

# Fast Obstacle k-Nearest Neighbour Query on Navigation Mesh

## Final Presentation

Shizhe Zhao (27505928)

Supervisors: David Taniar, Daniel Harabor



# Outline

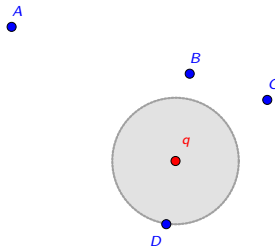
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- 2 Related works
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# Traditional k-Nearest Neighbor

k-Nearest Neighbor:

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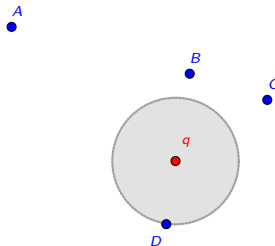


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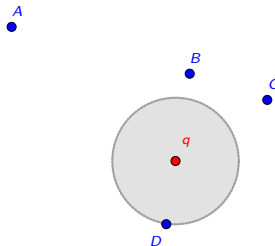


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(e.g.  $\{A, B, C, D\}$ )

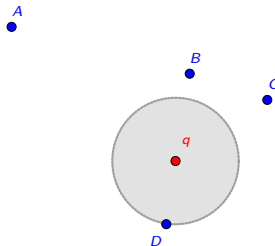


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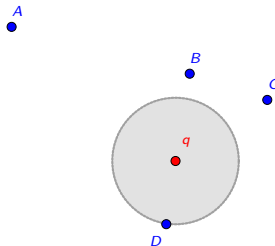
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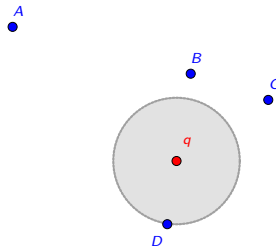
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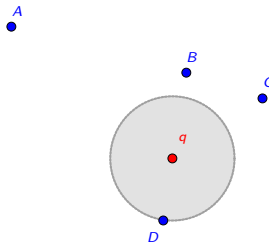
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  - top  $k$  nearest targets regarding *Euclidean distance*  $d_e$
- the circle indicates that  $D$  is the nearest neighbor of  $q$





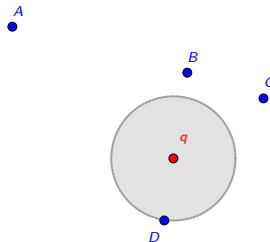
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- traditional kNN has been well studied.
- when take obstacles into consideration...
- metric: Obstacle distance  $d_o$



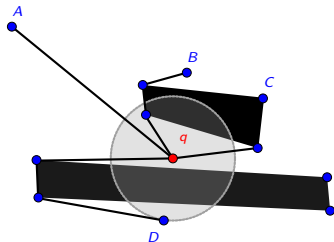
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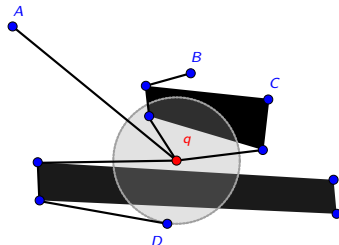
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# Application Scenario

In an industrial warehouse,  
 $q$  is a robot.  
It's interested in the closest storage  
locations,  
but it can not cross obstacles



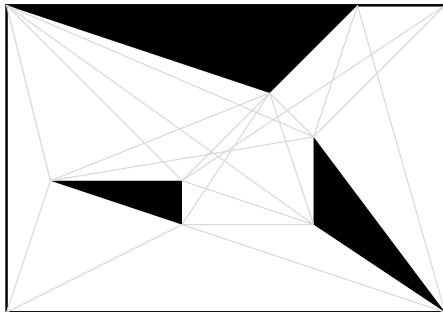
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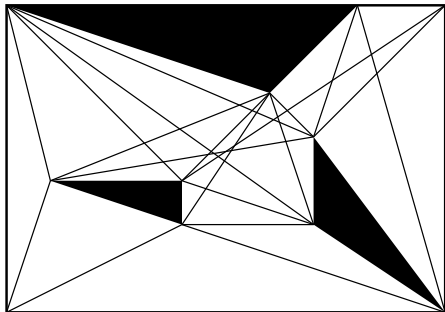
# How to compute Obstacle Distance

- Existing works rely on *visibility graph* (VG)
  - any pair of visible points has an edge
- Run shortest path algorithm on VG (e.g. *Dijkstra*)
- Number of edge: up to  $O(V^2)$   
( $V$ : the number of vertex)



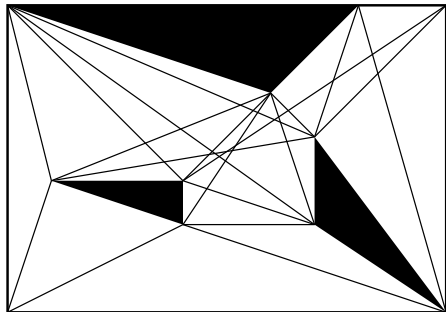
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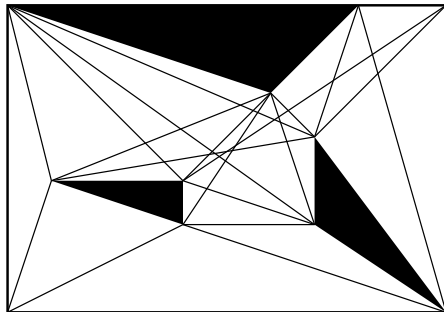
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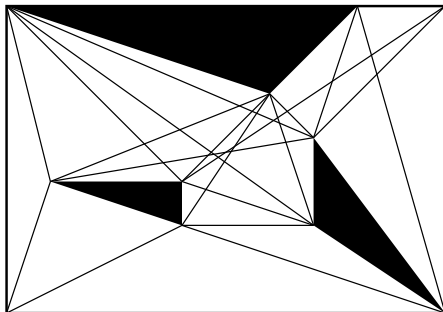
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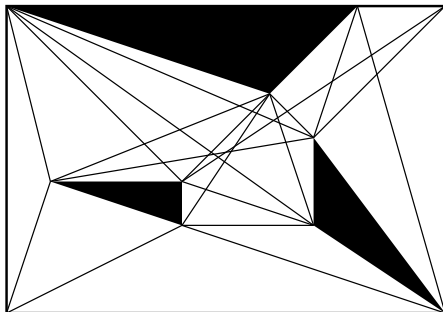
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- Motivation: only consider query related area
- *Zhang, EDBT 2004: Local Visibility Graph (LVG)*



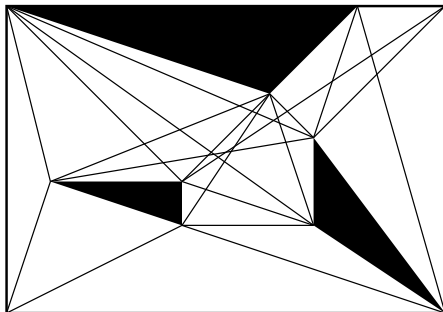
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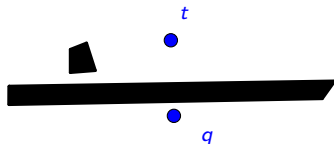
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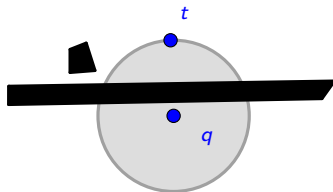
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- Given:  $q, t$
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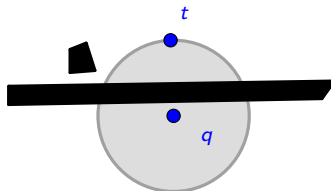
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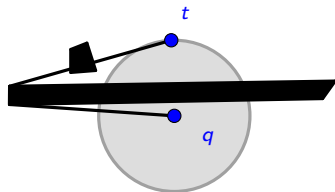
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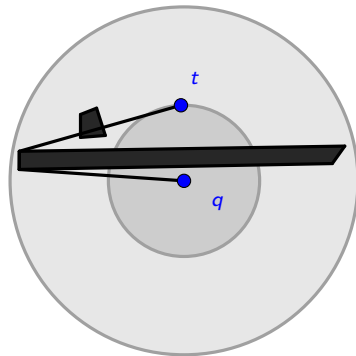
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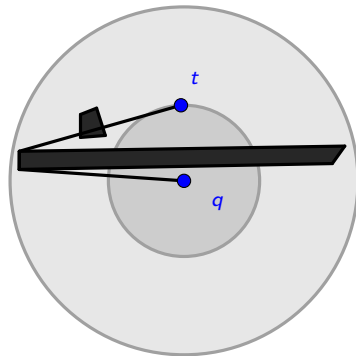
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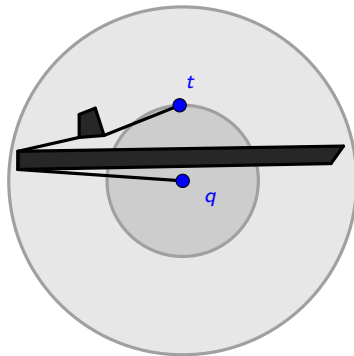
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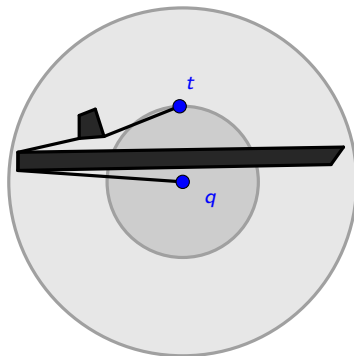
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- However ...



# Disadvantages

It has some disadvantages:

- Costly online visibility checking
- An incremental construction can easily reach to  $O(V^2)$  edges
- Duplicated effort:  
the VG is discarded each time the  $q$  changes



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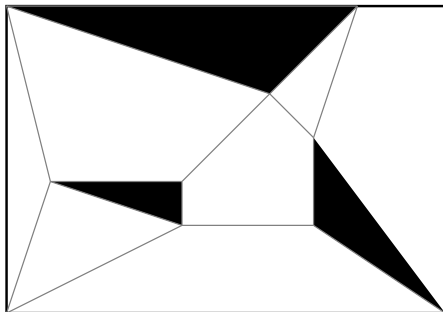
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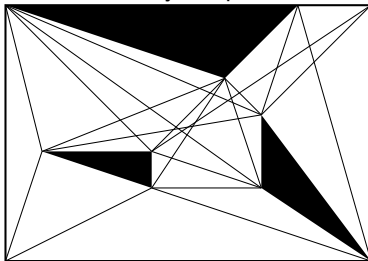
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- traversable space  $\Rightarrow$  convex polygons

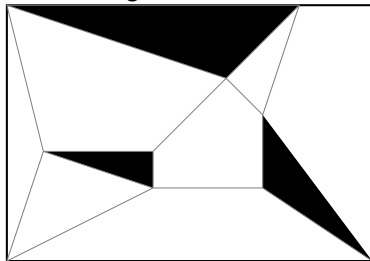


# Advantage

Visibility Graph

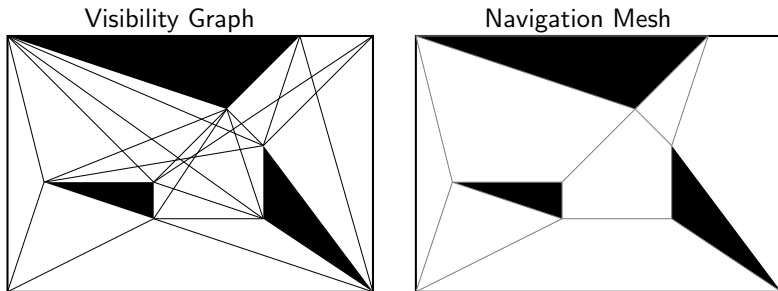


Navigation Mesh





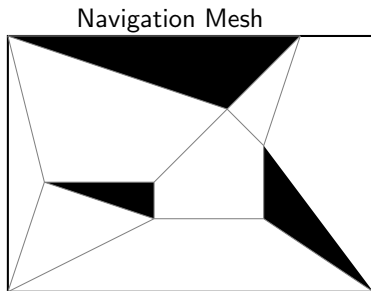
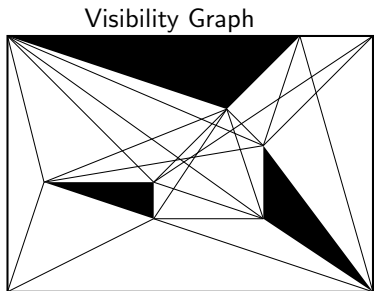
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We can easily preprocess the entire map!



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How to compute obstacle distance on a navigation mesh?



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- But a recent work in 2017: *Polyanya*
  - fast, optimal, flexible
  - a new direction for Obstacle kNN query



# What's the *Polyanya*?

- Given:
  - a map with polygonal obstacles
  - $q$ : query point
  - $t$ : target
  - a precomputed navigation mesh
  - convex polygon: all inside points are visible
- find the shortest path along meshes

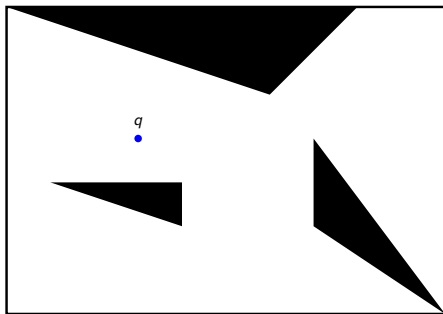


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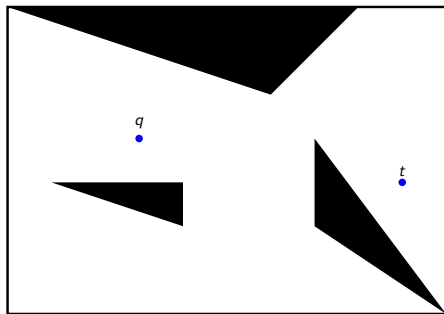


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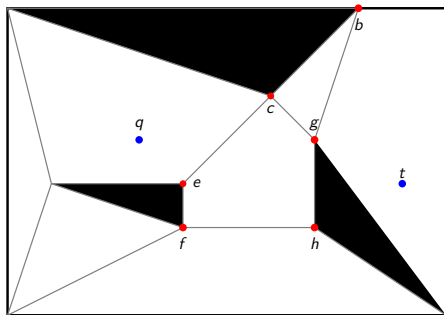
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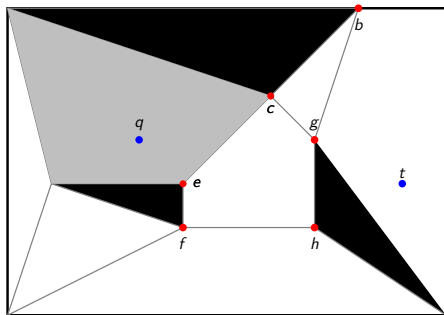


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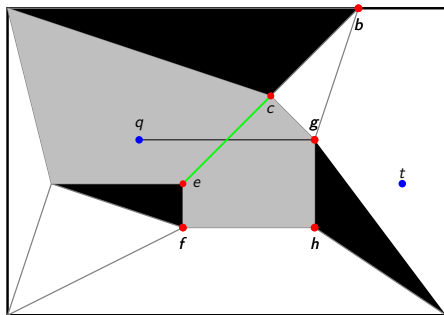
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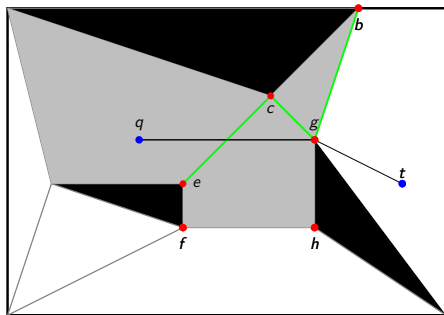


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*Polyanya* is an  $A^*$  like algorithm, it has three components

- 1 Search Node
- 2 Successors
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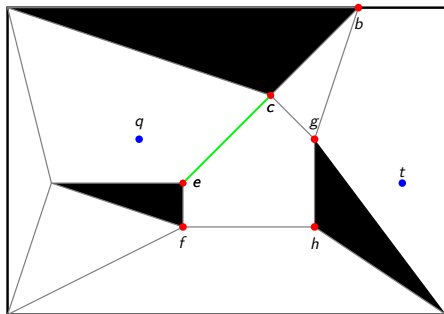
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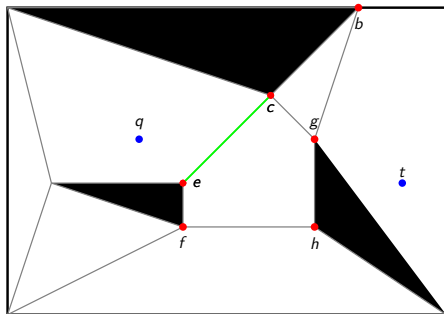
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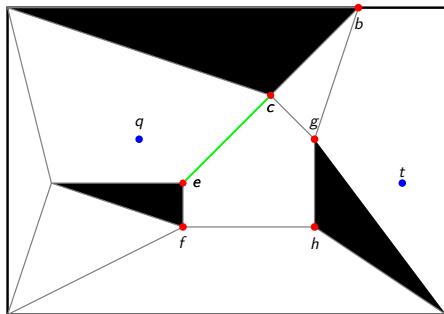
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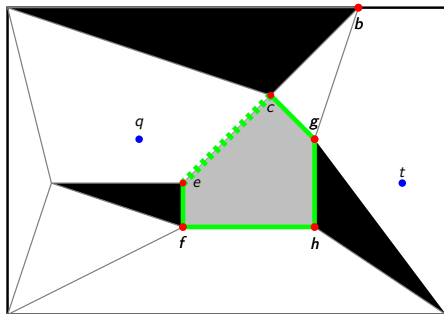
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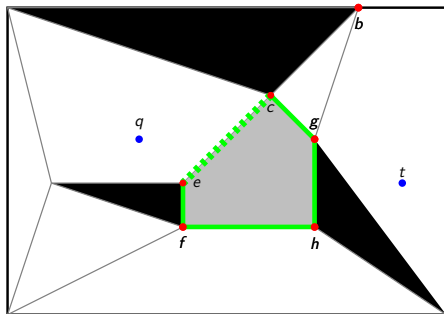
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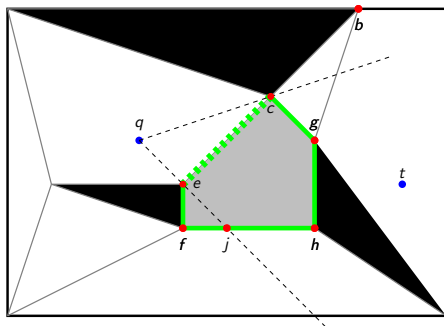
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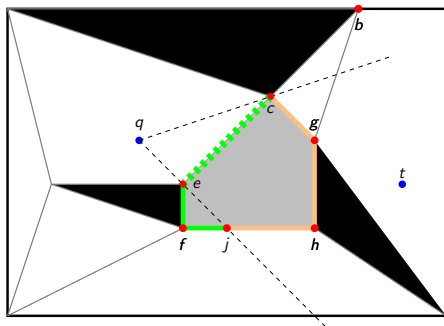
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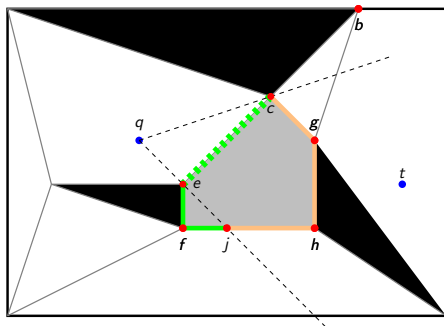
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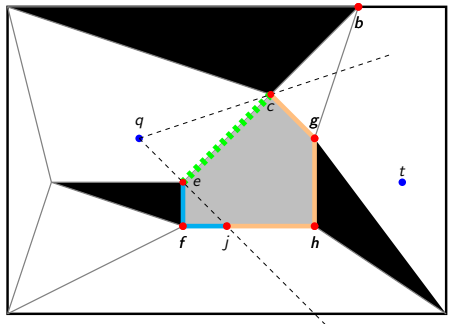
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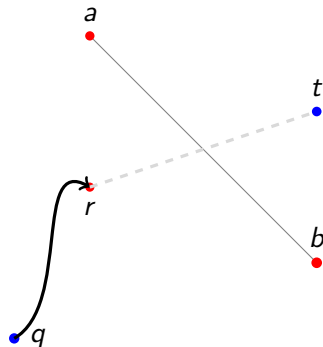
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# Polyanya: Evaluation Function

Evaluation function of a search node  $(r, l)$  has:

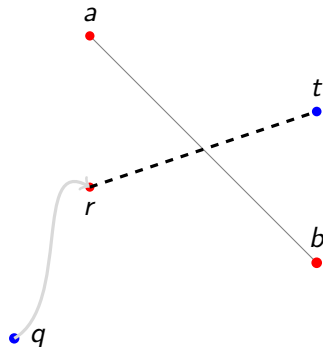
- *g-value*:  
 $|shortestPath(q, r)|$   
 (certain)
- *h-value*:  $r$  to  $t$  cross  $l$   
 (underestimation)
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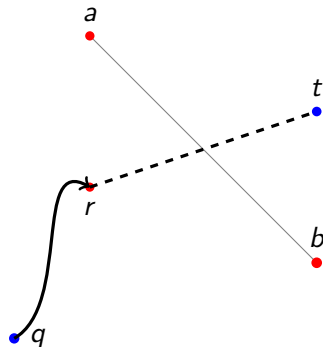
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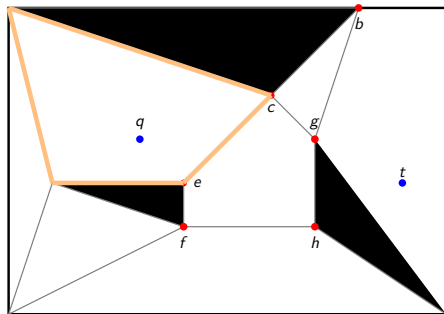
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# Polyanya: Example

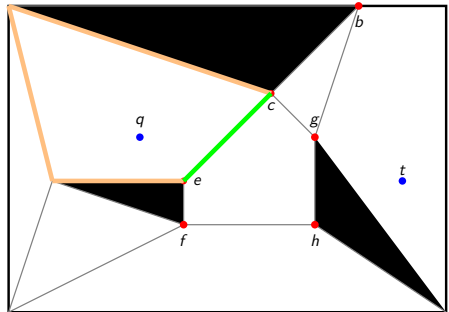
Initial Search Nodes are edges of mesh that contains the  $q$ .





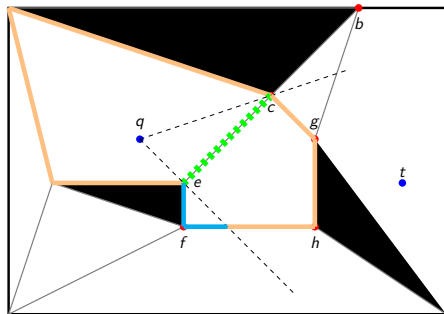
# Polyanya: Example

Search Node  $(q, [e, c])$  has the best estimation, so popped out



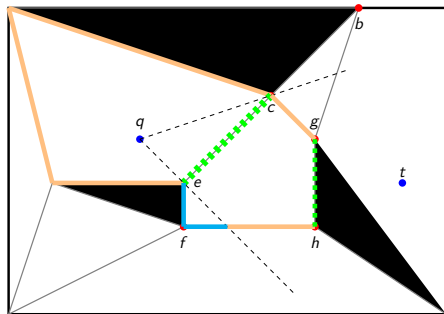
# Polyanya: Example

Expand successors in adjacent mesh.



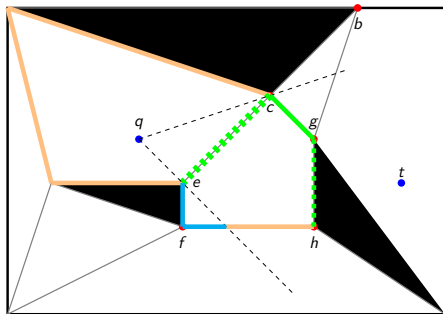
# Polyanya: Example

Pop  $(q, [g, h])$ ,  
adjacent to obstacle,  
so we discard it.



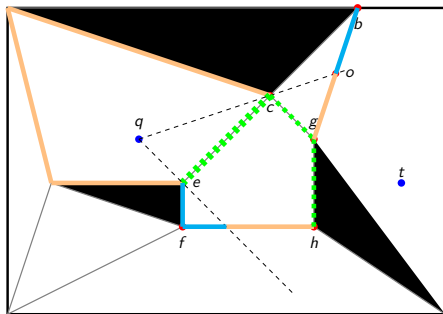
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$\text{Pop}(q, [c, g]).$



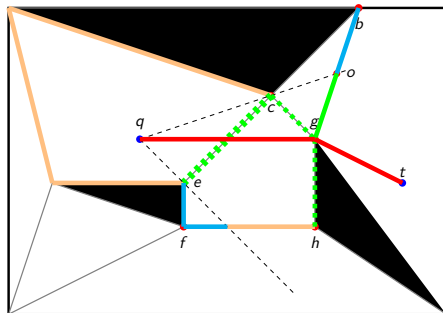
# Polyanya: Example

Expand successors.



## Polyanya: Example

Pop ( $q, [g, o]$ ),  
the adjacent mesh contains  $t$ .  
**We've found the shortest path!**



# Outline

- 1 Introduction
- 2 Related works
- 3 Challenges
- 4 New Framework
- 5 My research**
- 6 Experiments
- 7 Conclusion and future work
- 8 End



# My Research

- *Polyanya* only work for single pair shortest path
- My research:
  - multi-targets search based on framework of *Polyanya*
  - with good scalability





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# Proposed algorithm 1: brute-force *Polyanya*

A naive solution is calling *Polyanya* for each target:

```
for t in targets:  
    polyanya.run(q, t)
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- Drawback: inefficient when targets many.



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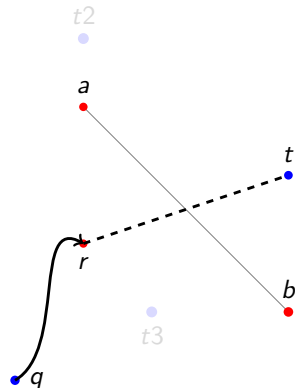
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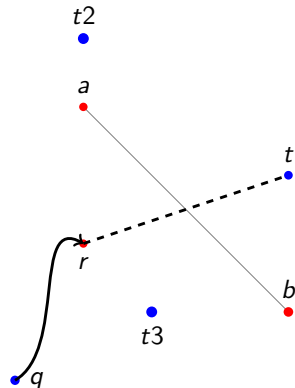
# Proposed algorithm 2: interval heuristic

- Let's review the evaluation function in *Polyanya*
- When there are multiple targets...
  - *h-value* shouldn't be affected by a specific target
- How about remove  $t$  from *h-value*?



# Proposed algorithm 2: interval heuristic

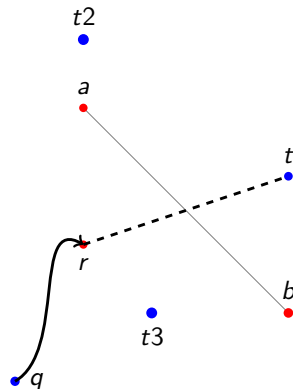
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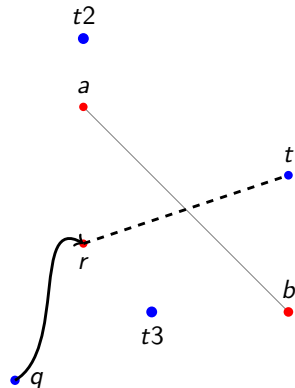
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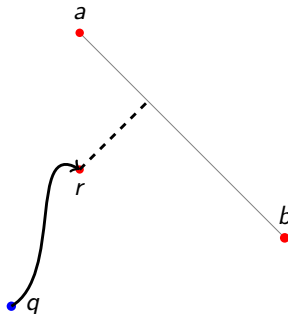
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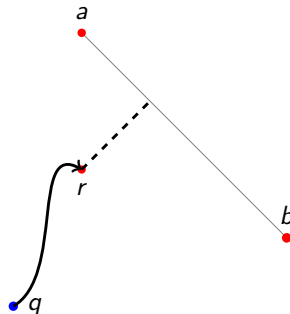
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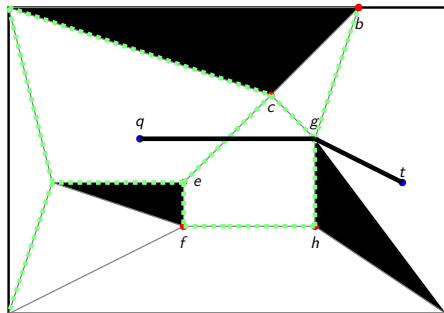
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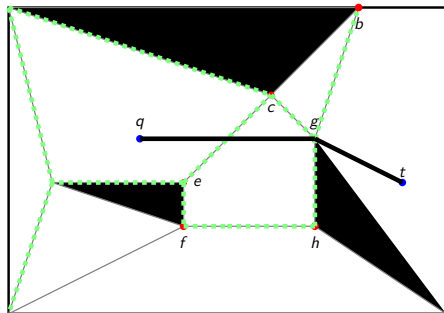
# Interval heuristic: drawback

- *interval heuristic* causes redundant expansions
- especially in sparse targets scenario
- e.g.: query is "nearest storage locations where capacity  $\geq 100$ ".
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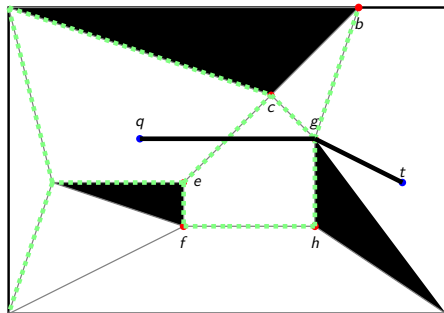
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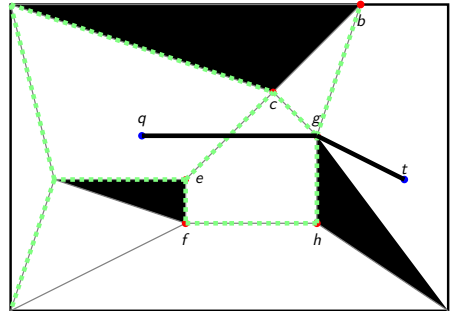
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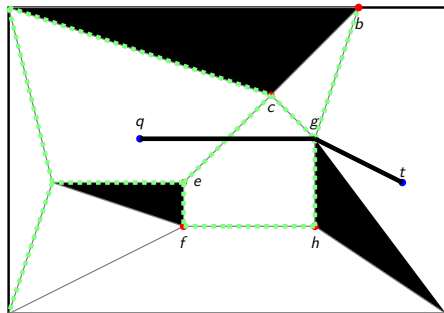
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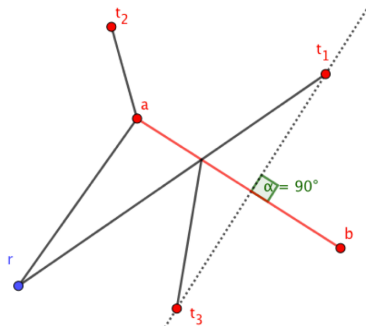
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 $h_p(\text{node}, t)$  equals:

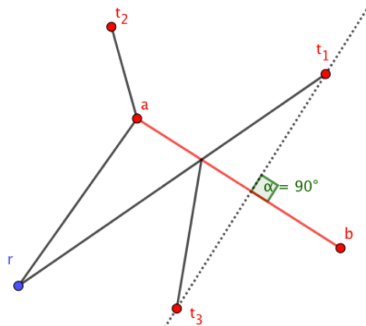
- Case 1:  $d_e(r, t_1)$
- Case 2:  $d_e(r, a) + d_e(a, t_2)$
- Case 3: when  $r$  and  $t_3$  at same side, compute mirror point of  $t_3$ , and go to Case 1 or Case 2



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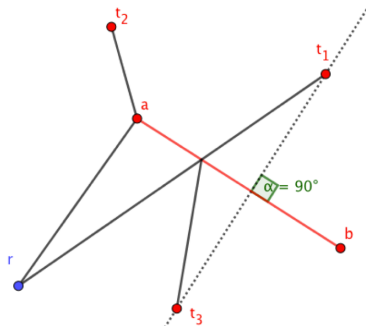
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When there are multiple targets ...



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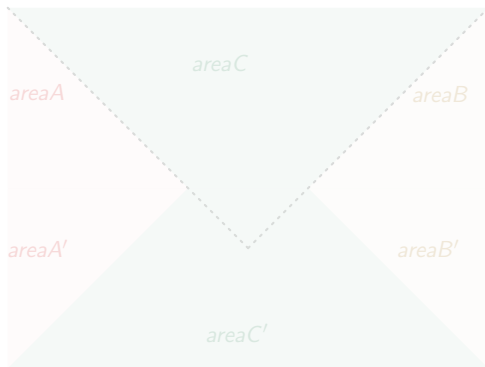
closest target of search node is a target  $t$  that  $h_p(\text{node}, t)$  is minimal.

How to find the closest target for a search node?



## Proposed algorithm 3: target heuristic

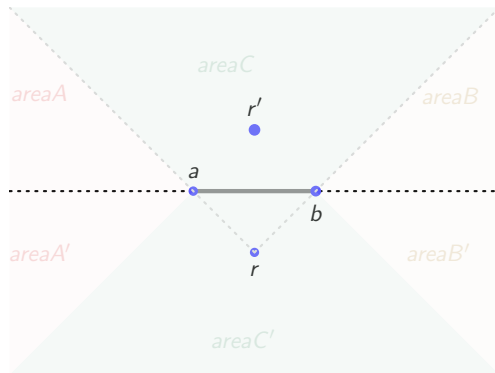
- In Case 3, instead of flipping targets, we can flip the  $r$
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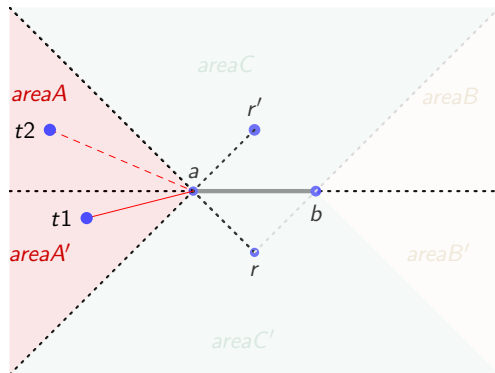
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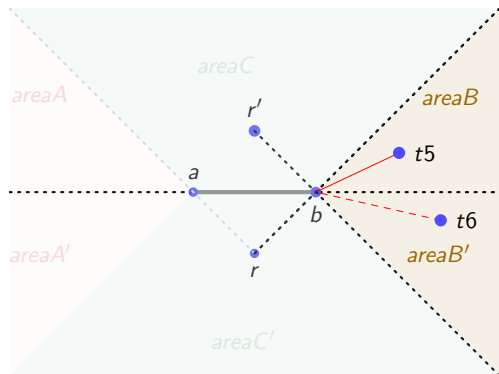


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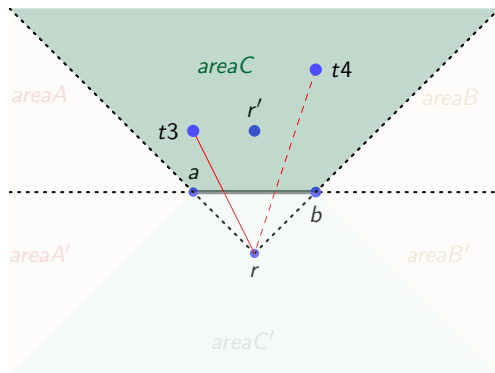
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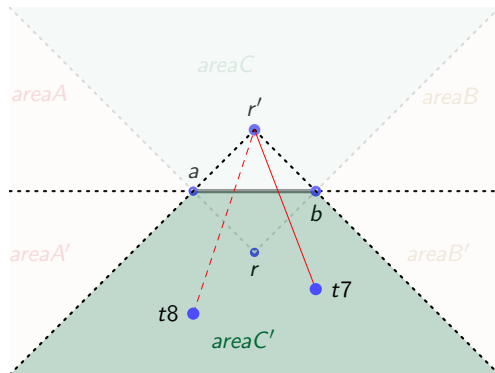
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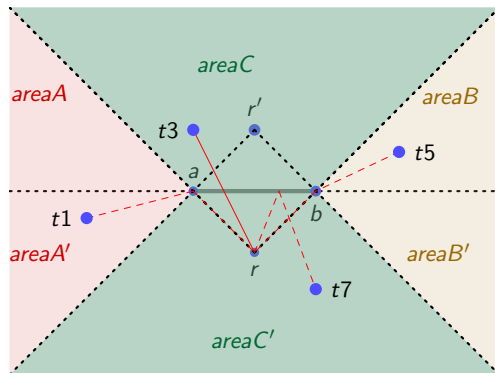
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- $NN_e(areaC, r)$  or
- $NN_e(areaC', r')$
- Choose the best



## Proposed algorithm 3: target heuristic

- For each successor, assign the closest target to it

- Correctness:

Proposed algorithm 3 is correct because it maintains the monotonicity property between the closest target of a search node and the closest target of its successor.



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### Lemma

*Non-decreasing property: Whenever the closest target of a search node changes, the  $h$ -value never decrease.*





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- Four *R-tree* queries for each search node is expensive



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- Four *R-tree* queries for each search node is expensive
- So we are looking for further refinements...



# Proposed algorithm 3: target heuristic refinements

- Lazy query



# Proposed algorithm 3: target heuristic refinements

## ■ Lazy query

### Definition

In expansion, instead of finding a new target, successors can inherit the closest target from their parent if the *h-value* doesn't change.



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*In this case, it is impossible to find a target with less *h-value*.*



# Proposed algorithm 3: target heuristic refinements

## ■ Reassignment





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### Definition

Once  $t$  be retrieved, we must reassign another target to those search nodes who are regarding  $t$  as their closest target



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*Lazy reassignment doesn't change relative expansion order.*



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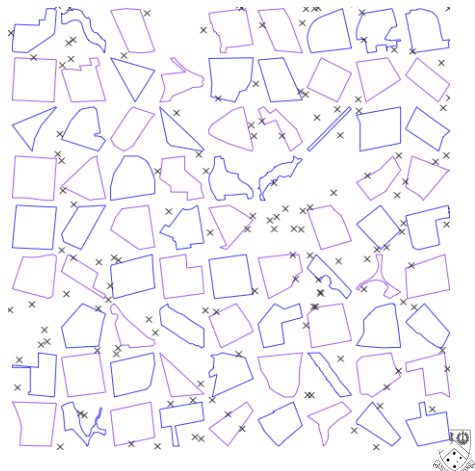
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# Benchmark Problem

Dataset in *Zhang, EDBT 2004*: no longer available, so we generate new benchmark problems:

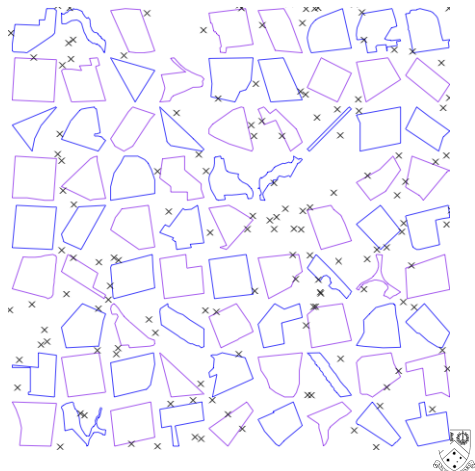
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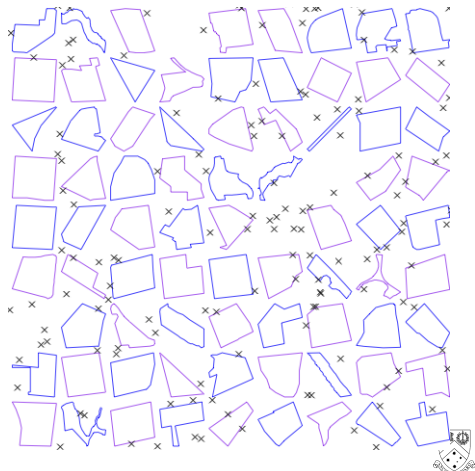




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# Competitors

There are two types of test case:

- Dense targets:  $|T| \approx |O|, |O| \approx 9000$
- Sparse targets:  $|T| \leq 10, |O| \approx 9000$

In dense targets experiments, we compare between:

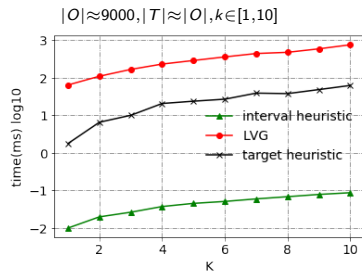
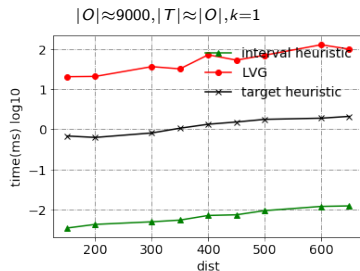
- *LVG* (from *Zhang, EDBT 2004*)
- Interval heuristic
- Target heuristic

In sparse targets experiments, we compare between:

- brute-force Polyanya
- Interval heuristic
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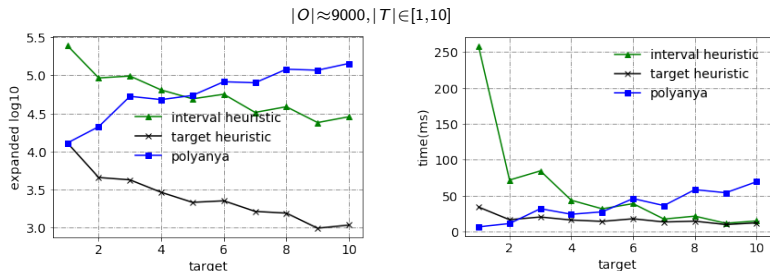
# Dense targets



- *Interval heuristic* is three order of magnitude faster than *LVG*, in all aspects.



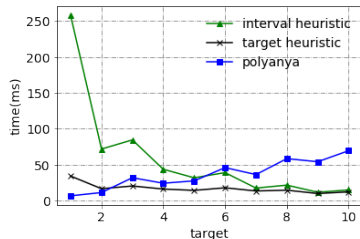
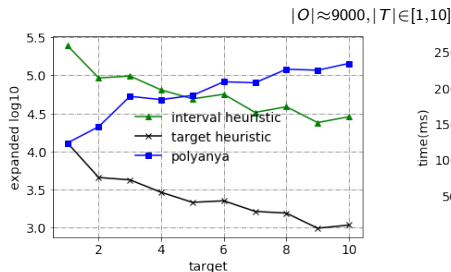
# Sparse targets: fix $k = 1$



- *Target heuristic* always has smaller search space. (left)
- It gradually lose such advantage when  $|T|$  increase. (right)
- Reason: the costly heuristic function.



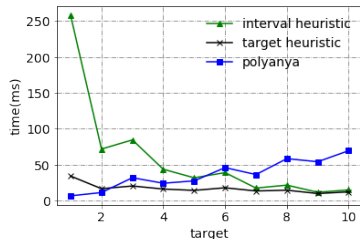
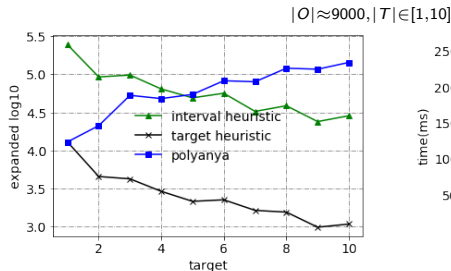
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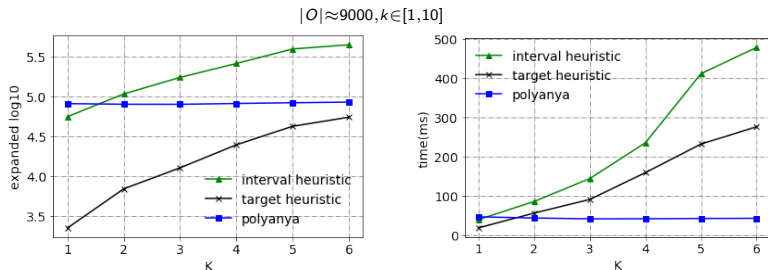
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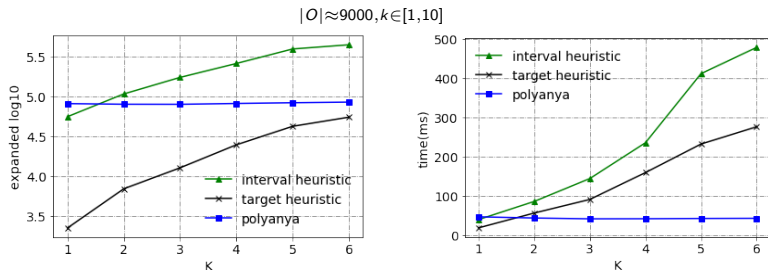
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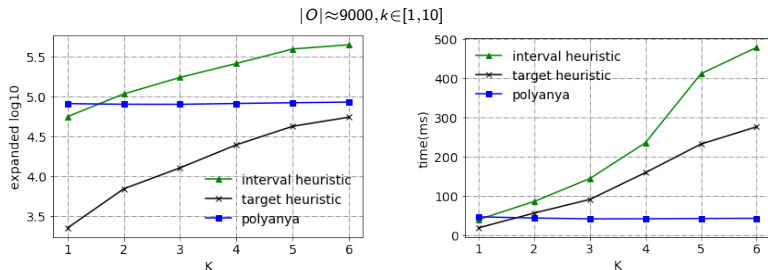


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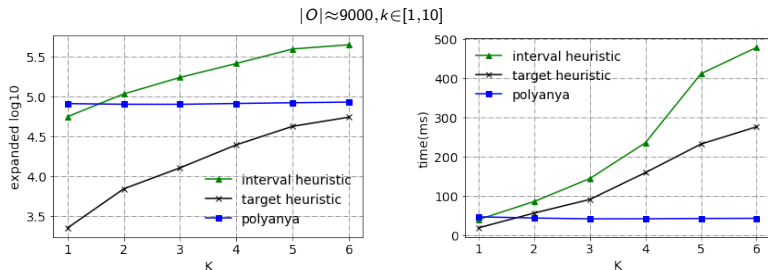
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# Outline

- 1 Introduction
- 2 Related works
- 3 Challenges
- 4 New Framework
- 5 My research
- 6 Experiments
- 7 Conclusion and future work**
- 8 End



# Conclusion

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- *Interval heuristic* works well when targets are many
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# Future works 1: improve other query processing

- Proposed algorithms can be used to speed up other types of spatial query which need to compute obstacle distance, e.g. *Obstacle Reverse Nearest Neighbor*.



## Future works 2: improve *target heuristic*

- *Target heuristic* cost  $\approx 80\%$  of total run time in *R-tree* query.
- Improve it by combining four queries into one, or using more suitable datastructure.





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# End

# Q & A



End

Thank you!

