

Re-Practical Examination

11 June 2016

Time allowed: 2 hours

Instructions (please read carefully):

1. This is an **open-book exam**.
2. This practical exam consists of **three** questions. The time allowed for solving this quiz is **2 hours**.
3. The maximum score of this quiz is **30 marks** and you will need to answer all three questions to achieve the maximum score. Note that the number of marks awarded for each question **IS NOT** correlated with the difficulty of the question. If you are taking this quiz as a re-exam, your maximum score will be capped at **20 marks**.
4. You are advised to attempt all questions. Even if you cannot solve a question correctly, you are likely to get some partial credit for a credible attempt.
5. Your answers should be submitted on Coursemology.org. You will be allowed to run some public tests cases to verify that your submission is correct. Note that you can run the test cases on Coursemology.org up to a **maximum of 5 times** because they are only for checking that your code is submitted correctly. You are expected to test your own code for correctness using IDLE and not on Coursemology.org. Do however ensure that you submit your answers correctly by running the test cases at least once.
6. In case there are problems with Coursemology.org, you are also provided with the template `repractical-template.py` to work with. If Coursemology.org fails, you will be required to rename your file `repractical-exam-<mat no>.py` where `<mat no>` is your matriculation number and upload the file to the Re-Practical Exam folder in IVLE Workbin. You should only upload one file. If you upload multiple files, we will choose one at random for grading.
7. Please note that it shall be your responsibility to ensure that your solution is submitted correctly to Coursemology (or uploaded to IVLE, if there are problems) at the end of the examination. Failure to do so will render you liable to receiving a grade of **ZERO** for the Practical Exam, or the parts that are not uploaded correctly. You have been warned.
8. Please note that while sample executions are given, it is not sufficient to write programs that simply satisfy the given examples. Your programs will be tested on other inputs and they should exhibit the required behaviours as specified by the problems to get full credit. There is no need for you to submit test cases.

GOOD LUCK!

Question 1 : Circular Primes [10 marks]

The number, 197, is called a *circular prime* because all rotations of the digits: 197, 971, and 719, are themselves prime. There are thirteen such primes below 100: 2, 3, 5, 7, 11, 13, 17, 31, 37, 71, 73, 79, and 97. In this question, we will count these circular primes. Note that we are talking about rotation and NOT permutation of the digits.

A. [Warm Up] Write a function `rotations` that will take as arguments a positive integer n and return a list of all the rotations for the number with no repetitions. The order within the list doesn't matter. [5 marks]

Sample execution:

```
>>> rotations(1)
[1]

>>> rotations(11)
[11]

>>> rotations(101)
[101, 11, 110]

>>> rotations(123)
[123, 231, 312]

>>> rotations(221)
[221, 212, 122]

>>> rotations(1231)
[1231, 2311, 3112, 1123]

>>> rotations(1212)
[1212, 2121]
```

B. [Count Circular Primes] Write a function `count_circular_primes` that will take as arguments a positive integer n and return the number of circular primes $\leq n$. [5 marks]

To help you out, the following is the code for `is_prime`:

```
def is_prime(n):
    if n==1:
        return False
    for i in range(2,int(sqrt(n))+1):
        if n%i == 0:
            return False
    return True
```

Sample execution:

```
>>> count_circular_primes(2)
1

>>> count_circular_primes(4)
2

>>> count_circular_primes(13)
6

>>> count_circular_primes(57)
9

>>> count_circular_primes(100)
13
```

Question 2 : Tyrion's Flight Mania [10 marks]

After trying his luck with the dragons of the *Khaleesi*, Tyrion Lannister has *time-travelled* to the modern day. He is now fixated upon machines that fly common people over large distances – the airplanes. He is quite interested in knowing who owns how many of these airplanes, which are the most popular ones and how they interconnect several modern cities on planet earth. With the help of his friend Lord Varys, Tyrion has managed to get a flight routes dataset. Your task is to use the sacred magic of Python on this flight routes dataset and answer the following questions that Tyrion has posed. And it's in your best interests to do so; because a Lannister always pays his debts!

The flight data is provided in the accompanying file `flight_routes.csv` where each entry contains the following information:

- Airline : 2-character IATA code that uniquely identifies an airline operating the route
- Source airport : 3-character IATA code that uniquely identifies the source airport
- Destination airport : 3-character IATA code that uniquely identifies the destination airport
- Aircraft type(s) : Alphanumeric code(s) to identify particular plane(s) used on the flight route.

Note that (i) Each route is defined by a source-destination pair of airports and several airlines would operate on a route. For a route, there is only **one entry** per airline to indicate that the airline serves that route. (ii) For a given route, an airline could fly different aircrafts depending upon the number of bookings for a particular flight. For example, Singapore Airlines (SQ) operates four different aircrafts on the route from Singapore (SIN) to Beijing (PEK), namely – 772, 77W, 773 and 333. These are unique codes illustrating different aircrafts.

You do not have to worry about the codes used for airlines, airports or aircrafts and they are to be treated merely as keys.

A. [Number of Flights] Help Tyrion to easily find out the number of **direct** flights available if he wants to fly from one city to another. Thus, write a function `get_num_flights` that takes in a source airport, a destination airport and the name of the file containing the flights data. The function should return the number of direct flights available between the source and destination airports. It returns zero, if no direct flights are available.

Note: In reality, one airline could operate several direct flights on a route. However, for simplicity all these flights are represented as a single flight per airline in this dataset. So do not be alarmed if the numbers look too small to be believable. [2 marks]

Sample execution:

```
>>> get_num_flights('VIE', 'HAM', 'flight_routes.csv')
1

>>> get_num_flights('SIN', 'MNL', 'flight_routes.csv')
3

>>> get_num_flights('SIN', 'HAV', 'flight_routes.csv')
0
```

B. [Airport Hubs] The airports that act as connecting points for several domestic or international flights are called the *airports hubs*. Needless to say, they are also one of the busiest airports in terms of the number of flights that arrive **and** depart. Write a function `get_top_k_hubs` that takes in a value `k` and the `flights` dataset to return the list of top `k` hubs. The returned list should consist of tuples of the form `(airport, flights_count)` which would be arranged in descending order of the number of flights. If there are airports that serve equivalent number of flights as that of the k^{th} airport, include them in the list as well. Also, if there is any tie within the top-`k`, then the airports should be listed in an alphabetical order. In case the `k` is greater than the total number of airports in the data file, your solution should include all the airports.

[4 marks]

Sample execution:

```
>>> get_top_k_hubs(1, 'flight_routes.csv')
[('SIN', 224)]

>>> get_top_k_hubs(2, 'flight_routes.csv')
[('SIN', 224), ('MNL', 144)]

>>> get_top_k_hubs(3, 'flight_routes.csv')
[('SIN', 224), ('MNL', 144), ('CGN', 134)]

>>> get_top_k_hubs(4, 'flight_routes.csv')
[('SIN', 224), ('MNL', 144), ('CGN', 134), ('CTU', 122)]
```

C. [Flight Search] Not all airports are connected by direct flights and sometimes you need to make transfers, typically at the airport hubs. When Tyrion would fly from one city to another, depending upon his mood he would be willing to change flights, or not. Write a function `search_routes` that takes source airport, destination airport, the flights dataset and the **maximum** number of hops as input. The function should return the list of all possible routes in the **increasing order** of number of hops. Each route would be presented as a list of airports. Also no route would involve visiting the same airport twice (i.e. no loops) for obvious reasons. An empty list should be returned if no route is found for the specified maximum number of hops. Your solution should work for any number of maximum hops. Also there should be no duplicate routes in the returned list of routes.

[4 marks]

Sample execution:

```
>>> search_routes('LED','NBC','flight_routes.csv',1)
[['LED', 'NBC']]

>>> search_routes('LED','NBC','flight_routes.csv',2)
[['LED', 'NBC'], ['LED', 'DME', 'NBC']]

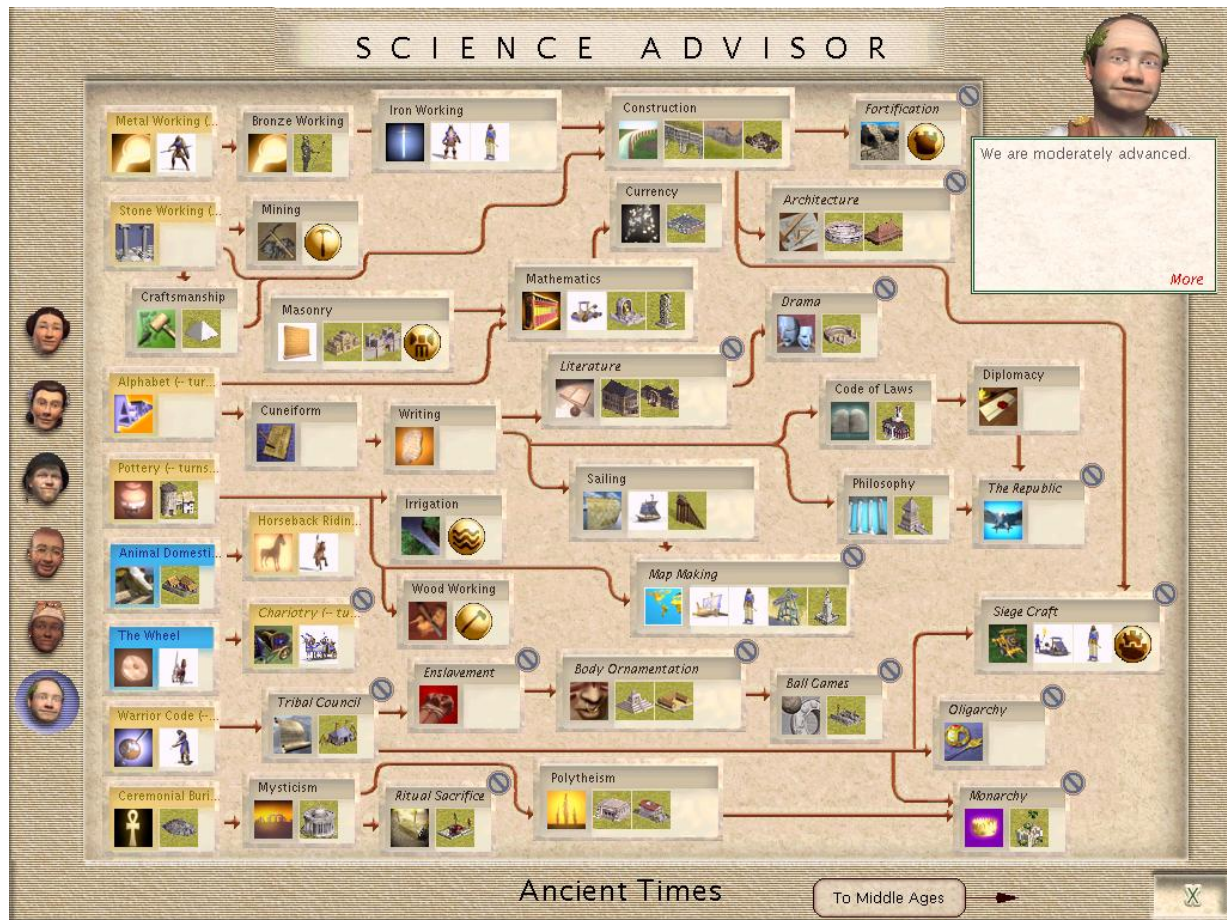
>>> search_routes('LED','NBC','flight_routes.csv',3)
[['LED', 'NBC'], ['LED', 'DME', 'NBC'], ['LED', 'KZN', 'DME', 'NBC'],
 ['LED', 'KZN', 'SVX', 'NBC'], ['LED', 'UUA', 'DME', 'NBC'],
 ['LED', 'ASF', 'DME', 'NBC'], ['LED', 'SCW', 'SVX', 'NBC'],
 ['LED', 'OVB', 'SVX', 'NBC'], ['LED', 'DYU', 'DME', 'NBC'],
 ['LED', 'DYU', 'SVX', 'NBC'], ['LED', 'LBD', 'DME', 'NBC'],
 ['LED', 'CSY', 'DME', 'NBC'], ['LED', 'MCX', 'DME', 'NBC'],
 ['LED', 'SKX', 'DME', 'NBC'], ['LED', 'VOZ', 'DME', 'NBC']]
```

In the third sample execution above, there is no entry such as `['LED', 'KZN', 'LED', 'NBC']` because although valid, it has a loop. For routes that have the same number of hops, the sequence in which they appear in the list doesn't matter. Note that since this is a real world data, it may not be perfect – it is possible that it may contain an airport from which there are no outgoing flights.

Question 3 : Learning to Make Games [10 marks]

After learning how to program, you decided to take up an internship at a game company, where they are doing a remake of the classic strategy game *Civilization*. *Civilization* is an empire-building game where the gamer controls a civilization and attempts to lead it to greatness.

One core aspect of the game is *research*, where the player can invest research points to try to unlock in-game abilities via research. A typical research tree is shown here:



Basically, the technologies are organized with a set of dependencies. One may only attempt to research and unlock more advanced technologies only after the pre-requisite technologies have been researched. Your job is to implement this technology tree as a new class `TechTree`. An empty `TechTree` can be constructed by passing a string `name` which would be the name of the `TechTree`. A `TechTree` supports the following methods.

- `get_name()` returns the name of the technology tree.
- `add_tech(tech)` adds a new technology `tech` into the technology tree and returns `True` if the operation is successful, or `False` if it fails because the `tech` is already in the tree.
- `add_dependency(parent, child)`: adds a parent technology as a dependency for the child technology, i.e. child can only be unlocked if the parent is already unlocked and returns `True` if the operation is successful. This method returns `False` if the operation fails because either parent or child are not in the tree. The parameters `parent` and `child` are both strings identifying the corresponding tech.

- `get_parents(tech)` return the list of direct pre-requisites for the specified technology. Or `False` if `tech` is not in the tree. The sequence of parents in the returned list doesn't matter. Also if the `tech` has no parents i.e. it is the root node, `get_parents(tech)` should return an empty list.
- `get_ancestors(tech)` return the full list of pre-requisites technologies for the specified technology. Or `False` if `tech` is not in the tree. The sequence of ancestors in the returned list doesn't matter. Also if the `tech` has no ancestors i.e. it is the root node, `get_ancestors(tech)` should return an empty list.
- `unlock(tech)` attempts to unlock the specified technology. This will succeed and return `True` only if all the pre-requisites have already been unlocked. Returns `False` if the `tech` is already unlocked or if the pre-requisites have not been unlocked.
- `is_unlocked(tech)` returns `True` if the `tech` is unlocked and `False` otherwise.
- `has_loop()` returns `True` if there is a problem with the technology tree, i.e. there is a loop (which means that the tree is bugged since it would be impossible to unlock the technologies in the loop). Method returns `False` if the tech tree is "normal", i.e. no loops.

You are welcome to define additional helper methods if you think they are helpful.

Sample execution (newlines added for readability):

```
>>> tt = TechTree("civilization")
>>> tt.add_tech("metal working")
>>> tt.add_tech("stone working")
>>> tt.add_tech("bronze working")
>>> tt.add_tech("iron working")
>>> tt.add_tech("construction")
>>> tt.add_tech("mining")
>>> tt.add_tech("craftsmanship")
>>> tt.add_dependency("metal working", "bronze working")
>>> tt.add_dependency("bronze working", "iron working")
>>> tt.add_dependency("iron working", "construction")
>>> tt.add_dependency("stone working", "mining")
>>> tt.add_dependency("stone working", "craftsmanship")
>>> tt.add_dependency("craftsmanship", "construction")
>>> tt.add_dependency("stone working", "construction")

>>> tt.get_parents("mining")
['stone working']

>>> tt.get_ancestors("mining")
['stone working']

>>> tt.get_parents("construction")
['iron working', 'craftsmanship', 'stone working']
```



```
>>> tt.get_ancestors("construction")
['stone working', 'craftsmanship', 'iron working', 'bronze working', 'metal working']

>>> tt.is_unlocked("stone working")
False

>>> tt.unlock("stone working")
True

>>> tt.is_unlocked("stone working")
True

>>> tt.is_unlocked("construction")
False

>>> tt.unlock("construction")
False

>>> tt.is_unlocked("construction")
False

>>> tt.has_loop()
False

>>> tt.add_dependency("construction", "stone working")
>>> tt.has_loop()
True
```