Expt. 7c: Optimizing gas chromatography separations with simplex optimization

Prelab Assignment

- 1. a) Use Google Scholar to find a paper in the primary scientific literature that reports separating the components of a "BTEX" mixture by gas chromatography. Use the Copley library website (or other site) to access the paper. Upload this paper into your ELN prelab.
 - b) List the 6 compounds that are present in a BTEX mixture.
 - c) Record the details of the separation described in the paper. What column was used (Length, i.d., stationary phase, and stationary phase thickness)?
 - d) What was the mobile phase "carrier" gas and flow rate?
 - e) What was the temperature or temperature gradient program?
 - f) What solvent focusing or cold trapping used?
- 2. Make sure your Jupyter notebook from last week is completed at least to the point where you add a column of zeros to your 2-D data array (the 4th code block). (We'll be working from there this week in lab.) Please upload the notebook to your ELN pre-lab, so Dr. D can check that you've made it that far.
- 3. Set up your ELN Data & Obs section with a goal statement, the procedure in 2-column format, and some data tables ready to go.

Lab exercise part 1: Simulator accuracy and carrier gas replacement

Have one person in your lab group register on the Restek corporate website to gain access to the EZGC Chromatograph Modeler program (https://www.restek.com/proezgc). Although having to register is lame, this does allow you to save your favorite separation conditions (so you are less likely to lose your work if there is an internet hiccup). Under the *compounds* tab, type in the names of the 6 components of a BTEX mixture, each on its own line. Press the *solve* button to see Restek's suggestions for separation. In this simulator, the resolution of each peak listed is with its closest neighbor in either direction. Notice that "results were found on 6 stationary phases." Look through these six results. Which components of a BTEX mixture are the most difficult to separate?

Look up the boiling points of the 3 xylene isomers in a BTEX mixture, and record them in your ELN. (They are not identical.) Does this information explain your previous answer? Why / why not?

In the GC simulator, select the stationary phase that is most like the one used in the paper you selected. (Determining this similarity may take some internet research.) Set all of the simulator parameters as closely as possible to those in the paper. Note that you must click "Custom" in the Results tab to be able

to make changes in the Control Parameters tab. Click "Vacuum" if trying to simulate a GCMS method, or "Atm" if any other detector was used. **Make a table** comparing reported retention times from the paper and the simulator predictions in the ELN Data & Obs. In a third column, calculate the absolute value of the difference between them, $|\Delta t_r|$. How accurate is the simulator, in terms of retention order?

What is the average $|\Delta t_r|$ error and standard deviation of the simulator's predictions? (You may use Python, Excel, or a calculator to answer this last question.)

There is an ongoing shortage of helium, which has caused some GC operators to switch to other mobile phase "carrier gases". Planning how to switch over a method from one carrier gas to another is one of the purposes of this GC simulator. **Make a second table** and record the simulator's retention times and resolution for each peak with helium, leaving room for a matching dataset using nitrogen as the carrier gas. Switch the carrier gas from helium to nitrogen in the simulator. Do you have to raise or lower the column flow to get the retention times to where they were before?

Can you get the retention times to be essentially the same with nitrogen as they were with helium? How close can you match them? Include this data and the optimized nitrogen gas pressure in your ELN.

Once you change the pressure in this way, is the resolution of the chromatogram using nitrogen comparable to the resolution in the original one with helium? Or are there significant differences?

Given that a tank of ultra-high-purity nitrogen is much cheaper than a tank of UHP helium, which carrier gas would you recommend for this separation?

Lab exercise part 2: Optimizing gradient separations

For this part, we will use the **simplex optimization** technique for optimizing the GC separation of a fragrance sample with 10 components. To set up the simulator, select "Compounds," and then "Search by phase." Choose a Stabilwax stationary phase, then select the "flavors and fragrances" library. From the long list of scent molecules, select (-)-isopulegol, (*E*)-ocimene, (*R*)-carvone, α -humulene, α -phellandrene, α -terpinene, α -terpineol, β -caryophyllene, β -myrcene, and citral. (Citral has two isomers which are automatically included when you select it.) Click "solve."

Select the Conditions tab, and in the Results area at the bottom, click "Custom." (This allows you to change the Control Parameters.) Under Carrier Gas, select Helium. Under Control Parameters, switch from vacuum to Atm. You are now simulating a GC instrument with a detector that does not pull a vacuum on the end of the column (in other words, *not* a mass spectrometer). Set up the following parameters:

Column: Stabilwax with dimensions of 30m length, 0.25 mm inner diameter, 0.5 µm film thickness

Column flow: 2.5 mL/min
Oven program: Ramps
Number of ramps: 1
Initial temp = 50 C
Initial hold time = 2 min
Ramp rate = 10 C/min
Final temp = 200 C

Control method: Constant Flow

As you make these changes, you will see that each one causes changes in the chromatogram, both in resolution and in retention order. I've highlighted 8 of them in red – the first three you normally get to choose only when buying a column, and the last five you can vary for a given run. Of course, with a simulator, we get to vary all 8 for a given run. This is like having an infinite supply of columns to play with. You can see why Restek, a column manufacturer, maintains this simulator website.

Once you set all the parameters correctly, you will see that the first two peaks elute with only 0.4 resolution – clearly not what we want. Your goal in part 2 of the lab today is to optimize the separation by varying FOUR parameters following the strategy of simplex optimization. Your first task is to select 4 parameters from the ones highlighted in red on the previous page – at least one of them must involve the *oven program*:

- 1.
- 2.
- 3.
- 4.

Optimization setup. Next, we need to plan 5 experiments – representing the 1^{st} four-dimensional simplex with its 5 corners – where the four parameters you've chosen are varied over 2-3 values within the "starting simplex range" listed in Table 1. Note that the starting simplex ranges listed in the table cover 20 - 40% of the total available range for each parameter. This is a general experimental design principle, and consistent with the starting ranges in the 2-D simplex exercise we did in class. (In Table 1, all 8 parameters are listed, because I don't know which 4 you will select.)

Table 1: Parameters for Optimization

| Parameter | Total range available | Starting simplex range |
|--------------------------------------|--------------------------|------------------------|
| Column flow (mL/min) | 0 – 4 | 1.5 – 2.5 |
| Column length (m) | 10 – 60 | 15 – 30 |
| Column inner diameter (mm) | 0.1 - 0.53 | 0.15 - 0.25 |
| Stationary phase film thickness (µm) | 0.1 - 2 | 0.25 - 1 |
| Initial oven temperature (C) | -20 to 200 | 40 – 80 |
| Initial temperature hold time (min) | 0 – 10 | 1 – 4 |
| Temperature ramp rate (C/min) | 2-50 | 10 – 20 |
| Final oven temperature (C) | 150 – 260 | 180 – 220 |

Build a table like the sample one below in your ELN, with the four parameters you've selected. (Your four parameters cannot be the same four as in the sample table.) The first row should match the current settings on the EZGC simulator -- the simulator currently holds the results of Experiment 1! Then, plan Experiments 2, 3, 4, and 5, according to the following guidelines:

- No two experiments should be identical.
- For your 4 selected parameters, pick 2-3 values spanning the starting simplex range
- Distribute these values **randomly** to experiments 2, 3, 4 and 5! (Don't distribute them all low to high, for example.)

Here's what my Table 2 looked like when I finished the plan for the initial simplex set of experiments. I colored the conditions blue (for high), black (for middle) and red (for low) for each parameter to help me see that they were randomly distributed:

| Table 2: | Simplex | optimization | summary | (exampl | e) |) |
|----------|---------|--------------|---------|---------|----|---|
|----------|---------|--------------|---------|---------|----|---|

| Vertex # | Col length | Col diam. | Col film | Flow rate | Response | Vertices retained |
|----------|------------|-----------|----------|-----------|----------|-------------------|
| (Expt #) | (m) | (mm) | (µm) | (mL/min) | | after expt. |
| 1 | 30 | 0.25 | 0.5 | 2.5 | | |
| 2 | 20 | 0.25 | 0.25 | 2 | | |
| 3 | 15 | 0.18 | 0.25 | 2.5 | | |
| 4 | 20 | 0.25 | 0.5 | 1.5 | | |
| 5 | 20 | 0.15 | 1 | 2 | | |
| 6 | | | | | | |

The next step is to decide on the **definition of the response** – this is a number that we'll be trying to maximize (or minimize). As you know, we want all peaks to be resolved with R = 1.5 (or greater), and we want the last peak's retention time to be as short as possible. We therefore need to combine these goals into one numerical summary. Here is my idea:

Response =
$$\frac{(\text{minimum } R)^2}{t_r \text{ of last peak}}$$

The bigger the minimum resolution (between the two closest peaks), and the smaller the last peak retention time, the larger the response number will be. Thus my optimization goal will be to maximize *Response*. I think resolution is more important, however, so I squared *R* in my definition so that it will have a bigger impact in my optimization. You group is free to propose your own definition of response – and whether it needs to be maximized or minimized!

Our group defines the response as follows:

Response =

Will this response need to be maximized or minimized?

At this point, flag down Dr. D, and have me OK the first 5 experiments and the definition of response that you plan to use. Once I do that, you can run experiments 2-5 on the GC simulator, and calculate the response in each case, filling in your own table in the ELN. Here's what my table looked like at that point:

Table 2: Simplex optimization summary (example)

| Vertex # (Expt #) | Col length (m) | Col diam. (mm) | Col film (µm) | Flow rate (mL/min) | Response | Vertices retained after expt. |
|-------------------|----------------|-------------------|---------------|--------------------|------------------------|-------------------------------|
| 1 | 30 | 0.25 | 0.5 | 2.5 | $0.4^2/13.91 = 0.0115$ | |
| 2 | 20 | 0.25 | 0.25 | 2 | $1.7^2/10.85 = 0.2664$ | |
| 3 | 15 | 0.18 | 0.25 | 2.5 | $2.2^2/9.82 = 0.4929$ | |
| 4 | 20 | 0.25 | 0.5 | 1.5 | $0^2/13.11 = 0$ | |
| 5 | 20 | 0.15 | 1 | 2 | $0.5^2/15.28 = 0.0164$ | |
| 6 | | | | | | |

Simplex walking. Now that you've run the 5 experiments defining the simplex, it's time to *let the simplex method decide what to do next*. First, reject the experiment that gave the worst response – in my example, expt 4. (This means you retain the other 4 vertices or experiments – 1,2,3,5 in my example.) Then, calculate the Experiment 6 value for each parameter, using the familiar rule:

Next value = 2*(average of retained experiment values) - (rejected experiment value)

For example, based on my above table, the next column length I should try will be

$$2*(30+20+15+20)/4 - 20 = 22.5 \text{ m}$$

(If you want to do these calculations in Excel to speed things up, you may do so.) I've completed my plan for Experiment 6 in the table below, using the simplex rules. Note that my experiment 4 gave the worst results, and column diameter was high and flow rate was low in that experiment. The simplex rules tell me to do my next experiment with a low column diameter and a high flow rate!

Table 2: Simplex optimization summary (example)

| Vertex # (Expt #) | Col length (m) | Col diam. (mm) | Col film (µm) | Flow rate (mL/min) | Response | Vertices retained after expt. |
|-------------------|----------------|-------------------|---------------|--------------------|------------------------|-------------------------------|
| 1 | 30 | 0.25 | 0.5 | 2.5 | $0.4^2/13.91 = 0.0115$ | na |
| 2 | 20 | 0.25 | 0.25 | 2 | $1.7^2/10.85 = 0.2664$ | na |
| 3 | 15 | 0.18 | 0.25 | 2.5 | $2.2^2/9.82 = 0.4929$ | na |
| 4 | 20 | 0.25 | 0.5 | 1.5 | $0^2/13.11 = 0$ | na |
| 5 | 20 | 0.15 | 1 | 2 | $0.5^2/15.28 = 0.0164$ | 1,2,3,5 |
| 6 | 22.5 | 0.165 | 0.5 | 3 | | |

Your group's task is to take your optimization out to Experiment 12. Extend your summary table to show the conditions for each experiment, the response, the vertices retained after each experiment. Don't forget about rules 3 and 4! After 12 experiments, highlight the optimal set of conditions that you have found using the technique of simplex optimization, like in my example below.

IMPOTANT NOTE: In my optimization, I got the best results by using a **modified rule 4**: if the simplex rules suggested a negative (impossible) film thickness, I interpreted this as a request to use a thinner film than before. So, rather than setting the result to zero, I substituted the negative thickness with the smallest film thickness that is commercially available (0.1 um). This modification allowed my simplex to walk uphill instead of floundering around.

Here is my example table after 12 experiments. Notice that I used a highlighter to keep track of my current simplex vertices:

Table 2: Simplex optimization summary (completed example)

| Vertex # | Col length | Col diam. | Col film | Flow rate | Response | Vertices retained |
|-------------------------------------|------------|-----------|----------|-----------|--------------------------------------|---------------------|
| (Expt #) | (m) | (mm) | (µm) | (mL/min) | | after expt. |
| 1 | 30 | 0.25 | 0.50 | 2.5 | $0.4^2/13.91 = 0.0115$ | na |
| 2 | 20 | 0.25 | 0.25 | 2.0 | $1.7^2/10.85 = 0.2664$ | na |
| 3 best response | 15 | 0.18 | 0.25 | 2.5 | $2.2^2/9.82 = 0.4929$ | na |
| 4 | 20 | 0.25 | 0.50 | 1.5 | $0^2/13.11 = 0$ | na |
| 5 | 20 | 0.15 | 1.00 | 2.0 | $0.5^2/15.28 = 0.0164$ | 1,2,3,5 (reject4) |
| 6 | 22.5 | 0.17 | 0.50 | 3.0 | $0.3^2/12.94 = 0.0070$ | 2,3,5,6 (reject1*) |
| 7 | 8.8 | 0.10 | 0.50 | 2.3 | $1.6^2/10.8 = 0.2370$ | 2,3,5,7 (reject6) |
| 8 | 9.4 | 0.20 | 0.50 | 1.4 | $1.6^2/10.64 = 0.2406$ | 2,3,7,8 (reject5) |
| 9 fastest baseline separation | 6.6 | 0.20 | 0.10# | 2.1 | $1.5^2/6.14 = \frac{0.3664}{0.3664}$ | 2,3,8,9 (reject7) |
| 10 | 16.7 | 0.30 | 0.10 | 1.7 | $1.6^2 / 8.59 = 0.2980$ | 2,3,9,10 (reject8) |
| 11 | 19.8 | 0.3 | 0.10# | 2.8 | $1.8^2 / 8.16 = 0.3971$ | 3,9,10,11 (reject2) |
| 12 | 9 | 0.2 | 0.10# | 2.5 | $1.6^2/6.19 = 0.4136$ | |

^{*}rule 3 invoked: if new vertex point is worst, reject 2nd worst point to keep simplex from backtracking. #modified rule 4 invoked: simplex rules suggested a negative film thickness, so I substituted the lowest one available from Restek.

In 7 steps (Expts. 6 - 12), my simplex optimization was not able to find a higher response than Expt. 3 (a lucky guess!), but it *was* able to reduce the time to get a baseline separation by 3.5 minutes! Summarize what your simplex was able to achieve in its 7 steps.

Lab exercise part 3: Calculating resolution

Now we'll try to finish the Jupyter notebook from Expt 7b – we still have a way to go there! Our goal today is to enhance our coding skills by creating peak-recognition algorithms that will locate and integrate all peaks, independently determine their retention times, and calculate their $W_{1/2}$ peak widths. We will then use this to determine the resolution between adjacent peaks, and the relative response of the virtual detector to the 10 analyte species.