Archaic cuneiform numbers

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	Uruk III & earlier	ED – Ur III	OB & later
Numerals	This proposal		
Numerals		Existing Xsux	
Non-numeric signs	Future Pcun		

Table 1: Usage of existing, proposed, and future characters across functions and time periods.

1 Summary

This document proposes encoding some numerals used in the Uruk and Early Dynastic periods in conjunction with the Sumero-Akkadian cuneiform script¹ and the proto-cuneiform script². The proposed characters are listed in section 2.

The non-numeric signs of proto-cuneiform will be the subject of a separate proposal; we need only note here that the divergence between the approaches to character identity in modern scholarship requires that proto-cuneiform be disunified from cuneiform: proto-cuneiform is effectively treated as an undeciphered script. In contrast, the cuneiform encoding model is semantic, requiring an understanding of the text to correctly encode it.

However, the *numerals* used in proto-cuneiform should be unified with ones used in the Early Dynastic period, for the reasons set forth in section 4. The proposed "curved", or "curviform", numerals³ should however *not* be unified with the already-encoded cuneiform numerals⁴. Since the encoding proposals for the cuneiform script twenty years ago provisionally considered the curviform numerals to be glyph variants of the cuneiform numerals, a detailed rationale is provided in section 3, including compatibility considerations in section 3.7.

The overall picture of unifications and disunifications over time is illustrated in table 1. The Script_Extensions property assignments in section 2.2 reflect the overlap.

[TODO(egg): Mention the other sections here too.]

2 Proposed changes to the Standard

- 2.1 Summary of proposed characters
- 2.2 Properties
- 2.3 Character names list
- 2.4 Core specification text

3 Rationale for curviform-cuneiform disunification

TODO(egg): blurb.

 $^{^1} ISO$ 15924: Xsux, Script property value long name: Cuneiform; encoded since Unicode Version 5.0. $^2 ISO$ 15924: Pcun, not yet encoded.

 $^{^{3}}$ ▷ -III 1-9(aš° = N_{1}), · -# 1-5(u° = N_{14}), ▷ -||| 1-9(ŋeš₂° = N_{34}), ▷ -||| 1-5(ŋeš'u° = N_{48}), etc. 4 ▷ -||| 1-9(aš), <-||| 1-9(neš₂), \[\] - \[\] 1-5(ŋeš'u), etc.

3.1 The cuneiform encoding model

As outlined in, *e.g.*, [UTR56], the cuneiform encoding model is diachronic; each character may have wildly different glyphs depending on time period and region. For instance, the sign IM may resemble in texts from Early Dynastic IIIa Šuruppag as in the character code charts, if later in the third millenium⁵, if in Old Babylonian cursive, if in Neo-Assyrian, but is always encoded as U+1214E CUNEIFORM SIGN IM.

This encoding model allows for the interoperable representation of editions of diachronic reference works such as sign lists⁶ and dictionaries⁷, and of composite texts⁸. By being compatible with similarly diachronic transliteration practice (that is, by avoiding distinctions finer than those made in transliteration), the encoding model also allows for automated conversion of transliterated corpora to cuneiform, which has proven useful as a processing step in analyses such as [Rom24; JJ24]⁹. The diachronic approach is also useful for pedagogical applications¹⁰.

3.2 Arguments for curviform-cuneiform unification

In this context, the argument was made in [And04], as part of discussion of the cuneiform encoding¹¹ that the curviform numerals, which occasionally appear in the Ur III period and are used heavily in the Early Dynastic period, were a stylistic distinction unifiable with the cuneiform digits, and that an archaizing Ur III font or an Early Dynastic font could have curviform glyphs for the appropriate characters.

Some co-occurrence of curviform and cuneiform digits was known and acknowledged. [Ando4, p. 3] cites [NDE93, p. 62], which is a copy of [P020054], an Early Dynastic IIIb administrative tablet from Nirsu. The excerpt cited, lines 1–3 of column 1 of the obverse, is as follows:

 $^{^5} Merging$ with U+1224E $\mbox{\em NI}_2.$

⁶Notably [VT+14] and the online edition of [Bor10] in [Jim+23, Signs].

⁷Notably [TJV17] and the online edition of [Sch10] in [Jim+23, Dictionary].

 $^{^8}$ For example, there are Neo-Assyrian and Neo-Babylonian copies parts of the laws of **以工》** (41年), as well as Old Babylonian copies in both archaizing and cursive styles. Because of damage on the stele [P249253], some sections are known only from those copies. See [Oel22, pp. 110 sqq.].

 $^{^9}$ Attendees may recall the summary given on the third day of UTC #180, as recorded in [Con24]. Other readers may refer to [Svä+24, pp. 242, 148].

¹⁰ For instance, Old Babylonian grammar may be taught in the Neo-Assyrian script, as in [Cap02].

¹¹At that time scoped to the répertoire of the Ur III period and later, see [EF03, p. 1], although many disunifications, such as & ≠ & ↑, were informed by Early Dynastic distinctions.

¹²As noted in [Pow87, p. 466], this sign has a very short "tail" in this period, so that it is wider than it is tall, and can at first seem like a large — in copies. The photos in CDLI clearly show that this is in fact a vertical wedge.

¹³ Note that ED IIIb \langle numerals have a somewhat different appearance from those of the Ur III period

tug_x(LAK483)-si-ga-kam¹⁴ deep ploughing

The argument made in [And04, p. 4] is that this is comparable to a stylistic distinction such as 15

465 metres, equal lengths 198 metres, equal widths this field: 9, 18 hectares, deeply ploughed

where the numerals have the same structure ([Ando4] contrasts this to the different structures of ASCII digits and roman numerals). That document further claims that "the number signs do not normally carry in their individual signs the meaning of what they are used to measure", and that curviform and cuneiform numerals "are not normally mixed together in a single numerical expression", noting the exceptions of [P232278; P232280]. In addition, [Ando4, p. 4] points out that the cuneiform numeric signs are descended from the curviform ones (this is undisputed), and claims there is only a small re-allocation of the function of signs (from P- to I-numerals). It therefore comes to the conclusion that the use of curviform numerals should be seen as a formatting distinction, rather than one that should be represented in plain text, and insists that the encoding should capture the lineal historical descent of those signs, presumably to take advantage of the benefits of diachronic encoding described in section 3.1.

Although they had been part of the preliminary proposal [EFT03], the curviform numerals were therefore removed from [EFT04b] and [EFT04a], which both state that "The distinction between curved numerals and their cuneiform descendants is treated as glyphic for the purposes of the present proposal; this issue will need to be revisited in subsequent encoding phases."

The time has come to revisit this issue. As we will see in section 3.3, numerals can only be interpreted in the context of what they measure *i.e.*, as part of a metrological system. In section 3.4 we will see that in some periods:

- the functions and use of the numerals vary beyond the mere ▷/! switch;
- the contrast between curviform and cuneiform numerals is commonly used to distinguish metrological systems;
- some metrological systems commonly mix curviform and cuneiform in single numerical expressions.

used in this transcription; the sign **≪** in [P020054] looks more like Ur III ❖.

¹⁴Transliteration after [Lec20, p. 8].

¹⁵We have taken the liberty of adjusting the analogy to use measures approximately equal to those in [P020054], instead of a field of five by twenty-five metres.

3.3 Metrology

Edubba'a D

Before diving into the usage of the curviform numerals in the Early Dynastic period to explain the constrast with cuneiform numerals, it is useful to understand the usage of the already-encoded characters in the Ur III and Old Babylonian periods.

As is well known¹⁶ a sexagesimal place value system (SPVS) was used in Mesopotamia from the late third millenium onwards. One should bear in mind, however, that other systems were used; the SPVS was primarily used in calculations, with results being expressed in non-positional systems [Robo8, p. 76; Rob22]. The digits 1–59 of the SPVS have inner structure which is reflected in the encoding: the digits 1–9 are the individual characters [-\ff#, the multiples of ten (10–50) are \(-\frac{\pi}{\pi}\), but the other digits 11–59 are sequences \(\frac{\pi}{\pi}\), the multiples of ten (10–50) are \(\frac{\pi}{\pi}\), but the other digits 11–59 are sequences \(\frac{\pi}{\pi}\), the multiples of ten (10–50) are \(\frac{\pi}{\pi}\), but the other digits 11–59 are sequences \(\frac{\pi}{\pi}\), in effect the base-sixty digits are themselves written in base ten, with a different set of symbols for the tens place. This reflects the origin of the sexagesimal place value system; it derives from a non-positional system, hereafter the cuneiform discrete counting system \(S_{\pi}\). Which had different signs for the units \(\frac{\pi}{\pi}\), three thousand six hundreds \(\frac{\pi}{\pi}\), and thirty-six thousands \(\frac{\pi}{\pi}\).

3.3.1 The discrete counting system

The relations between the values of the signs in the cuneiform discrete counting system may be summarized by the following factor diagram¹⁷, where the number over arrow indicates the multiple of the preceding sign (right of the arrow) corresponding to the following sign (left).

3.3.2 The area system

The discrete counting system was not the only non-positional system in use in the Ur III and Old Babylonian periods; different systems were in use depending on what was being counted or measured. For instance, field areas were measured using the following system, where for the named units we have provided the name

¹⁶See, e.g., [Uni16, Section 22.3.3 "Non-Decimal Radix Systems", sub "Cuneiform Numerals"].

¹⁷These diagrams, which have become standard in discussions of Mesopotamian metrology, originate with [Fri78, p. 10], where they are called *step-diagrams*.

of the unit in transliterated Sumerian, normalized Old Babylonian Akkadian, and the approximate metric equivalent [Frio7, p. 378; Rob19]:

$$\Leftrightarrow \stackrel{10}{\leftarrow} \Leftrightarrow \stackrel{6}{\leftarrow} \stackrel{10}{\longleftarrow} \stackrel{3}{\longleftarrow} \stackrel{1}{\leftarrow} \stackrel{6}{\longleftarrow} \stackrel{2}{\longleftarrow} \stackrel{2}{\longleftarrow} \stackrel{2}{\longleftarrow} \stackrel{2}{\longleftarrow} \stackrel{1}{\longleftarrow} \stackrel{1}{\longrightarrow} \stackrel{1}{\longleftarrow} \stackrel{1}{\longleftarrow} \stackrel{1}{\longrightarrow} \stackrel{1}{\longrightarrow} \stackrel{1}{\longleftarrow} \stackrel{1}{\longleftarrow} \stackrel{1}{\longleftarrow} \stackrel{1}{\longrightarrow} \stackrel{1}{\longrightarrow$$

Note that for the range of areas given above ¹⁸, this system does not use any symbols separate from the numerals for the individual units ($ub\hat{u}m$, $ik\hat{u}m$, eblum, and $b\bar{u}rum$). As mentioned in [Rob19], the whole numeric expression for the area would be followed by the sign \mathbf{m} functioning as punctuation ¹⁹, but the numerals are tied to the metrology; thus a surface of 5 $b\bar{u}r\bar{u}$ 1 eblum 4 $ik\hat{u}$ (100 $ik\hat{u}$, 36 ha) would be written ²⁰ \mathbf{m} \mathbf{m} . Contrast this with systems where the same numerals are used for different units, and overt units are used, as in "88 acres 3 roods 33 perches". Note also that the same signs are shared between multiple systems, with different relations; the ŠAR₂ sign \diamond is equal to sixty times the U sign \lt in the area system, but to three hundred and sixty times \lt in the discrete counting system.

3.3.3 The capacity system

Another such system of note is the one for capacities²¹ [Frio7, p. 376; Rob19],

where the numerals for ban_2 are +, \neq , \neq , \neq , and \neq , and those for bariga are \neq , \neq , and \neq (contrast ordinary \parallel and \parallel) otherwise used with \mid -numerals). As described in [Hue11, p.585 with notes (b) and (f)], the sign GUR \neq \mid , while it is used only with volumes in excess of one gur, is written after the whole expression, after the overt unit sign \Rightarrow if present, and after the word for "grain" if present, as in

$$3554 \text{ gur}$$
 3 ban_2 6 sila_3 of grain.

Observe that while large numbers of gur follow²³ system $S_{\text{Ur III}/OB}$, the use of horizontal (AŠ) numerals for the gur disambiguates from the vertical bariga, as $\langle I \pm I \rangle$

$$\underbrace{\diamondsuit \not\models \stackrel{10}{\longleftrightarrow} \diamondsuit \not\models \stackrel{6}{\longleftrightarrow} \diamondsuit \stackrel{10}{\longleftrightarrow} \diamondsuit \stackrel{6}{\longleftrightarrow} \diamondsuit \stackrel{10}{\longleftrightarrow} \diamondsuit \stackrel{6}{\longleftrightarrow} \diamondsuit \stackrel{10}{\longleftrightarrow} \diamondsuit \stackrel{6}{\longleftrightarrow} \diamondsuit \stackrel{10}{\longleftrightarrow} \diamondsuit \stackrel{1$$

¹⁸For areas smaller than a quarter $ik\hat{u}m$, an overt unit is used, with 1 $m\bar{u}$ sarum (36 m²) written [ﷺ, equal to one hundredth of an $ik\hat{u}m$, then sexigesimally subdivided in 60 m (shekels). For areas greater than 3600 $b\bar{u}r\bar{u}$, the ♦- and ♦-numerals are reused with a suffix m (gal, Sumerian: big), as follows [Robo8, p.295 with notes b and c; Frio7, p. 378; Rob19]:

¹⁹TODO(egg): acknowledge Proust 2020 but note that this is irrelevant to encoding concerns

²¹Used for volumes of grain, but also oil, dairy products, beer, etc., as well as to express the capacity of boats; volumes of earthworks instead use system $G_{\text{Ur III}/OB}$ based on a height of one cubit, see[Pow87, p. 488; Robo8, p. 294; Rob19].

²²From P309594.

²³A larger unit, the guru₇ (*karûm*, grain heap), is sometimes used instead, with — **□▶** (1 *karûm* = 3600 kurrū). See [Frio7, p. 415; Rob19].

would be 10 gur 1 bariga, and (-# would be 11 gur; again even with some overt units, most of the numerals that participate in a metrological system have an interpretation dependent on that system. To quote [Robo8, p. 78]: "The SPVS temporarily changed the status of numbers from properties of real-world objects to independent entities that could be manipulated without regard to [...] metrological system. [...] Once the calculation was done, the result was expressed in the most appropriate metrological units and thus re-entered the natural world as a concrete quantity."

This intertwining of units and numerals explains the large number of alreadyencoded numeral series:

- I-# used in $S_{Ur III/OB}$ and the SPVS as well as with overt units;
- \leftarrow with used in $G_{\text{Ur III}/OB}$, of which \leftarrow are also used in $S_{\text{Ur III}/OB}$ and the SPVS as well as with overt units;
- I-W used in $S_{Ur III/OB}$, and sometimes with overt units;
- K-W used in $S_{\text{Ur III/OB}}$;
- \diamondsuit \diamondsuit used in $S_{\text{Ur III/OB}}$ and $G_{\text{Ur III/OB}}$;

 \diamondsuit \diamondsuit used in $S_{\text{Ur III/OB}}$ and $G_{\text{Ur III/OB}}$;
- \leftarrow used in $C_{\text{Ur III/OB}}$ as well as with overt units of the weight system;
- +, \ddagger , \ddagger , \ddagger , \ddagger used in $C_{\text{Ur III/OB}}$;
- $I, I, II, II used in C_{Ur III/OB}$ —note the overlap with I-III;
- \prec and \bowtie used in $G_{\text{Hr III}/OB}$.

3.3.4 The length system

In the Ur III and Old Babylonian periods, lengths are expressed using overt units counted with $\$ - and $\$ -numerals with their system $S_{Ur \text{ III}/OB}$ values²⁴. Since it does not have any unusual numerals, this system would not in itself be of much relevance to character encoding, but we present it here as background for its Early Dynastic counterpart presented in section 3.4. Metrological tables use the following units [Fri07, p. 118; Rob19]:

Two more units appear occasionally [Pow87, p. 459; Frio7, p. 118; Rob19]:

| ※ ※
$$\leftarrow \stackrel{30}{\leftarrow}$$
 | $\stackrel{6}{=}$ | $\stackrel{10}{=}$ $\stackrel{10}{\leftarrow}$ | $\stackrel{2}{=}$ $\stackrel{6}{=}$ $\stackrel{10}{=}$ $\stackrel{6}{=}$ $\stackrel{10}{=}$ $\stackrel{6}{=}$ $\stackrel{10}{=}$ $\stackrel{10}{=}$

In addition, there are Akkadian names for the half-rope and half-reed, see [Pow87, pp. 463 sq.].

²⁴Adjacent units are no more than a factor of 60 apart, so higher numerals such as ₹ or ♦ are not

²⁵TODO

3.3.5 Fractions

TO_D0

3.4 Early metrology

At first sight, the metrological systems from the Early Dynastic period match the ones previously mentioned. In particular, the discrete counting system used in the Early Dynastic period (and earlier in the Uruk period) clearly mirrors system $S_{\rm Ur, III/OB}$ [Frio7, p. 374; DE87, pp. 127, 165]:

$$\bullet \xleftarrow{10} \bullet \xleftarrow{6} \bullet \xrightarrow{10} \overset{10}{\smile} \overset{6}{\smile} \bullet \xrightarrow{10} \smile. \tag{S}$$

Likewise the area system used in the Early Dynastic IIIb period mirrors system $G_{\text{Ur} \text{III}/OB}$ [Dei22, p. 72; NDE93, p. 63; Frio7, p. 378; Gom16]:

$$\bullet \xleftarrow{10} \bullet \xleftarrow{6} \stackrel{10}{\Leftarrow} \xleftarrow{10} \bullet \xleftarrow{3} \bullet \xleftarrow{6} \triangleright, \qquad (G_{\rm ED\,IIIb})$$

As noted in [And04, p. 4] (see section 3.2), the vertical $\[\]$ from $S_{Ur \, III/OB}$ becomes a horizontal $\[\]$ in system $\[\]$. It is however far from the only case of such a reallocation of function. The earlier form of System G was [DE87, pp. 141, 165; Frio7, p. 378]:

Observe that, as noted in [DE87, p. 142], $^{\odot}$ changes meaning from 10 $^{\bullet}$ in system G to 10 $^{\bullet}$ in system $G_{\text{ED IIIb}}$. System G is used in the Uruk period, but also in the ED I–II period (it is the "area 2" system in [Chao3], whereas $G_{\text{ED IIIb}}$ is the "area 1" system).

The length system Early Dynastic IIIb of the state of Lagaš is of particular interest. As described in [Pow87, p. 466; Lec20, pp. 289 sq.], lengths are expressed in rods, but the unit sign V is generally omitted; in addition, only ten of rods are used; these are equal to one rope, but the sign I is not written either. Length shorter than one rope are expressed in half-ropes using the 1/2 sign I (again with no I), and then in reeds, with the sign I3. Effectively, this yields the following factor diagram:

This is the system that was used to express the sides of the field in [P020054] discussed in section 3.2. In that tablet and others from the same period, such as the ones, areas are expressed in system $G_{\rm ED~IIIb}$, with curviform numerals²⁶; in the absence of overt units, such as when dealing with length that are integer multiples of a half-rope²⁷, the use of curviform or cuneiform numerals therefore disambiguates a numeric expression between an area and a length, and therefore the interpretation of its numerals between systems $G_{\rm ED~IIIb}$ and $L_{\rm ED~IIIb}$. The sign GAN₂ , which would also disambiguate the interpretation as an area, is sometimes used after areas in ED IIIb Lagaš, but not systematically; in particular the area of the first field

 $^{^{26}}$ TODO(egg): Note the handful of late Urukagina tablets that start to have cuneiform areas.

 $^{^{27}}$ This is the case of the sides of the field in [P020054, obv. ii 2–3].

in [P020054] does not use this suffix. See [Lec20] for many examples with and

[Pow87, p. 466] notes that reeds "are regularly written with the normal, cuneiform end of the stylus. Higher units are usually written with the reversed (round) end of the stylus." Powell does not elaborate on the specifics of this mixed use of numerals, but a cursory search in CDLI finds many occurrences: [TODO(egg): cite VS 14, 100, 130, 74, VS25, 83... Just search the downloaded ATF pile for @c.*disz@t\) gi These expressions use an explicit sign $V \cong I$ (counted in multiples of ten) or II. This notation—but not its use of curviform numerals—is remarked on in [Lec20, p.290 with note 27], which cites several of the instances listed above. It seems to be typical of texts about dykes. These match the following factor diagrams:

$$\underbrace{\triangleright}_{\stackrel{?}{\longleftarrow}}^{2} \stackrel{10}{\longleftarrow} \stackrel{10}{\longleftarrow} \stackrel{1}{\longleftarrow} . \qquad (L'_{\text{ED IIIb}})$$

$$\underbrace{\stackrel{10}{\longleftarrow} \stackrel{6}{\longleftarrow} \stackrel{2}{\longleftarrow} \stackrel{2}{\longleftarrow} \stackrel{10}{\longleftarrow} \stackrel{10}{\longrightarrow} \stackrel{10}{\longleftarrow} \stackrel{10}{\longrightarrow} \stackrel{10}{\longleftarrow} \stackrel$$

Lengths of Early Dynastic IIIb dykes from Nirsu are far from the only numeric expressions that mix curviform and cuneiform numerals.

The capacity system in Ebla uses the following units²⁹:

TODO liquid capacities use sila apparently.

The $\Box \Diamond \bot$ and $\lhd \biguplus \exists \exists$ are generally counted using curviform numerals, and the smaller units using cuneiform I numerals. Indeed, a search on [Mil+07] for co-occurrences of ★ ⇔ with either of ♠ L or ◄ 土 Ħ finds the following expressions³⁰:

- 1. [P240532, verso 4, 9] ▷ ₩ 전 ₩ 4 □ 32 ₩ ▷ < 4□
- 2. [P240548, verso 1, 1] ▷□ ₩ Ⅲ ※ ← 3. [P240655, recto 7, 9] ▷□ ※ L³³ ₩ ▷ 〈◆□
- 4. [P240579, verso 4, 3] ₽¬¬¬ ⊥ ¶ V < ∢□
- 6. [P240609, verso 3, 1] ▷◁ 丑 Ⅲ ★ ↔

²⁸TODO(egg): Note that one unit may be omitted if the other is present

²⁹TODO mention the other one citing Chambon and the footnote in Archi

³⁰We cite here only one attestation per tablet; most tablets contain several expressions mixing curviform 덕 土田 and larger with cuneiform 🏴 and smaller. In all cases the transcriptions given here are based on the EbDA transliterations, but the shape and orientation of the numerals was checked31 on a photograph (from EbDA unless noted otherwise).

 $^{^{31}}$ As we will see in Section 3.6.1, CDLI transliterations indicate numeral shape; however, as of this writing, they do so incorrectly on the Ebla corpus, claiming that all numerals are curviform, so we were not able to rely on them in this specific case.

³²ba-ri₂-zu₂, a variant spelling.

³³ Short for ⋤� ⊥.

³⁴ **III** ★ ← not legible on the EbDA photo.

- 13. [P241904, recto 1, 1]³⁶ B □ L W³⁷ V (□

Note that higher numbers of $\Box \diamondsuit \bot$ are expressed in hundreds, as is typical in Ebla [Arc15, p. 33]

[TODO(egg):Eblaite capacities [P240964] TODO(egg): There are $\eta e \tilde{s}_2$ gubar TODO(egg): the diš are unusual in P240964]

$$\begin{array}{c}
\stackrel{5}{\longrightarrow} \stackrel{10}{\longrightarrow} \stackrel{5}{\longrightarrow} \stackrel{6}{\longrightarrow} \stackrel{10}{\longrightarrow} \stackrel{2}{\longrightarrow} \stackrel{5}{\longrightarrow} \stackrel{11}{\longrightarrow} \stackrel{6}{\longrightarrow} \stackrel{11}{\longrightarrow} \stackrel{11}{\longrightarrow} \stackrel{6}{\longrightarrow} \stackrel{11}{\longrightarrow} \stackrel{11}{\longrightarrow} \stackrel{10}{\longrightarrow} \stackrel{$$

3.4.1 Use in modern publications

3.5 Non-numeric usage

打害人名菲兰 人名苏兰 医多种冠 订发 呱卜写度叫 鞣利血 呱唑 节束者打罪 克克氏性 计多价证据 法人员 机阻力 计图式 化压力

The beginning of the scribal art is a single wedge. That one has six pronunciations; it also stands for 'sixty'. Do you know its reading?

Examenstext A

[TODO(egg): In a footnote, comment on the ♥〈⟨□ situation.]

3.6 Limited benefits of diachronic encoding for numerals

[Composite texts dating back to the period where curved numerals are in use tend to be limited to lexical texts, which do not usually have numbers. When they do, diachronic encoding is prevented by diš-aš distincitons anyway. Administrative texts, which are where numbers are most prominent, are not composite.]

[Diachronic reference works tend to not include numbers, or when they do, to treat them specially (for intance, they are shown at the end of sign lists such as TODO).]

[The overarching goal of having consistent representation for equivalent numeric expressions from different periods is quickly foiled by changes in metrology.]

Note that in [Rom24] [TODO(egg): Cite the GitHub repository], as in many other such analyses, numbers are removed as an early step in processing; these therefore would not benefit from diachrony in the encoding of numeric expressions.

³⁵ From CDLI photo.

³⁶From photo in [Arc89, p. 6].

³⁷Laid out as !!!!; on stacking patterns see Section 6.2.

- 3.6.1 Compatibility with transliteration
- 3.7 Compatibility considerations
- 3.7.1 The case of ŠAR₂

4 Rationale for ED-Uruk numeral unification

5 Considerations on individual numeral series

[TODO Document to the extent possible the metrological systems in which each sign is used. Note the disunification of N9 and N10 from 4(ban₂@c) and 5(ban₂@c).]

6 Characters not included in this proposal

6.1 Missing numerals

 $(N_{17}, 12N_{14}, \text{ etc.})$ 7(diš $ten\hat{u}$)

6.2 Stacking patterns

(... are a mess, vary within Uruk, and are not transliterated/documented by Englund, so let's not go there for now.)

6.3 Matters for higher-level protocols

Rotated bits: https://cdli.mpiwg-berlin.mpg.de/artifacts/101087

7 Acknowledgements

TODO(egg): Something about the Vanséveren fonts

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