

MAT1105 Lineær algebra og numeriske metoder

OBLIG 1

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Seksjon 1.5

Oppgave 5)

a)

$$A = \begin{pmatrix} 1 & 0 & -3 \\ -2 & -3 & 2 \end{pmatrix} \quad x = \begin{pmatrix} -2 \\ 3 \\ -1 \end{pmatrix}$$
$$Ax = \begin{pmatrix} 1 * (-2) + 0 * 3 + (-3) * (-1) \\ (-2) * (-2) + (-3) * 3 + 2 * (-1) \end{pmatrix} = \begin{pmatrix} 1 \\ -7 \end{pmatrix}$$

b)

$$A = \begin{pmatrix} 2 & 0 \\ 3 & 1 \\ 6 & -2 \end{pmatrix} \quad x = \begin{pmatrix} 3 \\ -2 \end{pmatrix}$$
$$Ax = \begin{pmatrix} 2 * 3 + 0 * (-2) \\ 3 * 3 + 1 * (-2) \\ 6 * 3 + (-2) * (-2) \end{pmatrix} = \begin{pmatrix} 6 \\ 7 \\ 22 \end{pmatrix}$$

c)

$$A = \begin{pmatrix} 2 & 1 & 0 \\ -3 & 4 & -2 \\ 1 & -3 & 2 \end{pmatrix} \quad x = \begin{pmatrix} 4 \\ 0 \\ 3 \end{pmatrix}$$
$$Ax = \begin{pmatrix} 2 * 4 + 1 * 0 + 0 * 3 \\ (-3) * 4 + 4 * 0 + (-2) * 3 \\ 1 * 4 + (-3) * 0 + 2 * 3 \end{pmatrix} = \begin{pmatrix} 8 \\ -18 \\ 10 \end{pmatrix}$$

Oppgave 7)

Vi benytter $X=50$, $Y=70$ og $Z=80$.

$$A = \begin{pmatrix} 0.7 & 0.3 & 0.4 \\ 0.1 & 0.5 & 0.2 \\ 0.2 & 0.2 & 0.4 \end{pmatrix} \quad b = \begin{pmatrix} 50 \\ 70 \\ 80 \end{pmatrix}$$

I dette tilfellet finner vi at handlevognene fordeler seg med 88 vogner X, 56 vogner Y og 56 vogner Z.

$$A \cdot b = \begin{pmatrix} 0.7 * 50 + 0.3 * 70 + 0.4 * 80 \\ 0.1 * 50 + 0.5 * 70 + 0.2 * 80 \\ 0.2 * 50 + 0.2 * 70 + 0.4 * 80 \end{pmatrix} = \begin{pmatrix} 88 \\ 56 \\ 56 \end{pmatrix}$$

Seksjon 1.6

Oppgave 6)

Vi har gitt følgende matriser:

$$A = \begin{pmatrix} 0 & 1 \\ 0 & 2 \end{pmatrix} \quad B = \begin{pmatrix} 1 & 1 \\ 3 & 4 \end{pmatrix} \quad C = \begin{pmatrix} 2 & 5 \\ 3 & 4 \end{pmatrix} \quad D = \begin{pmatrix} 3 & 7 \\ 0 & 0 \end{pmatrix}$$

Regner ut AB:

$$AB = \begin{pmatrix} 0*1 + 1*3 & 0*1 + 1*4 \\ 0*1 + 2*3 & 0*1 + 2*4 \end{pmatrix} = \begin{pmatrix} 3 & 4 \\ 6 & 8 \end{pmatrix}$$

Regner ut AC:

$$AC = \begin{pmatrix} 0*2 + 1*3 & 0*5 + 1*4 \\ 0*2 + 2*3 & 0*5 + 2*4 \end{pmatrix} = \begin{pmatrix} 3 & 4 \\ 6 & 8 \end{pmatrix}$$

Finner med dette at AB=AC.

Deretter regner vi ut AD, og finner at AD=0:

$$AD = \begin{pmatrix} 0*3 + 1*0 & 0*7 + 1*0 \\ 0*3 + 2*0 & 0*7 + 2*0 \end{pmatrix} = \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix}$$

Oppgave 14)

Benytter Python til å løse oppgaven, kode vises nedenfor.

```

1 import numpy as np
2
3 # Oppgaver til seksjon 1.6
4
5 # 1a)
6 print("\n1a\n")
7
8 A = np.array([[1,-2], [3,1]])
9 B = np.array([[2,-1], [1,2]])
10
11 print(A, "\n")
12 print(B, "\n")
13 print(f"AB =\n", np.dot(A, B), "\n")
14 print(f"BA = \n", np.dot(B, A), "\n")
15
16 # 1b)
17 print("\n1b\n")
18
19 A = np.array([[1,-1,0], [-2,0,1], [-1,2,1]])
20 B = np.array([[0,2,1], [-1,-2,0], [3,-1,2]])
21
22 print(A, "\n")

```

```

23 print(B, "\n")
24 print(f"AB =\n", np.dot(A, B), "\n")
25 print(f"BA =\n", np.dot(B, A), "\n")
26
27 # 2)
28 print("\n2\n")
29
30 A = np.array([[1,-2,3], [0,-1,2]])
31 B = np.array([[2,1], [0,-3], [1,0]])
32
33 print(A, "\n")
34 print(B, "\n")
35 print(f"AB =\n", np.dot(A, B), "\n")
36
37 # 3)
38 print("\n3\n")
39
40 A = np.array([[1,-2], [3,0], [-1,2]])
41 B = np.array([[2,1,0], [-3,1,1]])
42
43 print(A, "\n")
44 print(B, "\n")
45 print(f"AB =\n", np.dot(A, B), "\n")

```

Nedenfor vises output fra terminalen, formattert og fjernet overflødig informasjon:

```

1a
AB =
[[ 0 -5]
 [ 7 -1]]
BA =
[[-1 -5]
 [ 7  0]]

```

```

1b
AB =
[[ 1  4  1]
 [ 3 -5  0]
 [ 1 -7  1]]
BA =
[[-5  2  3]
 [ 3  1 -2]
 [ 3  1  1]]

```

```

2
AB =
[[5 7]
 [2 3]]

```

3

AB =

$$\begin{bmatrix} 8 & -1 & -2 \end{bmatrix}$$

$$\begin{bmatrix} 6 & 3 & 0 \end{bmatrix}$$

$$\begin{bmatrix} -8 & 1 & 2 \end{bmatrix}$$

Seksjon 1.7

Oppgave 5)

$$A^{-1} = \begin{pmatrix} 1 & 4 \\ 2 & 9 \end{pmatrix} \quad B^{-1} = \begin{pmatrix} 8 & 3 \\ 2 & 1 \end{pmatrix}$$

$$(AB)^{-1} = B^{-1}A^{-1}$$

$$B^{-1}A^{-1} = \begin{pmatrix} 8*1 + 3*2 & 8*4 + 3*9 \\ 2*1 + 1*2 & 2*4 + 1*9 \end{pmatrix} = \begin{pmatrix} 14 & 59 \\ 4 & 17 \end{pmatrix} = (AB)^{-1}$$

Oppgave 8)

$$(AB)^T = B^T A^T$$

$$(AB)^{-1} = B^{-1}A^{-1}$$

$$((AB)^{-1})^T = (B^{-1}A^{-1})^T$$

$$(B^{-1}A^{-1})^T = (A^{-1})^T (B^{-1})^T$$

$$((AB)^T)^{-1} = (A^{-1})^T (B^{-1})^T \square$$

Seksjon 1.8

Oppgave 10)

a)

$$a = \begin{bmatrix} 3 & -2 & -1 \\ 1 & 4 & 3 \\ 2 & 1 & 7 \end{bmatrix}$$

$$\det(a) = 3 * \begin{vmatrix} 4 & 3 \\ 1 & 7 \end{vmatrix} - (-2) * \begin{vmatrix} 1 & 3 \\ 2 & 7 \end{vmatrix} + (-1) * \begin{vmatrix} 1 & 4 \\ 2 & 1 \end{vmatrix}$$

$$\det(a) = 3 * (4 * 7 - 3 * 1) - (-2) * (1 * 7 - 3 * 2) + (-1) * (1 * 1 - 4 * 2)$$

$$= 3 * (28 - 3) + 2 * (7 - 6) - 1 * (-7) = 75 + 2 + 7 = 84$$

b)

$$b = \begin{bmatrix} -2 & 4 & 0 \\ -2 & 3 & 3 \\ 1 & 0 & 4 \end{bmatrix}$$

$$\det(b) = (-2) * \begin{vmatrix} 3 & 3 \\ 0 & 4 \end{vmatrix} - 4 * \begin{vmatrix} -2 & 3 \\ 1 & 4 \end{vmatrix} + 0 * \begin{vmatrix} -2 & 3 \\ 1 & 0 \end{vmatrix}$$

$$\begin{aligned} \det(b) &= -2 * (3 * 4 - 3 * 0) - 4 * (-2 * 4 - 3 * 1) + 0 * (-2 * 0 - 3 * 1) \\ &= -2 * 12 - 4 * -11 = 20 \end{aligned}$$

c)

$$c = \begin{bmatrix} 1 & 2 & 3 \\ -2 & 5 & 4 \\ 3 & -3 & -1 \end{bmatrix}$$

$$\det(c) = 1 * \begin{vmatrix} 5 & 4 \\ -3 & -1 \end{vmatrix} - 2 * \begin{vmatrix} -2 & 4 \\ 3 & -1 \end{vmatrix} + 3 * \begin{vmatrix} -2 & 5 \\ 3 & -3 \end{vmatrix}$$

$$\begin{aligned} \det(c) &= 1 * (5 * (-1) - 4 * (-3)) - 2 * ((-2) * (-1) - 4 * 3) + 3 * ((-2) * (-3) - 5 * 3) \\ &= 7 - (-20) + -27 = 0 \end{aligned}$$