## Fylgiblað með lokaprófi í Tölvugrafík Formúlur:

$$sx = Ax + C$$
  $sy = By + D$  
$$A = \frac{V \cdot r - V \cdot l}{W \cdot r - W \cdot l}$$
  $C = V \cdot l - AW \cdot l$  
$$B = \frac{V \cdot t - V \cdot b}{W \cdot t - W \cdot b}$$
  $D = V \cdot b - BW \cdot b$ 

$$a \circ b = b \circ a$$
,  $(a+c) \circ b = a \circ b + c \circ b$ ,  $(sa) \circ b = s(a \circ b)$ ,  $|b|^2 = b \circ b$   
 $b \circ c = |b||c|\cos\theta \Leftrightarrow \cos\theta = \hat{b} \circ \hat{c}$ 

$$c = Kv + Mv^{\perp}, \qquad K = \frac{c \circ v}{|v|^2}, \qquad M = \frac{c \circ v^{\perp}}{|v|^2}$$
  
 $r = a - 2(a \circ \hat{n})\hat{n}$ 

$$i = (1, 0, 0), \quad j = (0, 1, 0), \quad k = (0, 0, 1)$$
  
 $a \times b = (a_Y b_Z - a_Z b_Y)i + (a_Z b_X - a_X b_Z)j + (a_X b_Y - a_Y b_X)k$   
 $i \times j = k, \quad j \times k = i, \quad k \times i = j$   
 $a \times b = -b \times a, \quad a \times (b + c) = a \times b + a \times c, \quad (sa) \times b = s(a \times b)$ 

PNF: 
$$n \circ (R - C) = 0$$
,  $n_X x + n_Y y + n_Z z = n \circ (C - (0,0,0))$   

$$t_{hit} = \frac{n \circ (B - A)}{n \circ c}$$

$$\begin{pmatrix} c & -s & 0 \\ s & c & 0 \\ 0 & 0 & 1 \end{pmatrix}, \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & c & -s & 0 \\ 0 & s & c & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}, \begin{pmatrix} c & 0 & s & 0 \\ 0 & 1 & 0 & 0 \\ -s & 0 & c & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}, \begin{pmatrix} c & -s & 0 & 0 \\ s & c & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

 $u \times v = n$ ,  $v \times n = u$ ,  $n \times u = v$ 

$$(x^*, y^*, z^*) = \left(N \frac{P_X}{-P_Z}, N \frac{P_Y}{-P_Z}, \frac{aP_Z + b}{-P_Z}\right), \quad top = N \tan\left(\frac{angle}{2}\right)$$

$$R = \begin{pmatrix} \frac{2N}{right - left} & 0 & \frac{right + left}{right - left} & 0 \\ 0 & \frac{2N}{top - bott} & \frac{top + bott}{top - bott} & 0 \\ 0 & 0 & \frac{-(F + N)}{F - N} & \frac{-2FN}{F - N} \\ 0 & 0 & -1 & 0 \end{pmatrix}$$

$$I = I_a \rho_a + I_d \rho_d \cdot lambert + I_s \rho_s \cdot phong^f$$

$$lambert = \max\left(0, \frac{s \circ m}{|s||m|}\right), \quad phong = \max\left(0, \frac{h \circ m}{|h||m|}\right)$$

$$\begin{bmatrix} u_{x} & u_{y} & u_{z} & -eye \cdot u \\ v_{x} & v_{y} & v_{z} & -eye \cdot v \\ n_{x} & n_{y} & n_{z} & -eye \cdot n \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$lerp(A, B, t) = (1 - t)A + tB$$