

Archaic cuneiform numbers

Robin Leroy, Anshuman Pandey, and Steve Tinney

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1 Summary

2 Background

The Unicode Standard includes some cuneiform numbers: 𐎶–𐎶𐎵 1–9(diš) and 𐎶–𐎶𐎵 1–9(aš), 𐎶–𐎶𐎵 1–5(u), 𐎶–𐎶𐎵 1–9(ḫeš₂), 𐎶–𐎶𐎵 1–5(ḫeš₃u), etc., used in the Sumerian-Akkadian Cuneiform script (ISO 15924: Xsux, Script property value long name: Cuneiform).

In the investigation that led to their encoding in Unicode Version 5.0, it was thought appropriate to unify these with the earlier curviform numerals 𐎶–𐎶𐎵 1–9(aš^c = N_1), 𐎶–𐎶𐎵 1–5(u^c = N_{14}), 𐎶–𐎶𐎵 1–9(ḫeš₂^c = N_{34}), 𐎶–𐎶𐎵 1–5(ḫeš₃u^c = N_{48}), etc., see L2/04-099. While the curviform numerals sometimes co-occur with the cuneiform ones, this was analysed as a stylistic distinction which should not be encoded in plain text. It has now become apparent that a distinction needs to be

made for the adequate representation of Early Dynastic (ED) texts and scholarship pertaining to them.

In addition, these numerals will be needed for the representation of proto-cuneiform texts from the earlier archaic period. The non-numeric signs of proto-cuneiform (ISO 15924: P_{cun}) will be the subject of a separate proposal; we need only note here that the divergence between the approaches to character identity in modern scholarship requires that proto-cuneiform be disunified from cuneiform: proto-cuneiform is effectively treated as an undeciphered script. In contrast, the cuneiform encoding model is semantic, requiring an understanding of the text to correctly encode it.

The use of the curviform numeric signs is however understood, as we will discuss in Section 3; further, the conventions used for archaic numerals are also used when discussing ED numerals, see Section 7. As a result, the same numerals can be used when encoding archaic and ED texts, and in order to avoid issues ambiguities in representation when converting from transliteration, these should be unified. The overall picture of unifications and disunifications would be as follows:

	Uruk III & earlier	ED – Ur III	OB & later
Non-numeric signs	Future Pcun	Existing Xsux	
Numbers	This proposal	This proposal + Existing Xsux	Existing Xsux

3 Metrologies

正統五年五月
正統六年五月
正統七年五月

I want to write tablets: the tablet of 1 gur of barley to 600 gur; the tablet of 1 shekel of silver to 10 minas [...]

Edubba'a D

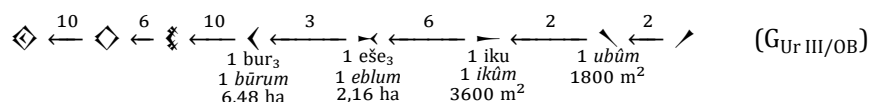
In order to explain why $\text{TODO}:n$ more numerals are needed, it is useful to first recall why we have so many kinds of cuneiform numerals already.

As is well known¹ a sexagesimal place value system (SPVS) was used in Mesopotamia from the late third millenium onwards. One should bear in mind, however, that other systems were used; the SPVS was primarily used in calculations, with results being expressed in non-positional systems [Rob08, p. 76; Rob22]. The digits 1–59 of the SPVS have inner structure which is reflected in the encoding: the digits 1–9 are the individual characters $\text{I} \text{---} \text{IX}$, the multiples of ten (10–50) are $\text{X} \text{---} \text{XL}$, but the other digits 11–59 are sequences $\text{XI} \text{---} \text{XLIX}$; in effect the base-sixty digits are themselves written in base ten, with a different set of symbols for the tens place. This reflects the origin of the sexagesimal place value system; it derives from a *non-positional* system, hereafter the *cuneiform discrete counting system* $\text{S}_{\text{Ur III/OB}}$, which had different signs for the units $\text{I} \text{---} \text{IX}$, tens $\text{X} \text{---} \text{XL}$, sixties $\text{I} \text{---} \text{LX}$ (with larger wedges than the units), six hundreds $\text{X} \text{---} \text{XVI}$, three thousand six hundreds $\text{X} \text{---} \text{XVI}$, and thirty-six thousands $\text{X} \text{---} \text{XVI}$.

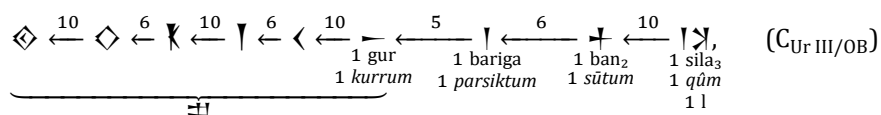
¹See, e.g., *The Unicode Standard*, Version 16.0, Section 22.3.3 *Non-Decimal Radix Systems*, sub “Cuneiform Numerals”.

$$\diamond \xleftarrow{10} \diamond \xleftarrow{6} \blacklozenge \xleftarrow{10} \blacktriangledown \xleftarrow{6} \blacktriangleleft \xleftarrow{10} \blacktriangledown \quad (\text{S}_{\text{Ur III/OB}})$$

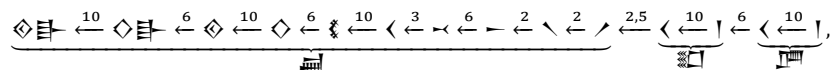
The discrete counting system was not the only non-positional system in use in the Ur III and Old Babylonian periods; different systems were in use depending on what was being counted or measured. For instance, field areas were measured using the following system, where for the named units we have provided the name of the unit in transliterated Sumerian, normalized Old Babylonian Akkadian, and the approximate metric equivalent:








Another such system of note is the one for capacities⁵ [Fri07, p. 376; Rob19],



³For areas smaller than a quarter *ikûm*, an overt unit is used, with 1 *mûšarum* (36 m²) written 𒍪𒍪, equal to one hundredth of an *ikûm*, then sexagesimally subdivided in 60 𒍪 (shekels). For areas greater than 3600 *bûrû*, the 𒄩- and 𒄪-numerals are reused with a suffix 𒍪 (gal, Sumerian: big), as follows:



⁵Used for volumes of grain, but also oil, dairy products, beer, etc., as well as to express the capacity of boats; volumes of earthworks instead use **GUR III/05** based on a height of one cubit, see[**Pow87**, p. 488; **Rob08**, p. 294; **Rob19**].

while it is used only with volumes in excess of one gur, the sign GUR  is written after the whole expression, after the overt unit sign  if present, and after the word for “grain” if present, as in  (3554 gur 3 ban₂ 6 sila₃ of grain⁶), see [Hue11, p.585 with notes (b) and (f)]. Observe that while large numbers of gur follow⁷ system S_{Ur III/OB}, the use of horizontal (AŠ) numerals for the gur disambiguates with the vertical bariga, as  would be 10 gur 1 bariga, and  would be 11 gur; again even with some overt units, most of the numerals are tied to the metrology.

- $\mathbb{I}-\mathbb{W}$ used in $S_{U^{\text{III}}/OB}$ and the SPVS as well as with overt units;
- $\mathbb{L}-\mathbb{X}$ used in $G_{U^{\text{III}}/OB}$, of which $\mathbb{L}-\mathbb{X}$ are also used in $S_{U^{\text{III}}/OB}$ and the SPVS as well as with overt units;
- $\mathbb{I}-\mathbb{W}$ used in $S_{U^{\text{III}}/OB}$ and the SPVS;
- $\mathbb{L}-\mathbb{X}$ used in $C_{U^{\text{III}}/OB}$ as well as in the weight system;
- $\mathbb{L}, \mathbb{L}, \mathbb{L}, \mathbb{L}, \mathbb{L}$ used in $C_{U^{\text{III}}/OB}$;
- $\mathbb{L}, \mathbb{L}, \mathbb{L}, \mathbb{L}$ used in $C_{U^{\text{III}}/OB}$ —note the overlap with $\mathbb{I}-\mathbb{W}$;
- \mathbb{L} and \mathbb{L} used in $G_{U^{\text{III}}/OB}$.

4 Arguments for curviform-cuneiform unification

(GED IIIb)

⁶From P309594.

- [Rob22] E. Robson. “Overview of Metrological Systems”. In: *The Digital Corpus of Cuneiform Mathematical Texts*. 2022.
eprint: <http://oracc.org/dccmt/Metrology/>.