Archaic cuneiform numbers

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Contents

1	Summary	1		
2	Background	1		
3	Metrologies	2		
4	Arguments for curviform-cuneiform unification			
5	Problems with unification: Early metrology			
6	Problems with unification: Non-numeric usage 6.1 The case of ŠAR ₂	4 4		
7	Compatibility with transliteration			
8	The necessity of ED-Uruk numeral identification			
9	Characters not included in this proposal 9.1 Missing numerals	4 4		
	9.2 Stacking patterns	4		

1 Summary

2 Background

The Unicode Standard includes some cuneiform numbers: $-\frac{1}{2}$ 1–9(diš) and $-\frac{1}{2}$ 1–9(aš), $-\frac{1}{2}$ 1–5(u), $-\frac{1}{2}$ 1–9(neš₂), $-\frac{1}{2}$ 1–5(neš'u), etc., used in the Sumero-Akkadian Cuneiform script (ISO 15924: Xsux, Script property value long name: Cuneiform).

 made for the adequate representation of Early Dynastic (ED) texts and scholarship pertaining to them.

In addition, these numerals will be needed for the representation of protocuneiform texts from the earlier archaic period. The non-numeric signs of protocuneiform (ISO 15924: Pcun) will be the subject of a separate proposal; we need only note here that the divergence between the approaches to character identity in modern scholarship requires that proto-cuneiform be disunified from cuneiform: proto-cuneiform is effectively treated as an undeciphered script. In contrast, the cuneiform encoding model is semantic, requiring an understanding of the text to correctly encode it.

The use of the curviform numeric signs is however understood, as we will discuss in Section 3; further, the conventions used for archaic numerals are also used when discussing ED numerals, see Section 7. As a result, the same numerals can be used when encoding archaic and ED texts, and in order to avoid issues ambiguities in representation when converting from transliteration, these should be unified. The overall picture of unifications and disunifications would be as follows:

	Uruk III & earlier	ED – Ur III	OB & later
Non-numeric signs	Future Pcun	Existing Xsux	
Numbers	This proposal	This proposal	Existing Xsux
		+ Existing Xsux	

3 Metrologies

Edubba'a D

In order to explain why TODO:*n* more numerals are needed, it is useful to first recall why we have so many kinds of cuneiform numerals already.

As is well known¹ a sexagesimal place value system (SPVS) was used in Mesopotamia from the late third millenium onwards. One should bear in mind, however, that other systems were used; the SPVS was primarily used in calculations, with results being expressed in non-positional systems. The digits 1–59 of the SPVS have inner structure which is reflected in the encoding: the digits 1–9 are the individual characters ¹-\; the multiples of ten (10–50) are <-\; but the other digits 11–59 are sequences <¹-\; in effect the base-sixty digits are themselves written in base ten, with a different set of symbols for the tens place. This reflects the origin of the sexagesimal place value system; it derives from a non-positional system, hereafter the cuneiform discrete counting system S_{Ur III/OB}, which had different signs for the units ¹-\; tens <-\; sixties \sqrt{-\; with larger wedges than the units}, six hundreds \sqrt{-\; with larger wedges than they six thousands \sqrt{-\; with larger wedges than they six they six they six they six

¹See, e.g., The Unicode Standard, Version 16.0, Section 22.3.3 Non-Decimal Radix Systems, sub "Cuneiform Numerals".

The relations between the values of the signs in the cuneiform discrete counting system may be summarized as follows, where the number over arrow indicates the multiple of the preceding sign (right of the arrow) corresponding to the following sign (left).

The discrete counting system was not the only non-positional system in use in the Ur III and Old Babylonian periods; different systems were in use depending on what was being counted or measured. For instance, field areas were measured using the following system, where for the named units we have provided the name of the unit in transliterated Sumerian, normalized Old Babylonian Akkadian, and the approximate metric equivalent:

Another such system of note is the one for volumes,

$$\underbrace{\diamondsuit \not\models \stackrel{10}{\longleftrightarrow} \diamondsuit \not\models \stackrel{6}{\longleftrightarrow} \diamondsuit \stackrel{10}{\longleftrightarrow} \diamondsuit \stackrel{6}{\longleftrightarrow} \underbrace{^{10}}_{\longleftrightarrow} (\stackrel{3}{\longleftrightarrow} \stackrel{6}{\longleftrightarrow} \stackrel{2}{\longleftrightarrow} \stackrel{2}{\longleftrightarrow} \stackrel{2}{\longleftrightarrow} \stackrel{2}{\longleftrightarrow} \stackrel{2}{\longleftrightarrow} \stackrel{2}{\longleftrightarrow} \stackrel{10}{\longleftrightarrow} \stackrel{1}{\longleftrightarrow} \stackrel{1$$

 $^{^2}$ For areas smaller than a quarter $ik\hat{u}m$, an overt unit is used, with 1 $m\bar{u}$ sarum (36 m^2) written ! $\stackrel{\text{init}}{\approx}$ 1, equal to one hundredth of an $ik\hat{u}m$, then sexigesimally subdivided in 60 $\stackrel{\text{init}}{=}$ 1 (gal, Sumerian: big), as follows:

 $^{^3}$ As in the surface of the field of 1 4 1 3 (Apisal) reported on 1 102305 r. 1.

of grain⁴). Observe that while large numbers of gur follow⁵ system $S_{Ur\,III/OB}$, the use of horizontal (AŠ) numerals for the gur disambiguates with the vertical bariga, as $\langle 1 \pm 1 \rangle$ would be 10 gur 1 bariga, and $\langle -1 \pm 1 \rangle$ would be 11 gur; again even with some overt units, most of the numerals are tied to the metrology.

This intertwining of units and numerals explains the large number of alreadyencoded numeral series:

- !-₩ used in S_{Ur III/OB} and the SPVS as well as with overt units;
- \leftarrow wsed in $G_{Ur\ III/OB}$, of which \leftarrow are also used in $S_{Ur\ III/OB}$ and the SPVS as well as with overt units;
- ¶-₩Ψ used in S_{Ur III/OB} and the SPVS;
- — -₩₩ used in C as well as in the weight system;
- 十, 丰, 肆, 敢, 敢 used in TODO;
- \, \, \, \, \, \\ used in C—note the overlap with \, \-\, \\;
- \prec and \rightleftarrows used in $G_{Ur III/OB}$.
- 4 Arguments for curviform-cuneiform unification
- 5 Problems with unification: Early metrology
- 6 Problems with unification: Non-numeric usage

The beginning of the scribal art is a single wedge. That one has six pronunciations; it also stands for 'sixty'. Do you know its reading?

Examenstext A

- 6.1 The case of ŠAR₂
- 7 Compatibility with transliteration
- 8 The necessity of ED-Uruk numeral identification
- 9 Characters not included in this proposal
- 9.1 Missing numerals

ED 《十二年本书

9.2 Stacking patterns

⁴From <mark>P309594</mark>.

⁵A larger unit, the guru₇ (*karûm*, grain heap), is sometimes used instead, with **— ৣ → ☆ ☆** (1 *karûm* = 3600 kurrū).