Twelve cuneiform tenû numerals

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1 Summary

This document proposes filling the Cuneiform Numbers and Punctuation block with twelve cuneiform numerals used in the third millennium.

Three of those are additional numerals in the AŠ (or DIŠ) $ten\hat{u}$ series, $7 \sim -9 \sim$, where $1 \sim -1 \sim 1$ through $1 \sim -1 \sim 1$ are already encoded. Their glyphic range and usage, as well as possible reasons for their absence in the current version of the Standard, are discussed in §??.

The other proposed characters constitute a new series of numerals, formed by $\$ numerals crossing an $\$ wedge. They are discussed in \S_4 .

2 Proposed changes to the Standard

2.1 Core specification text

No change is needed in the core specification.

2.2 Code charts

The code charts for the affected block, including the character names list with proposed informative aliases, cross references, and informative notes, are shown on the following pages. A plain text file containing the NamesList.txt lines is attached to this document.

2.3 Properties

Add to the respective UCD files the lines given in this section. These are available as plain text files attached to this document. Changes to derived files are not listed.

- 2.3.1 Name, General_Category, Numeric_Value, etc.
- 2.3.2 Line_Break
- **2.3.3** Script
- 2.3.4 Script_Extensions
- 2.3.5 Block

3 DIŠ *tenû* numerals

This section discusses the following proposed characters:

- U+1246F [♠] CUNEIFORM NUMERIC SIGN SEVEN ASH TENU
- U+12475

 [♠] CUNEIFORM NUMERIC SIGN EIGHT ASH TENU
- U+12476 ♠ CUNEIFORM NUMERIC SIGN NINE ASH TENU

3.1 Name

The existing numerals in the $^{\ }$ series are named U+12039 $^{\ }$ Cuneiform sign ash zida tenu for the first one and U+1244a–U+1244E $^{\ }$ - $^{\ }$ Cuneiform numeric sign n ash tenu for the others.

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- 135 -
              h) DIE SCHIEFEN KEILE UND DIE WINKELHAKEN (für die Einheiten von
                 1-9, neben den senkrechten keilförmigen Zahlenzeichen).
a) bei | : RTC. 276: K# #
             Bart. III 118, 249: 3 gin igi-4-gál \ ₹ še.
Legr. TRU. 310: ud - ≪ ₹ kam.
             Gen. TD. 5487: ( áb.
b) vor kam und àm:
              Bart. III 152, 398: dub- - am
             Legr. TRU. 42: a-du-(-kam
                              a-du ≪-kam
                              a-du ⋘- kam
                              a-du -kam
             Legr. TRU. 346: 1 máš-qal-še 444-kam-uš
1 udu-še ≪-kam-uš

Siehe: itu-šu-∭-ša; itu šu-∭-ša; itu šu-≪-ša.
c) nach gud, áb, anše, zux Bezeichnung des Alters.
         ITT. III, II 4956: 20 ab - 4 - še 3 qa - ta
         /77. III II 6090: 3 anše-sal-Y; 1 anše-nita Y;
         Pinch AT. I. 53: 3 gud 1; 1 ab 1;
         Bart. III 106, 191: 3 anše-nita 1
         ITT. II, I. 6965: 20 zu-gud- 15 zu-gud 1.
```

Figure 1: [Sch35, p. 135]

In modern transliteration, $\$ numerals are described as - $ten\hat{u}$ (ATF: asz@t) or ! $ten\hat{u}$ (ATF: disz@t), the latter being more common⁴. Informative aliases using $di\check{s}$ $ten\hat{u}$ have been recommended for the existing characters in [L2/24-239]. The proposed names use ASH TENU for consistency with the already-encoded characters, and the proposed annotations include informative aliases with $di\check{s}$ $ten\hat{u}$.

Figure 2: [Sch35, p. 132]

3.2 Ur III usage

As described in [Sch35, p. 135] (see Figure 1), slanted signs are used in Ur III economic texts primarily in subtractive notation with \(\bullet^5 \) lal^6, as well as for ordinals \(\bullet^7 \) and for ages of animals in years\(\bullet^8 \).

¹TODO also note gunû but contrast CROSSING rather than gi-li-mu-u, SQUARED rather than li-mu-bu i-gi-gu-ub-bu-u2

²Note that while the third millennium I and ⊥ are related by a 45° rotation, in the Neo-Assyrian style used by this list, these signs look like I and ∓, so that only one wedge is slanted, as noted in [Gong2000].

 $^{^3}$ TODO something on spelling out names ኦጠኔ-ተልፈንኦነሙ ga-na te-nu-u $_2$ and *ልዓን-ኦነሙ \check{se} te-nu-u; ku te-nu-u, etc.

⁴For an example of a transliteration using aš tenû, see [**Greco2021**]; note that only the HTML version uses aš tenû. the PDF uses diš.

 $^{^5}$ As noted in [L2/24-210R, p. 25 n. 40], the sign [(lal, "minus") is often ligated with the following numerals, with the subtrahend placed under a sometimes considerably enlarged [, similar to the layout of the radical in modern mathematical notation, see, e.g., [P020092, rev. 3 1, 2]. The font used in this document ligates or kerns $^{^{^{\prime}}}$ subtrahends, but does not enlarge the $^{^{\prime}}$.

⁶Also transliterated la₂, as in [CDLI]. In the transliterated Ur III corpus on [CDLI], out of 3304 occurrences of (disz@t), 1971 are in $\lceil n \rceil$ 1a2 n(disz@t).

 $^{^{7}}$ 1583 out of 3304 occurrences are $n \setminus \diamondsuit n(\texttt{disz@t})$ -kam, including 647 after \sqcap

 $^{^8}$ 203 occurrences of gu4, ab2, ansze, or dur3 $n({ t disz@t})$

 $^{^9}$ Of the 1971 Ur III occurrences of lal $\,n({\tt disz@t}),$ 1930 are with $n \le 2,$ of which 1823 with n = 1.

 $^{^{10}}$ 430 occurrences of n(disz@t)-kam are on lines starting with mu, of which 308 are in $\langle K$.

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thus ➡ ₩ ♦ for "the 7th day" or ➡ 《 ₩ ♦ for "the 28th day".

The rarity of the higher $\$ numerals in the Ur III corpus likely explains the absence of $7\$ -9 $\$ from the répertoire of Unicode Version 5.0, which was aiming to encode a répertoire appropriate for the Ur III period and later.

3.3 Early Dynastic usage

The situation is different in the Early Dynastic corpus. As described in [L2/24-210R], \ numerals are used in many Early Dynastic metrological systems, and in particular in the Early Dynastic IIIb length system

The use of \setminus numerals for ordinals, especially for days, is more prevalent in the Early Dynastic period than in the Ur III period, and the use of subtractive notation is less frequent in these numbers. We therefore find many attestations of $n \rightarrow n$ in $n \rightarrow n$. TODO(egg) Figures.

In Ebla, the \ numerals are primarily used in subtractive notation, see [Gor24, p. 88 n. 298, p. 120 n. 465, p. 167 n. 739, p. 180 n. 801]. However, contrary to Ur III, \ numerals remain used for large subtrahends, thus [Gor24, p. 101 n. 355] cites occurrences of \ for 36 and \ for \ (a) \ (b) \ (a) \ (b) \ (a) \ (b) \ (c) \ (c)

¹¹Of those, 34 have 7 ∰ ₦₽ and 9 have ∰ ₦₽.

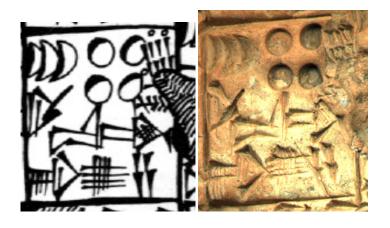
¹²Recall that **⟨!! ! !** *mi-at* is Eblaite for "hundred", see [Arc15, p. 33; L2/24-210R, p. 27].



Figure 3: 【《 13 篇 44 位 1501 m" (first width of a field) in [P221254], dated to the reign of 出 句 14 位 14 6. Left: Copy from [AllottedelaFuÿe1920]. Right: [CDLI] photograph.



Figure 4: 《知 到 回 "21 m of reed-bed dyke" (attributed to 止於 the farmer) in [P221266, obv. 1 1], dated to the reign of 具 (Left: Copy from [AllottedelaFuÿe1920]. Right: [LouvreCollections] photograph.



¹³TODO something about rhomboidal numerals, cite [Gor24].

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3.4 Stacking patterns

4 AŠ×(DIŠ *tenû*) numerals

https://cdli.mpiwg-berlin.mpg.de/artifacts/452986/reader/209489 https://cdli.mpiwg-berlin.mpg.de/artifacts/467743/reader/213564

4.1 Stacking patterns

The subsequent mu-iti system, which saw limited use at the end of the presargonic and the beginning of the Old Akkadian periods, seems, on its surface, to be a rational development from the system it replaced; the basis of a 30-day month carries on (cf. for instance the texts B. Foster, Umma in the Sargonic Period [Hamden 1982] pl. 18, Nr 37, discussed by J. Friberg, Scientific American 250/2 [Feb. 1984] 114 and Foster, ASJ 4 [1982] 43 obv iii9-11) and, for a period at least, a graphically comparable method of representing year dates, with now vertical strokes impressed on either side of the long horizontal, was used (the date of the text BIN 8, 117, - 4, which both Powell, HUCA 49, 9 and B. Foster, Or.NS 48 (1979) 156 and USP p. 7 read 7 (mu) 1 (iti) 7 (ud), should be registered with some scepticism). Only here is the refinement of day added, so that documents

Figure 6: TODO note that this should cite BIN 8, 116, not 117.

A connection of IM with the later usage of im(.ma) (presargonic Lagash and later; Akkadian šaddaqdi/a(m) with lexical equivalent MU.IM.MA [MSL 5, 65:195]), meaning "previous (year)" is not apparent. For the latter usage cf. particularly DP 280 (= 281), a presargonic temple document which "loads onto the backs" (gu₂.ne.ne.a e.ne.gar) of the fisheries foremen Ne.sag and Lugal.ša₃.la₂.tuku the quota arrears of im.im.ma.kam —, im.ma.kam —— and mu.a.kam ——, that is of the year before last = year one (of the king Urukagina [second regnal year]), of last year = year 2 and of this year = year 3 Also DP 243 goats of various colors / maš im.ma.kam / ditto / maš mu.a.kam and DP 94. maš im.ma as delivery arrears noted after grown nannies (ud₅) and before maš ša₃.HI (/mu.a.kam, "of the current year"), further maš im.ma = maš.gal.gal in the summation rev i2 (see footnote 17 to the notations of the type ——). A parallel usage is found in the Old Akkadian text ITT 2/1, 3078 obv 1-4. 3 1/2 ma.na siki / [i]m.ma.kam / 1 gu₂ la₂.4 ma.na siki / mu.a.kam. It would seem difficult to reconcile this clear usage im = "previous year" with the often translated im = "account tablet" (im = clay)

Figure 7: TODO

Acknowledgements

The *CuneiformComposite* font by Steve Tinney is used when referring to the reference glyphs for already-encoded cuneiform. *Noto Sans Cuneiform*, by Monotype Imaging, is used to for most of the cuneiform text in this document, with modifications (cuneiform glyph for \diamondsuit ŠAR₂, corrected glyps for \blacksquare UN and \blacksquare VALAM per [Uni16], alternate glyph $\$ for $\$). Arabic text is set in *Scheherazade New* by SIL International; Traditional Chinese text is set in *Noto Serif TC* by Ken Lunde et al.; monospace text is set in *Consolas* by Luc(as) de Groot; the remainder of the text is set in *Cambria* and *Cambria Math* by Monotype Imaging and Tiro Typeworks.

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