

Archaic cuneiform numbers

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1 Summary

2 Background

[TODO(egg): Restructure this. The internal references are all garbled.]

The Unicode Standard includes some cuneiform numbers: 𐎶–𐎶𐎵 1–9(diš) and 𐎶–𐎶𐎵𐎶 1–9(aš), 𐎶–𐎶𐎵 1–5(u), 𐎶–𐎶𐎵𐎶 1–9(ḫeš₂), 𐎶–𐎶𐎵 1–5(ḫeš₂u), etc., used in the Sumero-Akkadian Cuneiform script (ISO 15924: Xsux, Script property value long name: Cuneiform).

In the investigation that led to their encoding in Unicode Version 5.0, it was thought appropriate to unify these with the earlier curviform numerals 𐎶–𐎶𐎵 1–9(aš^c = N_1), 𐎶–𐎶𐎵 1–5(u^c = N_{14}), 𐎶–𐎶𐎵𐎶 1–9(ḫeš₂^c = N_{34}), 𐎶–𐎶𐎵𐎶 1–5(ḫeš₂u^c = N_{48}), etc., see [Ando4]. While the curviform numerals sometimes co-occur with the cuneiform ones, this was analysed as a stylistic distinction which should not be encoded in plain text. It has now become apparent that a distinction needs to be

made for the adequate representation of Early Dynastic (ED) texts and scholarship pertaining to them.

In addition, these numerals will be needed for the representation of proto-cuneiform texts from the earlier archaic period. The non-numeric signs of proto-cuneiform (ISO 15924: P_{cun}) will be the subject of a separate proposal; we need only note here that the divergence between the approaches to character identity in modern scholarship requires that proto-cuneiform be disunified from cuneiform: proto-cuneiform is effectively treated as an undeciphered script. In contrast, the cuneiform encoding model is semantic, requiring an understanding of the text to correctly encode it.

The use of the curviform numeric signs is however understood, as we will discuss in Section 3; further, the conventions used for archaic numerals are also used when discussing ED numerals, see Section 7. As a result, the same numerals can be used when encoding archaic and ED texts, and in order to avoid issues ambiguities in representation when converting from transliteration, these should be unified. The overall picture of unifications and disunifications would be as follows:

	Uruk III & earlier	ED – Ur III	OB & later
Non-numeric signs	Future P _{cun}	Existing X _{sux}	
Numbers	This proposal	This proposal + Existing X _{sux}	Existing X _{sux}

3 Metrologies

𒄩 𒂍𒄩𒂍𒄩𒂍𒄩 𒄩𒄩
𒄩 𒂍 𒄩𒂍𒄩 𒂍𒄩 𒂍𒄩
𒄩 𒂍𒄩𒂍𒄩 𒂍𒄩 𒂍𒄩𒂍𒄩

I want to write tablets: the tablet of 1 gur of barley to 600 gur; the tablet of 1 shekel of silver to 10 minas [...]

Edubba'a D

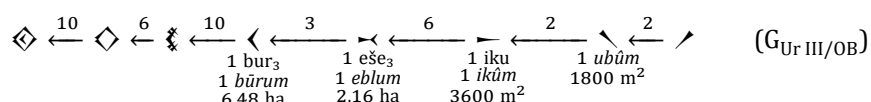
In order to explain why TODO:*n* more numerals are needed, it is useful to first recall why we have so many kinds of cuneiform numerals already.

As is well known¹ a sexagesimal place value system (SPVS) was used in Mesopotamia from the late third millenium onwards. One should bear in mind, however, that other systems were used; the SPVS was primarily used in calculations, with results being expressed in non-positional systems [Rob08, p. 76; Rob22]. The digits 1–59 of the SPVS have inner structure which is reflected in the encoding: the digits 1–9 are the individual characters 𒄩–𒄩𒄩, the multiples of ten (10–50) are 𒄩–𒄩𒄩, but the other digits 11–59 are sequences 𒄩–𒄩𒄩𒄩; in effect the base-sixty digits are themselves written in base ten, with a different set of symbols for the tens place. This reflects the origin of the sexagesimal place value system; it derives from a *non-positional* system, hereafter the *cuneiform discrete counting system* S_{Ur III/OB}, which had different signs for the units 𒄩–𒄩𒄩, tens 𒄩–𒄩𒄩, sixties 𒄩–𒄩𒄩𒄩 (with larger wedges than the units), six hundreds 𒄩–𒄩𒄩, three thousand six hundreds 𒄩–𒄩𒄩𒄩𒄩, and thirty-six thousands 𒄩–𒄩𒄩𒄩𒄩.

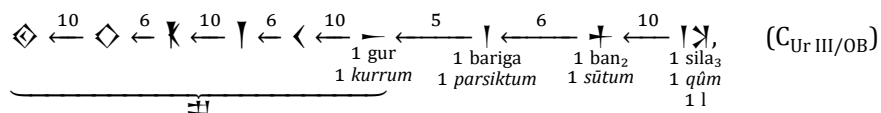
¹See, e.g., [Uni16, Section 22.3.3 “Non-Decimal Radix Systems”, sub “Cuneiform Numerals”].

$$\diamond \xleftarrow{10} \diamond \xleftarrow{6} \nabla \xleftarrow{10} \nabla \xleftarrow{6} \triangleleft \xleftarrow{10} \nabla \quad (\text{S}_{\text{Ur III/OB}})$$

The discrete counting system was not the only non-positional system in use in the Ur III and Old Babylonian periods; different systems were in use depending on what was being counted or measured. For instance, field areas were measured using the following system, where for the named units we have provided the name of the unit in transliterated Sumerian, normalized Old Babylonian Akkadian, and the approximate metric equivalent [Fri07, p. 378; Rob19]:










Another such system of note is the one for capacities⁵ [Fri07, p. 376; Rob19],





²These diagrams, which have become standard in discussions of Mesopotamian metrology, originate with [Fri8, p. 10], where they are called *step-diagrams*.
























⁵Used for volumes of grain, but also oil, dairy products, beer, etc., as well as to express the capacity of boats; volumes of earthworks instead use system **GUR III/08** based on a height of one cubit, see[**Pow87**, p. 488; **Rob08**, p. 294; **Rob19**].

As described in [Hue11, p.585 with notes (b) and (f)], the sign GUR , while it is used only with volumes in excess of one gur, is written after the whole expression, after the overt unit sign  if present, and after the word for “grain” if present, as in





       ⁶
3554 gur 3 ban₂ 6 sila₃ of grain.

Observe that while large numbers of gur follow⁷ system $S_{Ur\ III/OB}$, the use of horizontal (AŠ) numerals for the gur disambiguates from the vertical bariga, as  would be 10 gur 1 bariga, and  would be 11 gur; again even with some overt units, most of the numerals are tied to the metrology.

This intertwining of units and numerals explains the large number of already-encoded numeral series:


- - used in $S_{Ur\ III/OB}$ and the SPVS as well as with overt units;
- - used in $G_{Ur\ III/OB}$, of which - are also used in $S_{Ur\ III/OB}$ and the SPVS as well as with overt units;
- - used in $S_{Ur\ III/OB}$ and the SPVS;
- - used in $C_{Ur\ III/OB}$ as well as in the weight system;
- , , , ,  used in $C_{Ur\ III/OB}$;
- , , ,  used in $C_{Ur\ III/OB}$ —note the overlap with -;
-  and  used in $G_{Ur\ III/OB}$.


4 Arguments for curviform–cuneiform unification

As outlined in, *e.g.*, [UTR56], the cuneiform encoding model is diachronic; each character may have wildly different glyphs depending on time period and region. For instance, the sign IM may resemble  in texts from Early Dynastic IIIa Šuruppag as in the character code charts,  later in the third millennium⁸,  in Old Babylonian cursive,  in Neo-Assyrian, but is always encoded as U+1214E CUNEIFORM SIGN IM.

This encoding model allows for the interoperable representation of editions of diachronic reference works such as sign lists⁹ and dictionaries¹⁰, and of composite texts¹¹. By being compatible with similarly diachronic transliteration practice (that is, by avoiding distinctions finer than those made in transliteration), the encoding model also allows for automated conversion of transliterated corpora to cuneiform, which has proven useful as a processing step in analyses such as [Rom24; JJ24]¹². The diachronic approach is also useful for pedagogical applications¹³.


























⁶From P309594.

⁷A larger unit, the guru₇ (*karûm*, grain heap), is sometimes used instead, with  (1 *karûm* = 3600 kurrû). See [Fri07, p. 415; Rob19].

⁸Merging with U+1224E  NI₂.

⁹Notably the online edition of [Ryk10] in [Jim+23, Signs], as well as [VT+14].

¹⁰Notably the online edition of [Sch10] in [Jim+23, Dictionary], as well as [TJV17].

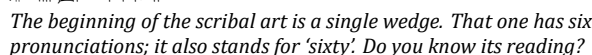
¹¹For example, there are Neo-Assyrian and Neo-Babylonian copies parts of the laws of                         

Indeed, some metrological systems from the Early Dynastic period match the ones previously mentioned. In particular, the discrete counting system used in the Early Dynastic period (and earlier in the Uruk period) clearly mirrors system $S_{Ur III/OB}$ [Fri07, p. 374; DE87, pp. 127, 165]:

Likewise the area system used in the Early Dynastic IIIb period mirrors system $G_{Ur-III/OB}$ [Fri07, p. 378; Gombert2016]:

5 Problems with unification: Early metrology

6 Problems with unification: Non-numeric usage



Examenstext A

6.1 The case of ŠAR₂

7 Compatibility with transliteration

8 The necessity of ED-Uruk numeral identification

9 Characters not included in this proposal

9.1 Missing numerals

 $(N_{17}, 12N_{14}, \text{etc.})$

9.2 Stacking patterns

(... are a mess, vary within Uruk, and are not transliterated/documented by Englund, so let's not go there for now.)

¹⁴At that time scoped to the *répertoire* of the Ur III period and later, see [EF03, p. 1], although many disunifications, such as $\text{𒀭} \neq \text{𒀭}$, were informed by Early Dynastic distinctions.

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