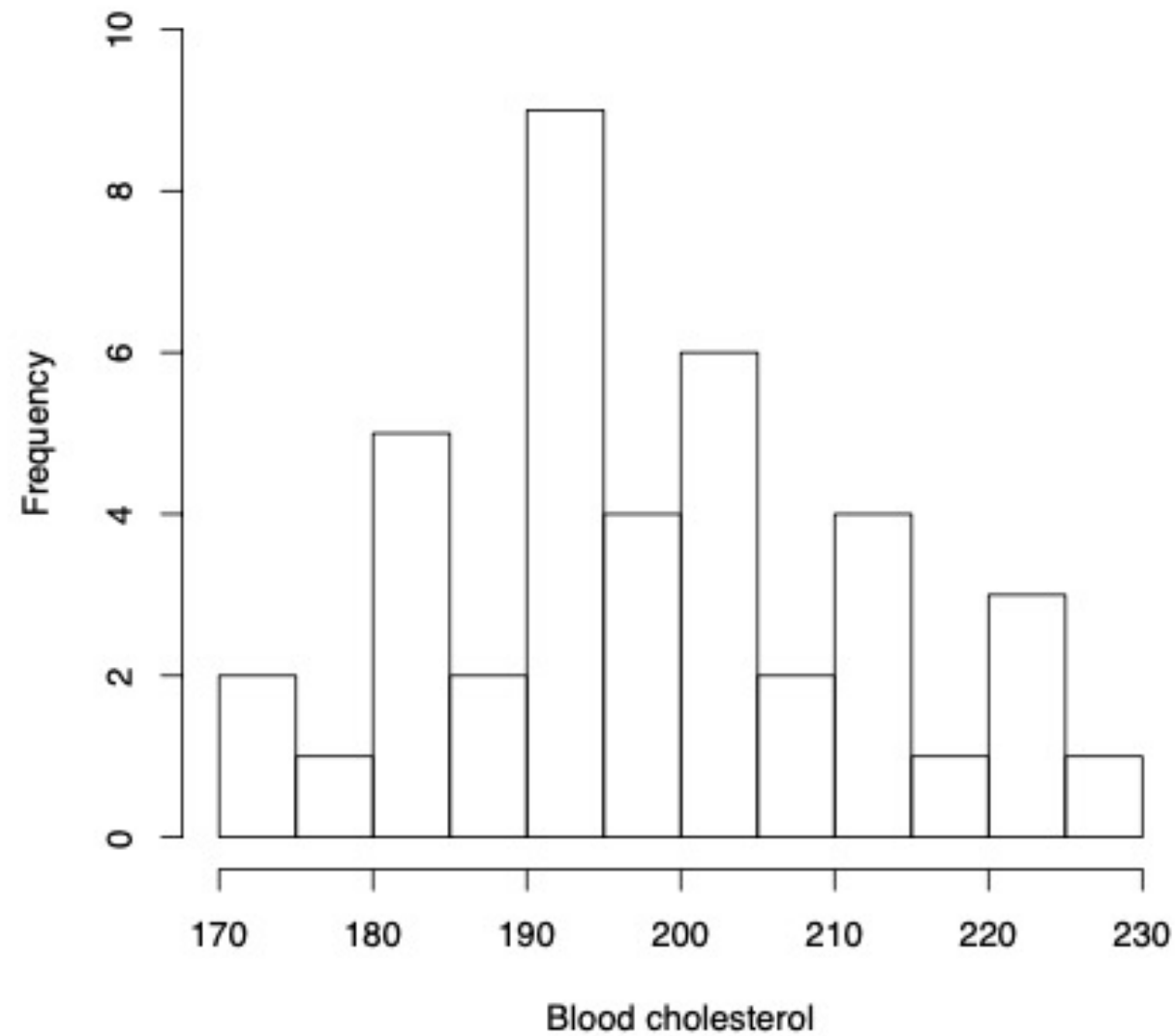
Bar Chart of Cholesterol Levels



Histogram



Histogram



Histogram

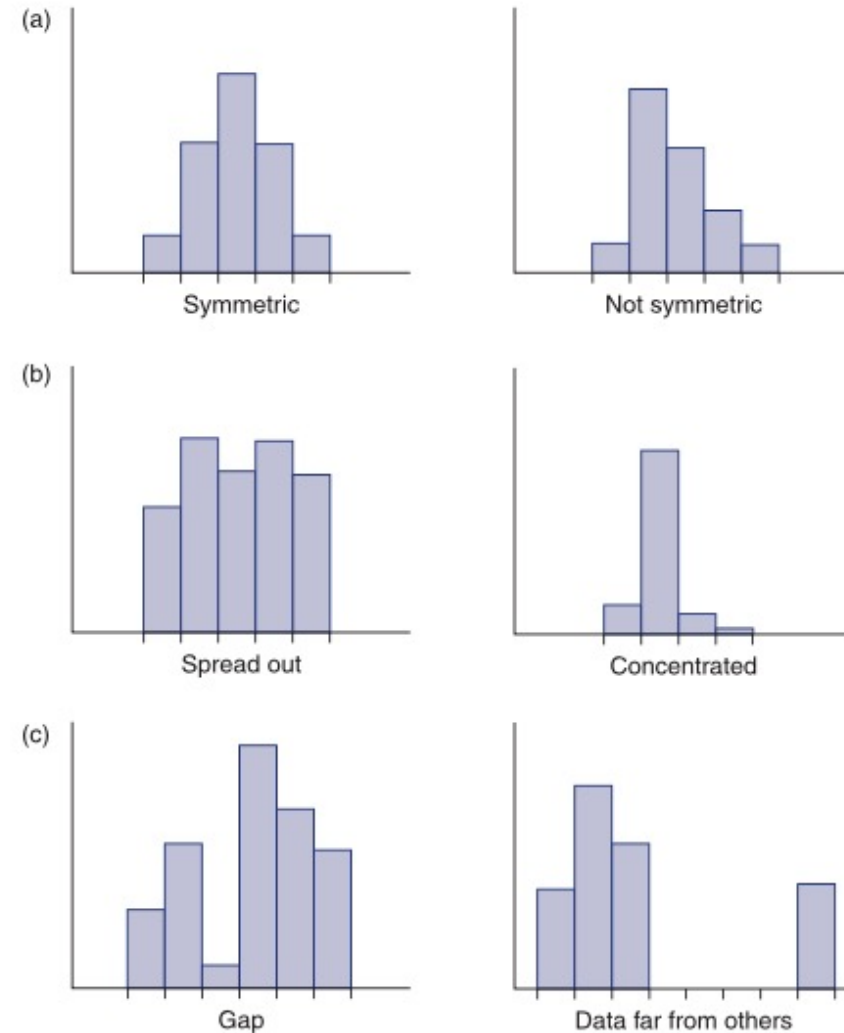


FIGURE 2.8

Characteristics of data detected by histograms. (a) symmetry, (b) degree of spread and where values are concentrated, and (c) gaps in data and data far from others.

Table 2.9 Class Frequencies of Systolic Blood Pressure of Two Groups of Male Workers

Blood pressure	Number of workers	
	Aged 30–40	Aged 50–60
Less than 90	3	1
90–100	17	2
100–110	118	23
110–120	460	57
120–130	768	122
130–140	675	149
140–150	312	167
150–160	120	73
160–170	45	62
170–180	18	35
180–190	3	20
190–200	1	9
200–210		3
210–220		5
220–230		2
230–240		1
Total	2540	731

Table 2.10 Relative Class Frequencies of Blood Pressures

Blood pressure	Percentage of workers	
	Aged 30–40	Aged 50–60
Less than 90	0.12	0.14
90–100	0.67	0.27
100–110	4.65	3.15
110–120	18.11	7.80
120–130	30.24	16.69
130–140	26.57	20.38
140–150	12.28	22.84
150–160	4.72	9.99
160–170	1.77	8.48
170–180	0.71	4.79
180–190	0.12	2.74
190–200	0.04	1.23
200–210		0.41
210–220		0.68
220–230		0.27
230–240		0.14
Total	100.00	100.00

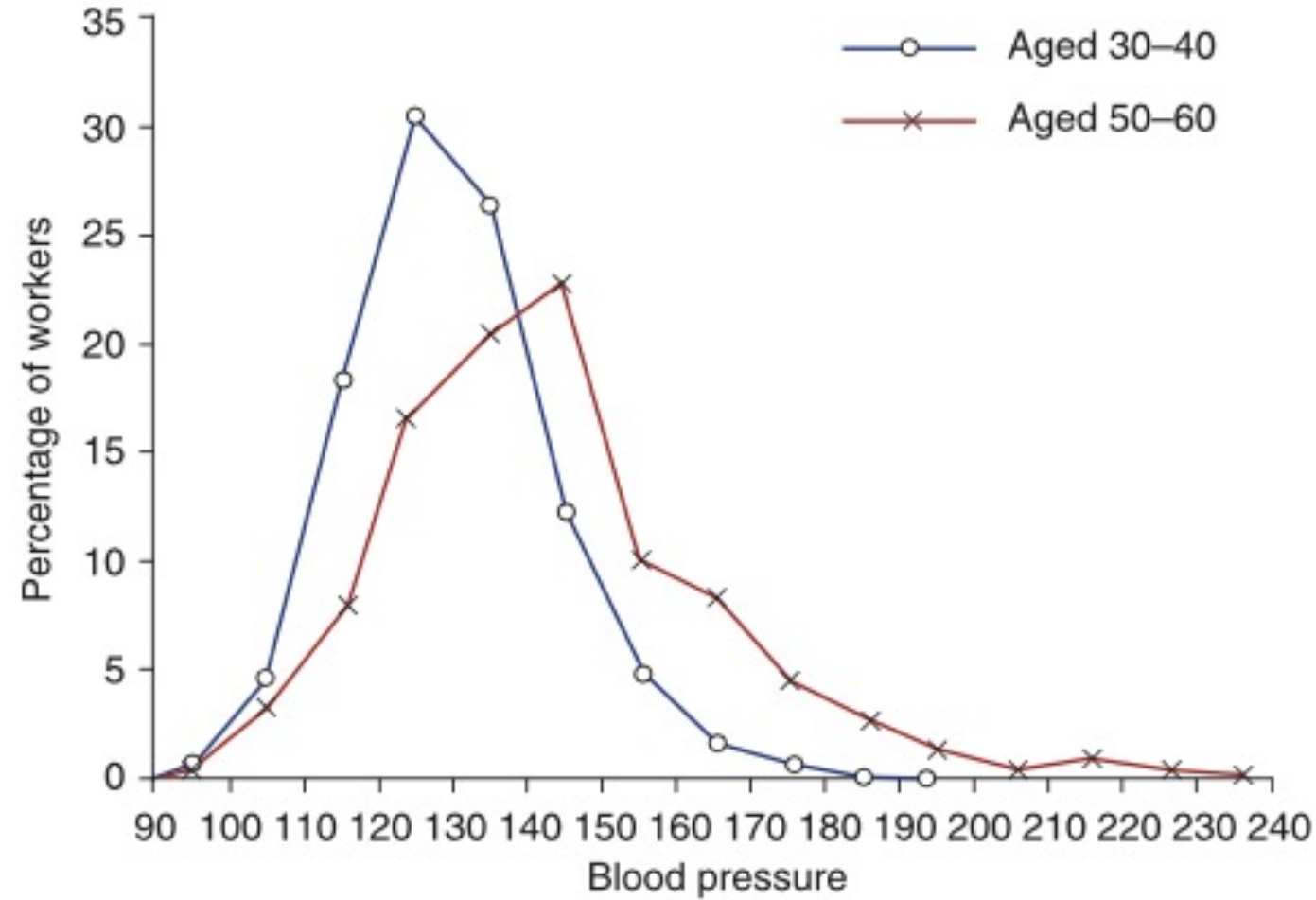


FIGURE 2.10

Relative frequency polygons for the data of Table 2.10.

Brief Summary

- Statistics is a discipline concerned with collection, organization, analysis and interpretation of data
- The aim is to infer information regarding the population using sample data
- There are two kinds of variables:
 - Categorical – nominal, binary, ordinal, count
 - Continuous – interval, ratio
- We may summarize a categorical variable using frequency, relative frequency and/or percentage tables
- We may visually display a categorical variable using bar charts, etc.