Archaic cuneiform numbers

Robin Leroy, Anshuman Pandey, and Steve Tinney 2024-08-18

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1 Summary

This document proposes encoding some numerals used in the Uruk and Early Dynastic periods in conjunction with the Sumero-Akkadian cuneiform script¹ and the proto-cuneiform script². The proposed characters are listed in section 2.

The non-numeric signs of proto-cuneiform will be the subject of a separate proposal; we need only note here that the divergence between the approaches to character identity in modern scholarship requires that proto-cuneiform be disunified from cuneiform: proto-cuneiform is effectively treated as an undeciphered script. In contrast, the cuneiform encoding model is semantic, requiring an understanding of the text to correctly encode it.

However, the *numerals* used in proto-cuneiform should be unified with ones used in the Early Dynastic period, for the reasons set forth in section 4. The proposed "curved", or "curviform", numerals³ should however *not* be unified with the already-encoded cuneiform numerals⁴. Since the encoding proposals for the cuneiform script twenty years ago provisionally considered the curviform numerals to be glyph variants of the cuneiform numerals, a detailed rationale is provided in section 3, including compatibility considerations in section 3.7.

The overall picture of unifications and disunifications over time is illustrated in table 1. The Script_Extensions property assignments in section 2.2 reflect the overlap.

[TODO(egg): Mention the other sections here too.]

	Uruk III & earlier	ED – Ur III	OB & later
Numerals	This proposal		
Numerals		Fyictin	a Yeny
Non-numeric signs	Future Pcun	Existing Xsux	

Table 1: Usage of existing, proposed, and future characters across functions and time periods.

 $^{^1\}text{ISO}$ 15924: Xsux, Script property value long name: Cuneiform; encoded since Unicode Version 5.0. ^2ISO 15924: Pcun, not yet encoded.

 $^{3 - \}mathbb{H} \ 1 - 9(a\S^c = N_1), - \mathbb{H} \ 1 - 5(u^c = N_{14}), - \mathbb{H} \ 1 - 9(ne\S_2^c = N_{34}), - \mathbb{H} \ 1 - 5(ne\S^a_1^c = N_{48}), \text{ etc.}$

2 Proposed changes to the Standard

- 2.1 Summary of proposed characters
- 2.2 Properties
- 2.3 Character names list
- 2.4 Core specification text

3 Rationale for curviform-cuneiform disunification

TODO(egg): blurb.

3.1 The cuneiform encoding model

As outlined in, *e.g.*, [UTR56], the cuneiform encoding model is diachronic; each character may have wildly different glyphs depending on time period and region. For instance, the sign IM may resemble in texts from Early Dynastic IIIa Šuruppag as in the character code charts, if later in the third millenium⁵, if in Old Babylonian cursive, if in Neo-Assyrian, but is always encoded as U+1214E CUNEIFORM SIGN IM.

This encoding model allows for the interoperable representation of editions of diachronic reference works such as sign lists⁶ and dictionaries⁷, and of composite texts⁸. By being compatible with similarly diachronic transliteration practice (that is, by avoiding distinctions finer than those made in transliteration), the encoding model also allows for automated conversion of transliterated corpora to cuneiform, which has proven useful as a processing step in analyses such as [Rom24; JJ24]⁹. The diachronic approach is also useful for pedagogical applications¹⁰.

3.2 Arguments for curviform-cuneiform unification

In this context, the argument was made in [L2/04-099], as part of discussion of the cuneiform encoding¹¹ that the curviform numerals, which occasionally appear in the Ur III period and are used heavily in the Early Dynastic period, were a stylistic distinction unifiable with the cuneiform digits, and that an archaizing Ur III font or an Early Dynastic font could have curviform glyphs for the appropriate characters.

Some co-occurrence of curviform and cuneiform digits was known and acknowledged. [L2/04-099, p. 3] cites [NDE93, p. 62], which is a copy of [P020054], an

 $^{^5}$ Merging with U+1224E NI_2 .

⁶Notably [VT+14] and the online edition of [Bor10] in [Jim+23, Signs].

⁷Notably [TJV17] and the online edition of [Sch10] in [Jim+23, Dictionary].

 $^{^8}$ For example, there are Neo-Assyrian and Neo-Babylonian copies parts of the laws of ** (**) (**), as well as Old Babylonian copies in both archaizing and cursive styles. Because of damage on the stele [P249253], some sections are known only from those copies. See [Oel22, pp. 110 sqq.].

⁹Attendees may recall the summary given on the third day of UTC #180, as recorded in [L2/24-159]. Other readers may refer to [Svä+24, pp. 242, 148].

¹⁰For instance, Old Babylonian grammar may be taught in the Neo-Assyrian script, as in [Cap02].

¹¹At that time scoped to the répertoire of the Ur III period and later, see [L2/03-162, p. 1], although many disunifications, such as & ≠ &H, were informed by Early Dynastic distinctions.

Early Dynastic IIIb administrative tablet from Nirsu. The excerpt cited, lines 1–3 of column 1 of the obverse, is as follows:

tug_x(LAK483)-si-ga-kam¹⁴ deep ploughing

The argument made in [L2/04-099, p. 4] is that this is comparable to a stylistic distinction such as ¹⁵

465 metres, equal lengths 198 metres, equal widths this field: 9, 18 hectares, deeply ploughed

where the numerals have the same structure ([L2/04-099] contrasts this to the different structures of ASCII digits and roman numerals). That document further claims that "the number signs do not normally carry in their individual signs the meaning of what they are used to measure", and that curviform and cuneiform numerals "are not normally mixed together in a single numerical expression", noting the exceptions of [P232278; P232280]. In addition, [L2/04-099, p. 4] points out that the cuneiform numeric signs are descended from the curviform ones (this is undisputed), and claims there is only a small re-allocation of the function of signs (from P- to 1-numerals). It therefore comes to the conclusion that the use of curviform numerals should be seen as a formatting distinction, rather than one that should be represented in plain text, and insists that the encoding should capture the lineal historical descent of those signs, presumably to take advantage of the benefits of diachronic encoding described in section 3.1.

Although they had been part of the preliminary proposal [L2/03-393R], the curviform numerals were therefore removed from [L2/04-036] and [L2/04-189], which both state that "The distinction between curved numerals and their cuneiform descendants is treated as glyphic for the purposes of the present proposal; this issue will need to be revisited in subsequent encoding phases."

The time has come to revisit this issue. As we will see in section 3.3, numerals can only be interpreted in the context of what they measure *i.e.*, as part of a metrological system. In section 3.4 we will see that in some periods:

¹²As noted in [Pow87, p. 466], this sign has a very short "tail" in this period, so that it is wider than it is tall, and can at first seem like a large ← in copies. The photos in CDLI clearly show that this is in fact a vertical wedge.

 $^{^{13}}$ Note that ED IIIb ⟨ numerals have a somewhat different appearance from those of the Ur III period used in this transcription; the sign ⟨⟨ in [P020054] looks more like Ur III \(\frac{1}{2} \).

¹⁴Transliteration after [Lec20, p. 8].

¹⁵We have taken the liberty of adjusting the analogy to use measures approximately equal to those in [P020054], instead of a field of five by twenty-five metres.

- the functions and use of the numerals vary beyond the mere ▷/! switch;
- the contrast between curviform and cuneiform numerals is commonly used to distinguish metrological systems;
- some metrological systems commonly mix curviform and cuneiform in single numerical expressions.

3.3 A primer on classic Ur III and Old Babylonian metrologies

Edubba'a D

Before diving into the usage of the curviform numerals in the Early Dynastic period to explain the constrast with cuneiform numerals, it is useful to understand the usage of the already-encoded characters in the Ur III and Old Babylonian periods.

3.3.1 The discrete counting system

The relations between the values of the signs in the cuneiform discrete counting system may be summarized by the following factor diagram¹⁷, where the number over arrow indicates the multiple of the preceding sign (right of the arrow) corresponding to the following sign (left).

¹⁶See, e.g., [Uni16, §22.3.3, sub "Cuneiform Numerals"].

¹⁷These diagrams, which have become standard in discussions of Mesopotamian metrology, originate with [Fri78, p. 10], where they are called *step-diagrams*.

3.3.2 The area system

The discrete counting system was not the only non-positional system in use in the Ur III and Old Babylonian periods; different systems were in use depending on what was being counted or measured. For instance, field areas were measured using the following system, where for the named units we have provided the name of the unit in transliterated Sumerian, normalized Old Babylonian Akkadian, and the approximate metric equivalent [Frio7, p. 378; Rob19]:

$$\Leftrightarrow \stackrel{10}{\longleftrightarrow} \diamondsuit \stackrel{6}{\longleftrightarrow} \stackrel{1}{\longleftarrow} \stackrel{10}{\longleftrightarrow} \stackrel{3}{\longleftrightarrow} \stackrel{6}{\longleftrightarrow} \stackrel{1}{\longleftrightarrow} \stackrel{10}{\longleftrightarrow} \stackrel{1}{\longleftrightarrow} \stackrel{10}{\longleftrightarrow} \stackrel{1$$

Note that for the range of areas given above 18 , this system does not use any symbols separate from the numerals for the individual units ($ub\hat{u}m$, $ik\hat{u}m$, eblum, and $b\bar{u}rum$). As mentioned in [Rob19], the whole numeric expression for the area would be followed by the sign \blacksquare functioning as punctuation 19 , but the numerals are tied to the metrology; thus a surface of 5 $b\bar{u}r\bar{u}$ 1 eblum 4 $ik\hat{u}$ (100 $ik\hat{u}$, 36 ha) would be written 20 《 \prec \equiv \blacksquare . Contrast this with systems where the same numerals are used for different units, and overt units are used, as in "88 acres 3 roods 33 perches" or Ξ 頃八畝五分九厘. Note also that the same signs are shared between multiple systems, with different relations; the ŠAR $_2$ sign \diamondsuit is equal to sixty times the U sign \lt in the area system, but to three hundred and sixty times \lt in the discrete counting system.

3.3.3 The capacity system

Another such system of note is the one for capacities²¹ [Frio7, p. 376; Rob19],

where the numerals for ban_2 are +, \neq , \neq , \neq , and \neq , and those for bariga are \downarrow , \downarrow , \uparrow , and \uparrow (contrast ordinary \uparrow and \uparrow otherwise used with \uparrow -numerals). As described in [Hue11, p. 585 with notes (b) and (f)], the sign GUR \rightleftharpoons , while it is used only with volumes in excess of one gur, is written after the whole expression, after the overt unit sign \nearrow if present, and after the word for "grain" if present, as in

$$\underbrace{\diamondsuit \not\models \stackrel{10}{\longleftrightarrow} \diamondsuit \not\models \stackrel{6}{\longleftrightarrow} \diamondsuit \stackrel{10}{\longleftrightarrow} \diamondsuit \stackrel{6}{\longleftrightarrow} \diamondsuit \stackrel{10}{\longleftrightarrow} \diamondsuit \stackrel{6}{\longleftrightarrow} \diamondsuit \stackrel{10}{\longleftrightarrow} \diamondsuit \stackrel{$$

¹⁸For areas smaller than a quarter $ik\hat{u}m$, an overt unit is used, with 1 $m\bar{u}$ sarum (36 m²) written l $\stackrel{\blacksquare}{\cong}\Box$, equal to one hundredth of an $ik\hat{u}m$, then sexigesimally subdivided in 60 $\stackrel{\blacksquare}{\coprod}$ (shekels). For areas greater than 3600 $b\bar{u}r\bar{u}$, the \diamondsuit - and \diamondsuit -numerals are reused with a suffix $\stackrel{\blacksquare}{\Longrightarrow}$ (gal, Sumerian: big), as follows [Robo8, p. 295 with notes b and c; Frio7, p. 378; Rob19]:

 $^{^{19}\}mbox{TODO(egg)}:$ acknowledge Proust 2020 but note that this is irrelevant to encoding concerns

²⁰As in the surface of the field of || | | | | | | (the city of Apisal) reported on [P102305, r. 1]

 $^{^{21}}$ Used for volumes of grain, but also oil, dairy products, beer, etc., as well as to express the capacity of boats; volumes of earthworks instead use system $G_{\text{Ur III}/OB}$ based on a height of one cubit, see[Pow87, p. 488; Robo8, p. 294; Rob19].

Observe that while large numbers of gur follow²³ system $S_{\text{Ur III}/OB}$, the use of horizontal (AS) numerals for the gur disambiguates from the vertical bariga, as would be 10 gur 1 bariga, and **⟨−**♯ would be 11 gur; again even with some overt units, most of the numerals that participate in a metrological system have an interpretation dependent on that system.

This intertwining of units and numerals explains the large number of alreadyencoded numeral series:

- I-# used in $S_{Ur III/OB}$ and the SPVS as well as with overt units;
- \leftarrow wsed in $G_{\text{Ur III}/\text{OB}}$, of which \leftarrow are also used in $S_{\text{Ur III}/\text{OB}}$ and the SPVS as well as with overt units;
- I-W used in $S_{\text{Ur III/OB}}$, and sometimes with overt units;
- K-W used in $S_{\text{Ur III/OB}}$;
- \diamond \diamond used in $S_{\text{Ur III/OB}}$ and $G_{\text{Ur III/OB}}$;
 \diamond \diamond used in $S_{\text{Ur III/OB}}$ and $G_{\text{Ur III/OB}}$;
- - used in $C_{\text{Ur III}/\text{OB}}$ as well as with overt units of the weight system;
- 十, 丰, 隼, 卧, 鼣 used in $C_{\text{Ur III}/OB}$;
- I, I, I used in $C_{\text{Ur III/OB}}$ —note the overlap with I-I;
- \prec and \rightleftarrows used in $G_{\text{Ur III}/\text{OB}}$.

Only in the SPVS did numerals exist truly independently of metrology; to quote [Robo8, p. 78]: "The SPVS temporarily changed the status of numbers from properties of real-world objects to independent entities that could be manipulated without regard to [...] metrological system. [...] Once the calculation was done, the result was expressed in the most appropriate metrological units and thus re-entered the natural world as a concrete quantity."

The length system 3.3.4

In the Ur III and Old Babylonian periods, lengths are expressed using overt units counted with \P - and \P -numerals with their system $S_{\text{Ur III}/OB}$ values²⁴. Since it does not have any unusual numerals, this system would not in itself be of much relevance to character encoding, but we present it here as background for its Early Dynastic counterpart presented in section 3.4. Metrological tables use the following units [Frio7, p. 118; Rob19]:

Two more units appear occasionally [Pow87, p. 459; Frio7, p. 118; Rob19]:

| ** **
$$\leftarrow$$
 ** \leftarrow **

²²From [**P309594**].

 $^{^{23}}$ A larger unit, the guru $_{7}$ (karûm, grain heap), is sometimes used instead, with m- 멸冷m+<= \diamondsuit $m\pm$ (1 karûm = 3600 kurrū). See [Frio7, p. 415; Rob19].

 $^{^{24}}$ Adjacent units are no more than a factor of 60 apart, so higher numerals such as \P or \diamondsuit are not used.

²⁵TODO

In addition, there are Akkadian names for the half-rope and half-reed, see [Pow87, pp. 463 sq.].

3.3.5 Fractions

TODO

3.4 Curviform numerals in early metrologies

At first sight, the metrological systems from the Early Dynastic period match the ones previously mentioned. In particular, the discrete counting system used in the Early Dynastic period (and earlier in the Uruk period) clearly mirrors system $S_{\text{Ur,III/OR}}$ [Frio7, p. 374; DE87, pp. 127, 165]:

$$\bullet \xleftarrow{10} \bullet \xleftarrow{6} \bullet \xrightarrow{10} \triangleright \xrightarrow{6} \bullet \xrightarrow{10} \triangleright. \tag{S}$$

Likewise the area system used in the Early Dynastic IIIb period mirrors system $G_{\text{Ur III}/\text{OB}}$ [Dei22, p. 72; NDE93, p. 63; Frio7, p. 378; Gom16]:

$$\bullet \xleftarrow{10} \bullet \xleftarrow{6} \overset{10}{\Leftarrow} \xleftarrow{10} \bullet \xleftarrow{3} \bullet \xleftarrow{6} \triangleright, \qquad (G_{\rm ED\,IIIb})$$

As noted in [L2/04-099, p. 4] (see section 3.2), the vertical $\[\]$ from $S_{Ur \, III/OB}$ becomes a horizontal $\[\]$ in system S. It is however far from the only case of such a reallocation of function. The earlier form of System G was [DE87, pp. 141, 165; Frio7, p. 378]:

Observe that, as noted in [DE87, p. 142], $^{\odot}$ changes meaning from 10^{\bullet} in system G to 10^{\bullet} in system G is used in the Uruk period, but also in the ED I–II period (it is the "area 2" system in [Cha03], whereas $G_{\rm ED\,IIIb}$ is the "area 1" system).

3.4.1 Field lengths in Nirsu

The length system Early Dynastic IIIb of the state of Lagaš is of particular interest. As described in [Pow87, p. 466; Lec20, pp. 289 sq.], lengths are expressed in rods, but the unit sign \checkmark is generally omitted; in addition, only tens of rods are used; these are equal to one rope, but the sign \checkmark is not written either. Length shorter than one rope are expressed in half-ropes using the 1/2 sign \checkmark (again with no \checkmark), and then in reeds, with the sign \checkmark 3. Effectively, this yields the following factor diagram:

$$\begin{array}{c|c}
 & 6 & 2 \\
\hline
 & 1 \text{ e\S{e}_2=10 nindan} \\
 & 1 \text{ rope=10 rods} \\
 & 60 \text{ m}
\end{array}$$

$$\begin{array}{c}
 & 10 \\
\text{gi} \\
\text{reed} \\
 & 3 \text{ m}
\end{array}$$

$$(L_{\text{ED IIIb}})$$

This is the system that was used to express the sides of the field in [P020054] discussed in section 3.2. In that tablet and others from the same period, such as the ones discussed in [Lec20] areas are expressed in system $G_{\rm ED~IIIb}$, with curviform numerals²⁹; in the absence of overt units, such as when dealing with length that

 $^{^{28} \}text{Note that the reeds are counted using } \textit{tenû} \text{ numerals, \nwarrow, $^{\$}$, etc.}$

 $^{^{29}\}text{TODO(egg)}$: Note the handful of late Urukagina tablets that start to have cuneiform areas.

3.4.2 Dyke lengths in Nirsu

[Pow87, p. 466] notes that reeds "are regularly written with the normal, cuneiform end of the stylus. Higher units are usually written with the reversed (round) end of the stylus." [TODO(egg): also mention Krebernik 1998 p. 303 with note 686.] Powell does not elaborate on the specifics of this mixed use of numerals, but a cursory search in CDLI finds many occurrences³¹, such as:

These expressions use an explicit sign \slash (counted in multiples of ten) or \slash . This notation—but not its use of curviform numerals—is remarked on in [Lec20, p. 290 with note 27], which cites several of the instances listed above. It seems to be typical of texts about dykes. These³⁴ match the following factor diagram:

$$\underbrace{\stackrel{10}{\longrightarrow}}_{\text{Will}} \stackrel{6}{\longrightarrow} = \underbrace{\stackrel{2}{\longrightarrow}}_{\text{I}_{35}} \stackrel{10}{\longleftarrow} \underbrace{\stackrel{10}{\longrightarrow}}_{\text{H}_{35}} \stackrel{6}{\longleftarrow} \stackrel{\#}{\longrightarrow} \underbrace{\stackrel{3}{\longrightarrow}}_{\text{II}_{10}} \stackrel{10}{\longrightarrow}_{\text{II}_{10}}$$

3.4.3 Grain in Ebla

Lengths of Early Dynastic IIIb dykes from Nirsu are far from the only numeric expressions that mix curviform and cuneiform numerals.

 $^{^{30}}$ This is the case of the sides of the field in [P020054, obv. ii 2–3].

 $^{^{31}}$ A search for curviform numerals followed by some number of reeds counted in ($ten\hat{u}$) cuneiform numerals currently finds 125 occurrences across 47 tablets.

 $^{^{32}}$ CDLI only has a copy, but a photo may be found in [Lec12, p. 82]. On that photo the $\blacksquare \triangleright \parallel \cdot$ is not visible. Lecompte notes that the copy is faithful; indeed another $\blacksquare \triangleright \parallel \cdot$ can be seen both on the copy and the photo on obv. 2, 2.

³³ From copy.

 $^{^{34}}$ TODO Cite also DP 568, the one with lacktriangle and lacktriangle even though it has no reeds.

 $^{^{35}\}mbox{TODO(egg)}\mbox{:}$ Note that one unit may be omitted if the other is present

The system of grain³⁶ capacities in Ebla uses the following units³⁷:

The $\Box \Delta \bot$ and $\Box \Box \Box$ are generally counted using curviform numerals, and the smaller units using cuneiform I numerals. Indeed, a search on [Mil+07] for cooccurrences of $* \hookrightarrow$ with either of $\Box \hookrightarrow \bot$ or $\lhd \boxminus$ finds the following expres-

- 2. [P240548, verso 1, 1] □□ H Ⅲ H ↔
- 3. [P240655, recto 7, 9] → ₩ L 41 ₩ V { 41
- 4. [P240579, verso 4, 3] BPT \$\times \tag{\text{IIV}}
- 5. [P240675, verso 2, 2] D 無 日田 W V (年)
- 6. [P240609, verso 3, 1] □□ ∄ 珊 Ⅲ ★ ↔

- 13. [P241904, recto 1, 1] 46 B 🗘 L W 47 以 4 🖽

Note that higher numbers of ➡️ L are expressed in hundreds (mi-at (and then thousands (li-im >), as is typical in Ebla [Arc15, p. 33], e.g., in [P240532,

At a glance it seems that 🕽 are counted with cuneiform numerals and higher units with curviform ones,

$$\underbrace{\begin{array}{c}
\frac{5}{3} & \triangleright & 6 & \bullet & \bullet \\
\hline
\text{All } & \bullet & \bullet \\
\hline
\text{All } & \bullet & \bullet \\
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\end{array}}_{4} \underbrace{\left(\begin{array}{c}
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but we have not investigated this thoroughly.

³⁷TODO mention the other one citing Chambon and the footnote in Archi

³⁸We cite here only one attestation per tablet; most tablets contain several expressions mixing curviform 🗗 🖽 and larger with cuneiform 🎹 and smaller. In all cases the transcriptions given here are based on the EbDA transliterations, but the shape and orientation of the numerals was checked³⁹ on a photograph (from EbDA unless noted otherwise).

³⁹As we will see in Section 3.6.1, CDLI transliterations indicate numeral shape; however, as of this writing, they do so incorrectly on the Ebla corpus, claiming that all numerals are curviform, so we were not able to rely on them in this specific case.

- 40ba-ri₂-zu₂, a variant spelling.
- ⁴¹Short for □ L.
- ⁴²Note the omitted \Box \bot .
- ⁴³Instead of the expected **Ⅳ** [].
- ⁴⁵From CDLI photo.
- ⁴⁶From photo in [Arc89, p. 6].
- ⁴⁷Laid out as **!!!!**; on stacking patterns see Section 6.2.

³⁶Liquid capacities use a different system [Arc15, p. 229 with note 12]:

of decreasing fractions $^1/_n$ of this measure, whereby "n" was determined by the number of oblique impressions made by the rounded end of a thin stylus around a central point in a specific sign. Thus $\Xi=^1/_2$ N_{39} , $\varpi=^1/_3$ N_{39} , and so on. The first sign of the latter units, N_{34}

Figure 1: TODO [Eng98, p. 113]

For instance, the first line contains the notations $1N_{34}$ $1N_{39_0}$; $2N_{20}$, which can be translated "60 of the (grain rations containing) = (of grain); (grain involved:) $2 \bullet$ (of ground barley)". This calculation contradicts the assumed numerical relationship $10N_1 = 1N_{14}$, since as was well known the measure represented by the sign N_{39} was 1/5 of that represented by N_1 , so that $60 \times 1/5 = 12$ and not 20, as $2N_{14}$ would imply. Instead of relying on complicated

Figure 2: TODO [Eng98, p. 116]

These expressions match the following factor diagram:

3.4.4 Use in modern publications

Because of their prevalence in the Uruk and Early Dynastic periods, the proposed numerals are used modern publications discussing metrology in those periods, as illustrated in Figures 1–10.

Since they contrast with the cuneiform numerals, they likewise appear contrastively in such publications. A remarkable example of that is found in Figure 10. The partial transliteration " 4^{P} ' a_3 -da-um 4^{T} aktum 4^{P} ib $_2$ tu $_9 \times 3^{\text{T}}$ sa $_6$ gunu $_3$ " is used to illustrate a discussion of the interpretation of the contrast between $^{\text{P}}$ and $^{\text{T}}$ numerals. More conventional transliterations 49 might omit the numeral shapes entirely, e.g., 4 ' a_3 -da-um 4 aktum 4 ib $_2$ tu $_9 \times 3$ sa $_6$ gunu $_3$, which would obviously be inadequate in this context. There are transliteration conventions that are more explicit about numeral shape, e.g., 4 (as $^{\text{C}}$) ' a_3 -da-um 4 (dis $^{\text{C}}$) aktum 4 (as $^{\text{C}}$) ib $_2$ tu $_9 \times 3$ (dis $^{\text{C}}$) sa $_6$ gunu $_3$, but the result would be less readable. See Section 3.6.1 for a discussion of transliteration conventions for numerals.

Die halbkreisförmigen Griffeleindrücke gehen manchmal in mehr oder weniger eckige Formen über (\P)⁸⁸⁵. Es gibt aber auch Einer in Form von regelrechten – meist mehr oder weniger schräggestellten – Keilen (\P), die öfters neben halbrunden Einern vorkommen und mit diesen kontrastieren⁶⁸⁶. Selten treten mit \triangledown gebildete Zahlen auf⁶⁸⁷ (sie entsprechen den bariga-Zahlen im Hohlmaßsystem, s.u. 7.4).

Figure 3: TODO [Kre98, p. 303]

formed by only two signs $\ \$ and $\ \$, repeated as many times as necessary; this type of notation is highly standardized. Second, the order of magnitude of the numbers noted in this system is not indicated: 1, 60, 60², 60³, 1/60, 1/60², etc. are written in the same way, with the vertical wedge $\ \ \$. The third feature concerns the exact function of

Figure 4: TODO [Cha12, p. 58]

one step. The scribes of the Early Dynastic Period (c. 2600 BC), for instance, represented the number 648,000 with:

Figure 5: TODO [Cha12, p. 59]⁵⁰

repetition of the same sign refers to both the capacity unit signified—often but not necessarily written immediately afterwards—and its value. The units of measurement are written in descending order from left to right—just as we would write 3 km, 120 m, 50 cm. For example:

DD še bar ∇ ba-rí-zu

'3 gubar (capacity units) and 1 parīsu'.

Figure 6: TODO [Cha12, p. 61]

This is particularly true of the signs \bowtie , \bowtie , \bowtie and \bowtie , whose form explicitly denotes the fractions 1/6, 2/6, 3/6, and 4/6 of the barig capacity measure written \bigcirc in Mesopotamia—also transcribed by Assyriologists as 1 bán, 2 bán, 3 bán, and 4 bán with reference to the bán measure worth 1/6 of the barig. At Ebla, the sign \bigcirc is most often associated with the *parīsu* measure, while the signs \bowtie , \bowtie , \bowtie , and \bowtie refer to 1, 2, 3,

Figure 7: TODO [Cha12, p. 64]

shape. The principle of notation is additive: each sign is noted as many times as necessary (e.g., transliterated as $2(\bar{s}ar_2)$ $1(ge\bar{s}'u)$ 3(u), means $2 \times 3600 + 1 \times 600 + 3 \times 10$). The system is based on an alternation of factors ten and

Figure 8: TODO

might think of one fabric and a half, ¹¹ but the presence of notations with " $2^D 2^U$ ", " $3^D 3^U$ ", and " $6^D 6^U$ " (Fig. 1) elements excludes that one deals with fractions, as these notations are not consistent with those of Šuruppag's weight measurement system. ¹² The notation " 1^D gada" in o. ii 1 and r. vi 1, along with the total of "39"



Fig. 1. Combinations of numerals attested in Š. 742.

Figure 9: Discussion of the contrast between ▶ and ¬ numerals in [Gor23, p. 162].

```
as, for example, in TM.75.G.3125 = ARET III 107 o. iv 1, "4^{\mathbf{D}} 'a_3-da-um<sup>tu9</sup>-2 4^{\mathbf{D}} aktum 4^{\mathbf{D}} ib<sub>2</sub><sup>tu9</sup>×3 3^{\mathbf{D}} sa<sub>6</sub> gunu<sub>3</sub>" (Fig. 2).
```

Figure 10: Transliteration in [Gor23, p. 163] of [P242293, recto 4, 1] incorporating untransliterated numerals.

3.5 Non-numeric usage

```
钉里选 下索击击
```

The beginning of the scribal art is a single wedge. That one has six pronunciations; it also stands for 'sixty'51. Do you know its reading?52

Examenstext A

Many of the cuneiform numerals are used with a logographic or phonetic value. For example, the sign - has, *inter alia*, the values $a\check{s}$ and rum. While the horizontal numerals are most frequently written written - in the Early Dynastic period⁵³, such non-numeric usage is almost always written -, for instance:

- in personal names in administrative texts, such as the following, which all contain
 □ numerals:
 - → إأ in [P010424; P010458; P010459] from ED IIIa أبو صلابيخ
 - → in [**P010960**] from ED IIIa Šuruppag,
 - **► I III** in [**P010964**] from ED IIIa Šuruppag,
 - 福世ー博 in [P251641] from ED IIIb Adab,
 - 灣野一園► in [P252866] from ED IIIb Adab,
 - ₱> **I** > in [**P298637**] from ED IIIb Umma;
- in the divine name * 妇以一上 in the lexical texts [**P010570**; **P010572**], where the entries are prefixed with □.

3.6 Limited benefits of diachronic encoding for numerals

[TODO Composite texts dating back to the period where curved numerals are in use tend to be limited to lexical texts, which do not usually have numbers. When they do, diachronic encoding is prevented by diš-aš distincitons anyway. Administrative texts, which are where numbers are most prominent, are not composite.]

 $[\]operatorname{coded} \operatorname{ib}_2 \times 3 \, ! = \operatorname{III} \times \times \operatorname{III} = \operatorname{III} \times .$

 $^{^{49}}$ TODO cite the EbDA one.

 $^{^{50}}TODO(egg)$: On the order cite TSS 188, Friberg2007 p. 148 and any of the usual suspects on the haphazard order of signs in early texts; contrast P274845, P241764.

 $^{^{51}}$ The reader will recall that η eš $_2$ is written \P , with a larger wedge than \P ; however, these signs have merged by the Old Babylonian period when the first witnesses of Examenstext A are attested.

 $^{5^2}$ Besides 9^8_2 , a look at [VT+14] shows that the values dis, 9^8_3 , makkas, 9^8_4 , and 9^8_4 , and tal 9^8_4 are attested both in [TJV17] and in lexical lists. The sign is also used for the Akkadian word 9^8_4 in the Neo-Assyrian period.

⁵³A CDLI search for "(asz@c)" finds 3296 ED texts, while a search for "(asz)" finds 81 ED texts, of which 46 also contain "(asz@c)".

[TODO Diachronic reference works tend to not include numbers, or when they do, to treat them specially (for intance, they are shown at the end of sign lists such as TODO).]

[TODO The overarching goal of having consistent representation for equivalent numeric expressions from different periods is quickly foiled by changes in metrology.]

Note that in [Rom24] [TODO(egg): Cite the GitHub repository], as in many other such analyses, numbers are removed as an early step in processing; these therefore would not benefit from diachrony in the encoding of numeric expressions.

3.6.1 Compatibility with transliteration

TODO words [Robo8, p. 295] TODO cite [Molina2014]

3.7 Compatibility considerations

A disunification twenty years after the fact, affecting all numerals, would ordinarily be a serious compatibility issue. Fortunately, with one exception discussed below, we are not aware of any font using curviform glyphs for the already-encoded numerals. In fact we are not aware of any font designed for a style earlier than Old Babylonian, except for fonts mimicking the representative glyphs from the code charts, which are primarily Ur III, but sometimes earlier or later, as described in [UTR56, §2.4]. The lack of dedicated Ur III fonts may be explainable by the chartlike fonts⁵⁴ being good enough; the lack of Early Dynastic fonts, by the aforementioned issues with numeral identification making the representation of any text with numerals intractable.

3.7.1 The case of ŠAR₂

[TODO explain why this isn't a problem, effectively anyone who needs to cuneify $1(\tilde{s}ar_2^c)$ will also need to cuneify some of the numerals proposed here and will therefore not be using Unicode cuneiform.] [TODO U+122B9 CUNEIFORM SIGN SHAR2 represents both $1(\tilde{s}ar_2)$ and non-numeric $\tilde{s}ar_2$; it looks like \diamondsuit (so, like \diamondsuit) in all but lexical texts from Ebla and Šuruppag (and the archaizing vulture stele, where note that the scribe slipped into his modern ways once), where it looks like (TODO: the proposed character). The proposed character is to be used for $1(\tilde{s}ar_2^c)$. $1(\tilde{s}ar_2)$ does not exist back when non-numeric $\tilde{s}ar_2$ is curviform, so it works out.] [TODO Mention P222243]

3.8 Conclusions

4 Rationale for ED-Uruk numeral unification

5 Considerations on individual numeral series

[TODO Document to the extent possible the metrological systems in which each sign is used. Note the disunification of N9 and N10 from 4(ban₂@c) and 5(ban₂@c).]

⁵⁴Most prominently Noto Sans Cuneiform, a system font on both Windows—as part of Segoe UI Historic—and macOS.

6 Characters not included in this proposal

6.1 Missing numerals

 $(N_{17}, 12N_{14}, \text{etc.}) 7(\text{diš } ten\hat{u})$

6.2 Stacking patterns

(... are a mess, vary within Uruk, and are not transliterated/documented by Englund, so let's not go there for now.)

6.3 Matters for higher-level protocols

Rotated bits: https://cdli.mpiwg-berlin.mpg.de/artifacts/101087

Acknowledgements

TODO(egg): Something about the Vanséveren fonts

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