

Archaic cuneiform numbers

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1 Summary

This document proposes encoding some numerals used in the Uruk and Early Dynastic periods in conjunction with the Sumero-Akkadian cuneiform script¹ and the proto-cuneiform script². The proposed characters are listed in section 2.

The non-numeric signs of proto-cuneiform will be the subject of a separate proposal; we need only note here that the divergence between the approaches to character identity in modern scholarship requires that proto-cuneiform be disunified from cuneiform: proto-cuneiform is effectively treated as an undeciphered script. In contrast, the cuneiform encoding model is semantic, requiring an understanding of the text to correctly encode it.






However, the *numerals* used in proto-cuneiform should be unified with ones used in the Early Dynastic period, for the reasons set forth in section 4. The proposed “curved”, or “curviform”, numerals³ should however *not* be unified with the already-encoded cuneiform numerals⁴. Since the encoding proposals for the cuneiform script twenty years ago provisionally considered the curviform numerals to be glyph variants of the cuneiform numerals, a detailed rationale is provided in section 3, including compatibility considerations in section 3.7.









The overall picture of unifications and disunifications over time is illustrated in table 1. The Script_Extensions property assignments in section 2.2 reflect the overlap.

[TODO(egg): Mention the other sections here too.]

¹ISO 15924: Xsux, Script property value long name: Cuneiform; encoded since Unicode Version 5.0.

²ISO 15924: Pcun, not yet encoded.

³Impressed into clay using cylindrical styli, held either perpendicular to the tablet, yielding  (small cylinder) or  (large cylinder), or at a shallower angle:  (small cylinder),  (large cylinder). Some numerals are composed of multiple such impressions, e.g., .

⁴Impressed into clay using a trihedral stylus:  (stylus held horizontally),  (vertically),  (diagonally)  (diagonally with the stylus along its axis),  (stylus pressed deeper, forming a larger wedge),  (combining  and ) , etc.

	Uruk III & earlier	ED – Ur III	OB & later
Numerals	This proposal		
Non-numeric signs	Future Pkun	Existing Xsux	

Table 1: Usage of existing, proposed, and future characters across functions and time periods.

2 Proposed changes to the Standard

2.1 Summary of proposed characters

2.2 Properties





2.3 Character names list

2.4 Core specification text


3 Rationale for curviform–cuneiform disunification

TODO(egg): blurb.

3.1 The cuneiform encoding model

























As outlined in, *e.g.*, [UTR56], the cuneiform encoding model is diachronic; each character may have wildly different glyphs depending on time period and region. For instance, the sign IM may resemble  in texts from Early Dynastic IIIa Šuruppag as in the character code charts,  later in the third millennium⁵,  in Old Babylonian cursive,  in Neo-Assyrian, but is always encoded as U+1214E CUNEIFORM SIGN IM.

This encoding model allows for the interoperable representation of editions of diachronic reference works such as sign lists⁶ and dictionaries⁷, and of composite texts⁸. By being compatible with similarly diachronic transliteration practice, *i.e.*, by avoiding distinctions finer than those made in transliteration, the encoding model also allows for automated conversion of transliterated corpora to cuneiform, which has proven useful as a processing step in analyses such as [Rom24; JJ24]⁹. The diachronic approach is also useful for pedagogic applications¹⁰.

⁵Merging with U+1224E  NI₂.

⁶Notably [VT+14] and the online edition of [Bor10] in [Jim+23, Signs].

⁷Notably [TJV17] and the online edition of [Sch10] in [Jim+23, Dictionary].

⁸For example, there are Neo-Assyrian and Neo-Babylonian copies parts of the laws of                        

⁹Attendees may recall the summary given on the third day of UTC #180, as recorded in [L2/24-159]. Other readers may refer to [Svā+24, pp. 242, 148].

¹⁰For instance, Old Babylonian grammar may be taught in the Neo-Assyrian script, as in [Cap02].

3.2 Arguments for curviform–cuneiform unification

In this context, the argument was made in [L2/04-099], as part of discussion of the cuneiform encoding¹¹ that the curviform numerals, which occasionally appear in the Ur III period and are used heavily in the Early Dynastic period, were a stylistic distinction unifiable with the cuneiform digits, and that an archaizing Ur III font or an Early Dynastic font could have curviform glyphs for the appropriate characters.

Some co-occurrence of curviform and cuneiform digits was known and acknowledged. [L2/04-099, p. 3] cites [NDE93, p. 62], which is a copy of [P020054], an Early Dynastic IIIb administrative tablet from Nirsu. The excerpt cited, lines 1–3 of column 1 of the obverse, is as follows:

1 ¹²	<	+	≡	𐎶	𐎶	𐎶
1(NĖŠ ₂)	1(U)	1/2(DIŠ)	5(DIŠ <i>tenû</i>)	gi	us ₂	sa ₂
	7.5 (ropes)		5	reed	side	equal
𐎶 ¹³	≡	𐎶	𐎶	𐎶		
3(U)	6(DIŠ <i>tenû</i>)	gi	sa ₂	sa ₂		
3(ropes)	6	reed	front	equal		
𐎶𐎶𐎶	•	•	▷	◁		
ašag-bi	1(BUR ₃)	1(EŠE ₃)	1(IKU)	1/2(IKU)		
this field						

𐎶𐎶𐎶𐎶𐎶
tug_x(LAK483)-si-ga-kam¹⁴
deep ploughing

The argument made in [L2/04-099, p. 4] is that this is comparable to a stylistic distinction such as¹⁵

465 metres, equal lengths
198 metres, equal widths
this field: 9, 18 hectares, deeply ploughed

where the numerals have the same structure ([L2/04-099] contrasts this to the different structures of ASCII digits and roman numerals). That document further claims that “the number signs do not normally carry in their individual signs the meaning of what they are used to measure”, and that curviform and cuneiform numerals “are not normally mixed together in a single numerical expression”, noting the exceptions of [P232278; P232280]. In addition, [L2/04-099, p. 4] points out that the cuneiform numeric signs are descended from the curviform ones (this is undisputed), and claims there is only a small re-allocation of the function of signs (from ▷ to 1 numerals). It therefore comes to the conclusion that the use of

¹¹At that time scoped to the répertoire of the Ur III period and later, see [L2/03-162, p. 1], although many disunifications, such as 𐎶 ≠ 𐎶, were informed by Early Dynastic distinctions.

¹²As noted in [Pow87, p. 466], this sign has a very short “tail” in this period, so that it is wider than it is tall, and can at first seem like a large — in copies. The photos in CDLI clearly show that this is in fact a vertical wedge.

¹³Note that ED IIIb < numerals have a somewhat different appearance from those of the Ur III period used in this transcription; the sign 𐎶 in [P020054] looks more like Ur III 𐎶.

¹⁴Transliteration after [Lec20, p. 325].

¹⁵We have taken the liberty of adjusting the analogy to use measures approximately equal to those in [P020054], instead of a field of five by twenty-five metres.

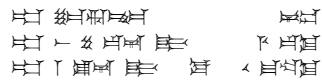
curviform numerals should be seen as a formatting distinction, rather than one that should be represented in plain text, and insists that the encoding should capture the lineal historical descent of those signs, presumably to take advantage of the benefits of diachronic encoding described in section 3.1.

Although they had been part of the preliminary proposal [L2/03-393R], the curviform numerals were therefore removed from [L2/04-036] and [L2/04-189], which both state that “The distinction between curved numerals and their cuneiform descendants is treated as glyphic for the purposes of the present proposal; this issue will need to be revisited in subsequent encoding phases.”

The time has come to revisit this issue. As we will see in section 3.3, numerals can only be interpreted in the context of what they measure *i.e.*, as part of a metrological system. In section 3.4 we will see that in some periods:

- the functions and use of the numerals vary beyond the mere \triangleright / \lvert switch;
- the contrast between curviform and cuneiform numerals is commonly used to distinguish metrological systems;
- some metrological systems commonly mix curviform and cuneiform in single numerical expressions.

3.3 A primer on classic Ur III and Old Babylonian metrologies


 I want to write tablets: the tablet of
 1 cor of barley to 600 cor; the tablet
 of 1 shekel of silver to 10 minas [...]
 Edubba'a D

Before diving into the usage of the curviform numerals in the Early Dynastic period to explain the contrast with cuneiform numerals, it is useful to understand the usage of the already-encoded characters in the Ur III and Old Babylonian periods.

As is well known¹⁶ a sexagesimal place value system (SPVS) was used in Mesopotamia from the late third millennium onwards. One should bear in mind, however, that other systems were used; the SPVS was primarily used in calculations, with results being expressed in non-positional systems [Rob08, p. 76; Rob22]. The digits 1–59 of the SPVS have inner structure which is reflected in the encoding: the digits 1–9 are the individual characters \lvert – |||| , the multiples of ten (10–50) are < – <|||| , but the other digits 11–59 are sequences < – <|||| ; in effect the base-sixty digits are themselves written in base ten, with a different set of symbols for the tens place. This reflects the origin of the sexagesimal place value system; it derives from a *non-positional* system, hereafter the *cuneiform discrete counting system* $S_{\text{Ur III/OB}}$, which had different signs for the units \lvert – |||| , tens < – <|||| , sixties |||| (with larger wedges than the units), multiples of six hundred |||| , multiples of three thousand six hundreds |||| , and multiples of thirty-six thousand |||| .

¹⁶See, e.g., [Uni16, §22.3.3, sub “Cuneiform Numerals”].

3.3.1 The discrete counting system

The relations between the values of the signs in the cuneiform discrete counting system may be summarized by the following factor diagram¹⁷, where the number over arrow indicates the multiple of the preceding sign (right of the arrow) corresponding to the following sign (left).

$$\diamond \xleftarrow{10} \diamond \xleftarrow{6} \text{𐎶} \xleftarrow{10} \text{𐎵} \xleftarrow{6} \text{𐎴} \xleftarrow{10} \text{𐎳} \quad (S_{\text{Ur III/OB}})$$

For example, the number $1729 = ((2 \times 10 + 8) \times 6 + 4) \times 10 + 9 = 28 \times 60 + 49$ would be written 𐎶𐎵𐎴𐎳𐎲𐎱 in the discrete counting system, and 𐎶𐎵𐎴𐎳𐎲𐎱 in the sexagesimal place value system.

3.3.2 The area system

The discrete counting system was not the only non-positional system in use in the Ur III and Old Babylonian periods; different systems were in use depending on what was being counted or measured. For instance, field areas were measured using the following system, where for the named units we have provided the name of the unit in transliterated Sumerian, normalized Old Babylonian Akkadian, and the approximate metric equivalent [Fri07, p. 378; Rob19]:

$$\diamond \xleftarrow{10} \diamond \xleftarrow{6} \text{𐎶} \xleftarrow{10} \text{𐎵} \xleftarrow{3} \text{𐎴} \xleftarrow{6} \text{𐎳} \xleftarrow{2} \text{𐎲} \xleftarrow{2} \text{𐎱} \quad (G_{\text{Ur III/OB}})$$

bur_3	eše_3	iku	ubûm
$bûrum$	$eblum$	$ikûm$	1800 m^2
$6,48 \text{ ha}$	$2,16 \text{ ha}$	3600 m^2	

Note that for the range of areas given above¹⁸, this system does not use any symbols separate from the numerals for the individual units (*ubûm*, *ikûm*, *eblum*, and *bûrum*). As mentioned in [Rob19], the whole numeric expression for the area would be followed by the sign 𐎶 functioning as punctuation¹⁹, but the numerals are tied to the metrology; thus a surface of 5 *bûr* 1 *ebel* 4 *ikû* (100 *ikû*, 36 ha) would be written²⁰ 𐎶𐎵𐎴𐎳𐎲𐎱. Contrast this with systems where the same numerals are used for different units, and overt units are used, as in “88 acres 3 roods 33 perches” or 五頃八畝五分九厘. Note also that the same signs are shared between multiple systems, with different relations; the sign \diamond is equal to sixty times 𐎴 in the area system, but to three hundred and sixty times 𐎴 in the discrete counting system.

¹⁷These diagrams, which have become standard in discussions of Mesopotamian metrology, originate with [Fri78, p. 10], where they are called *step-diagrams*.

¹⁸For areas smaller than a quarter *ikûm*, an overt unit is used, with 1 *mûšarum* (36 m²) written 𐎶𐎵, equal to one hundredth of an *ikûm*, then sexagesimally subdivided in 60 𐎶 (shekels). For areas greater than 3600 *bûrû*, the \diamond and \diamond numerals are reused with a suffix 𐎶 (gal, Sumerian: big), as follows [Rob08, p. 295 with notes b and c; Fri07, p. 378; Rob19]:

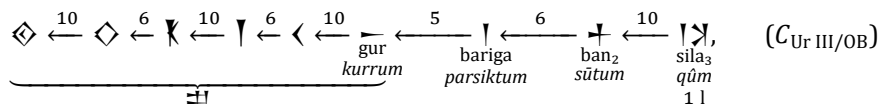
$$\diamond \text{𐎶} \xleftarrow{10} \diamond \text{𐎶} \xleftarrow{6} \diamond \xleftarrow{10} \diamond \xleftarrow{6} \text{𐎶} \xleftarrow{10} \text{𐎵} \xleftarrow{3} \text{𐎴} \xleftarrow{6} \text{𐎳} \xleftarrow{2} \text{𐎲} \xleftarrow{2} \text{𐎱} \xleftarrow{2,5} \text{𐎶} \xleftarrow{10} \text{𐎶} \xleftarrow{6} \text{𐎶} \xleftarrow{10} \text{𐎶}.$$

¹⁹TODO(egg): acknowledge Proust 2020 but note that this is irrelevant to encoding concerns






²⁰As in the surface of the field of 𐎶𐎵𐎴𐎳𐎲𐎱 (the city of Apisal) reported on [P102305, r. 1]

3.3.3 The capacity system

Another such system of note is the one for capacities²¹ [Fri07, p. 376; Rob19],



where the numerals for ban₂ are 𐎶, 𐎷, 𐎸, 𐎹, and 𐎺, and those for bariga are 𐎶, 𐎷, 𐎸, and 𐎹 (contrast ordinary 𐎶 and 𐎷 otherwise used with 𐎶 numerals). As described in [Hue11, p. 585 with notes (b) and (f)], the sign 𐎶𐎶 GUR, while it is used only with volumes in excess of one gur, is written after the whole expression, after the overt unit sign 𐎶 if present, and after the word for “grain” if present, as in

 354 gur
  3 ban₂
  6
  sila₃
  of grain.

Observe that while large numbers of gur follow²³ system $S_{\text{Ur III/OB}}$, the use of horizontal (AŠ) numerals for the gur disambiguates from the vertical bariga, as $\langle \text{I} \text{---} \text{II} \rangle$ would be 10 gur 1 bariga, and $\langle \text{---} \text{II} \rangle$ would be 11 gur; again even with some overt units, most of the numerals that participate in a metrological system have an interpretation dependent on that system.

This intertwining of units and numerals explains the large number of already-encoded numeral series:

- \mathbb{I} - \mathbb{W} used in $S_{\text{Ur III/OB}}$ and the SPVS as well as with overt units;
- \mathbb{L} - \mathbb{X} used in $G_{\text{Ur III/OB}}$, of which \mathbb{L} - \mathbb{X} are also used in $S_{\text{Ur III/OB}}$ and the SPVS as well as with overt units;
- \mathbb{I} - \mathbb{W} used in $S_{\text{Ur III/OB}}$, and sometimes with overt units;
- \mathbb{L} - \mathbb{X} used in $S_{\text{Ur III/OB}}$;
- \mathbb{L} - \mathbb{X} used in $S_{\text{Ur III/OB}}$ and $G_{\text{Ur III/OB}}$;
- \mathbb{L} - \mathbb{X} used in $S_{\text{Ur III/OB}}$ and $G_{\text{Ur III/OB}}$;
- \mathbb{L} - \mathbb{X} used in $C_{\text{Ur III/OB}}$ as well as with overt units of the weight system;
- \mathbb{L} , \mathbb{L} , \mathbb{L} , \mathbb{L} , \mathbb{L} used in $C_{\text{Ur III/OB}}$;
- \mathbb{L} , \mathbb{L} , \mathbb{L} , \mathbb{L} used in $C_{\text{Ur III/OB}}$ —note the overlap with \mathbb{L} - \mathbb{W} ;
- \mathbb{L} and \mathbb{L} used in $G_{\text{Ur III/OB}}$.

Only in the SPVS did numerals exist truly independently of metrology; to quote [Robo8, p. 78]: “The SPVS temporarily changed the status of numbers from properties of real-world objects to independent entities that could be manipulated without regard to [...] metrological system. [...] Once the calculation was done, the result was expressed in the most appropriate metrological units and thus re-entered the natural world as a concrete quantity.”

²¹Used for volumes of grain, but also oil, dairy products, beer, etc., as well as to express the capacity of boats; volumes of earthworks instead use system $G_{Ur III/OB}$ based on a height of one cubit, see[[Pow87](#), p. 488; [Rob08](#), p. 294; [Rob19](#)].

²²From [P309594].

²³A larger unit, the guru₇ (*karûm*, grain heap), is sometimes used instead, with 𐎧𐎠𐏀𐎥𐎡𐏁 = 𐎧𐎠𐏀𐎥𐎡𐏁𐎢𐎺 (1 *karûm* = 3600 *kurrû*). See [Fri07, p. 415; Rob19].

3.4.1 Field lengths in Nirsu

The length system of the Early Dynastic IIIb state of Lagaš is of particular interest. As described in [Pow87, p. 466; Lec20, pp. 289 sq.], lengths are expressed in rods, but the unit sign ∇ is generally omitted; in addition, only tens of rods are used; these are equal to one rope, but the sign 𒌦 is not written either. Length shorter than one rope are expressed in half-rope using the 1/2 sign 𒌦 (again with no 𒌦), and then in reeds, *with* the sign 𒌦 . Effectively, this yields the following factor diagram:

$$\begin{array}{c} \nabla \xleftarrow{6} \text{ } \xleftarrow{2} \text{ } \text{𒌦} \xleftarrow{10} \text{ } \text{𒌦} \text{ } \text{𒌦}^{28} \\ \text{1 eše}_2=10 \text{ nindan} \\ \text{1 rope}=10 \text{ rods} \\ \text{60 m} \qquad \qquad \text{gi} \\ \qquad \qquad \qquad \text{reed} \\ \qquad \qquad \qquad \text{3 m} \end{array} \quad (L_{\text{ED IIIb}})$$

This is the system that was used to express the sides of the field in [P020054] discussed in section 3.2. In that tablet and others from the same period, such as the ones discussed in [Lec20], areas are expressed in system $G_{\text{ED IIIb}}$, with curviform numerals²⁹; in the absence of overt units, such as when dealing with length that are integer multiples of a half-rope³⁰, the use of curviform or cuneiform numerals therefore disambiguates a numeric expression between an area and a length, and therefore the interpretation of its numerals between systems $G_{\text{ED IIIb}}$ and $L_{\text{ED IIIb}}$. The sign 𒌦 , which would also disambiguate the interpretation as an area, is sometimes used after areas in ED IIIb Lagaš, but not systematically; in particular the area of the first field in [P020054] does not use this suffix. See [Lec20] for many examples with and without 𒌦 .

3.4.2 Dyke lengths in Nirsu

[Pow87, p. 466] notes that reeds “are regularly written with the normal, cuneiform end of the stylus. Higher units are usually written with the reversed (round) end of the stylus.” [TODO(egg): also mention Krebern timer 1998 p. 303 with note 686.] Powell does not elaborate on the specifics of this mixed use of numerals, but a cursory search in CDLI finds many occurrences³¹, such as:

- [P221305, obv. 1, 4]³² $\text{𒌦} \text{ } \text{𒌦} \text{ } \text{𒌦} \text{ } \text{𒌦} \text{ } \text{𒌦} \text{ } \text{𒌦}$
- [P020129, rev. 2, 1] $\text{𒌦} \text{ } \text{𒌦} \text{ } \text{𒌦} \text{ } \text{𒌦} \text{ } \text{𒌦} \text{ } \text{𒌦}$
- [P221291, rev. 5, 1]³³ $\text{𒌦} \text{ } \text{𒌦} \text{ } \text{𒌦} \text{ } \text{𒌦} \text{ } \text{𒌦} \text{ } \text{𒌦}$
- [P221266, rev. 2, 1] $\text{𒌦} \text{ } \text{𒌦} \text{ } \text{𒌦} \text{ } \text{𒌦}$

These expressions use an explicit sign 𒌦 (counted in multiples of ten) or 𒌦 . This notation—but not its use of curviform numerals—is remarked on in [Lec20, p. 290 with note 27], which cites several of the instances listed above. It seems to be typical of texts about dykes. These³⁴ can be summarized by the following factor

²⁸Note that the reeds are counted using *tenû* numerals, 𒌦 , 𒌦 , 𒌦 , etc.

²⁹TODO(egg): Note the handful of late Urukagina tablets that start to have cuneiform areas.

³⁰This is the case of the sides of the field in [P020054, obv. ii 2–3].

³¹A search for curviform numerals followed by some number of reeds counted in (*tenû*) cuneiform numerals currently finds 125 occurrences across 47 tablets.

³²CDLI only has a copy, but a photo may be found in [Lec12, p. 82]. On that photo the $\text{𒌦} \text{ } \text{𒌦} \text{ } \text{𒌦}$ is not visible. Lecompte notes that the copy is faithful; indeed another $\text{𒌦} \text{ } \text{𒌦} \text{ } \text{𒌦}$ can be seen both on the copy and the photo on obv. 2, 2.

³³From copy.

³⁴TODO Cite also DP 568, the one with 𒌦 and 𒌦 even though it has no reeds.

diagram:

$$\underbrace{\text{eye} \xleftarrow{10} \text{triangle} \xleftarrow{6} \bullet}_{\text{val}^{35}} = \underbrace{\text{triangle} \xleftarrow{2} \text{triangle} \xleftarrow{10} \text{triangle} \xleftarrow{6} \text{triangle} \xleftarrow{3} \text{triangle} \xleftarrow{3} \text{triangle}}_{\text{val}^{35}} \quad (L'_{\text{ED IIIb}})$$






3.4.3 Grain in Nirsu

TODO note the $\mathbb{H} \simeq \langle \mathbb{H} \rangle$.

3.4.4 Grain in Ebla

Lengths of Early Dynastic IIIb dykes from Nirsu are far from the only numeric expressions that mix curviform and cuneiform numerals.

The system of grain³⁶ capacities in Ebla uses the following units³⁷:

 $\xleftarrow{2}$  $\xleftarrow{\frac{5}{2}}$  $\xleftarrow{4}$  $\xleftarrow{6}$ 




gu₂-bar ba-ri₂-zu nin₄ nin₂-sagšu an-zam_x

The \curvearrowright and \curvearrowright are generally counted using curviform numerals, and the smaller units using cuneiform \uparrow numerals. Indeed, a search on [Mil+07] for co-occurrences of \curvearrowright with either of \curvearrowright or \curvearrowright finds the following expressions³⁸:

1. [P240532, *verso* 4, 9]  ⁴⁰ 𓆎𓆎𓆎𓆏𓆑𓆑𓆑
2. [P240548, *verso* 1, 1]  𓆏𓆑𓆑𓆑𓆑𓆑𓆑
3. [P240655, *recto* 7, 9]  ⁴¹ 𓆎𓆎𓆎𓆏𓆑𓆑𓆑
4. [P240579, *verso* 4, 3]  𓆏𓆑𓆑𓆑𓆑𓆑𓆑
5. [P240675, *verso* 2, 2]  𓆏𓆑𓆑𓆑𓆑𓆑𓆑
6. [P240609, *verso* 3, 1]  𓆏𓆑𓆑𓆑𓆑𓆑𓆑
7. [P240533, *recto* 3, 3]  𓆏𓆑𓆑𓆑𓆑𓆑𓆑
8. [P240697, *recto* 1, 5]  ⁴² 𓆏𓆑𓆑𓆑𓆑𓆑𓆑
9. [P240653, *recto* 6, 2]  𓆏𓆑𓆑𓆑𓆑𓆑𓆑

³⁵TODO(egg): Note that one unit may be omitted if the other is present



³⁶Liquid capacities use a different system [Arc15, p. 229 with note 12]:


 $\xleftarrow{30}$

 $\xleftarrow{6}$


At a glance it seems that \triangleright are counted with cuneiform numerals and higher units with curviform ones, thus

but we have not investigated this thoroughly.

³⁷TODO mention the other one citing Chambon and the footnote in Archi

³⁸We cite here only one attestation per tablet; most tablets contain several expressions mixing cuneiform  and larger with cuneiform  and smaller. In all cases the transcriptions given here are based on the EbDA transliterations, but the shape and orientation of the numerals was checked³⁹ on a photograph (from EbDA unless noted otherwise).

³⁹As we will see in Section 3.7.2, CDLI transliterations indicate numeral shape; however, as of this writing, they do so incorrectly on the Ebla corpus, claiming that all numerals are curviform, so we were not able to rely on them in this specific case.

⁴⁰ba-ri₂-zu₂, a variant spelling.

⁴¹Short for $\Box \perp$.

⁴²Note the omitted $\square \Diamond \perp$.

of decreasing fractions $\frac{1}{n}$ of this measure, whereby "n" was determined by the number of oblique impressions made by the rounded end of a thin stylus around a central point in a specific sign. Thus $\frac{1}{2} = \frac{1}{2} N_{30}$, $\frac{1}{3} = \frac{1}{3} N_{30}$, and so on. The first sign of the latter units, N_{34} ,

Figure 1: TODO [Eng98, p. 113]

10. [P240654, recto 2, 6]                                      

For instance, the first line contains the notations $1N_{34} 1N_{390} ; 2N_{20}$, which can be translated "60 of the (grain rations containing) (of grain); (grain involved:) 2 • (of ground barley)". This calculation contradicts the assumed numerical relationship $10N_1 = 1N_{14}$, since as was well known the measure represented by the sign N_{39} was $1/5$ of that represented by N_1 , so that $60 \times 1/5 = 12$ and not 20, as $2N_{14}$ would imply. Instead of relying on complicated

Figure 2: TODO [Eng98, p. 116]

Die halbkreisförmigen Griffelindrücke gehen manchmal in mehr oder weniger eckige Formen über (∇)⁶⁸⁵. Es gibt aber auch Einer in Form von regelrechten – meist mehr oder weniger schräggestellten – Keilen (\backslash), die öfters neben halbrunden Einern vorkommen und mit diesen kontrastieren⁶⁸⁶. Selten treten mit ∇ gebildete Zahlen auf⁶⁸⁷ (sie entsprechen den biga-Zahlen im Hohlmaßsystem, s.u. 7.4).

Figure 3: TODO [Kreg98, p. 303]

TODO figure

Figure 4: TODO [Cha03, p. 6]

formed by only two signs Υ and \angle , repeated as many times as necessary; this type of notation is highly standardized. Second, the order of magnitude of the numbers noted in this system is not indicated: 1, 60, 60², 60³, 1/60, 1/60², etc. are written in the same way, with the vertical wedge Υ . The third feature concerns the exact function of

Figure 5: TODO [Cha12, p. 58]

one step. The scribes of the Early Dynastic Period (c. 2600 BC), for instance, represented the number 648,000 with: $\Upsilon\Upsilon\Upsilon\bullet\bullet\bullet$ but never with the repetition $\Upsilon\Upsilon\Upsilon\Upsilon\Upsilon\Upsilon$.

Figure 6: TODO [Cha12, p. 59]⁵⁰

repetition of the same sign refers to both the capacity unit signified—often but not necessarily written immediately afterwards—and its value. The units of measurement are written in descending order from left to right—just as we would write 3 km, 120 m, 50 cm. For example:

$\Upsilon\Upsilon\Upsilon$ še bar ∇ ba-rí-zu

'3 gubar (capacity units) and 1 parisu'.

Figure 7: TODO [Cha12, p. 61]

This is particularly true of the signs ∇ , ∇ , ∇ and ∇ , whose form explicitly denotes the fractions 1/6, 2/6, 3/6, and 4/6 of the barig capacity measure written ∇ in Mesopotamia—also transcribed by Assyriologists as 1 bán, 2 bán, 3 bán, and 4 bán with reference to the bán measure worth 1/6 of the barig. At Ebla, the sign ∇ is most often associated with the parisu measure, while the signs ∇ , ∇ , ∇ and ∇ refer to 1, 2, 3,

Figure 8: TODO [Cha12, p. 64]


shape. The principle of notation is additive: each sign is noted as many times as necessary (e.g.,  transliterated as 2(šar₂) 1(geš'u) 3(u), means 2 × 3600 + 1 × 600 + 3 × 10). The system is based on an alternation of factors ten and

Figure 9: TODO

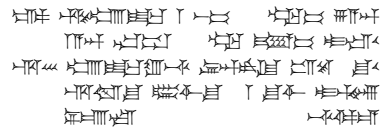
might think of one fabric and a half,¹¹ but the presence of notations with “2𐎶 2𐎶”, “3𐎶 3𐎶”, and “6𐎶 6𐎶” (Fig. 1) elements excludes that one deals with fractions, as these notations are not consistent with those of Šuruppag’s weight measurement system.¹² The notation “1𐎶 gada” in o. ii 1 and r. vi 1, along with the total of “39



Fig. 1. Combinations of numerals attested in Š. 742.

Figure 10: Discussion of the contrast between 𐎶 and 𐎵 numerals in [Gor23, p. 162].

3.5 Non-numeric usage



The beginning of the scribal art is a single wedge. That one has six pronunciations; it also stands for ‘sixty’⁵¹. Do you know its reading⁵²?

Examenstext A

Many of the cuneiform numerals are used with a logographic or phonetic value. For example, the sign 𐎶 has, *inter alia*, the values aš, rum, and dili. While the horizontal numerals are most frequently written 𐎶 in the Early Dynastic period⁵³, such non-numeric usage is almost⁵⁴ always written 𐎶, for instance:

— in personal names in administrative texts, such as the following, which all

⁵¹The reader will recall that 𐎶 is written 𐎶, with a larger wedge than 𐎶; however, these signs have merged by the time Examenstext A is composed.

⁵²Besides 𐎶, a look at [VT+14] shows that the values diš, ge₃, makkaš, san₂ak₄, and tal₄ are attested both in [TJV17] and in lexical lists. The sign is also used for the Akkadian word *ana* in the Neo-Assyrian period.

⁵³A CDLI search for “(asz@c)” finds 3296 ED texts, while a search for “(asz)” finds 81 ED texts, of which 46 also contain “(asz@c)”.

⁵⁴Exceptions are discussed in section 3.7.1.

as, for example, in TM.75.G.3125 = ARET III 107 o. iv 1, “4𐎶 𐎶a₃-da-um^{u9}-2 𐎶 4𐎶
aktum 4𐎶ib₂ 𐎶x₃ 𐎶sa₆ gunu₃” (Fig. 2).

Figure 11: Transliteration in [Gor23, p. 163] of [P242293, recto 4, 1] incorporating untransliterated numerals.

contain \triangleright numerals:

- 𒀭 in [P010424; P010458; P010459] from ED IIIa أبو صلابيخ ,
- 𒀭 in [P010960] from ED IIIa Šuruppag,
- 𒀭 in [P251641] from ED IIIb Adab,
- 𒀭 in [P252866] from ED IIIb Adab,
- 𒀭 in [P298637] from ED IIIb Umma;
- in the Sumerian word 𒀭 u_2 -rum, “property” in ED IIIb Nirsu administrative texts which contain \triangleright numerals, such as [P020006; P020008; P020018; P020024; P020030];
- in lexical texts:
 - in the divine name 𒀭 in the lexical texts [P010570; P010572], where the entries are prefixed with \triangleright .
 - in the word 𒀭 dili, “small fish” in [P010578], witness to Early Dynastic Fish,
 - in the same word with a determinative, 𒀭 dili^{ku₆}, in [P010586], witness to Early Dynastic Food, which starts with \triangleright numerals.

This is a clear contrast between 𒀭 and \triangleright in this period, and genuine ambiguity can arise if it is lost; for instance, the personal name 𒀭 occurs on its own line in the aforementioned administrative texts; a line $\triangleright \text{𒀭}$ would instead be read as “one slave”.

3.6 Limited benefits of diachronic encoding for numerals

The argument in favour of diachronic encoding is that it facilitates interoperability in a variety of use cases, as we have outlined in section 3.1. While these benefits are real and now visible for cuneiform signs, similar considerations are not generally applicable to curviform numerals.

Diachronic reference works such as sign lists and dictionaries tend to not include numbers, or when they do, they treat them separately, and include signs such as 𒀭 that have both numeric and non-numeric values in both the main list and the section on numbers. For instance, [Sch35, pp. 123 sqq.] lists all of 𒀭 together with \triangleright - 𒀭 , while 𒀭 , 𒀭 , and 𒀭 , and only those, appear at the beginning of the sign list, since they have non-numeric values⁵⁵. [Cat13, p. 58] has the numeric signs \triangleright , 𒀭 , 𒀭 , whereas non-numeric 𒀭 is at the beginning of the sign list, where its values *aš* and *rum* are listed. For signs with both non-numeric and numeric usage, [Dei22] writes *s. die Zahlz.* throughout the main list; LAK 1 𒀭 thus reappears at LAK 829 together with \triangleright , 𒀭 , and 𒀭 . One should note [Bor10], which has numbers throughout the sign list; but that sign list does not show glyphs predating the Old Babylonian period, nor does it comprehensively cover the numerals used in the Ur III and Old Babylonian periods, as, for instance, it does not have 𒀭 - 𒀭 used in system $G_{\text{Ur III/OB}}$.

Composite texts rarely have witnesses both from the Early Dynastic period and later; the kinds of texts that do, chiefly lexical and literary texts, do not contain numbers to the extent that administrative texts do. Further, there tend to be changes⁵⁶ to the text between Early Dynastic and later witnesses that prevent a diachronic encoding of such composites. For numerals, the switch from \triangleright to 𒀭 numerals prevents diachronic encoding even if \triangleright were unified with 𒀭 . For instance, the

⁵⁵Non-numeric values of 𒀭 were discussed in section 3.5; 𒀭 has the values *man₃* and *min₅*, and is used for the word *didli*, “several, various”; 𒀭 has the value *eš₆*.

⁵⁶TODO comment on the ED witnesses to the instructions of Šuruppag

lexical list Early Dynastic Food, already mentioned in section 3.5, contains some numbers, and has a witness from the Old Akkadian period covering these numbers: [P215653, a 1'-6']; however, they are written with 𐎶 numerals, whereas they are written with 𐎵 numerals in the Early Dynastic witnesses; since 𐎶 and 𐎵 are distinct⁵⁷ characters, the 𐎵-𐎶 unification does not help.

More generally, since numbers are so deeply tied to metrology, and since metrological systems change between the Early Dynastic and later periods⁵⁸, there is little opportunity for a diachronic representation of numeric quantities.

In the case of analyses such as [Romach2023], it is interesting to note that numeric expressions are removed prior to the conversion of the corpus to Unicode cuneiform for further analysis.

3.7 Compatibility considerations

A disunification twenty years after the fact, affecting all numerals, would ordinarily be a serious compatibility issue. Fortunately, with one exception discussed below, we are not aware of any font using curviform glyphs for the already-encoded numerals. In fact we are not aware of any font designed for a style earlier than Old Babylonian, except for fonts mimicking the representative glyphs from the code charts, which are primarily Ur III, but sometimes earlier or later, as described in [UTR56, §2.4]. The lack of dedicated Ur III fonts may be explainable by the chart-like fonts⁵⁹ being good enough for most purposes; the lack of Early Dynastic fonts, by the aforementioned issues with numeral unification making the representation of any text with numerals intractable.

3.7.1 The case of ŠAR₂

The character U+122B9 𐎶 CUNEIFORM SIGN SHAR2 has a circular reference glyph.

In most texts from the Early Dynastic IIIb and Old Akkadian period⁶⁰, a contrast between non-numeric šar₂ written 𐎶 and numeric 1(šar₂) written 𐎶 can be observed, similar to the contrast between 𐎶 and 𐎵 previously discussed in section 3.5. However, in lexical lists from Šuruppag and Ebla⁶¹, as well as in the *Stèle des vautours*, non-numeric šar₂ is curviform:

- 𐎶 𐎶 𐎶 𐎶 and 𐎶 𐎶 𐎶 𐎶 in [P010566];
- 𐎶 𐎶 and 𐎶 𐎶 in [P010576];
- 𐎶 𐎶 in [P240986]⁶²;

⁵⁷Besides the contrasts in numeric usage mentioned in section 3.3.3, these characters are clearly not unifiable because of the many contrasts in non-numeric usage between them; several values of 𐎶 which are not shared with 𐎶 have already been mentioned, but perhaps most striking is the fact that, in the Neo-Assyrian period, 𐎶 is used for the preposition *ina*, “in”, and 𐎶 for the preposition *ana*, “to”.

⁵⁸TODO cite a few things here.

⁵⁹Most prominently Noto Sans Cuneiform, a system font on both Windows—as part of Segoe UI Historic—and macOS.







⁶⁰For example, in personal names:


- 𐎶 𐎶 𐎶 𐎶 in [P020019] from ED IIIb Nirsu;
- 𐎶 𐎶 𐎶 𐎶 in [P020182], also from ED IIIb Nirsu;
- 𐎶 𐎶 𐎶 in [P222186] from ED IIIb Umma;
- 𐎶 𐎶 𐎶 in [P235312] from Old Akkadian Umma.





⁶¹TODO Mention other ways in which these are archaizing

⁶²From copy in [ELLeS].








—   in [P222399, obv. 17, 9, 18, 11, 22, 12]⁶³.















It *would* be disruptive to the diachronic representation of text if non-numeric šar₂ were to have two different representations. The character U+122B9 CUNEIFORM SIGN SHAR2 should therefore be used in those cases, with its curviform glyph , identical to the glyph of the proposed U+12579  CUNEIFORM NUMERIC SIGN ONE N45. Since the archaizing style of texts wherein non-numeric šar₂ is curviform solidly predates the transition from  to  in the relevant metrological systems, there is no need to represent a - contrast, so these characters can have the same glyph in specialist archaizing Early Dynastic fonts.











Since cuneiform U+122B9 CUNEIFORM SIGN SHAR2 effectively merges with U+1212D  CUNEIFORM SIGN HI, the reference glyph should remain as it is, *i.e.*, curviform, so that the contrast between reference glyphs remains clear; see [UTR56, §2.4]. Since system fonts follow the reference glyphs, and since extant specialist fonts target styles where U+122B9 is unambiguously cuneiform, there are no compatibility issues.




Note that in rare cases, such as [P222243] from ED IIIa Adab, non-numeric  (here with the value rum) is written . It is out of scope for this proposal to decide whether such occurrences should be treated as anomalous spellings, encoded as U+12550  CUNEIFORM NUMERIC SIGN ONE N01, or as stylistic distinctions, encoded as U+12038 CUNEIFORM SIGN ASH with a curviform glyph. In practice this would often be determined by the transliteration from which the cuneiform text is generated; it is noteworthy that as of this writing, the CDLI transliteration (UR2-1(aš@c)) and the ePSD2 one (uru₈^{rum}) of this word disagree on that aspect. Since  has a cuneiform reference glyph, this does not pose any compatibility concerns.

3.7.2 Transliteration

An important feature of the encoding is that, in order to support input and bulk conversion of transliterated corpora to Unicode cuneiform, it should not represent distinctions that are finer than those recorded in typical transliterations; thus, while some older forms of BIL₂ can be described as   NE  KASKAL or   NE  PAP⁶⁴, they are typically all transliterated bil₂, and therefore are all represented by the character U+1224B  CUNEIFORM SIGN NE SHESHIG, its name notwithstanding, as described in [UTR56, §2.5].

The situation is more complicated for numbers. Many transliterations do not represent the type of numeral used, instead interpreting the whole numeric expression and transcribing it with delimiters or units as needed to disambiguate. For instance,    from [P305639] may be transliterated as 95 gur, as in [Feuerherm2004]. The numerals may also be transliterated separately, but solely by their values in terms of the overt unit, as in EbDA transliterations: the aforementioned          from [P240533, recto 3, 3] is transliterated “20-1-1/2 gu₂-bar 7 nig₂-sagšu 2-1/2 an-zam_x⁶⁵ za”, reading both  and  as 1/2, but not distinguishing them.

In particular, these transliterations do not differentiate between  and  numerals, nor between  and  numerals. For instance, the aforementioned      

⁶³Note however    on [P222399, obv. 6, 17]. Curviform non-numeric šar₂ is clearly archaizing in ED IIIb Nirsu; one might suppose that the scribe slipped into their modern ways here. TODO add a photo.

⁶⁴As on [P249253].

⁶⁵As of this writing, EbDA actually has an-zam_x, with U+1D6A GREEK SUBSCRIPT SMALL LETTER CHI.

𐎶 𐎶𐎵 𐎶𐎵 𐎶𐎵 𐎶𐎵 𐎶𐎵 from [P242293, recto 4, 1] is transliterated “4 ‘a₃-da-um^{tug₂}-II 4 aktum^{tug₂} 4 ib₂-III gun₃ sa₆^{tug₂}” in EbDA, with no distinction between the 𐎶 and 𐎶𐎵. Since 𐎶 and 𐎶 numerals are separately encoded, the numeric expressions in such transliterations cannot be transformed into Unicode cuneiform without additional context, regardless of curviform–cuneiform unification.

In metrological systems such as systems $G_{Ur III/OB}$ and $C_{Ur III/OB}$ where some units are indicated by the type of numeral rather than an overt unit sign, it is common practice to add the unit in parentheses in transliteration; for instance, 𐎶𐎵 𐎶𐎵 𐎶𐎵 𐎶𐎵 𐎶𐎵 from [P386847] is transliterated “1(eše₃) 5½ iku⁶⁶ 7 sar” in [Feuerherm2004], and 𐎶𐎵 𐎶𐎵 𐎶𐎵 𐎶𐎵 𐎶𐎵 from [P307255] is transliterated “1(n⁶⁷) 2(b) 7 ½ sila₃” in [Feuerherm2004].

This practice has been generalized to systematically indicate numeral shape; this is in particular the case in CDLI, where the transliterations of some of the above examples are “1(gesz2) 3(u) 5(asz) gur” for 𐎶𐎵 𐎶𐎵 𐎶𐎵, “1(esze3) 5(iku) 1/2(iku) GAN2 7(disz) sar” for 𐎶𐎵 𐎶𐎵 𐎶𐎵 𐎶𐎵 𐎶𐎵, and “3(barig) 2(ban2) 7(disz) 1/2(disz) sila₃” for 𐎶𐎵 𐎶𐎵 𐎶𐎵 𐎶𐎵. CDLI and ePSD2 both distinguish curviform from cuneiform numerals in transliteration: the length 𐎶𐎵 𐎶𐎵 𐎶𐎵 𐎶𐎵 𐎶𐎵 𐎶𐎵 from [P020129, rev. 2, 1] is transliterated “6(gesz2@c) 3(u@c) {ninda}nindax(DU) 1/2(asz@c) 4(disz@t) gi” in CDLI, and “6(geš₂^c) 3(u^c) ninda ninda_x(DU) 1/2(aš^c) 4(diš^t) gi” in ePSD2. Another example is [Molina2014], which uses 1a for 𐎶, 1d for 𐎶, 1ac for 𐎶, 1dc or ½dc for 𐎶 depending on reading, etc. The literature on the Uruk and Early Dynastic I–II periods uses a different set of transliteration conventions that also disambiguate numeral shapes, as will be discussed in section 4.

While there exist transliterations that distinguish 𐎶 from 𐎶 but not 𐎶 from 𐎶, such as the ones used in [DCCMT], the trend, especially in more recent works in third millennium studies, seems to be to represent numeral shape; for example, [Maiocchi2024] gave an example of the input syntax used by the new “Urban Economy Begins” project as “10 + 5c(GUR) + 2(BARIGA) + 1(BAN2)” for 𐎶𐎵 𐎶𐎵 𐎶𐎵 𐎶𐎵, with a c indicating that the GUR numerals are curviform, and the parenthetical GUR indicating that these are 𐎶 rather than 𐎶 numerals.

3.8 Conclusions

Co-occurrences of curviform and cuneiform numerals are not anecdotal in the Early Dynastic period. Instead, they represent contrasts between metrological systems, between individual units within metrological system, and between numeric usage and phonetic or logographic usage. This contrastive usage is reflected in modern publications.

While it would be technically possible to handle this contrast as a stylistic distinction, this approach has no real benefit, and is highly inconvenient, as it requires single numeric expressions to systematically use multiple fonts. Further, if that contrast is lost in plain-text interchange, the text can be misinterpreted: 𐎶𐎵 is a length of three ropes, but 𐎶𐎵 is an area of three bur₃; 𐎶𐎵 could be read as one 𐎶𐎵 and one 𐎶𐎵, where 𐎶𐎵 would be one and a half 𐎶𐎵; 𐎶𐎵 is a personal name, but 𐎶𐎵 would be “one slave”.

At the same time, contrary to most disunifications, the separate encoding of curviform numerals poses no serious compatibility issues for existing fonts or encoded corpora, nor does it, in general, introduce new issues with transliterated

⁶⁶TODO say something about this reading

⁶⁷TODO comment on nigida.

third millenium corpora. The oddity of ● requires some explanation, but does not pose any architectural issues, and is not fundamentally different from the other mergers and splits encountered in the cuneiform script.

4 Rationale for ED-Uruk numeral unification

TODO mention the bariga silliness in the CDLI transliteration of Gori's paper.

5 Considerations on individual numeral series

[TODO Document to the extent possible the metrological systems in which each sign is used. Note the disunification of N9 and N10 from 4(ban₂@c) and 5(ban₂@c).]

6 Characters not included in this proposal

6.1 Missing numerals

N13 not attested in CDLI (N_{17} , $12N_{14}$, etc.) 7(diš *tenû*)

6.2 Stacking patterns

(... are a mess, vary within Uruk, and are not transliterated/documented by Englund, so let's not go there for now.)

6.3 Matters for higher-level protocols

Rotated bits: <https://cdli.mpiwg-berlin.mpg.de/artifacts/101087>

Acknowledgements

TODO(egg): Something about the Vanséveren fonts

References

Artefacts

- | | |
|-----------|--|
| [P020054] | VAT 4731. [För16, 40 p.14]. Vorderasiatisches Museum.
CDLI: P020054 . |
| [P020129] | VAT 04713. Vorderasiatisches Museum.
CDLI: P020129 .
ORACC: epsd2/corpus/P020129 . |
| [P102305] | X.3.139. Michael C. Carlos Museum, Emory University.
CDLI: P102305 . |

- [P215653] AS 15375 21. Musée du Louvre.
CDLI: [P215653](#).
ORACC: [dcclt/corpus/P215653](#).
Louvre Collections: [ark:/53355/cl010436723](#).
- [P221266] AO 13825. Musée du Louvre.
CDLI: [P221266](#).
ORACC: [epsd2/corpus/P221266](#).
Louvre Collections: [ark:/53355/cl010138527](#).
- [P221291] AO 13850. Musée du Louvre.
CDLI: [P221291](#).
ORACC: [epsd2/corpus/P221291](#).
- [P221305] AO 13864. Musée du Louvre.
CDLI: [P221305](#).
ORACC: [epsd2/corpus/P221305](#).
- [P222399] *Stèle des vautours*. AO 50; AO 2346; AO 2347; AO 2348; AO 16109.
Musée du Louvre.
CDLI: [P222399](#).
- [P232278] *Gudea E*. AO 6. Musée du Louvre.
CDLI: [P232278](#).
ORACC: [etcstri/Q001544](#).
- [P232280] *Gudea G*. AO 7. Musée du Louvre.
CDLI: [P232280](#).
ORACC: [etcstri/Q001546](#).
- [P240531] TM.75.G.00265. Idlib, Syria: National Museum of Syria.
CDLI: [P240531](#).
EbDA: [1415](#).
- [P240532] TM.75.G.00266. Idlib, Syria: National Museum of Syria.
CDLI: [P240532](#).
EbDA: [1324](#).
- [P240533] TM.75.G.00267. Idlib, Syria: National Museum of Syria.
CDLI: [P240533](#).
EbDA: [1379](#).
- [P240548] TM.75.G.00302. Idlib, Syria: National Museum of Syria.
CDLI: [P240548](#).
EbDA: [1350](#).
- [P240579] TM.75.G.00341. Idlib, Syria: National Museum of Syria.
CDLI: [P240579](#).
EbDA: [1364](#).
- [P240609] TM.75.G.00440. Idlib, Syria: National Museum of Syria.
CDLI: [P240609](#).
EbDA: [1378](#).
- [P240653] TM.75.G.00535. Idlib, Syria: National Museum of Syria.
CDLI: [P240653](#).
EbDA: [1382](#).

- [P240654] TM.75.G.00536. Idlib, Syria: National Museum of Syria.
CDLI: [P240654](#).
EbDA: [1383](#).
- [P240655] TM.75.G.00537. Idlib, Syria: National Museum of Syria.
CDLI: [P240655](#).
EbDA: [1358](#).
- [P240675] TM.75.G.00557. Idlib, Syria: National Museum of Syria.
CDLI: [P240675](#).
EbDA: [1371](#).
- [P240697] TM.75.G.00579. Idlib, Syria: National Museum of Syria.
CDLI: [P240697](#).
EbDA: [1381](#).
- [P241708] TM.75.G.02143. Idlib, Syria: National Museum of Syria.
CDLI: [P241708](#).
EbDA: [3173](#).
- [P241904] TM.75.G.02346. [[Arc89](#), p. 6]. Idlib, Syria: National Museum of Syria.
CDLI: [P241904](#).
EbDA: [3183](#).
- [P242293] TM.75.G.03125. Idlib, Syria: National Museum of Syria.
CDLI: [P242293](#).
EbDA: [217](#).
- [P249253] *Code de Hammurabi*. Sb 8. Musée du Louvre.
CDLI: [P249253](#).

Unicode documents

- [L2/03-162] M. Everson and K. Feuerherm. *Basic principles for the encoding of Sumero-Akkadian Cuneiform*. 25th May 2003.
UTC: [L2/03-162](#).
- [L2/03-393R] M. Everson, K. Feuerherm and S. Tinney. *Preliminary proposal to encode the Cuneiform script in the SMP of the UCS*. 3rd Nov. 2003.
UTC: [L2/03-393R](#).
- [L2/04-036] M. Everson, K. Feuerherm and S. Tinney. *Revised proposal to encode the Cuneiform script in the SMP of the UCS*. 29th Jan. 2004.
UTC: [L2/04-036](#).
- [L2/04-099] L. Anderson. *Unification of Cuneiform Numbers*. 2004.
UTC: [L2/04-099](#).
- [L2/04-189] M. Everson, K. Feuerherm and S. Tinney. *Final proposal to encode the Cuneiform script in the SMP of the UCS*. 8th June 2004.
UTC: [L2/04-189](#).
- [L2/24-159] P. Constable, ed. *Minutes of UTC Meeting 180* (23rd–25th July 2024). 29th July 2024.
UTC: [L2/24-159](#).

- [Uni16] The Unicode Consortium. *The Unicode Standard*. Version 16.0.0. The Unicode Consortium, 10th Sept. 2024.
ISBN: 978-1-936213-34-4.
eprint: <https://www.unicode.org/versions/Unicode16.0.0/core-spec/>.
- [UTR56] R. Leroy, ed. *Unicode Cuneiform Sign Lists*. Unicode Technical Report #56.
eprint: <https://www.unicode.org/reports/tr56/>.

Other documents

- [Arc15] A. Archi. *Ebla and Its Archives. Texts, History, and Society*. Studies in ancient Near Eastern records 7. Walter de Gruyter, 2015.
ISBN: 978-1-61451-716-0.
DOI: [10.1515/9781614517887](https://doi.org/10.1515/9781614517887).
- [Arc89] A. Archi. “Tables de comptes eblaïtes”. In: *Revue d’assyriologie et d’archéologie orientale* 83.1 (1989). Ed. by P. Amiet and P. Garelli, pp. 1–6. ISSN: 0373-6032.
- [Bor10] R. Borger. *Mesopotamisches Zeichenlexikon*. Alter Orient und Altes Testament 305. Ugarit-Verlag, 2010.
- [Cap02] R. Caplice. *Introduction to Akkadian*. 4th ed. Editrice Pontificio Istituto Biblico, 2002.
ISBN: 88-7653-566-7.
- [Cat13] A. Catagnoli. *La paleografia dei testi dell’amministrazione e della cancelleria di Ebla*. Quaderni di Semitistica 9. Università di Firenze, 2013.
ISBN: 8890134054.
- [Cha03] G. Chambon. “Archaic Metrological Systems from Ur”. In: *Cuneiform Digital Library Journal* 2003.5 (23rd Dec. 2003). ISSN: 1540-8779.
eprint: http://cdli.ucla.edu/pubs/cdlj/2003/cdlj2003_005.html.
- [Cha12] G. Chambon. “Numeracy and Metrology”. In: *The Oxford Handbook of Cuneiform Culture*. Ed. by K. Radner and E. Robson. Oxford University Press, 18th Sept. 2012, pp. 51–67.
ISBN: 9780199557301.
DOI: [10.1093/oxfordhob/9780199557301.013.0003](https://doi.org/10.1093/oxfordhob/9780199557301.013.0003).
- [DE87] P. Damerow and R. K. Englund. “Die Zahlzeichensysteme der archaischen Texte aus Uruk”. In: M. W. Green and H. J. Nissen. *Zeichenliste der archaischen Texte aus Uruk*. Archaische Texte aus Uruk 2. An offprint of this chapter is available at <https://cdli.mpiwg-berlin.mpg.de/files-up/publications/englund1987a.pdf>. Gebr. Mann Verlag, 1987. Chap. 3, pp. 117–165.
- [Dei22] A. Deimel. *Liste der archaischen Keilschriftzeichen von Fara*. Wissenschaftliche Veröffentlichungen der Deutschen Orient-Gesellschaft 40. J. C. Hinrichs’sche Buchhandlung, 1922.

- [Eng98] R. K. Englund. "Texts from the Late Uruk Period". In: *Mesopotamien. Späturuk-Zeit und Frühdynastische Zeit*. Orbis Biblicus et Orientalis 160/1. 1998, pp. 13–233.
ISBN: 3-7278-1166-8.
- [För16] W. Förtsch. *Altbabylonische Wirtschaftstexte aus der Zeit Lugalanda's und Urukagina's*. Vorderasiatische Schriftdenkmäler der Königlichen Museen zu Berlin 14. J. C. Hinrichs, 1916.
- [Fri07] J. Friberg. *A Remarkable Collection of Babylonian Mathematical Texts. Manuscripts in the Schøyen Collection: Cuneiform Texts I*. Sources and Studies in the History of Mathematics and Physical Sciences. Springer, 2007.
ISBN: 978-0-387-34543-7.
- [Fri78] J. Friberg. *A Method for the Decipherment, through Mathematical and Metrological Analysis, of Proto-Sumerian and Proto-Elamite Semi-Pictographic Inscriptions*. The Third Millenium Roots of Babylonian Mathematics 1. Department of Mathematics, Chalmers University of Technology, 1978.
- [Gom16] B. Gombert. "ED IIIb metrology: texts from Lagaš". In: *CDLI:wiki. A Library of Knowledge of the Cuneiform Digital Library Initiative*. 12th Apr. 2016.
eprint: https://cdli.ox.ac.uk/wiki/doku.php?id=ed_iii_metrological_systems.
- [Gor23] F. Gori. "On Lapis Lazuli and Linen in Šuruppag Texts. An Analysis Through the Lens of Ebla Studies". In: *Studia Eblaitica* 9 (2023), pp. 160–166. ISSN: 2364-7124.
- [Hue11] J. Huehnergard. *A Grammar of Akkadian*. 3rd ed. Brill, 2011.
ISBN: 978-1-57506-941-8.
- [Jim+23] E. Jiménez, Z. Földi, A. Härtinen, A. Heinrich, T. Mitto, G. Rozzi, I. Khait, J. Laasonen, F. Simonjetz et al., eds. *electronic Babylonian Library*. 2023–.
eprint: <https://www.ebl.lmu.de/>.
- [JJ24] T. Jauhiainen and H. Jauhiainen. "Advancing Cuneiform Text Dating Through Automatic Analysis". 69th Rencontre Assyriologique Internationale (8th–12th July 2024). 11th July 2024 14:00.
- [Kre98] M. Krebern timer. "Die Texte aus Fāra und Tell Abū Šalābīḥ". In: *Mesopotamien. Späturuk-Zeit und Frühdynastische Zeit*. Orbis Biblicus et Orientalis 160/1. 1998, pp. 235–427.
ISBN: 3-7278-1166-8.
- [Lec12] C. Lecompte. "Des chiffres et des digues: à propos de deux textes présargoniques de Ġirsu et d'une notation numérique inhabituelle". In: *Altorientalische Forschungen* 39.1 (Dec. 2012), pp. 81–86.
DOI: [10.1524/aof.2012.0006](https://doi.org/10.1524/aof.2012.0006).
- [Lec20] C. Lecompte. "The Measurement of Fields During the Pre-sargonic Period". In: *Mathematics, Administrative and Economic Activities in Ancient Worlds*. Ed. by C. Michel and K. Chemla. Why the Sciences of the Ancient World Matter 5. Springer, 2020.

- [Mil+07] L. Milano, M. Maiocchi, F. Di Filippo, R. Orsini, E. Scarpa, M. Surdi et al., eds. *Ebla Digital Archives*. 2007–. eprint: <http://ebda.cnr.it/>.
- [NDE93] H. J. Nissen, P. Damerow and R. K. Englund. *Archaic Bookkeeping. Early Writing and Techniques of Economic Administration in the Ancient Near East*. Trans. by P. Larsen. The University of Chicago Press, 1993. ISBN: 0-226-58659-6.
- [Oel22] J. Oelsner. *Der Kodex Hammu-rāpi*. dubsar 4. Zaphon, 2022.
- [Pow87] M. Powell. “Maße und Gewichte”. In: *Reallexikon der Assyriologie und vorderasiatischen Archäologie*. Ed. by D. O. Edzard. Vol. 7 Libanukšabaš–Medizin. 1987–1990, pp. 457–530.
- [Rob08] E. Robson. *Mathematics in Ancient Iraq. A Social History*. Princeton University Press, 2008. ISBN: 978-0-691-09182-2.
- [Rob19] E. Robson. “Oracc metrology guidelines”. In: *Oracc: The Open Richly Annotated Cuneiform Corpus*. 18th Dec. 2019. ORACC: [doc/help/editinginf/metrology/metrologicaltables](http://oracc.org/doc/help/editinginf/metrology/metrologicaltables).
- [Rob22] E. Robson. “Overview of Metrological Systems”. In: *The Digital Corpus of Cuneiform Mathematical Texts*. 2022. ORACC: [dccmt/Metrology](http://oracc.org/dccmt/Metrology).
- [Rom24] A. Romach. “The Neo Assyrian Land Sale Documents from Dur-Katlimmu: A Stylometric Analysis of Their Scribal Features”. 69th Rencontre Assyriologique Internationale (8th–12th July 2024). 10th July 2024 12:00.
- [Sch10] W. Schramm. *Akkadische Logogramme*. Göttinger Beiträge zum Alten Orient 5. Universitätsverlag Göttingen, 2010. ISBN: 978-3-941875-65-4. DOI: [10.17875/gup2010-511](https://doi.org/10.17875/gup2010-511).
- [Sch35] N. Schneider. *Die Keilschriftzeichen der Wirtschaftsurkunden von Ur III*. Editrice Pontificio Istituto Biblico, 1935.
- [Svä+24] S. Svärd, M. Lorenzon, J. Töyräänvuori, J. Valk, T. Alstola, E. Bennett, R. Uotila and T. Auranen, eds. *RAI 69 Abstracts*. July 2024. eprint: https://www.helsinki.fi/assets/drupal/2024-07/RaiAbstractBookAjoitettuJaPäiväty_1.pdf.
- [TJV17] S. Tinney, P. Jones and N. Veldhuis, eds. *The electronic Pennsylvania Sumerian Dictionary*. 2nd ed. 2017–. eprint: <http://oracc.org/epsd2>.
- [VT+14] N. Veldhuis, S. Tinney et al., eds. *Oracc Sign List*. 2014–. eprint: <http://oracc.org/osl/>.