Archaic cuneiform numbers

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1 Summary

This document proposes encoding some numerals used in the Uruk and Early Dynastic periods in conjunction with the Sumero-Akkadian cuneiform script¹ and the proto-cuneiform script². The proposed characters are listed in section 2. Most of them were listed in [L2/23-190]; however, the present document provides a more detailed rationale for their encoding and additional information about their identity.

The non-numeric signs of proto-cuneiform will be the subject of a separate proposal; we need only note here that the divergence between the approaches to character identity in modern scholarship requires that proto-cuneiform be disunified from cuneiform: proto-cuneiform is effectively treated as an undeciphered script. In contrast, the cuneiform encoding model is semantic, requiring an understanding of the text to correctly encode it.

However, the *numerals* used in proto-cuneiform should be unified with ones used in the Early Dynastic period, for the reasons set forth in section 4. The proposed "curved", or "curviform", numerals³ should however *not* be unified with the already-encoded cuneiform numerals⁴. Since the encoding proposals for the cuneiform script twenty years ago provisionally considered the curviform numerals to be glyph variants of the cuneiform numerals, a detailed rationale is provided in section 3, including compatibility considerations in section 3.7.

The overall picture of unifications and disunifications over time is illustrated in table 1. The Script_Extensions property assignments in section 2.2 reflect the overlap. Many of these numerals are also used in proto-Elamite⁵ texts, where they are treated as identical characters in scholarship on proto-Elamite, so that

¹ISO 15924: Xsux, Script property value long name: Cuneiform; encoded since Unicode Version 5.0. ²ISO 15924: Pcun, not yet encoded.

³Impressed into clay using cylindrical styli, held either perpendicular to the tablet, yielding ● (small stylus) or ● (large stylus), or at a shallower angle: ▷, ▽ (small stylus), ▷ (large stylus). Some numerals are composed of multiple such impressions, *e.g.*, ▶ . The terms "curved", "curviform", and "round" can be found in the literature. We avoid the term "round" here as it has other meanings in the context of numbers. We use "curviform" in this document as, being the least common term, it is least likely to lead to confusion, and "CURVED" in the character names for consistency with documentation about the modifier @c used in machine readable ATF transliterations [inlineATF].

⁴Impressed into clay using a stylus with a trihedral end: — (stylus held horizontally), ↑ (vertically), ↑ (diagonally) ← (with the head of the stylus), ↑ (stylus pressed deeper, forming a larger wedge), ↑ (combining ↑ and ←), etc.

⁵ISO 15924: Pelm, not yet encoded.

they should be unified with the ones proposed in [L2/23-196]. However, in the interest of time, we do not provide a detailed rationale for this unification in this document, and we are not proposing that the numerals be given the corresponding Script_Extensions property value for now. Neither do we propose encoding any numerals that are solely attested in proto-Elamite texts, or well-attested in proto-Elamite texts but insufficiently attested in Uruk.

[TODO(egg): Mention the other sections here too.]

	Uruk III & earlier	ED – Ur III	OB & later
Numerals	This proposal		
ivumerais		Fyictin	a Yeny
Non-numeric signs	Future Pcun	Existing Xsux	

Table 1: Usage of existing, proposed, and future characters across functions and time periods.

2 Proposed changes to the Standard

- 2.1 Summary of proposed characters
- 2.2 Properties
- 2.3 Character names list
- 2.4 Core specification text

3 Rationale for curviform-cuneiform disunification

The numbering systems that use cuneiform numerals are descended from the ones that use curviform numerals, and many of the cuneiform signs have clear curviform counterparts across this transition. Co-occurrences are sometimes described by analogy to distinctions that are not the realm of plain text, as in [Powell1972] "in the same fashion as we use black and red ink"; however, we must bear in mind that such analogies are not made in the context of character encoding discussions. In 2004, the curviform numerals were deemed unencodable for the time being; however, closer inspection reveals that the distinction functions less like markup than was argued at the time, and that the unification is problematic.

3.1 The cuneiform encoding model

As outlined in, *e.g.*, [UTR56], the cuneiform encoding model is diachronic; each character may have wildly different glyphs depending on time period and region. For instance, the sign IM may resemble in texts from Early Dynastic IIIa Suruppag as in the character code charts, if later in the third millenium, in Old Babylonian cursive, in Neo-Assyrian, but is always encoded as U+1214E CUNEIFORM SIGN IM.

⁶Merging with U+1224E CUNEIFORM SIGN NI2.

This encoding model allows for the interoperable representation of editions of diachronic reference works such as sign lists and dictionaries, and of composite texts. By being compatible with similarly diachronic transliteration practice, *i.e.*, by avoiding distinctions finer than those made in transliteration, the encoding model also allows for automated conversion of transliterated corpora to cuneiform, which has proven useful as a processing step in analyses such as [Rom24; JJ24]¹⁰. The diachronic approach is also useful for pedagogic applications.

3.2 Arguments for curviform-cuneiform unification

In this context, the argument was made in [L2/04-099], as part of discussion of the cuneiform encoding 12 that the curviform numerals, which occasionally appear in the Ur III period and are used heavily in the Early Dynastic period, were a stylistic distinction unifiable with the cuneiform digits, and that an archaizing Ur III font or an Early Dynastic font could have curviform glyphs for the appropriate characters.

Some co-occurrence of curviform and cuneiform digits was known and acknowledged. [L2/04-099, p. 3] cites [NDE93, p. 62], which is a copy of [P020054], an Early Dynastic IIIb administrative tablet from Nirsu. The excerpt cited, lines 1–3 of column 1 of the obverse, is as follows:

```
<del>IM</del>
                                                                             ➾
                                      5(diš tenû)
1(\eta e \tilde{s}_2)
             1(u)
                       1/2(diš)
                                                         gi
                                                                    us_2
                                                                             sa_2
          7.5 (ropes)
                                                         reed
                                                                             equal
{{14}
                                                        ➾
                                              ∢⊟
3(u)
                6(diš tenû)
                                             saŋ
                                                        sa_2
3 (ropes)
                                   reed
                                             front
                                                       equal
量量
ašag-bi
                     1(bur<sub>3</sub>c)
                                   1(e\check{s}e_3^c)
                                                 1(iku<sup>c</sup>)
                                                             1/2(iku<sup>c</sup>)
 ašag=bi
 field=DEM15
```

tug_x(LAK483)-si-ga-kam tugsiga =ak =am -Ø ploughed=GEN=COP-3.SG.S

⁷Notably [OSL] and the online edition of [MZL] in [eBL, Signs].

⁸Notably [ePSD2] and the online edition of [Sch10] in [eBL, Dictionary].

⁹For example, there are Neo-Assyrian and Neo-Babylonian copies parts of the laws of ₩□ ★ ⟨ □ □ □ , as well as Old Babylonian copies in both archaizing and cursive styles. Because of damage on the stele [P249253], some sections are known only from those copies. See [Oel22, pp. 110 sqq.].

 $^{^{10}}$ Attendees may recall the summary given on the third day of UTC #180, as recorded in [L2/24-159]. Other readers may refer to [Svä+24, pp. 242, 148].

¹¹For instance, Old Babylonian grammar may be taught in the Neo-Assyrian script, as in [Cap02].

¹³As noted in [Pow87, p. 466], this sign has a very short "tail" in this period, so that it is wider than it is tall, and can at first seem like a large — in copies. The photos in CDLI clearly show that this is in fact a vertical wedge.

¹⁴Note that ED IIIb 〈 numerals have a somewhat different appearance from those of the Ur III period used in this transcription; the sign ⋘ in [P020054] looks more like Ur III ❖.

¹⁵Alternatively: area=POSS.3.SG.NH, "its area".

The argument made in [L2/04-099, p. 4] is that this is comparable to a stylistic distinction such as 16

465 metres, equal lengths 198 metres, equal widths this field is 9, 18 hectares of ploughed land

where the numerals have the same structure ([L2/04-099] contrasts this to the different structures of ASCII digits and roman numerals). That document further claims that "the number signs do not normally carry in their individual signs the meaning of what they are used to measure", and that curviform and cuneiform numerals "are not normally mixed together in a single numerical expression", noting the exceptions of [P232278; P232280]. In addition, [L2/04-099, p. 4] points out that the cuneiform numeric signs are descended from the curviform ones (this is undisputed), and claims there is only a small re-allocation of the function of signs (from to I numerals). It therefore comes to the conclusion that the use of curviform numerals should be seen as a formatting distinction, rather than one that should be represented in plain text, and insists that the encoding should capture the lineal historical descent of those signs, presumably to take advantage of the benefits of diachronic encoding described in section 3.1.

Although they had been part of the preliminary proposal [L2/03-393R], the curviform numerals were therefore removed from [L2/04-036] and [L2/04-189], which both state that "The distinction between curved numerals and their cuneiform descendants is treated as glyphic for the purposes of the present proposal; this issue will need to be revisited in subsequent encoding phases 17 ."

The time has come to revisit this issue. As we will see in section 3.3, numerals can only be interpreted in the context of what they measure, *i.e.*, as part of a metrological system. In section 3.4 we will see that in some periods:

- the functions and use of the numerals vary beyond the mere $\triangleright/!$ switch;
- the contrast between curviform and cuneiform numerals is commonly used to distinguish metrological systems;
- some metrological systems commonly mix curviform and cuneiform in single numerical expressions.

 $^{^{16}}$ We have taken the liberty of adjusting the analogy to use measures approximately equal to those in [Po20054], instead of a field of five by twenty-five metres.

¹⁷The cuneiform encoding process was planned in *stages* in [L2/03-162]. One might expect the second stage of encoding, which led to the creation of the Early Dynastic Cuneiform block, to incorporate the numerals needed for the representation and discussion of Early Dynastic texts; however, the proposal [**L2/12-208**] stated that "numerals have been omitted due to the complexity of numeral signs from this period. An expert in the metrology of this period must be consulted before these can be properly included."

3.3 A primer on classic Ur III and Old Babylonian metrologies

Edubba'a D

Before diving into the usage of the curviform numerals in the Early Dynastic period to explain the constrast with cuneiform numerals, it is useful to understand the usage of the already-encoded characters in the Ur III and Old Babylonian periods.

3.3.1 The discrete counting system

The relations between the values of the signs in the cuneiform discrete counting system may be summarized by the following factor diagram¹⁹, where the number over arrow indicates the multiple of the preceding sign (right of the arrow) corresponding to the following sign (left).

3.3.2 The area system

The discrete counting system was not the only non-positional system in use in the Ur III and Old Babylonian periods; different systems were in use depending on what was being counted or measured. For instance, field areas were measured using the following system, where for the named units we have provided the name of the unit in transliterated Sumerian, normalized Old Babylonian Akkadian, and

¹⁸See, e.g., [Uni16, §22.3.3, sub "Cuneiform Numerals"].

¹⁹These diagrams, which have become standard in discussions of Mesopotamian metrology, originate with [Fri78, p. 10], where they are called *step-diagrams*.

the approximate metric equivalent [Frio7, p. 378; Rob19]

$$\Leftrightarrow \stackrel{10}{\longleftrightarrow} \diamondsuit \stackrel{6}{\longleftrightarrow} \stackrel{10}{\diamondsuit} \stackrel{10}{\longleftrightarrow} \stackrel{3}{\longleftrightarrow} \stackrel{6}{\longleftrightarrow} \stackrel{10}{\longleftrightarrow} \stackrel{3}{\longleftrightarrow} \stackrel{6}{\longleftrightarrow} \stackrel{6}{\longleftrightarrow} \stackrel{2}{\longleftrightarrow} \stackrel{2}{\longleftrightarrow} \stackrel{2}{\longleftrightarrow} \stackrel{2}{\longleftrightarrow} \stackrel{2}{\longleftrightarrow} \stackrel{2}{\longleftrightarrow} \stackrel{2}{\longleftrightarrow} \stackrel{10}{\longleftrightarrow} \stackrel$$

Note that for the range of areas given above 20, this system does not use any symbols separate from the numerals for the individual units (ubûm, ikûm, eblum, and būrum). As mentioned in [Rob19], the whole numeric expression for the area would be followed by the sign if functioning as punctuation²¹, but the numerals are tied to the metrology; thus a surface of 5 būr 1 ebel 4 ikû (100 ikû, 36 ha) would be written²² ≪ ← ₩ 🕍 . Contrast this with systems where the same numerals are used for different units, and overt units are used, as in "88 acres 3 roods 33 perches" or 五頃八畝五分九厘. Note also that the same signs are shared between multiple systems, with different relations: the sign \diamondsuit is equal to sixty times \checkmark in the area system, but to three hundred and sixty times (in the discrete counting system.

3.3.3 The capacity system

Another such system of note is the one for capacities ²³ [Frio7, p. 376; Rob19],

where the numerals for ban₂ are +, \ddagger , \ddagger , \ddagger , and \ddagger , and those for bariga are \cdot , \cdot , \cdot , and \(\) (contrast ordinary \(\) and \(\) otherwise used with \(\) numerals). As described in [Hue11, p. 585 n. (b) and (f)], the sign ## GUR, while it is used only with volumes in excess of one gur, is written after the whole expression, after the overt unit sign if present, and after the word for "grain" if present, as in

Observe that while large numbers of gur follow²⁵ system $S_{\text{Ur III}/OB}$, the use of horizontal (AŠ) numerals for the gur disambiguates from the vertical bariga, as

$$\underbrace{\diamondsuit \not\models \stackrel{10}{\longleftrightarrow} \diamondsuit \not\models \stackrel{6}{\longleftrightarrow} \diamondsuit \stackrel{10}{\longleftrightarrow} \diamondsuit \stackrel{6}{\longleftrightarrow} \underbrace{^{10}}_{\longleftrightarrow} (\stackrel{3}{\longleftrightarrow} \overset{6}{\longleftrightarrow} -\stackrel{2}{\longleftrightarrow} \stackrel{2}{\longleftrightarrow} \stackrel{2}{\longleftrightarrow} \stackrel{2}{\longleftrightarrow} \stackrel{2}{\longleftrightarrow} \stackrel{10}{\longleftrightarrow} \stackrel{1}{\longleftrightarrow} \stackrel{$$

²⁰For areas smaller than a quarter *ikûm*, an overt unit is used, with 1 *mūšarum* (36 m²) written [] equal to one hundredth of an ikûm, then sexigesimally subdivided in 60 [m] (shekels). For areas greater than 3600 *būrū*, the ♦ and ♦ numerals are reused with a suffix 🖹 (gal, Sumerian: big), as follows [Robo8, p. 295 n. b and c; Frio7, p. 378; Rob19]:

²¹This sign is sometimes interpreted as a measurement unit, and transliterated iku, see, e.g., [Proust2020], or transliterations in [Feu04] discussed in section 3.7.2. Even with this interpretation, the sequence of numerals used, and the interpretation of numerals shared with other metrological systems, is specific to system $G_{\rm Ur~III/OB}$.

²As in the surface of the field of **|| ← | ⟩|** (the city of Apisal) reported on [P102305, r. 1]

²³Used for volumes of grain, but also oil, dairy products, beer, etc., as well as to express the capacity of boats; volumes of earthworks instead use system $G_{\text{Ur III/OB}}$ based on a height of one cubit, see [Pow87, p. 488; Robo8, p. 294; Rob19].
²⁴From [**P309594**].

²⁵A larger unit, the guru₁ (*karûm*, grain heap), is sometimes used instead, with — **□▶** (**< (1 karûm = 3600 kurrū). See [Frio7, p. 415; Rob19].

⟨ | ♯ | would be 10 gur 1 bariga, and ⟨ − ♯ | would be 11 gur; again even with some overt units, most of the numerals that participate in a metrological system have an interpretation dependent on that system.

This intertwining of units and numerals explains the large number of alreadyencoded numeral series:

- I-IIIII used in $S_{III}IIII/OB$ and the SPVS as well as with overt units;
- \leftarrow used in $G_{\text{Ur III}/OB}$, of which \leftarrow are also used in $S_{\text{Ur III}/OB}$ and the SPVS as well as with overt units;
- I-W used in $S_{Ur III/OB}$, and sometimes with overt units;
- \P - \P used in $S_{\text{Ur III/OB}}$;
- \diamond \diamond used in $S_{\text{Ur III/OB}}$ and $G_{\text{Ur III/OB}}$;
 \diamond \diamond used in $S_{\text{Ur III/OB}}$ and $G_{\text{Ur III/OB}}$;
- \leftarrow used in $\mathcal{C}_{\text{Ur III/OB}}$ as well as with overt units of the weight system;
- 十, ‡, 肆, 戡 used in C_{Ur III/OB};
- I, I, I used in $C_{Ur III/OB}$ —note the overlap with I-III;
- \Join and \Join used in $G_{\text{Ur III}/\text{OB}}$.

Only in the SPVS did numerals exist truly independently of metrology; to quote [Robo8, p. 78]: "The SPVS temporarily changed the status of numbers from properties of real-world objects to independent entities that could be manipulated without regard to [...] metrological system. [...] Once the calculation was done, the result was expressed in the most appropriate metrological units and thus re-entered the natural world as a concrete quantity."

3.3.4 The length system

In the Ur III and Old Babylonian periods, lengths are expressed using overt units counted with $\$ and $\$ numerals with their system $S_{\text{Ur} | \text{III}/\text{OB}}$ values²⁶. Since it does not have any unusual numerals, this system would not in itself be of much relevance to character encoding, but we present it here as background for its Early Dynastic counterpart presented in section 3.4. Metrological tables use the following units [Frio7, p. 118; Rob19]:

Two more units appear occasionally [Pow87, p. 459; Frio7, p. 118; Rob19]:

In addition, there are Akkadian names for the half-rope and half-reed, see [Pow87, pp. 463 sq.].

 $^{^{26}}$ Adjacent units are no more than a factor of 60 apart, so higher numerals such as \P or \diamondsuit are not

²⁷As indicated by the capitalization, the reading of this sign is unknown; see [Pow87, pp. 465 sqq.] for a discussion of various hypotheses.

3.3.5 Fractions

Fractions of the $ik\hat{n}m$, $N = \frac{1}{2}$ — and $N = \frac{1}{4}$ —, have already been encountered. In other contexts, the fraction $\frac{1}{2}$ is written $\frac{1}{4}$, and the fractions $\frac{1}{3}$ and $\frac{2}{3}$ are written $\frac{1}{4}$ and $\frac{1}{4}$. The latter two signs are derived from curviform signs \mathbb{F} and \mathbb{F} , which are already separately encoded; these are in turn derived from the sign \mathbb{F} ($\mathbb{S}U_2$), whose Early dynastic form resembles \mathbb{F} , and \mathbb{F} numerals; see [Powell1971]. The \mathbb{F} is sometimes omitted, as in [P240545; P221530; P221531; P271238; P274845].

3.4 Curviform numerals in early metrologies

At first sight, the metrological systems from the Early Dynastic period resemble the ones previously mentioned. In particular, the discrete counting system used in the Early Dynastic period (and earlier in the Uruk period) clearly mirrors system $S_{\text{Ur III}/OB}$ [Frio7, p. 374; DE87, pp. 127, 165]:

$$\bullet \stackrel{10}{\longleftarrow} \bullet \stackrel{6}{\longleftarrow} \stackrel{10}{\longleftarrow} \stackrel{10}{\longleftarrow} \stackrel{6}{\longleftarrow} \stackrel{10}{\longleftarrow} \stackrel{10}{\longleftarrow} . \tag{S}$$

Likewise the area system used in the Early Dynastic IIIb period for areas of one $ik\hat{u}m$ and greater mirrors system $G_{\text{Ur III}/\text{OB}}$ [LAK, p. 72; NDE93, p. 63; Frio7, p. 378; Lec16]:

$$\bullet \stackrel{10}{\longleftarrow} \bullet \stackrel{6}{\longleftarrow} * \stackrel{10}{\longleftarrow} \bullet \stackrel{3}{\longleftarrow} \stackrel{6}{\longleftarrow} \triangleright, \qquad (G_{\rm ED\,IIIb})$$

with consistent use of the numerals: \bullet corresponds to \langle , \bullet to \diamond , and \bullet to \diamond . An exception to this correspondence, noted in [L2/04-099, p. 4] (see section 3.2), is that the vertical I from $S_{\mathsf{Ur}\;\mathsf{III}/\mathsf{OB}}$ corresponds to a horizontal \triangleright in system S. This is however far from the only case of such a reallocation of function. The earlier form of System G is [DE87, pp. 141, 165; Frio7, p. 378]:

Observe that, as noted in [DE87, p. 142], \odot changes meaning from $10 \bullet$ in system G to $600 \bullet$ in system $G_{ED \, IIIb}$. System G is used in the Uruk period, but also in the ED I–II period (it is the "area 2" system in [Chao3], whereas $G_{ED \, IIIb}$ is the "area 1" system).

Another example of nontrivial correspondence between cuneiform and curviform numerals may be found by comparing the fractions the Early Dynastic IIIb area system²⁸,

with the numerals of a contemporaneous capacity system:

$$\underbrace{\stackrel{10}{\longleftarrow} \stackrel{6}{\longleftarrow} \stackrel{10}{\longleftarrow} \stackrel{4}{\longleftarrow} \stackrel{6}{\longleftarrow} \stackrel{4}{\longleftarrow}, \qquad (C_{\exists \forall \exists \exists \exists \{\}})$$

²⁸A variant is \bigcirc $\stackrel{10}{\leftarrow}$ $\stackrel{6}{\leftarrow}$ $\stackrel{10}{\leftarrow}$ $\stackrel{3}{\leftarrow}$ $\stackrel{6}{\leftarrow}$ $\stackrel{2}{\leftarrow}$ $\stackrel{7}{\leftarrow}$ $\stackrel{2}{\leftarrow}$ $\stackrel{2}{\leftarrow}$ $\stackrel{2}{\leftarrow}$ $\stackrel{2}{\leftarrow}$ $\stackrel{7}{\leftarrow}$, see [Powell1972].

²⁹The cuneiform counterpart is **√**.

system is recognizable, with \neg corresponding to \P for bariga, \P - E corresponding to \P - E for ban₂, and the II counted with \square rather than II numerals. However, the half- $\operatorname{Ik}\hat{u}m$ is counted with the same \triangledown as the bariga, whereas it uses a different sign, $\char`$, in the Old Babylonian system. As we will see, this is cannot be handled as a split, by giving $\char`$ the glyph $\char`$ in an Early Dynastic IIIb font, as the $\char`$ numeral series is also in use in that period.

3.4.1 Field lengths in Nirsu

The length system of the Early Dynastic IIIb state of Lagaš is of particular interest. As described in [Pow87, p. 466; Lec20, pp. 289 sq.], lengths are expressed in rods, but the unit sign \slash is generally omitted; in addition, only tens of rods are used; these are equal to one rope, but the sign \slash is not written either. Lengths shorter than one rope are expressed in half-ropes using the $\frac{1}{2}$ sign \slash (again with no \slash), and then in reeds, with the sign \slash , as follows:

This is the system that was used to express the sides of the field in [P020054] discussed in section 3.2. In that tablet and most others from the same period, such as the ones discussed in [Lec20], areas are expressed in system $G_{\rm ED~IIIb}$, with curviform numerals³³; in the absence of overt units, such as when dealing with length that are integer multiples of a half-rope³⁴, the use of curviform or cuneiform numerals therefore disambiguates a numeric expression between an area and a length, and thus the interpretation of its numerals between systems $G_{\rm ED~IIIb}$ and $L_{\rm ED~IIIb}$. The sign \Box , which would also disambiguate the interpretation as an area, is sometimes used after areas in ED IIIb Lagaš, but not systematically; in particular the area of the first field in [P020054] does not use this suffix. See [Lec20] for many examples with and without \Box . There are other such co-occurrences contrasting between metrological systems; for instance, [Kre98, p. 303 n. 686] mentions the use of cuneiform numerals for days and months³⁵.

3.4.2 Dyke lengths in Nirsu

[Pow87, p. 466] notes that reeds "are regularly written with the normal, cuneiform end of the stylus. Higher units are usually written with the reversed (round) end of the stylus." Powell does not elaborate on the specifics of this mixed use of numerals, but a cursory search in CDLI finds many occurrences³⁶, such as:

 $^{^{32} \}text{The reeds}$ are counted using $ten\hat{u}$ numerals, \nwarrow , \nwarrow , etc.

³⁴This is the case of the sides of the field in [P020054, obv. ii 2–3].

³⁵That note also mentions a contrast between the use of curviform numerals to count people and curviform numerals to count bread alotted to them in [P010876]; such contrasts are more akin to styling, and might not, on their own, justify the disunification.

 $^{^{36}}$ A search for curviform numerals followed by some number of reeds counted in ($ten\hat{u}$) cuneiform numerals currently finds 125 occurrences across 47 tablets.

- [P221305, obv. 1, 4]³⁷ DD 頂≪和無~目>Ⅱ×

These expressions use an explicit sign $V \cong I$ (counted in multiples of ten) or II. This notation—but not its use of curviform numerals—is remarked on in [Lec20, p. 290 n. 27], which cites several of the instances listed above. It seems to be typical of texts about dykes. These³⁹ can be summarized by the following factor diagram:

3.4.3 Butter, cheese and wheat in Nirsu

A similar mixture of cuneiform and curviform numerals may be observed with the capacity system; indeed, the previously described ± 4 (± 1) system uses \rightarrow numerals for \$\(\frac{1}{2}\) [Fri78, p. 43; Lec16]:

as in [P020016; P020065; P020090; P020092; P020137] and others, where ban₂ counted with ₹ numerals are followed by sila₃ counted with ↑ numerals. Curviform numerals are also used to count sila₃, but not⁴¹ as part of the # systems. This contrast can be seen in [P220927], which measures butter (\implies , i_3) with a different capacity system, using the ♠ (dug, "pot") of 20 ≯, with ▷ and • numerals 42 for both the and the \$\frac{1}{2}\$, thus [Pow87, pp. 504 sq.]

$$\underbrace{\bullet \overset{10}{\longleftrightarrow} \smile}_{=} \overset{2}{\longleftrightarrow} \underbrace{\bullet \overset{10}{\longleftrightarrow} \smile}_{?} \overset{\frac{3}{2}}{\longleftrightarrow} \stackrel{10}{\longleftrightarrow} \smile_{?} \overset{1}{\longleftrightarrow}_{?} \stackrel{1}{\longleftrightarrow}_{?} \stackrel{1}{\longleftrightarrow}_{?}$$

but counts cheese (\bowtie , ga'ar) using the \boxplus \sqsubseteq capacity system, with \searrow numerals for the 3.

³⁷CDLI only has a copy, but a photo may be found in [Lec12, p. 82]. On that photo the ▮► II * is not visible. Lecompte notes that the copy is faithful; indeed another \[\bigsir \big| \cdot \cdot \cdot \cdot \cap \] can be seen both on the copy and the photo on obv. 2, 2.

³⁸ From copy.

³⁹TODO Cite also DP 568, the one with \square and \square \square even though it has no reeds.

 $^{^{40}}$ With either unit omitted, as in the examples above, or both, as in [P020129, obv. 2, 1] \bigcirc \bullet \otimes \clubsuit

⁴¹As of this writing, the single occurrence of (ban2@c) followed by curviform numerals and sila3 in ED IIIb Nirsu transliterations on CDLI, 4(ban2@c) 3(asz@c) sila3 in [P221815], is incorrect: it should be 4(ban2@c) 3(disz@t) sila3.

 $^{^{42}}$ This tablet also uses subtractive notation: DD \clubsuit \sqcap "two pots minus one third (sila $_3$)", metrological systems discussed here; it appears in the ED IIIa period [Robo8, p. 77]. We shall not discuss it further, as presents no complexity for character encoding. It is noteworthy that the sign [(lal₂, "minus") is often ligated with the following numerals, with the subtrahend placed under a sometimes considerably enlarged Γ , similar to the layout of the radical in modern mathematical notation, see, e.g., [P020092].

Another capacity system in ED IIIb Ŋirsu is the ♯ < ᡮ , the gur of two ul:

$$\underbrace{\stackrel{10}{\leftarrow} \stackrel{\triangleright}{\smile} \stackrel{2}{\leftarrow} \triangledown \stackrel{6}{\leftarrow} \triangledown \stackrel{6}{\leftarrow} \checkmark }_{\exists 1 \cdot \langle C \rangle}) \qquad \qquad (C_{\exists 1 \cdot \langle C \rangle})$$

Here the ▷-\-▽ contrast occurs not only within the numerals of the system, but with its units; this is perhaps best illustrated by the expressions 🛎 💷 🧏

3.4.4 Grain in Ebla

The mixing of curviform and cuneiform numerals within a metrological system is not specific to Nirsu.

The system of grain⁴³ capacities in Ebla uses the following units⁴⁴:

The □ and □ □ are generally counted using curviform numerals, and the smaller units using cuneiform I numerals. Indeed, a search on [EbDA] for cooccurrences of either ★☆ or 🏿 🖈 with either of 🖈 🗘 or 🗗 🗏 finds the following expressions⁴⁵:

- 3. [P240655, recto 7, 9] DD ₩ L 48 ₩ 1 1 1
- 4. [P240579, verso 4, 3] BBD □ □ □ L IIV L □
- 5. [P240675, verso 2, 2] ▷ 縱 日出 ₩ W L (口)
- 6. [P240609, verso 3, 1] ▷◁∄珊 \\\
- 7. [P240533, recto 3, 3] ♣▷▽□♠L ₩V{←| ||+*-♦||
- 8. [P240697, recto 1, 5] ▷ ▽ ⁴⁹ ||]||| || * ↔

At a glance it seems that 🕽 are counted with cuneiform numerals and higher units with curviform ones,

but we have not investigated this thoroughly.

⁴⁴TODO mention the other one citing Chambon and the footnote in Archi

⁴⁵We cite here only one attestation per tablet; most tablets contain several expressions mixing curviform 🗗 🖽 and larger with cuneiform 🎹 and smaller. In all cases the transcriptions given here are based on the EbDA transliterations, but the shape and orientation of the numerals was checked 46 on a photograph (from EbDA unless noted otherwise).

⁴⁶As we will see in Section 3.7.2, CDLI transliterations indicate numeral shape; however, as of this writing, they do so incorrectly on the Ebla corpus, claiming that all numerals are curviform, so we were not able to rely on them in this specific case.

⁴⁷ba-ri₂-zu₂, a variant spelling.

⁴³Liquid capacities use a different system [Arc15, p. 229 n. 12]:

⁴⁸Short for 🛱 🛴

⁴⁹Note the omitted ☑ ↓ .

⁵⁰Instead of the expected ₩ 【 🖈 🗎 .

⁵¹ **!!!** ★ ← not legible on the EbDA photo.

3.4.5 Use in modern publications

Because of their prevalence in the Uruk and Early Dynastic periods, the proposed numerals are widely used in modern publications discussing metrology in those periods, as illustrated in Figures 3–16.

⁵²From CDLI photo.

⁵³From photo in [Arc89, p. 6].

⁵⁴Laid out as [[]]; on stacking patterns see Section 6.2.

⁵⁵The untransliterated text would be 器戶耳遭回▷器以數回數量 []; note the atomically encoded ib₂ × 3! = 至 × III = 至數.

⁵⁶TODO cite the EbDA one.

⁵⁷TODO(egg): On the order cite TSS 188, Friberg2007 p. 148 and any of the usual suspects on the haphazard order of signs in early texts; contrast P274845, P241764.

These metrological equations for the "unknowns" \emptyset , \circ , $\overline{\mathbb{V}}$, etc., can be treated exactly as ordinary equations for unknowns x, y, z,.... In particular, the equations can be simplified by subtraction of equal amounts from both sides of the identities. In this way the three equations above can be reduced to:

We can now read off from the first equation that 1° = 10° , and from the second that 1° = 6° . Then the third equation can be simplified (by "substitution" of these values into the equation), to the following reduced form:

```
1 Dell = 2 V 9 Da.
```

The most likely solution to this last equation is, of course,

```
1 DQ = 2 \overline{Q}, 1 DQ = 10 DQ.
```

Figure 1: TODO [Fri78, p. 15]

Thus, for instance, the original set of fractions σ , σ , and δ (1/2, 1/4 and 1/8 of an iku) in the Sumerian GANA system was after a time augmented through the addition of the new sub-unit SAR: $\frac{1}{2}$, equal to 1/100 of an iku (D). Similarly, the Sumerian weight unit "ma-na" which originally may have had only the sub-units σ sa-na (= 1/3 mana) and σ sa-na-bi (= 2/3 mana), and perhaps also gin: σ (= 1/60 mana), seems to have acquired, at some time or other, also the smaller sub-units

 σ (= 1/3 gin) , and m - Se(= 1/3 × 1/60 gin).

Figure 2: TODO [Fri78, p. 49]

Figure 3: TODO [Englund1988]

of decreasing fractions $^1/_n$ of this measure, whereby "n" was determined by the number of oblique impressions made by the rounded end of a thin stylus around a central point in a specific sign. Thus $\Xi=^1/_2$ N_{39} , $\varpi=^1/_3$ N_{39} , and so on. The first sign of the latter units, N_{34} ,

Figure 4: TODO [Eng98, p. 113]

For instance, the first line contains the notations $1N_{34} 1N_{396}$; $2N_{20}$, which can be translated "60 of the (grain rations containing) \rightleftharpoons (of grain); (grain involved:) $2 \bullet$ (of ground barley)". This calculation contradicts the assumed numerical relationship $10N_1 = 1N_{14}$, since as was well known the measure represented by the sign N_{39} was 1/5 of that represented by N_1 , so that $60 \times 1/5 = 12$ and not 20, as $2N_{14}$ would imply. Instead of relying on complicated

Figure 5: TODO [Eng98, p. 116]

Die halbkreisförmigen Griffeleindrücke gehen manchmal in mehr oder weniger eckige Formen über ($\sqrt[n]{}$)685. Es gibt aber auch Einer in Form von regelrechten – meist mehr oder weniger schräggestellten – Keilen (\mathbb{N}) , die öfters neben halbrunden Einern vorkommen und mit diesen kontrastieren 686 . Selten treten mit \odot gebildete Zahlen auf 687 (sie entsprechen den bariga-Zahlen im Hohlmaßsystem, s.u. 7.4).

Figure 6: TODO [Kre98, p. 303]

The calculations:									
Obv. i	1	60 × ¹ / ₅ ເ⊃	()	=	12 × ⋅ □ =	$2 \times 10^{\circ}$			
	2	$120 \times {}^{1}/_{10} \triangleright$	(⊠)	=	12 × ⋅ = =	$2 \times 10^{\circ}$			
	3	$120 \times {}^{1}/_{15} \triangleright$	(₹)	=	8 × 100 =	$1 \times 10^{\circ}$	$2 \times =$		
	4	$300 \times {}^{1}/_{20} \triangleright$	(ı⊠ı)	=	15 × ₪ =	$2 \times 10^{\circ}$	3 × ₁⊳		
	5	$600 \times ^{1}/_{25} \triangleright$	(129)	=	24 × ==	4 imes			
Rev. i	1	1200			1 × ¹• €.	1 × . • • ;	5 × 1⊳		
Obv. i	6	$6000^{1}\hspace{-0.1cm}/_{\hspace{-0.1cm}30}\hspace{0.05cm}$	$(GAR+6N_{57})$	= 1	200 × ₪ = 1 × 🎑	$3\times 100\mathrm{G}$	2 × 100		
ii	1	120 × ≈ 1/4 ▷	(DUG _a +U _{2a})	≈	30 × 1≥ =	5 ×	1 × ₁⇔	1 × 😓	
	2	$180 \times \frac{1}{5}$	(DUG+AŠa)	=	36 × ⋅ □ =	$6 \times 10^{\circ}$			
	3	$300 \times 1/_{15}$	(KAŠ _a)	=	20 × ₽ =	$3 \times \bullet$	$2 \times =$		
Rev. i	3	600			1 × °●.	4 × · • ;	3 × 1⊏	_1 × ▽	
					1 × ¹●:	1×.00;	5 × ₁□	='	
					1 × 🖸	3 imes 100	2×10^{-1}		
					1 × ¹•.	4×100	3× ₁⇨	1 × 🖘	
Grand total of groats used: $1 \times 2 \times $							4 × ₁⊳	1× 🖘	
Grand t	total	of malt used: 1N	8 × •.	4× ₽	1 × □				

Figure 6. Transliteration and calculations of MSVO 4, 66.

Figure 7: TODO [Englund2001]

strong similarities between "area" 1 and "area" 3 systems, the sign with two concentric discs (\bigcirc , notated N_{50}^{27}) remains problematic. It never appears in any numerical combination with the sign with a single disc (),

Figure 8: TODO [Chao3, p. 6]

 $1/_{15}$, etc., of gur, we would expect the metrogram gur to appear in sub-column ii. In a certain way, it does for larger measures: the notation T H could be understood as 1 ½ gur. 27 However, the metrogram gur does not appear for lower measures. It would not be consistent of the consistence of 21,600 etc. tent to attribute different functions to the same graphrme, according to the relative importance (be it great or small) of the quantity, so the signs + and + cannot be considered klasmatograms.

The signs iku and $e^{3}e_{3}$ constitute by themselves measures of surface areas. These measures are usually followed by the sign GAN_{2} , which means either surface or field and

Metrological tablets from the end of the 4th millenni-um (Nissen, Damerow and Englund 1993, 55-59, to MSVO 1, nos. 2-3) contain a discrete set of numerical

1(iku) represents a surface of 3600m² 1(eše₃) represents a surface of 21,600m² etc.

Figure 9: Discussion of Old Babylonian and fourth millenium area measures in [Proust2020]. The cuneiform text is Unicode-encoded.

formed by only two signs $\ \$ and $\ \$, repeated as many times as necessary; this type of notation is highly standardized. Second, the order of magnitude of the numbers noted in this system is not indicated: 1, 60, 60², 60³, 1/60, 1/60², etc. are written in the same way, with the vertical wedge $\ \ \$. The third feature concerns the exact function of

Figure 10: TODO [Cha12, p. 58]

one step. The scribes of the Early Dynastic Period (c. 2600 BC), for instance, represented the number 648, 000 with:

Figure 11: TODO [Cha12, p. 59]⁵⁷

repetition of the same sign refers to both the capacity unit signified—often but not necessarily written immediately afterwards—and its value. The units of measurement are written in descending order from left to right—just as we would write 3 km, 120 m, 50 cm. For example:

DDD še bar ∇ ba-rí-zu

'3 gubar (capacity units) and 1 parīsu'.

Figure 12: TODO [Cha12, p. 61]

This is particularly true of the signs \nearrow , \rightleftharpoons , \rightleftharpoons and \rightleftharpoons , whose form explicitly denotes the fractions 1/6, 2/6, 3/6, and 4/6 of the barig capacity measure written \bigcirc in Mesopotamia—also transcribed by Assyriologists as 1 bán, 2 bán, 3 bán, and 4 bán with reference to the bán measure worth 1/6 of the barig. At Ebla, the sign \bigcirc is most often associated with the *parīsu* measure, while the signs \triangleright , \rightleftharpoons , \rightleftharpoons , and \rightleftharpoons refer to 1, 2, 3,

Figure 13: TODO [Cha12, p. 64]

shape. The principle of notation is additive: each sign is noted as many times as necessary (e.g., transliterated as $2(\tilde{s}ar_2)$ $1(ge\tilde{s}'u)$ 3(u), means $2\times 3600+1\times 600+3\times 10$). The system is based on an alternation of factors ten and

Figure 14: TODO

might think of one fabric and a half, ¹¹ but the presence of notations with " $2^D 2^{\mathbb{T}'}$, " $3^D 3^{\mathbb{T}'}$ ", and " $6^D 6^{\mathbb{T}'}$ " (Fig. 1) elements excludes that one deals with fractions, as these notations are not consistent with those of Šuruppag's weight measurement system. ¹² The notation " 1^D gada" in o. ii 1 and r. vi 1, along with the total of "39

Fig. 1. Combinations of numerals attested in Š. 742.

Figure 15: Discussion of the contrast between ▷ and ¬ numerals in [Gor23, p. 162].

```
as, for example, in TM.75.G.3125 = ARET III 107 o. iv 1, "4D \,^{5}a_{3}da-um^{tu9}-2 \,^{6}4\overline{U} aktum 4D \,^{5}b_{2}^{tu9}\times 3\overline{U} \,^{5}sa_{8}\,gunu_{3}" (Fig. 2).
```

Figure 16: Transliteration in [Gor23, p. 163] of [P242293, recto 4, 1] incorporating untransliterated numerals.

3.5 Non-numeric usage

Examenstext A

Many of the cuneiform numerals are used with a logographic or phonetic value. For example, the sign — has, *inter alia*, the values aš, rum, and dili. While the horizontal numerals are most frequently written \triangleright in the Early Dynastic period⁶⁰, such non-numeric usage is almost⁶¹ always written —, for instance:

- in personal names in administrative texts, such as the following, which all contain ▷ numerals:
 - → إلى الله in [P010424; P010458; P010459] from ED IIIa أبو صلابيخ
 - → in [**P010960**] from ED IIIa Šuruppag,
 - 種世ー in [P251641] from ED IIIb Adab,
 - < IIIb Adab, rom ED IIIb Adab,
 - ₱>> **I** > in [**P298637**] from ED IIIb Umma;
- in lexical texts:
 - in the divine name *** ! ! !** in the lexical texts [**P010570**; **P010572**], where the entries are prefixed with **□**.
 - in the word ➤ dili, "small fish" in [P010578], witness to Early Dynastic Fish,
 - in the same word with a determinative, ¬ k dili^{ku6}, in [P010586], witness to Early Dynastic Food, which starts with □ numerals.

This is a clear contrast between - and \triangleright in this period, and genuine ambiguity can arise if it is lost; for instance, the personal name - $\triangleleft \Box$ occurs on its own line in the aforementioned administrative texts; a line $\triangleright \triangleleft \Box$ would instead be read as

 $^{^{58}} The\ reader\ will\ recall\ that\ \eta e \S_2$ is written \P , with a larger wedge than \P ; however, these signs have merged by the time Examenstext A is composed.

 $^{^{59}}$ Besides η es $_2$, a look at [OSL] shows that the values dis, ge $_3$, makkas, sa η tak $_4$, and tal $_4$ are attested both in [ePSD2] and in lexical lists. The sign is also used for the Akkadian word ana in the Neo-Assyrian period.

⁶⁰A CDLI search for "(asz@c)" finds 3296 ED texts, while a search for "(asz)" finds 81 ED texts, of which 46 also contain "(asz@c)".

⁶¹Exceptions are discussed in section 3.7.1.

3.6 Limited benefits of diachronic encoding for numerals

The argument in favour of diachronic encoding is that it facilitates interoperability in a variety of use cases, as we have outlined in section 3.1. While these benefits are real and now visible for cuneiform signs, similar considerations are not generally applicable to curviform numerals.

Diachronic reference works such as sign lists and dictionaries tend to not include numbers, or when they do, they treat them separately, and include signs such as — that have both numeric and non-numeric values in both the main list and the section on numbers. For instance, [KWU, pp. 123 sqq.] lists all of —— together with \square —— together with \square ——, while \square —, and \square —, and only those, appear at the beginning of the sign list, since they have non-numeric values \square [PTACE, p. 58] has the numeric signs \square —, , , , whereas non-numeric — is at the beginning of the sign list, where its values \square and \square are listed. For signs with both non-numeric and numeric usage, [LAK] writes n0. And n1. One should note [MZL], which has numbers at LAK 829 together with \square —, , and n1. One should note [MZL], which has numbers throughout the sign list; but that sign list does not show glyphs predating the Old Babylonian period, nor does it comprehensively cover the numerals used in the Ur III and Old Babylonian periods, as, for instance, it does not have used in system used in and includes signs such as includes and include signs such as includes and include signs such as includes and include signs such as includes and includes includes includes and includes includes

Composite texts rarely have witnesses both from the Early Dynastic period and later; the kinds of texts that do, chiefly lexical and literary texts, do not contain numbers to the extent that administrative texts do. Further, there tend to be changes 63 to the text between Early Dynastic and later witnesses that prevent a diachronic encoding of such composites. For numerals, the switch from \triangleright to ! numerals prevents diachronic encoding even if \triangleright were unified with \leftarrow . For instance, the lexical list Early Dynastic Food, already mentioned in section 3.5, contains some numbers, and has a witness from the Old Akkadian period covering these numbers: [P215653, a 1'-6']; however, they are written with ! numerals, whereas they are written with \triangleright numerals in the Early Dynastic witnesses; since ! and \leftarrow are distinct ! characters, the \triangleright - \vdash unification does not help.

More generally, since numbers are so deeply tied to metrology, and since metrological systems change between the Early Dynastic and later periods⁶⁵, there is little opportunity for a diachronic representation of numeric quantities.

In the case of analyses such as [Romach2023], it is interesting to note that numeric expressions are removed prior to the conversion of the corpus to Unicode cuneiform for further analysis.

 $^{^{62}}$ Non-numeric values of — were discussed in section 3.5; — has the values man₃ and min₅, and is used for the word didli, "several, various"; — has the value e \S_6 .

⁶³TODO comment on the ED witnesses to the instructions of Šuruppag

⁶⁴Besides the contrasts in numeric usage mentioned in section 3.3.3, these (already-encoded) characters were clearly not unifiable because of the many contrasts in non-numeric usage between them; several values of — which are not shared with ! have already been mentioned, but perhaps most striking is the fact that, in the Neo-Assyrian period, — is used for the preposition *ina*, "in", and ! for the preposition *ana*, "to".

⁶⁵TODO cite a few things here.

3.7 Compatibility considerations

A disunification twenty years after the fact, affecting all numerals, would ordinarily be a serious compatibility issue. Fortunately, with the exception of one character discussed below, we are not aware of any font using curviform glyphs for the already-encoded numerals. In fact we are not aware of any font designed for a style earlier than Old Babylonian, except for fonts mimicking the representative glyphs from the code charts, which are primarily Ur III, but sometimes earlier or later, as described in [UTR56, §2.4]. The lack of dedicated Ur III fonts may be explainable by the chartlike fonts⁶⁶ being good enough for most purposes; the lack of Early Dynastic fonts, by the aforementioned issues with numeral unification making the representation of any text with numerals intractable.

3.7.1 The case of ŠAR₂

The character U+122B9 ■ CUNEIFORM SIGN SHAR2 has a circular reference glyph.

In most texts from the Early Dynastic IIIb and Old Akkadian period⁶⁷, a contrast between non-numeric $\$ar_2$ written \diamondsuit and numeric $1(\$ar_2^c)$ written $\textcircled{\bullet}$ can be observed, similar to the contrast between \longleftarrow and \bowtie previously discussed in section 3.5. However, in lexical lists from $\verb§Suruppag§$ and $\verb§Ebla§^{68}$, as well as in the $St\`ele\ des\ vautours$, non-numeric $\$ar_2$ is curviform:

- * # and * # + = in [P010566];
- → → and ★ → in [P010576];
- \blacksquare **♠** in [P222399, obv. 17, 9, 18, 11, 22, 12]⁷⁰.

It would be disruptive to the diachronic representation of text if non-numeric $\operatorname{\check{s}ar_2}$ were to have two different representations. The character U+122B9 CUNEIFORM SIGN SHAR2 should therefore be used in those cases, with its curviform glyph \diamondsuit , identical to the glyph of the proposed U+12579 \blacksquare CUNEIFORM NUMERIC SIGN ONE N45. Since the archaizing style of texts wherein non-numeric $\operatorname{\check{s}ar_2}$ is curviform solidly predates the transition from \blacksquare to \diamondsuit in the relevant metrological systems, there is no need to represent a \diamondsuit - \blacksquare contrast, so these characters can have the same glyph in specialist archaizing Early Dynastic fonts.

Since cuneiform U+122B9 CUNEIFORM SIGN SHAR2 effectively merges with U+1212D CUNEIFORM SIGN HI, the reference glyph should remain as it is, *i.e.*, curviform, so that the contrast between reference glyphs within the Cuneiform block remains clear; see [UTR56, §2.4]. Since system fonts follow the reference glyphs, and since extant specialist fonts target styles where U+122B9 is unambiguously cuneiform, there are no compatibility issues.

⁶⁶Most prominently Noto Sans Cuneiform, a system font on both Windows—as part of Segoe UI Historic—and macOS.

⁶⁷For example, in personal names:

[—] 具食◇幫 in [P020019] from ED IIIb Nirsu;

[—] 澤下令 配料 in [P020182], also from ED IIIb Nirsu;

[—] **♦** ★ ♦ in [**P222186**] from ED IIIb Umma;

^{— 💾 🛠 🍴 ♦} in [**P235312**] from Old Akkadian Umma.

 $^{^{68}\}mbox{TODO}$ Mention other ways in which these are archaizing

⁶⁹From copy in [ELLes, No. 397].

 $^{^{70}}$ Note however * \Rightarrow \diamondsuit 包 on [P222399, obv. 6, 17]. Curviform non-numeric \sin_2 is clearly archaizing in ED IIIb Nirsu; one might suppose that the scribe slipped into their modern ways here. TODO add a photo.

Note that in rare cases, such as [P222243] from ED IIIa Adab, non-numeric — (here with the value rum) is written \triangleright . It is out of scope for this proposal to decide whether such occurrences should be treated as anomalous spellings, encoded as U+12550 \triangleright cuneiform numeric sign one NO1, or as stylistic distinctions, encoded as U+12038 CUNEIFORM SIGN ASH with a curviform glyph. in practice this would often be determined by the transliteration from which the cuneiform text is generated; it is noteworthy that as of this writing, the CDLI transliteration (UR2-1(aš@c)) and the ePSD2 one (uru₈rum) of this word disagree on that aspect. Since — has a cuneiform reference glyph, this does not pose any compatibility concerns.

3.7.2 Transliteration

The situation is more complicated for numbers. Many transliterations do not represent the type of numeral used, instead interpreting the whole numeric expression and transcribing it with delimiters or units as needed to disambiguate. For instance, [$\mbox{$\mathbb{M}$}\cong\mbox{$\mathbb{M}$}$] from [P305639] may be transliterated as 95 gur, as in [Feu04, vol. 2, p. 62]. The numerals may also be transliterated separately, but solely by their values in terms of the overt unit, as in EbDA transliterations: the aforementioned $\mbox{$\mathbb{M}$}$ $\mbox{$\mathbb{M}$

This practice has been generalized to systematically indicate numeral shape; this is in particular the case in CDLI, where the transliterations of some the above examples are "1(gesz2) 3(u) 5(asz) gur" for \(\mathbb{H}\) \(\mathbb{H}\), "1(esze3) 5(iku) 1/2(iku) GAN2 7(disz) sar" for \(\mathbb{H}\) \(\mat

⁷¹As on [P249253].

 $^{^{72}\}text{As}$ of this writing, EbDA actually has an-zam $_{\chi}$, with U+1D6A greek subscript small letter chi.

⁷³TODO say something about this reading

⁷⁴TODO comment on nigida.

3.8 Conclusions

Co-occurences of curviform and cuneiform numerals are not anecdotal in the Early Dynastic period, nor are they the result of scribal idosyncrasy. Instead, they represent systematic contrasts between metrological systems, between individual units within metrological system, and between numeric usage and phonetic or logographic usage. This contrastive usage is reflected in modern publications. The contrast frequently applies to individual numerals, rather than to the span of entire numeric expressions.

While it would be technically possible to handle this contrast as a stylistic distinction, this approach has no real benefit, and is highly inconvenient, as it would require any treatment of Early Dynastic administrative texts to use multiple cuneiform fonts, often within single numeric expressions. Further, if that contrast is lost in plain-text interchange, the text can be misinterpreted: (is a length of three ropes, but (is an area of three bur $_3$; (could be read as one () and one () where () would be one and a half ()) is a personal name, but () would be "one slave".

TODO mention the risk of confusion about character identity.

At the same time, contrary to most disunifications, the separate encoding of curviform numerals poses no serious compatibility issues for existing fonts or encoded corpora, nor does it, in general, introduce new issues with transliterated third millenium corpora. The oddity of requires some explanation, but does not pose any architectural issues, and is not fundamentally different from the other mergers and splits encountered in the cuneiform script.

4 Rationale for ED-Uruk numeral unification

A complete rationale for disunification between the non-numeric signs used in the fourth millenium and the already-encoded cuneiform signs will be given in the forthcoming proto-cuneiform encoding proposal. The core issue with extending the cuneiform script further back in time is that, since 1987, fourth millenium studies have used a different model of character identity and associated transliteration conventions, with names being given to structurally different glyphs, and no attempt being made at assigning phonetic values to them.

This is not a mere classification of glyph variants, as contrastive meanings of these systematic variants can often be reconstructed, with, e.g., signs KAŠa, KAŠb, and KAŠc, depicting filled jars with a spout (a), a handle (c), or neither (b), being understood as referring to containers of different substances, see [Englund2001]. However, not all identified systematic variants are understood, and the general approach to character identity is closer to that used for undeciphered or partially deciphered script.

As part of the development of these conventions, a classification of fourth millenium numeric signs was developed; see [DE87]. This classification assigns to each unit numerals an identifier formed by the letter N with a numeric subscript (sometimes with an additional alphabetic subscript): N_1 is \triangleright , N_{14} is \bullet , N_{34} is \triangleright , etc. Transliterations of numeric expression then use those to identify the type of number used, thus $5N_1$ is \triangleright , and $5N_{14}$ is \bullet .

In contrast with the use of parenthetical unit names, this approach does not require interpreting the quantity being counted. This is valuable in contexts where numerals are being used atypically, as conventional transliterations can otherwise force a dubious interpretation. For instance, the CDLI transliteration of problem of problem in [P283802] currently uses (barig@c) for the vertical numerals, since numerals are typically capacity measures; but [Gor23] interprets these instead as counting linen textiles. As a result, the fourth millenium conventions for numeral transliteration are used in Early Dynastic texts, especially those from the ED I–II period, even though the Sumerian text uses classical assyriological transliteration conventions.

While the non-numeric signs are treated as undeciphered, the metrological systems used in the fourth millenium are well understood, as can be seen in [DE87, p. 165]. As a result, contrary to the non-numeric proto-cuneiform conventions, these numeric transliteration conventions are compatible with the classical ones described in section 3.7.2; they are indeed used interchangeably, as in [P011104] which uses the notation u@f in [ePSD2], but N14@f in CDLI. Indeed, the numerals are used similarly in Early Dynastic metrological systems, and are visually identical.

A disunification of numerals between the third and fourth millenium would therefore induce confusion as to which numerals should be used in third millenium studies, and would needlessly duplicate the encoding of at least seventy characters; by splitting the attestations, these separate encoding proposals would run into additional difficulties to supply evidence for encoding.

Note that the structural variants designated by letters in fourth millenium notation have systematically been encoded, as they have occasionally be found to carry distinct numeric meaning. For instance, N_{30c} is listed as a variant of N_{30a} in [DE87, p. 166], where the numeric value of either in relation to N_{29a} is still unknown, but their values are found in [**Englund2004**] to be $= \frac{1}{10}$, whereas $= \frac{1}{6}$.

5 Considerations on individual numeral series

[TODO Document to the extent possible the metrological systems in which each sign is used. Note the disunification of N9 and N10 from $4(ban_2@c)$ and $5(ban_2@c)$.]

6 Characters not included in this proposal

6.1 Missing numerals

TODO N13 not attested in CDLI TODO (N_{17} not usefully numeric, $12N_{14}$ not encodable, etc.). Cite [DE87, p. 147] 7 and 8(diš $ten\hat{u}$) encodable, but not today; want to go into the Cuneiform Numbers and Punctuation block for sanity.

6.2 Stacking patterns

The already-encoded numerals in the Cuneiform Numbers and Punctuation block distinguish some $stacking\ patterns$; for instance 91 is encoded both as U+12446 $\mbox{\ mathematical mathem$

However, the stacking patterns from earlier periods are not separately encoded; for instance, in ED IIIb Nirsu, $\langle\!\langle 2(u)\rangle\rangle$ often has one $\langle\!\langle$ atop another. These older stacking patterns do not appear to be contrastive, are not marked in transliteration, and are not listed separately in sign lists nor assigned any different values. There is therefore no evidence of a need to encode them; instead, they should be considered style variants, and an ED IIIb Nirsu font should have an appropriate glyph for U+12399 $\langle\!\langle$ CUNEIFORM SIGN U U.

Likewise, many stacking patterns are attested for the curviform numerals proposed in this document, and it is not proposed to separately encode them; these distinctions would be incompatible with the state of the art in numeric transliterations, and are not needed to represent reference works. Idiosyncratic stacking patterns are in fact particularly common in Early Dynastic and earlier tablets, as they are structured in rectangular cases rather than lines, so that numerals may be laid out across the case in whichever way fits the available space; this is illustrated in Figure 17. Note also that the numerals need to be considerably enlarged in order to reproduce the layout of the tablets, so that \$ often spans two lines of cuneiform signs, as shown in Figure 18. This is impractical when these numerals are set in text that contrasts them with the larger \(\bigcirc\), and inconsistent with actual practice when typesetting these numerals, as illustrated in Figure 3: reproducing the layout of tablets is not within the scope of plain text.

The reference glyphs use stacking patterns that are common in the Early Dynastic period, but that are also attested in the Uruk period; the Uruk period also

⁷⁵The Sumerian word limmu means "four", so limmu and limmu₅ are still numbers. The distinction here is between usage in transliterations of phrases such as $\clubsuit \Leftrightarrow \P \Vdash \exists \blacksquare$ lugal an-ub-da limmu₅-ba-ke₄ (king of the four quarters) or of names, and of numeric expressions such as $\Vdash \exists \exists \blacksquare$ 4(diš) sila₃.



Figure 17: The layout of case [**P011099**]; the numeral \$\frac{1}{2}\$ is rotated to fit the rounded corner of the tablet.

Figure 18: The layout of case [**P020066**]; the numeral **\$** is spread across two lines. The text is read in the order **\$**▷▷ ★ ****, "twenty-two oxen, one year old".

frequently features numerals that use a more vertical layout, as illustrated in Figure 19. The later, more horizontal styles were chosen for two reasons: for the numerals used in the third and fourth millenium, usage in third millenium scholarship will be more frequent; and the horizontal layout poses fewer layout difficulties when set in lines of non-cuneiform text, as most modern scholarship is. Indeed, the absolute size of the indents \triangleright , \triangleright , \bullet , and \bullet must remain consistent across the numeral series, lest a \triangleright numeral be confused with an \triangleright numeral. Since the single indents are frequently used in running text, as illustrated in section 3.4.5, they need to be large enough that the vertical stacking patterns are impractical.

Variant stacking patterns, if needed, may be handled at a higher level as stylistic distinctions; Figure 19 uses OpenType stylistic alternates, and Figure 17 rotates the character \$\mathbf{s}\$, in both cases preserving the plain text backing.

6.3 Other glyph variants not reflected in transliteration

TODO Comment on the nameless variant glyphs from L2/23-190 and note that they are illustrating an even wider glyphic range as shown in [**Englund2001**].

Acknowledgements

TODO(egg): Something about the Vanséveren fonts

Figure 19: Three stacking patterns for U+12573 CUNEIFORM NUMERIC SIGN NINE N34. The one on the left is the reference glyph, used in Uruk III [P003499; P004430], and widely afterwards, *e.g.*, ED IIIa Šuruppag [P010678], ED IIIb Nirsu [P020057], Old Akkadian Umma [P212464]. The ones in the middle and right are used in two Uruk IV tablets [P001243; P004500]. All three Uruk examples are transliterated 9(N34) in CDLI.

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