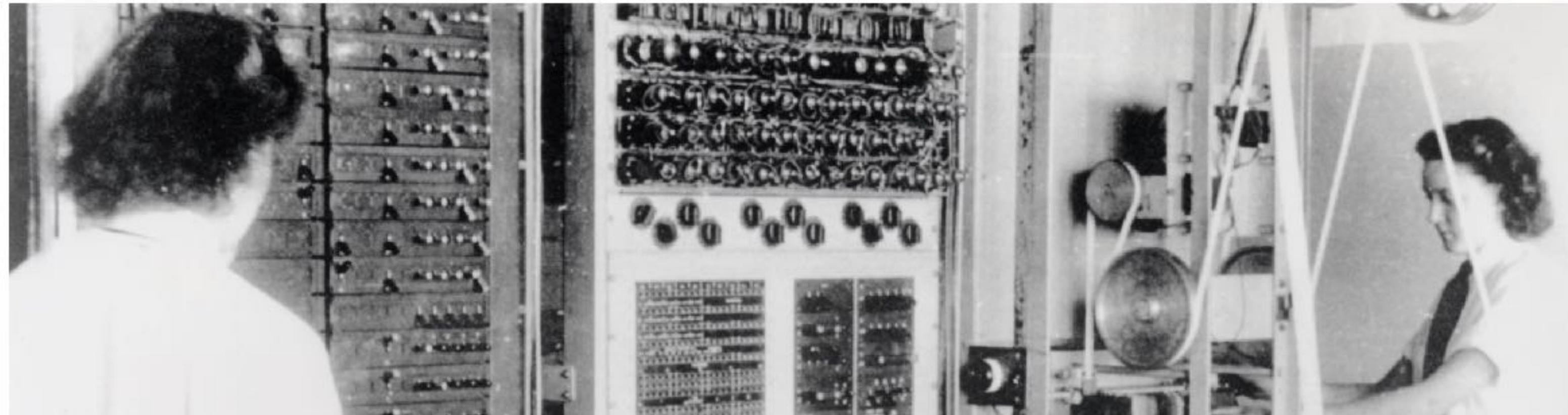


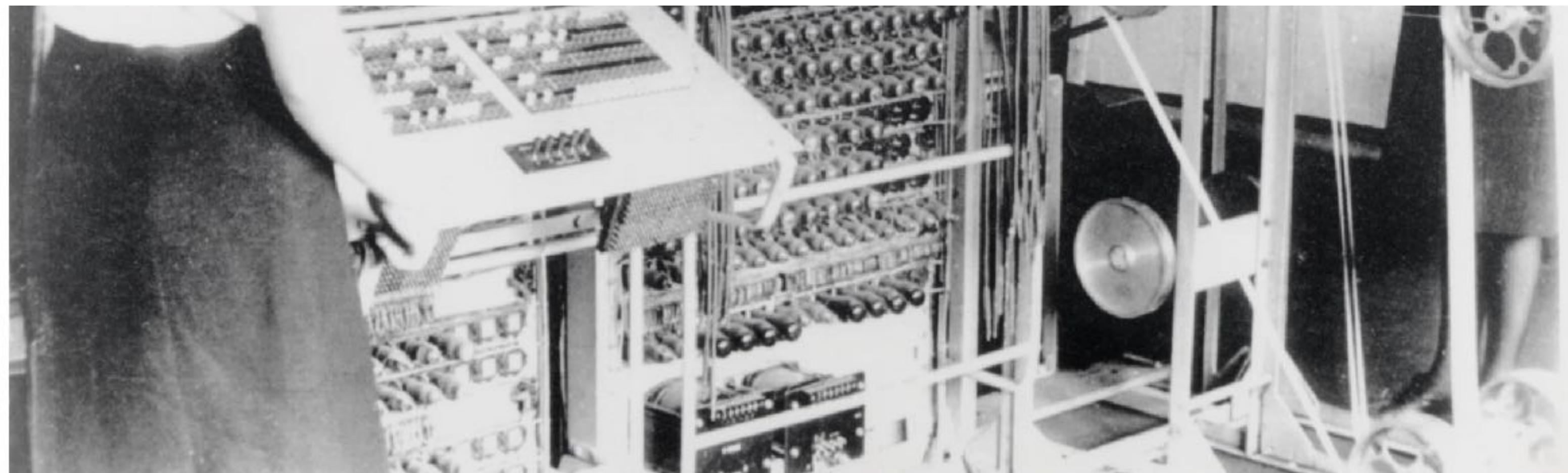


# PL/HCI Seminar (252R/279R)

MW 12-1:15 PM in LISE 303 ~~LISE 303~~ Pierce 209



Making communicating with computers more accessible:  
easier, faster, and safer

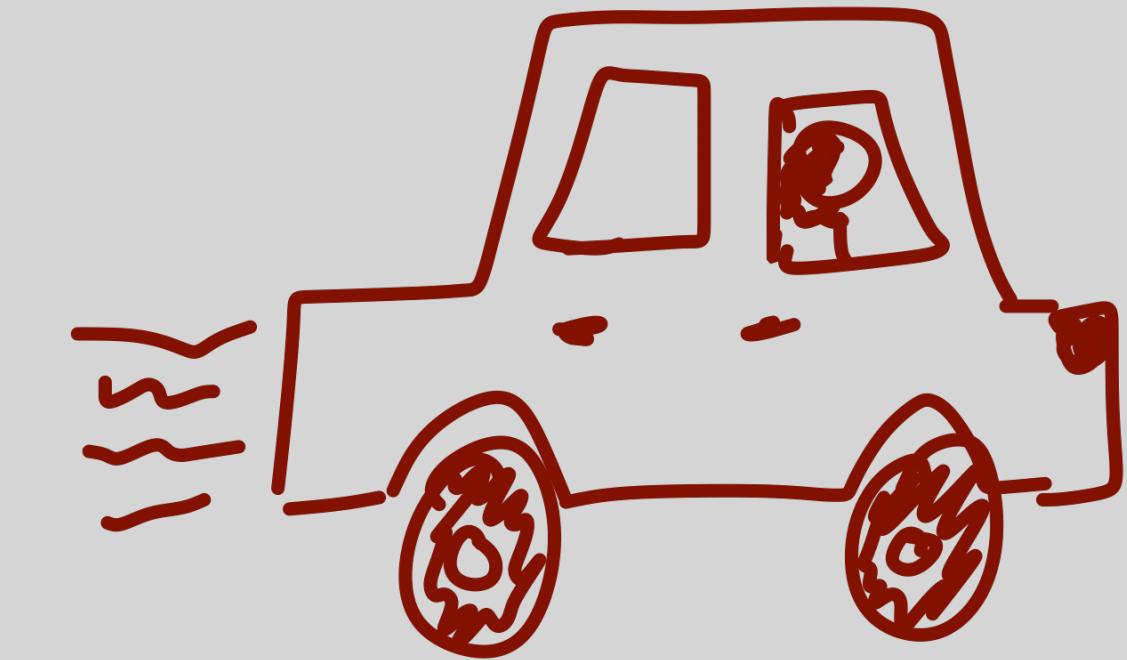
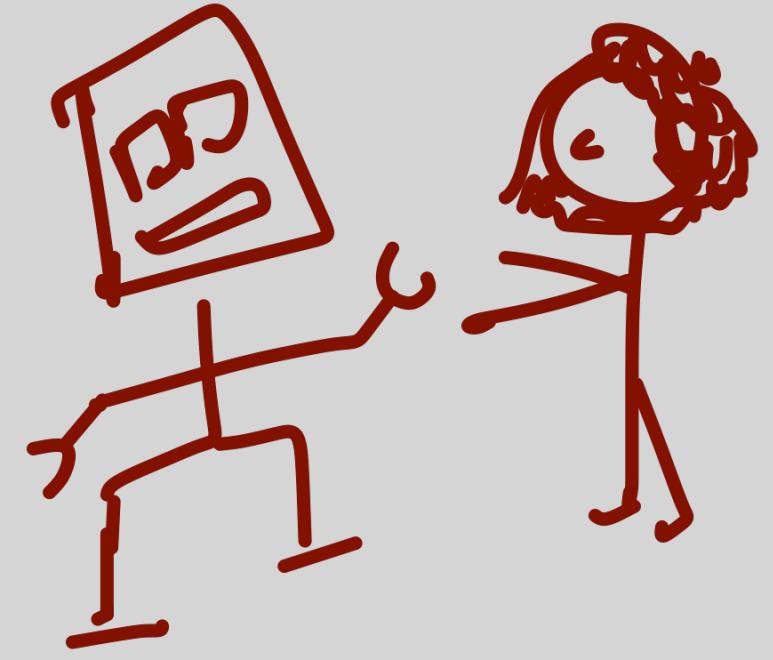


# Welcome!

- This is a graduate course; undergrads are welcome.
  - can have taken 152 or 179 and be just fine, not necessarily both
- You (as a student presenter) will present and lead discussion for at least one paper
- You (as a non-presenting student) will post questions and a summary of the design arguments by Friday of the previous week
- Key learning outcomes:
  - (279r) to look at scientific publications, identify the core design arguments, write new design arguments, and evaluate them
  - (252r) understand, design and implement language abstractions for solving a task
- Group projects will be composed of both “HCI folks” and “PL folks”

# Welcome!

- In undergraduate courses, you **consume knowledge** and practice applying it.
- In graduate courses like this one, you attempt to **generate new knowledge**.



I'm an HCI person.

I build novel interfaces and evaluate them in studies.



Since ~2015, I have found **PL technology** useful  
for providing the *magic* behind the screen.



**Harvard** John A. Paulson  
**School of Engineering**  
and Applied Sciences

PL/HCI Seminar (252R/279R)

# Evaluation is Hard.

But also, evaluation *with respect to what?*

# Outline

- 1. Design Arguments**
- 2. Some HCI evaluation techniques**
- 3. Means of communicating with computers**

# Design Arguments

## Evidence

How do you know?

## Need

### Need Thesis

*Stakeholders + Domain* Person **P** [in setting **S**]

*Core tension* wants to achieve goal **G** but obstacles **O<sub>1-N</sub>** get in the way. **Evidence**

Any solution also has to:  
satisfy constraints **X<sub>1-N</sub>**,  
minimize costs **Y<sub>1-N</sub>**,  
and avoid obstacles **Z<sub>1-N</sub>**.

How do existing approaches fail?

## Evidence

*Axioms* As designers, we bring the following principles and constraints **A<sub>1-N</sub>**.

### Approach Thesis

Our approach, \_\_\_\_\_,  
has characteristics **C<sub>1-N</sub>**  
that help stakeholders achieve their  
goal **G** while avoiding obstacles **O<sub>1-N</sub>**

What characteristics have you borrowed from solutions that succeeded in analogous settings?

What differentiates your approach from previous solutions that failed?

How have stakeholders responded to/been able to use your approach?

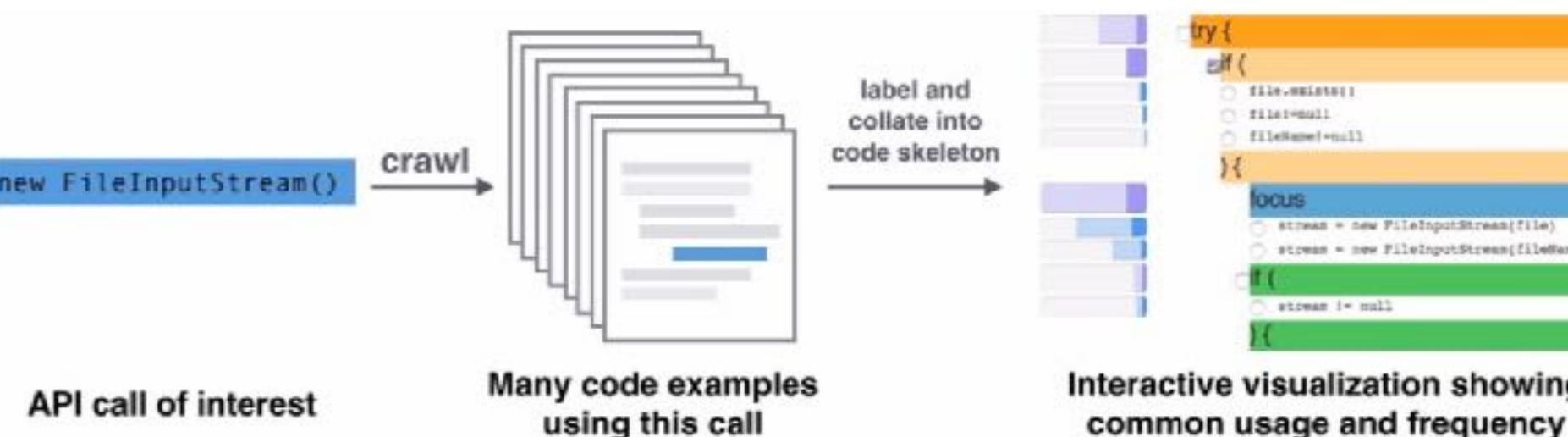
# Visualizing API Usage Examples at Scale

Elena L. Glassman<sup>‡\*</sup>, Tianyi Zhang<sup>||\*</sup>, Björn Hartmann<sup>‡</sup>, Miryung Kim<sup>||</sup>

<sup>‡</sup>\*UC Berkeley, Berkeley, CA, USA

<sup>||</sup>\*UC Los Angeles, Los Angeles, CA, USA

{eglassman, bjoern}@berkeley.edu, {tianyi.zhang, miryung}@cs.ucla.edu



**Figure 1.** EXAMPLOR takes a focal API call that a programmer is interested in, locates uses of that API call in a large corpus of mined code examples, and then produces an interactive visualization that lets programmers explore common usage patterns of that API across the corpus.

## ABSTRACT

Using existing APIs properly is a key challenge in programming, given that libraries and APIs are increasing in number and complexity. Programmers often search for online code examples in Q&A forums and read tutorials and blog posts to learn how to use a given API. However, there are often a massive number of related code examples and it is difficult for a user to understand the commonalities and variances among them, while being able to drill down to concrete details. We introduce an interactive visualization for exploring a large collection of code examples mined from open-source repositories at scale. This visualization summarizes hundreds of code examples in one synthetic code skeleton with statistical distributions for canonicalized statements and structures enclosing an API call. We implemented this interactive visualization for a set of Java APIs and found that, in a lab study, it helped users (1) answer significantly more API usage questions correctly and comprehensively and (2) explore how other programmers have used an unfamiliar API.

## INTRODUCTION

Learning how to correctly and effectively use existing APIs is a common task — and a core challenge — in software development. It spans all expertise levels from novices to professional software engineers, and all project types from prototypes to production code. The landscape of publicly available APIs is massive and constantly changing, as new APIs are created in response to shifting programmer needs. Within companies, the same is true, perhaps even more so: joining a company can require learning a whole new set of proprietary APIs before a developer becomes an effective contributor to the company codebase. Developers often are stymied by various learning barriers, including overly specific or overly general explanations of API usage, lack of understanding about the interaction between multiple APIs, lack of alternative uses, and difficulty identifying program statements and structures related to an API [11, 19, 5].

One study found that the greatest obstacle to learning an API is “insufficient or inadequate examples.” [19] Official documenta-

## ABSTRACT

Using existing APIs properly is a key challenge in programming, given that libraries and APIs are increasing in number and complexity. Programmers often search for online code examples in Q&A forums and read tutorials and blog posts to learn how to use a given API. However, there are often a massive number of related code examples and it is difficult for a user to understand the commonalities and variances among them, while being able to drill down to concrete details. We introduce an interactive visualization for exploring a large collection of code examples mined from open-source repositories at scale. This visualization summarizes hundreds of code examples in one synthetic code skeleton with statistical distributions for canonicalized statements and structures enclosing an API call. We implemented this interactive visualization for a set of Java APIs and found that, in a lab study, it helped users (1) answer significantly more API usage questions correctly and comprehensively and (2) explore how other programmers have used an unfamiliar API.

## INTRODUCTION

Learning how to correctly and effectively use APIs is a common task — and a core competency — for most software engineers, and all programmers. The landscape of APIs is massive and constantly changing in response to shifting program requirements. The same is true, perhaps even more so, for learning how a developer becomes an effective member of a codebase. Developers often face many barriers, including overly specific and inconsistent specifications of API usage, lack of understanding of the interactions between multiple APIs, lack of context for identifying program statements that use a specific API [11, 19, 5].

One study found that the greatest barrier to learning APIs was “*insufficient or inadequate examples*” [11].

# Outline

1. Design Arguments
2. Some HCI formative design and evaluation techniques
3. Means of communicating with computers

# Some HCI Formative Design Techniques

- Survey
- Interview
- Contextual inquiry
  - Observation in context
  - Requests for explanation
- Wizard of Oz
- Technology probe

# Some HCI Evaluation Techniques

- User study
  - Task design
  - Metrics
- Deployment
- Interview or survey of deployment participants
- Crowdsourcing, i.e., Amazon Mechanical Turk

# Outline

1. Design Arguments
2. Some HCI formative design and evaluation techniques
- 3. Means of communicating with computers**

# Communicating with Computers

- Human intent
  - Examples
  - Statement(s) in a programming language
  - Natural language
  - ...
- Computer's interpretation
  - Program
  - Behavior
    - Action in response to a human request
    - Results of running understood program on additional data

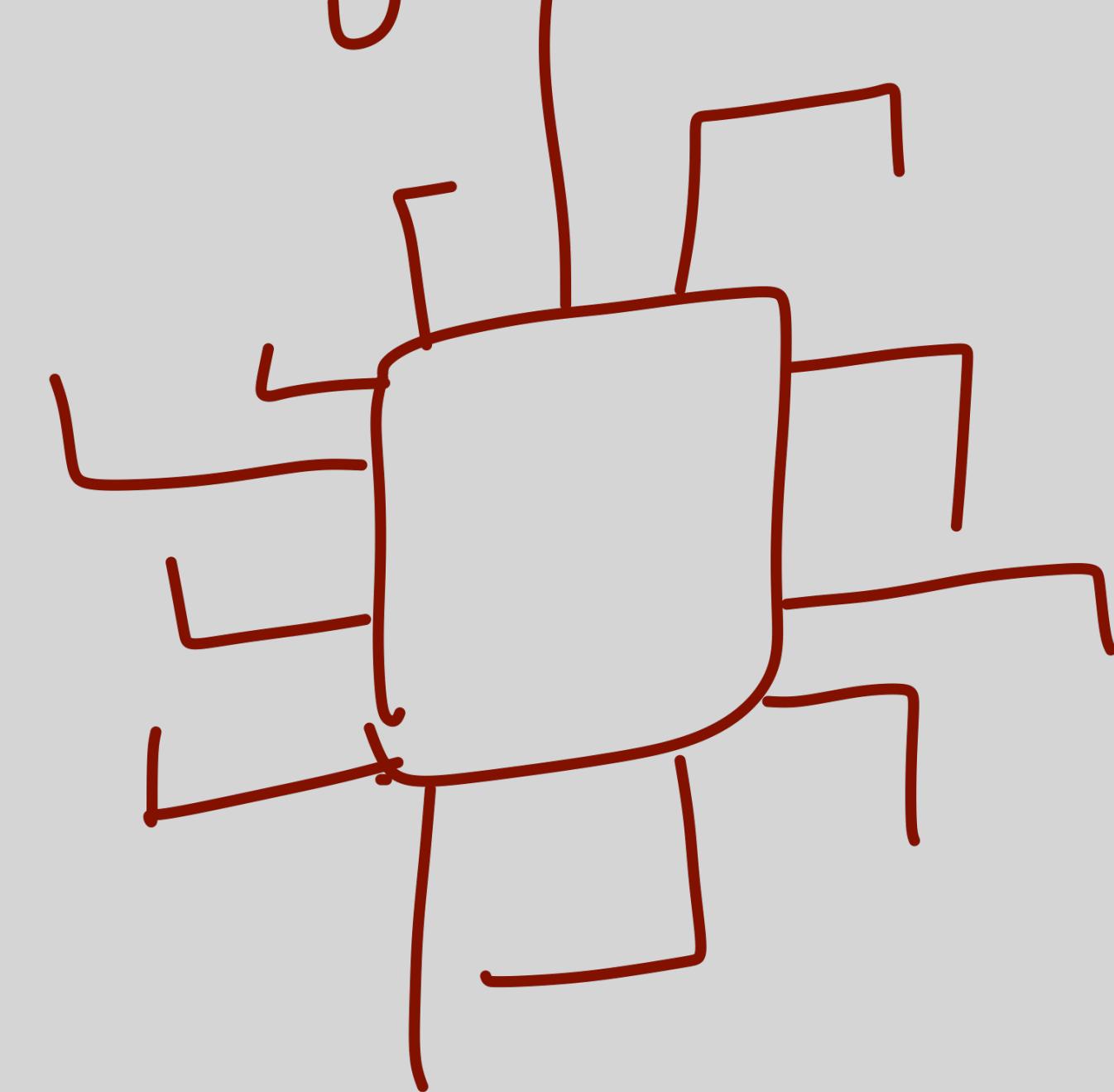
Human



capabilities

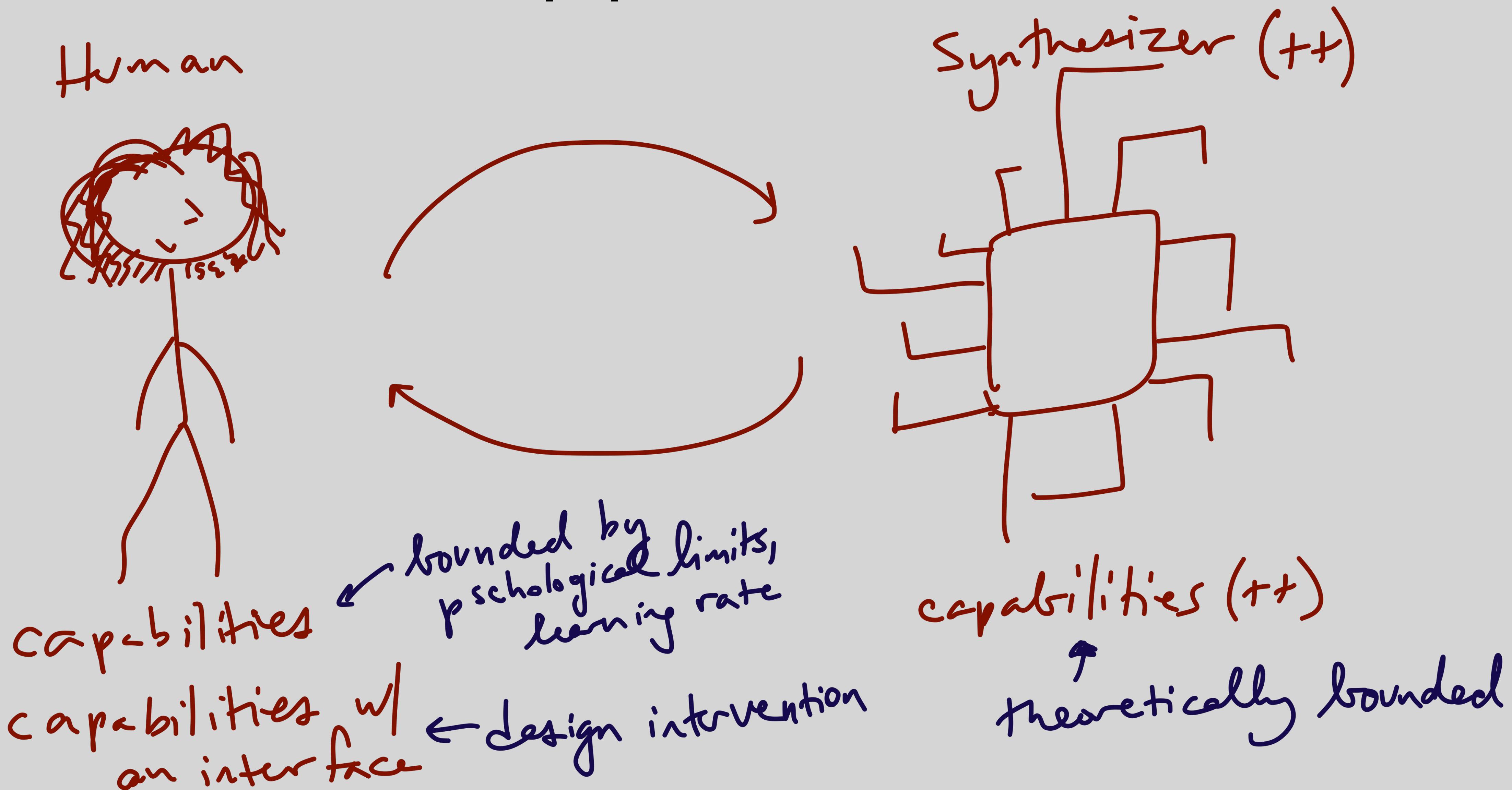
capabilities w/  
an interface

Synthesizer (++)

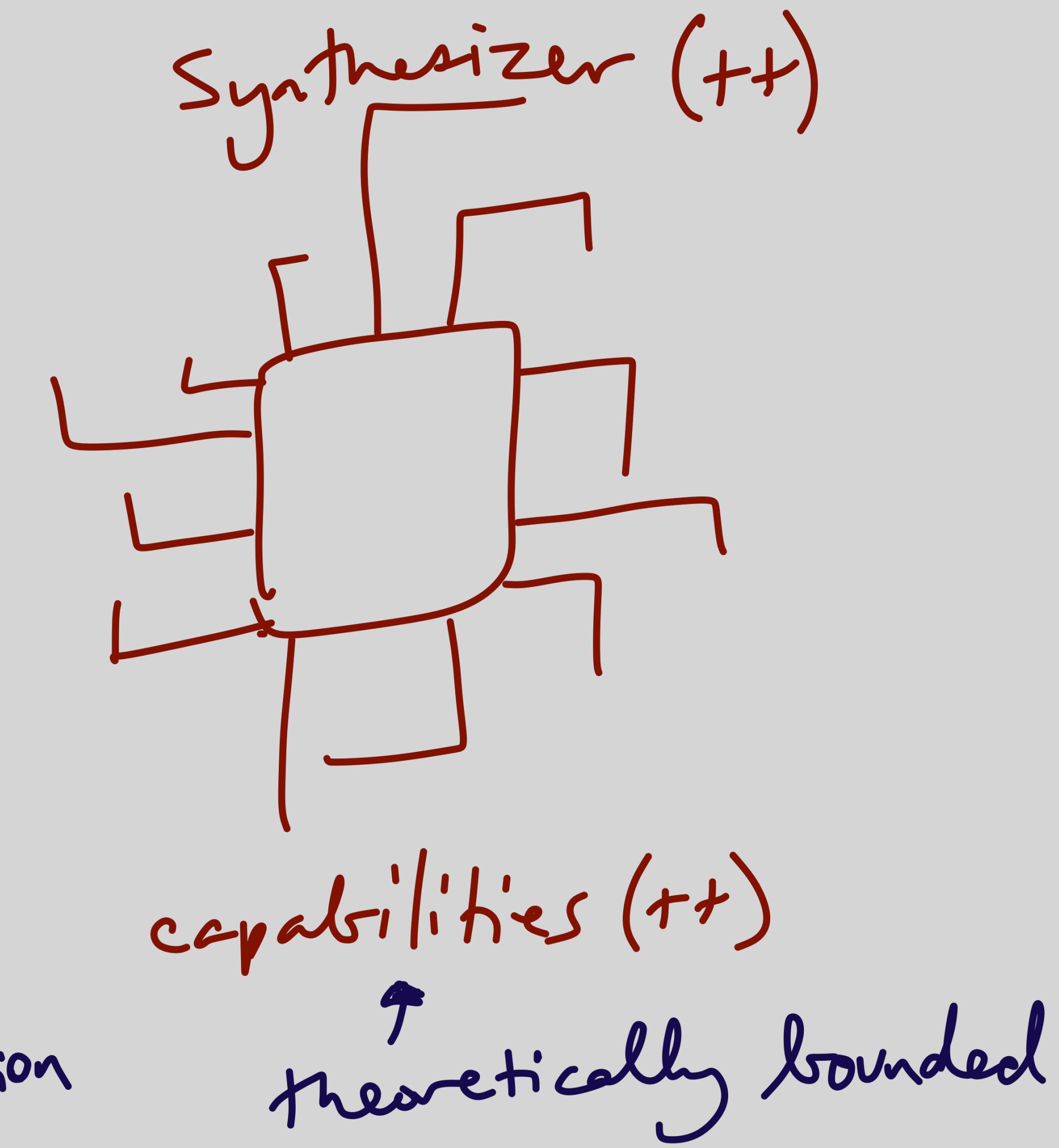
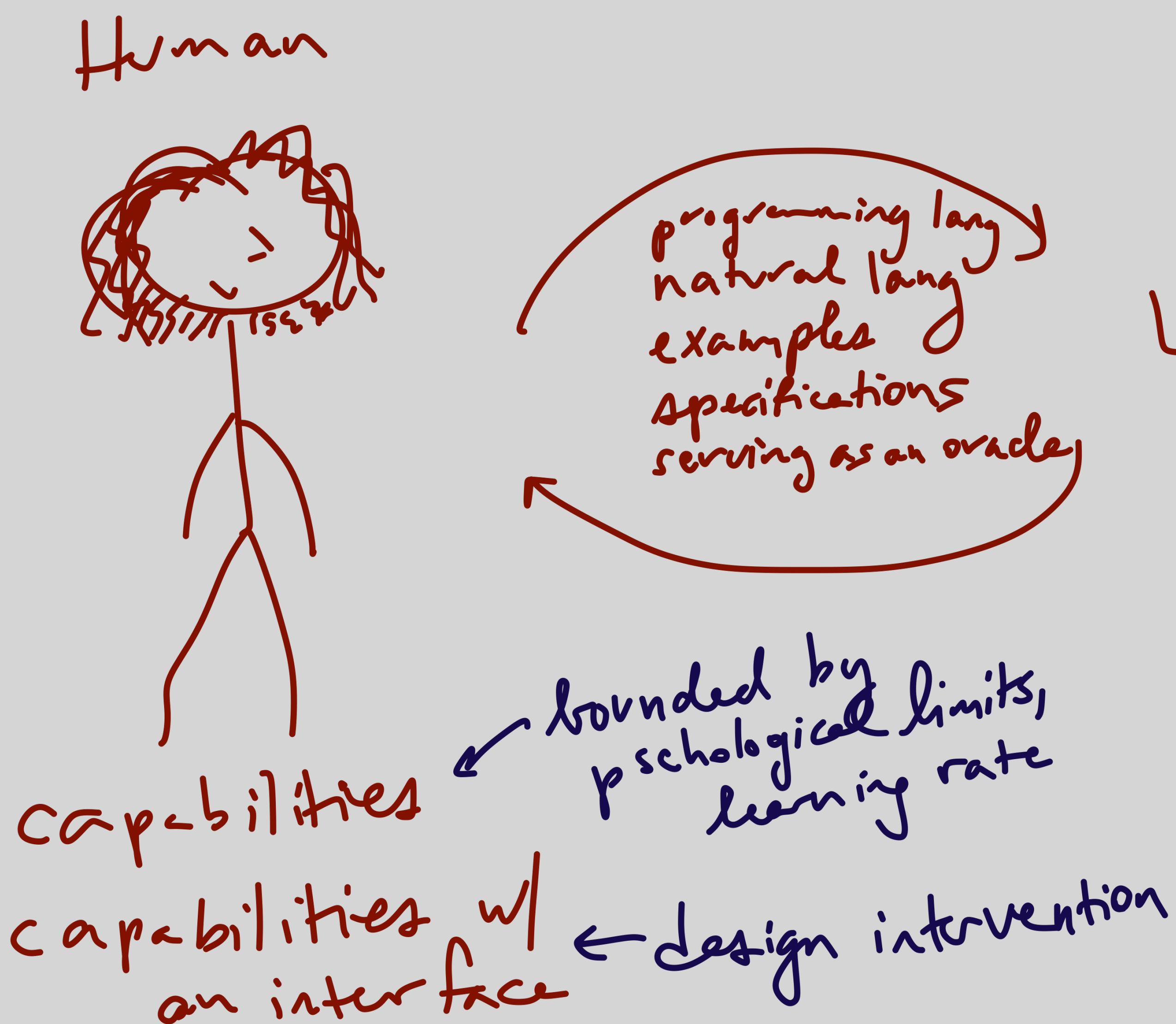


capabilities (++)

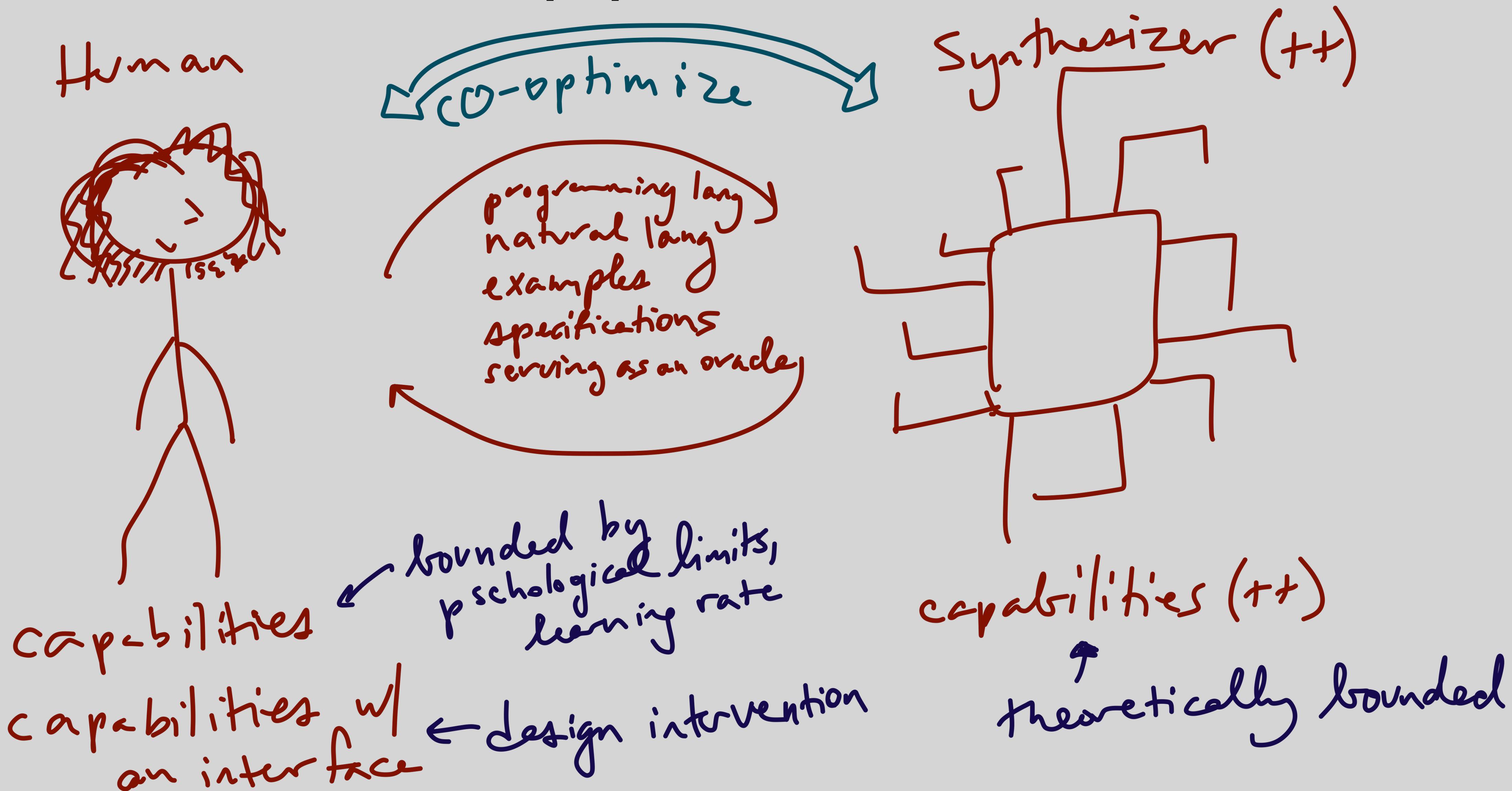
# Approach



# Approach

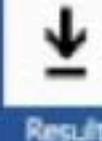
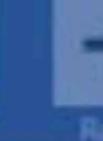


# Approach





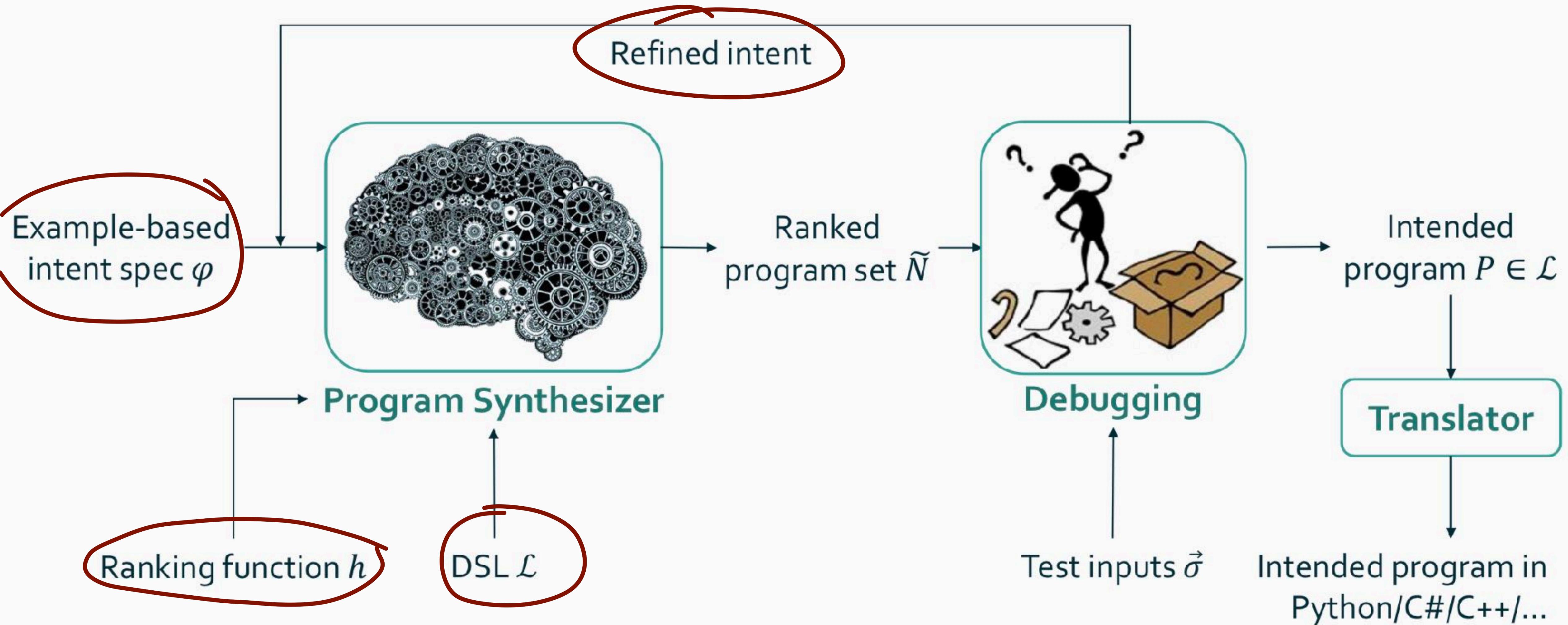
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- [1] A. Ahmed, A. W. Appel, C. D. Richards, K. N. Swadi, G. Tan, and D. C. Wang. Semantic foundations for typed assembly languages. *ACM Trans. Program. Lang. Syst.*, 32(3), 2010.
- [2] A. W. Appel. *Program Logics for Certified Compilers*. Cambridge University Press, 2014.
- [3] A. W. Appel and S. Blazy. Separation logic for small-step Cminor. In TPHOLs, volume 4732 of LNCS, pages 5–21. Springer, 2007.
- [4] A. W. Appel and D. A. McAllester. An indexed model of recursive types for foundational proof-carrying code. *ACM Trans. Program. Lang. Syst.*, 23(5):657–683, 2001.
- [5] Y. Bertot. Structural abstract interpretation: A formal study using Coq. In Language Engineering and Rigorous Software Development, LerNet Summer School, pages 153–194. Springer, 2008.
- [6] B. Blanchet, P. Cousot, R. Cousot, J. Feret, L. Mauborgne, A. Mine, D. Monniaux, and X. Rival. A static analyzer for large safety-critical software. In PLDI, pages 196–207. ACM, 2003.
- [7] S. Blazy, Z. Dargaye, and X. Leroy. Formal verification of a C compiler front-end. In Formal Methods, volume 4085 of LNCS, pages 460–475. Springer, 2006.
- [8] S. Blazy, V. Laporte, A. Maroneze, and D. Pichardie. Formal verification of a C value analysis based on abstract interpretation. In SAS, volume 7935 of LNCS, pages 324–344. Springer, 2013.
- [9] S. Boldo and G. Melquiond. Flocq: A unified library for proving floating-point algorithms in Coq. In ARITH, pages 243–252. IEEE, 2011.
- [10] T. Braibant, J.-H. Jourdan, and D. Monniaux. Implementing and reasoning about hash-consed data structures in Coq. *J. Autom. Reasoning*, 53(3):271–304, 2014.
- [11] D. Cachera, T. P. Jensen, D. Pichardie, and V. Rusu. Extracting a data flow analyser in constructive logic. *Theor. Comput. Sci.*, 342(1):56–78, 2005.
- [12] A. Chlipala. Modular development of certified program verifiers with a proof assistant. *J. Funct. Program.*, 18(5–6):599–647, 2008.
- [13] S. Cho, J. Kang, J. Choi, C.-K. Hur, and K. Yi. SparrowBerry: A verified validator for an industrial-strength static analyzer. <http://rcpas.snu.ac.kr/sparrowberry/>, 2013.
- [14] P. Cousot and R. Cousot. Abstract interpretation: A unified lattice model for static analysis of programs by construction or approximation of fixpoints. In POPL, pages 238–252. ACM, 1977.
- [15] P. Cousot and R. Cousot. Systematic design of program analysis frameworks. In POPL, page 269–282. ACM, 1979.
- [16] P. Cousot, R. Cousot, J. Feret, L. Mauborgne, A. Mine, and X. Rival. Why does Astree scale up? *Formal Methods in System Design*, 35(3):229–264, 2009.
- [17] P. Cousot, R. Cousot, J. Feret, L. Mauborgne, A. Mine, D. Monniaux, and X. Rival. Combination of abstractions in the Astree static analyzer. In ASIAN, volume 4435 of LNCS, pages 272–300. Springer, 2006.
- [18] A. Fouilhé, D. Monniaux, and M. Perin. Efficient generation of correctness certificates for the abstract domain of polyhedra. In SAS, volume 7935 of LNCS, pages 345–365. Springer, 2013.
- [19] A. Fouilhé and S. Bouleme. A certifying frontend for (sub)polyhedral abstract domains. In VSTTE, volume 8471 of LNCS, pages 200–215. Springer, 2014.
- [20] D. Greenaway, J. Andronick, and G. Klein. Bridging the gap: Automatic verified abstraction of C. In ITP, volume 7406 of LNCS, pages 99–115. Springer, 2012.
- [21] S. Gulwani, A. Tiwari, and G. C. Necula. Join algorithms for the theory of uninterpreted functions. In FSTTCS, volume 3328 of LNCS, pages 66–80. Springer, 2004.

BlueLabel	GreenLabel	YellowLabel
36 rows 3 columns		
[1] A. Ahmed, A. W. Appel, C. D. Richards, K. N. Swadi, G. Tan, and D. C. Wang. Semantic foundations for typed assembly languages. <i>ACM Trans. Program. Lang. Syst.</i> , 32(3), 2010.	A. Ahmed, A. W. Appel, C. D. Richards, K. N. Swadi, G. Tan, and D. C. Wang	A. Ahmed
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[11] D. Cachera, T. P. Jensen, D. Pichardie, and V. Rusu. Extracting a data flow analyser in constructive logic. <i>Theor. Comput. Sci.</i> , 342(1):56–78, 2005.	D. Cachera, T. P. Jensen, D. Pichardie, and V. Rusu	D. Cachera
[12] A. Chlipala. Modular development of certified program verifiers with a proof assistant. <i>J. Funct. Program.</i> , 18(5–6):599–647, 2008.		

# PROSE Architecture



Credit: Alex Polozov

“FlashFill in Excel is designed to cater to users that care not about the program but about its behavior on the small number of input rows in the spreadsheet.

Such users can simply eye-ball the outputs of the synthesized program and provide another example if they are incorrect.

	A	B	C
1	First Name	Last Name	Full Name
2	Jay	Shasthri	Jay Shasthri
3	Pratap	Pillai	Pratap Pillai
4	Madhu	Srivastava	Madhu Srivastava
5	Victoria	Marsh	Victoria Marsh
6	David	Pizarro	David Pizarro

[support.office.com](https://support.office.com)

However, this becomes much more cumbersome (or impossible) with a larger spreadsheet.”

- Lu et al. “Interactive Program Synthesis” (2017)

"We have observed that inspecting the synthesized program directly also does not establish enough confidence in it even if the user knows programming.

Two main reasons for this are  
(i) program readability, and  
(ii) *the users' uncertainty in the desired intent due to hypothetical unseen corner cases in the data.*"

	A	B	C
1	First Name	Last Name	Full Name
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3	Pratap	Pillai	Pratap Pillai
4	Madhu	Srivastava	Madhu Srivastava
5	Victoria	Marsh	Victoria Marsh
6	David	Pizarro	David Pizarro
-			

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# Discussion Preview

What is particularly hard about evaluating methods for communicating with computers?



**Harvard** John A. Paulson  
**School of Engineering**  
and Applied Sciences

PL/HCI Seminar (252R/279R)

# Evaluation

Why is it hard:  
some puzzlers from programming languages

puzzler 1  
easy vs safe

?

Array<Cat>

<:

Array<Animal>

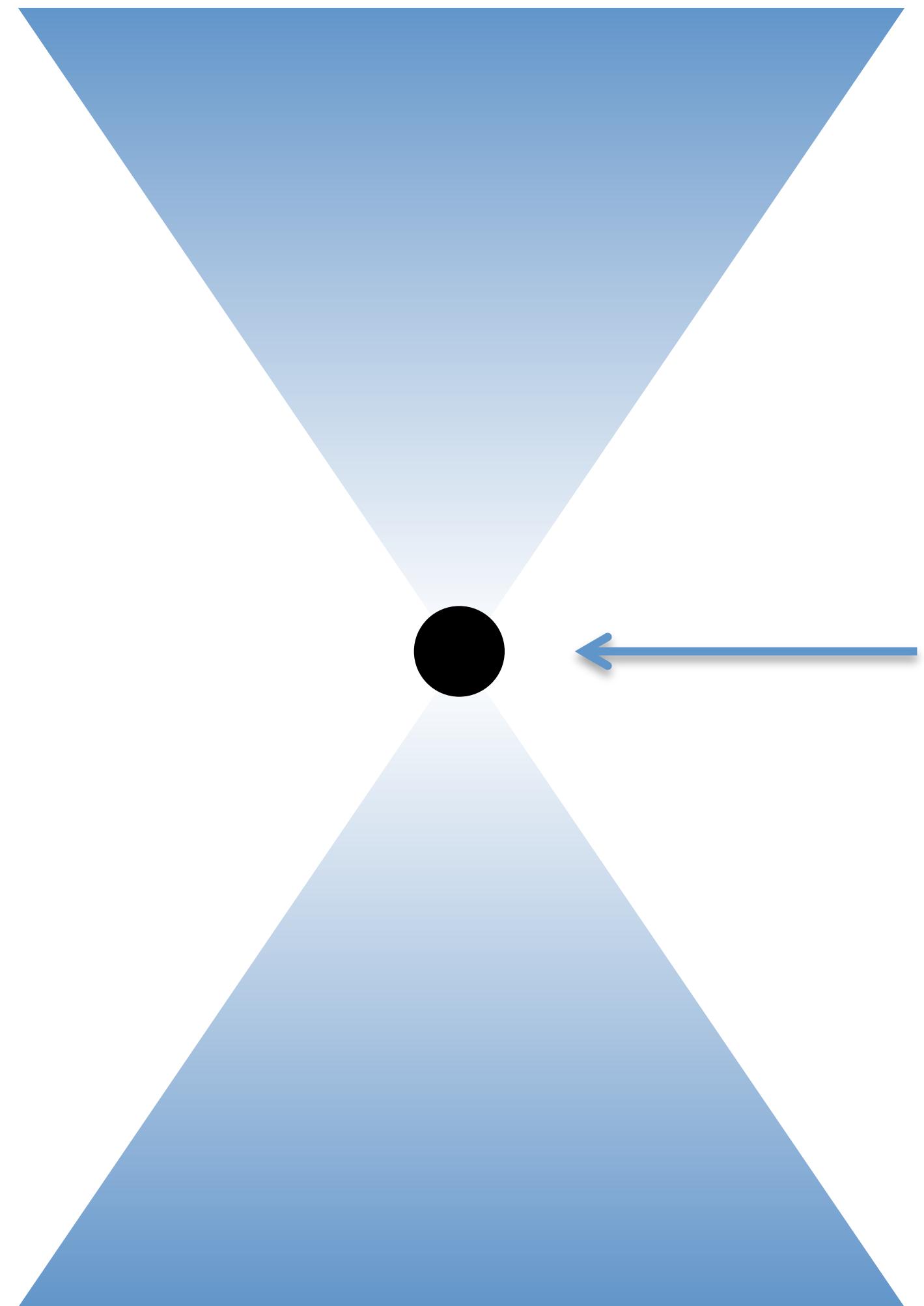
puzzler 2  
*semantics*

?

- let  $x = 1$  in  
let  $f = \text{let } x = 2 \text{ in } (\lambda y \rightarrow y+x)$   
let  $x = 3$  in  
 $f\ 0$
- Is the result 1, 2 or 3?

puzzler 3  
*cognitive overhead*

# Programmer

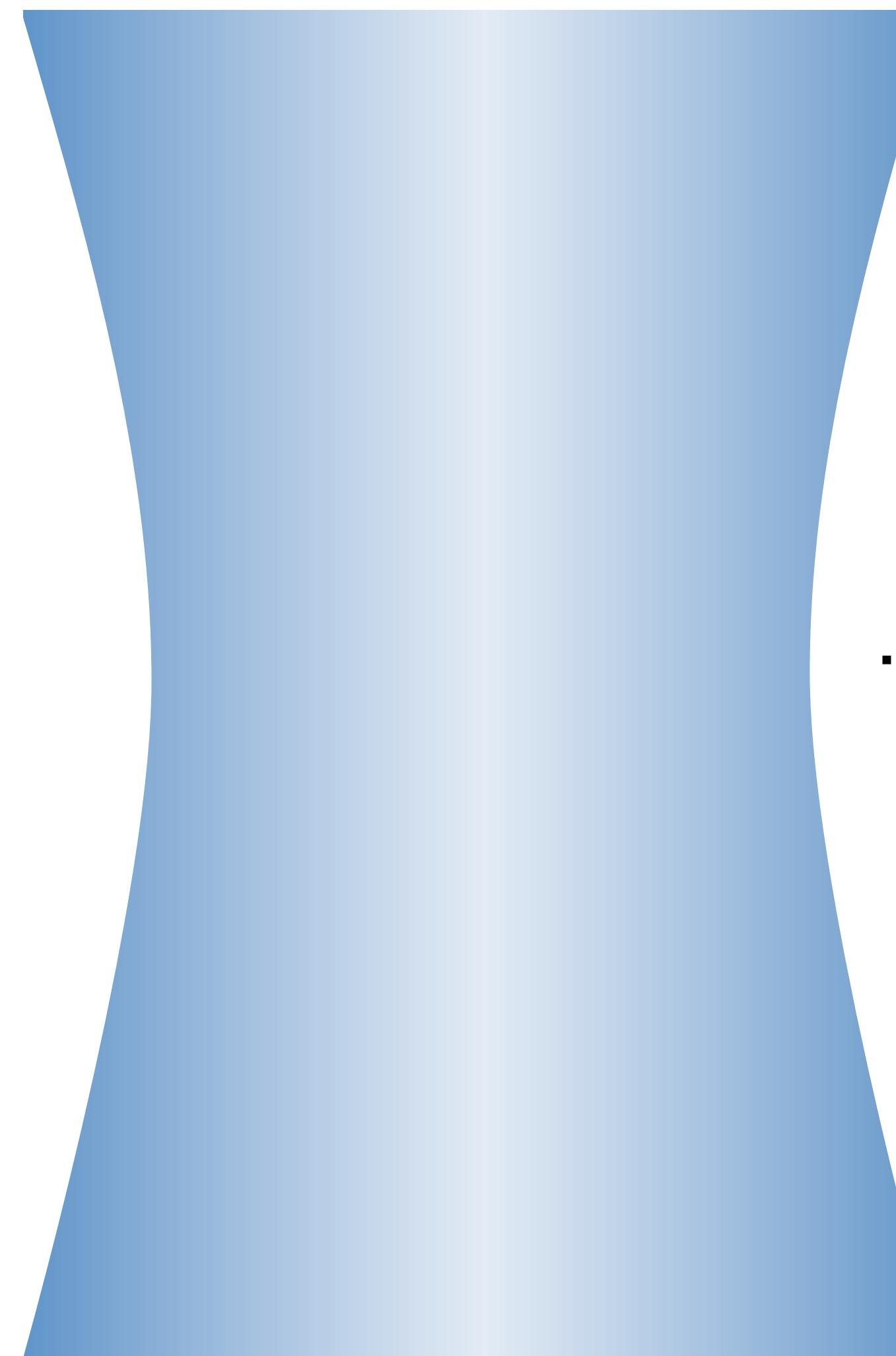


**general purpose compiler**

# Hardware

(illustration: Markus Püschel)

# Programmer



Hardware

- **horizontal and vertical extensibility**
- **generic optimizations** at each level (cse, dce, ...)

Matrix, Graph, ...

Array, Struct, Loop, ...

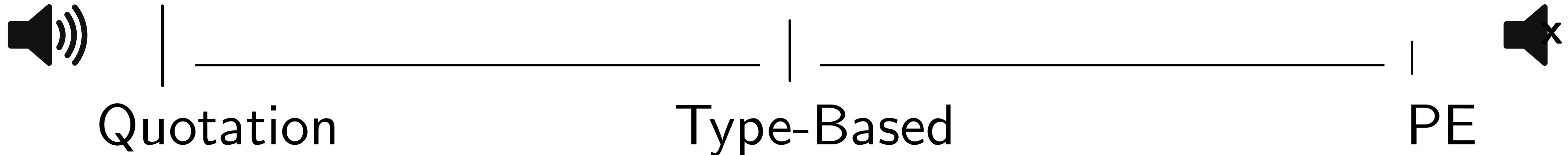
SIMD, GPU, cluster, ...

# Staging?

- multi-level language  
 $n \mid x \mid e @^b e \mid \lambda^b x. e \mid \dots$
- MetaML / MetaOCaml  
 $n \mid x \mid e \mid \lambda x. e \mid \langle e \rangle \mid \sim e \mid \text{run } e$
- Lightweight Modular Staging (LMS) in Scala  
driven by types:  $T$  vs  $\text{Rep}[T]$

“People confuse the familiar for the simple.  
For new features, people insist on LOUD  
explicit syntax. For established features,  
people want terse notation.”

*—Bjarne Stroustrup*



# Power in Scala

```
def square(x: Int): Int = x*x

def power(b: Int, n: Int): Int =
  if (n == 0) 1
  else if (n % 2 == 0) square(power(b, n/2))
  else b * power(b, n-1)

// power(2, 7) == 128
```

# Staged Power in Scala/LMS

```
def square(x: Rep[Int]): Rep[Int] = x*x

def power(b: Rep[Int], n: Int): Rep[Int] =
  if (n == 0) 1
  else if (n % 2 == 0) square(power(b, n/2))
  else b * power(b, n-1)

def snippet(b: Rep[Int]) = power(b, 7)
```

# Generated Power n=7

```
class Snippet extends ((Int)>(Int)) {
    def apply(x0:Int): Int = {
        val x1 = x0 * x0
        val x2 = x0 * x1
        val x3 = x2 * x2
        val x4 = x0 * x3
        x4
    }
}
```

# Power in OCaml

```
let square x = x * x

let rec power n x =
  if n = 0 then 1
  else if n mod 2 = 0 then square (power (n/2) x)
  else x * (power (n-1) x)

(* val power : int -> int -> int = <fun> *)
```

# Staged Power in MetaOCaml

```
let square x = x * x

let rec spower n x =
  if n = 0 then .<1>.
  else if n mod 2 = 0 then .<square .~(spower (n/2) x)>.
  else .<.~x * .~(spower (n-1) x)>.

(* val spower : int -> int code -> int code = <fun> *)
```

# Generated Code

```
let spower7_code = .<fun x -> .~(spower 7 .<x>.)>.;;

(*

val spower7_code : (int -> int) code = .<

fun x_1 ->

  x_1 * ((* CSP square *) (x_1 *
    ((* CSP square *) (x_1 * 1))))>.

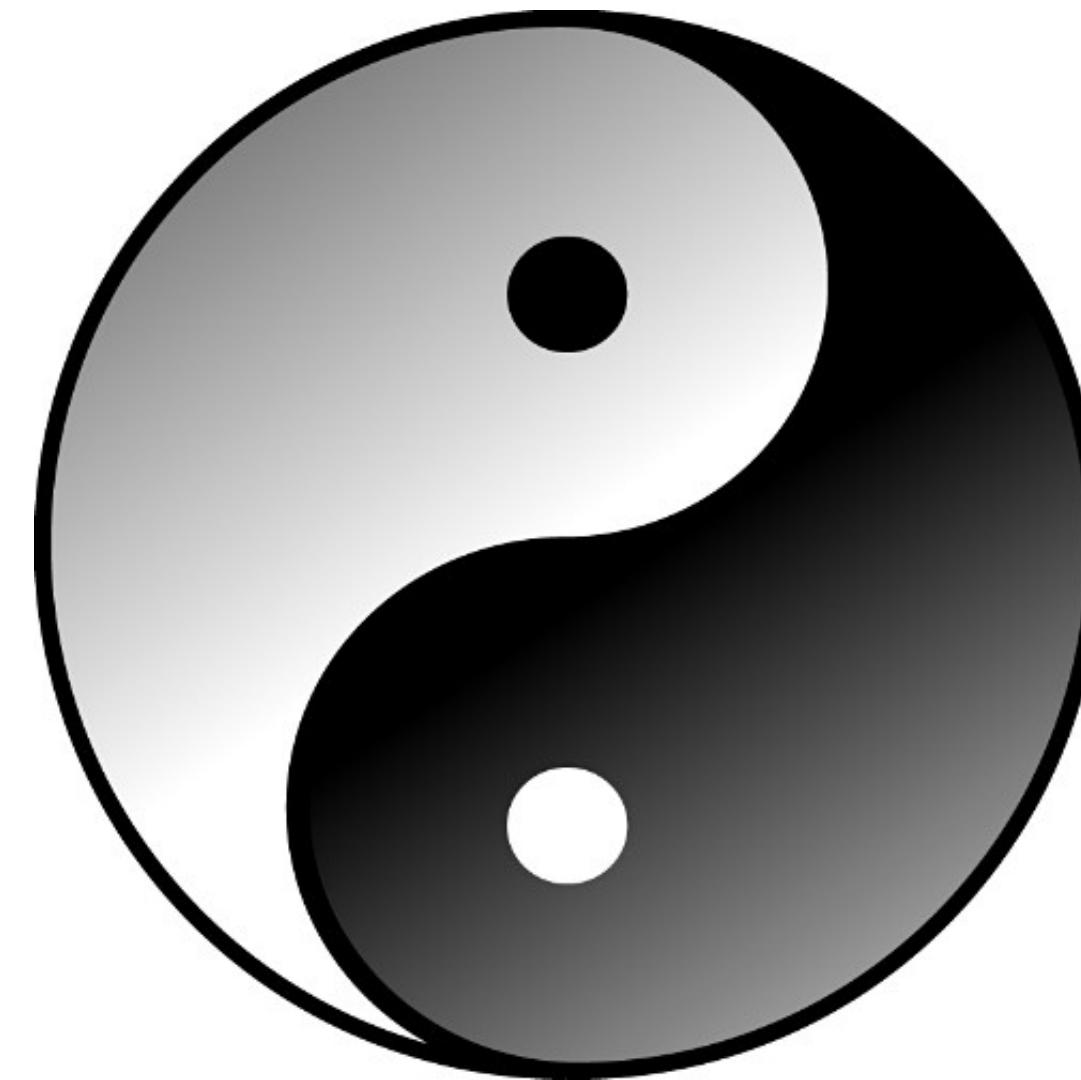
*)
```

# Program generically...



... and run specialized!

Program generically...  
(save human time)



... and run specialized!  
(save computer time)

A matrix vector product, where the matrix is known (static) but the vector is unknown (dynamic),

e.g., for a Hidden Markov Model (HMM) where a single transition matrix is multiplied by many different observation vectors.

*–Shonan Challenge for Generative Programming  
(PEPM’13)*

# Unstaged

```
def matrix_vector_prod(a: Array[Array[Int]],
                      v: Array[Int]) = {
    val n = a.length
    val v1 = new Array[Int](n)
    for (i <- (0 until n)) {
        for (j <- (0 until n)) {
            v1(i) = v1(i) + a(i)(j) * v(j)
        }
    }
    v1
}
```

# Shonan Challenge

```
def matrix_vector_prod(a0: Array[Array[Int]],
                      v: Rep[Array[Int]]) = {
    val n = a0.length
    val a = staticData(a0)
    val v1 = NewArray[Int](n)
    for (i <- (0 until n):Range) {
        val sparse = a0(i).count(_ != 0) < 3
        for (j <- unrollIf(sparse, 0 until n)) {
            v1(i) = v1(i) + a(i).apply(j) * v(j)
        }
    }
    v1
}
```

# Shonan Challenge

```
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        }
    }
    v1
}
```

# Example Matrix

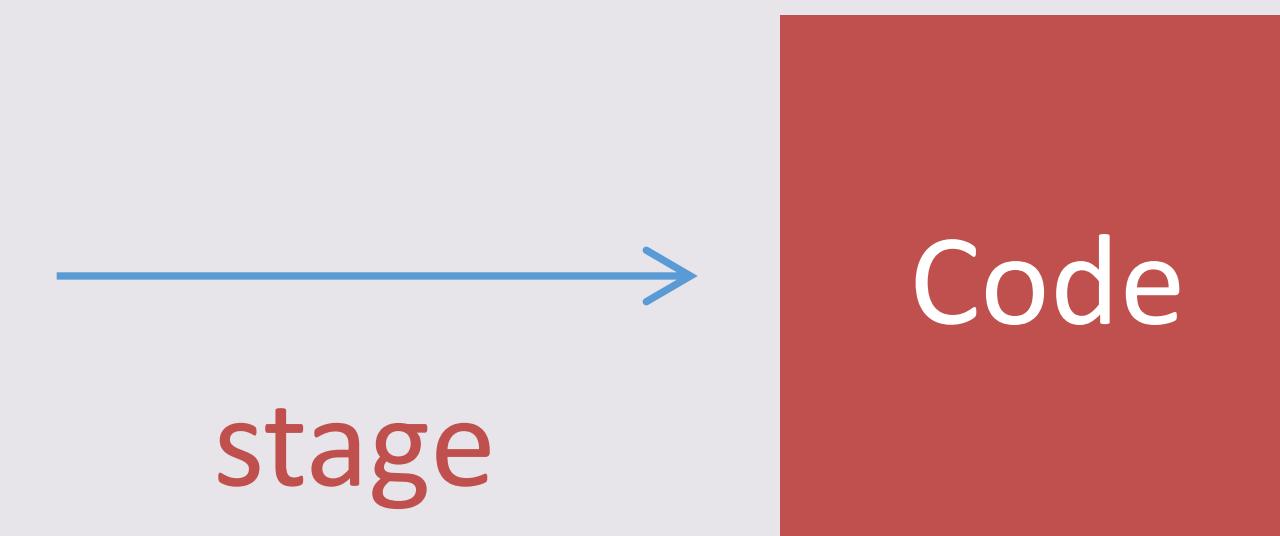
```
val a0 =  
    A(A(1, 1, 1, 1, 1), // dense  
      A(0, 0, 0, 0, 0), // null  
      A(0, 0, 1, 0, 0), // sparse  
      A(0, 0, 0, 0, 0),  
      A(0, 0, 1, 0, 1))
```

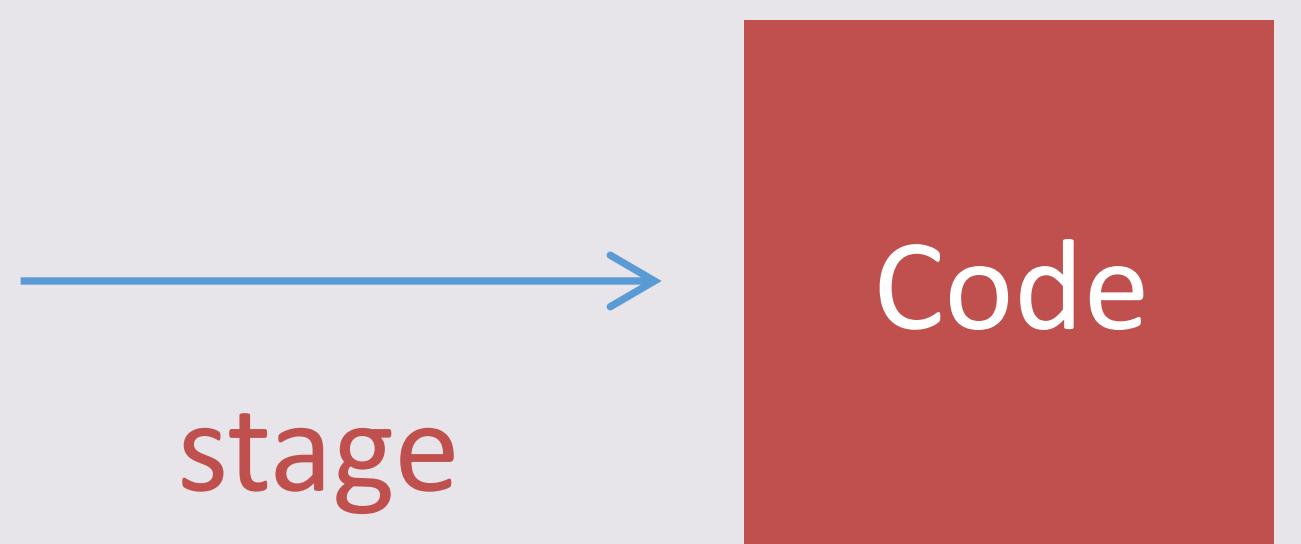
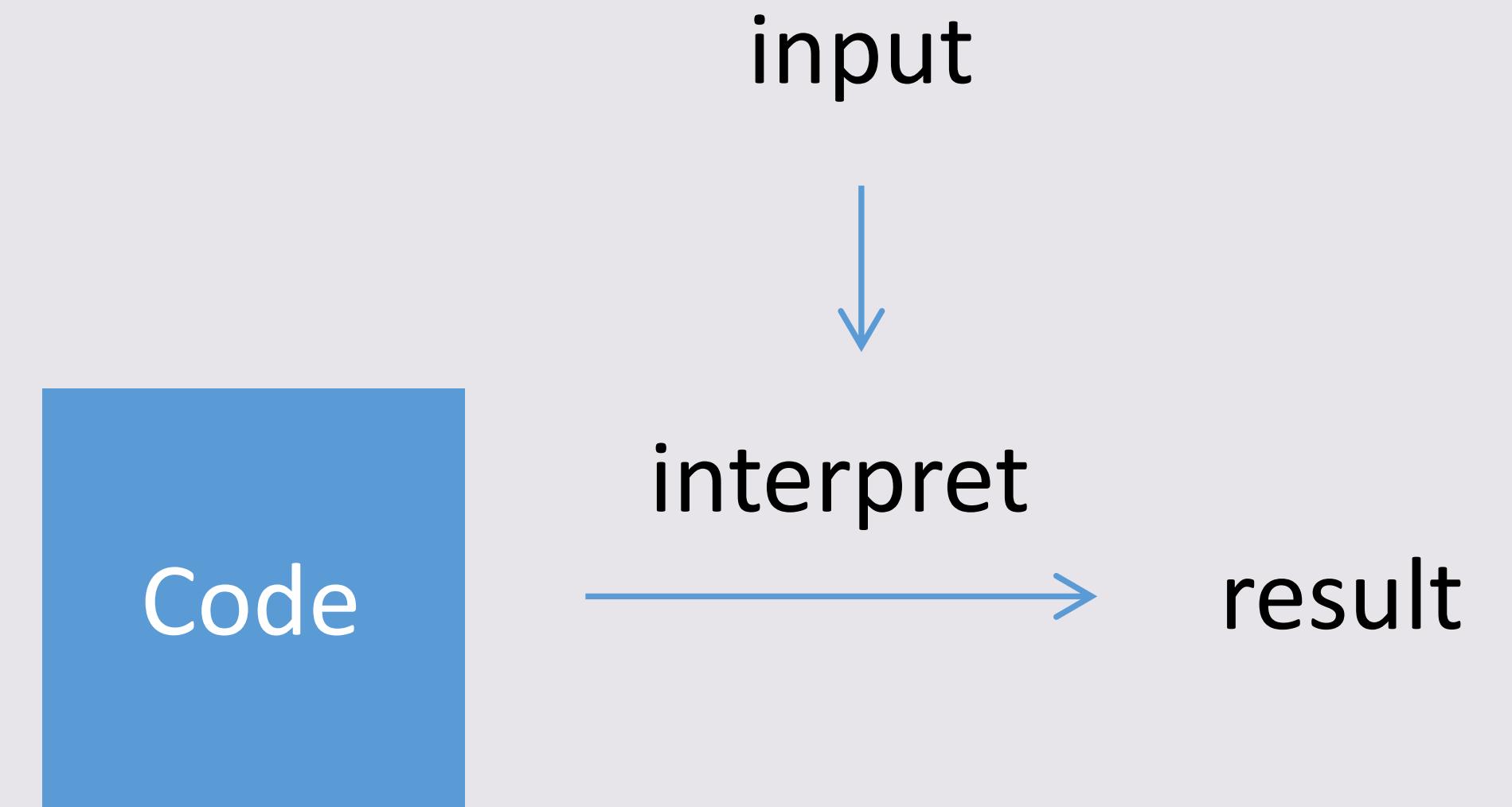
# Generated Code

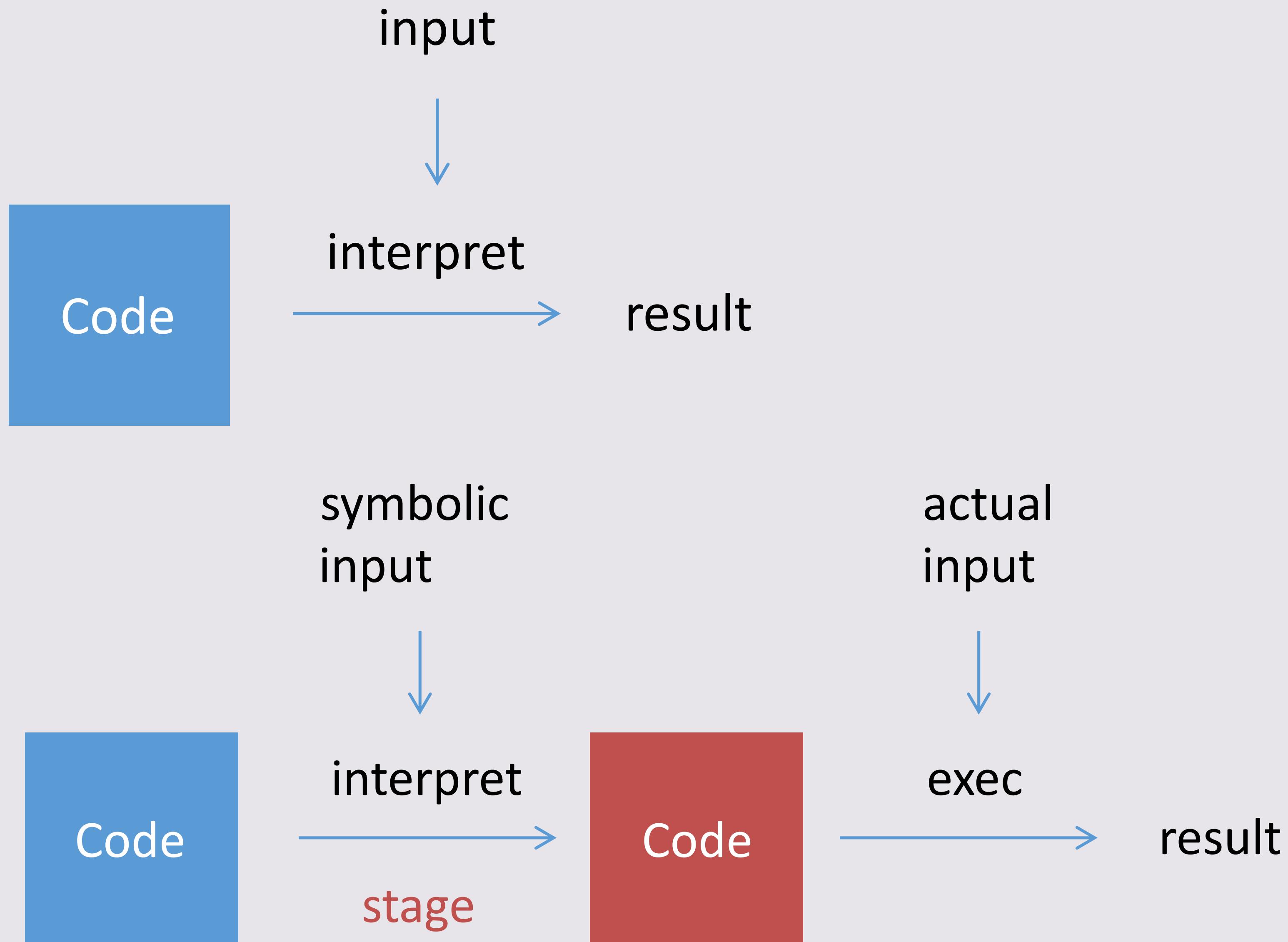
```
class Snippet(px6:Array[Int]) extends ((Array[Int])=>(Array[Int])) {  
    def apply(x0:Array[Int]): Array[Int] = { val x2 = new Array[Int](5)  
        val x6 = px6 // static data: Array(1,1,1,1,1)  
        var x4 : Int = 0  
        val x13 = while (x4 < 5) {  
            val x5 = x2(0); val x7 = x6(x4); val x8 = x0(x4)  
            val x9 = x7 * x8; val x10 = x5 + x9;  
            val x11 = x2(0) = x10  
            x4 = x4 + 1 }  
        val x14 = x2(1); val x17 = x2(1) = x14  
        val x22 = x2(2); val x24 = x2(2) = x22  
        val x19 = x0(2); val x25 = x22 + x19  
        val x26 = x2(2) = x25; val x27 = x2(3); val x29 = x2(3) = x27  
        val x30 = x2(4); val x32 = x2(4) = x30  
        val x33 = x30 + x19; val x34 = x2(4) = x33  
        val x21 = x0(4); val x35 = x33 + x21; val x36 = x2(4) = x35  
        x2 }}}
```

# Turning Interpreters into Compilers

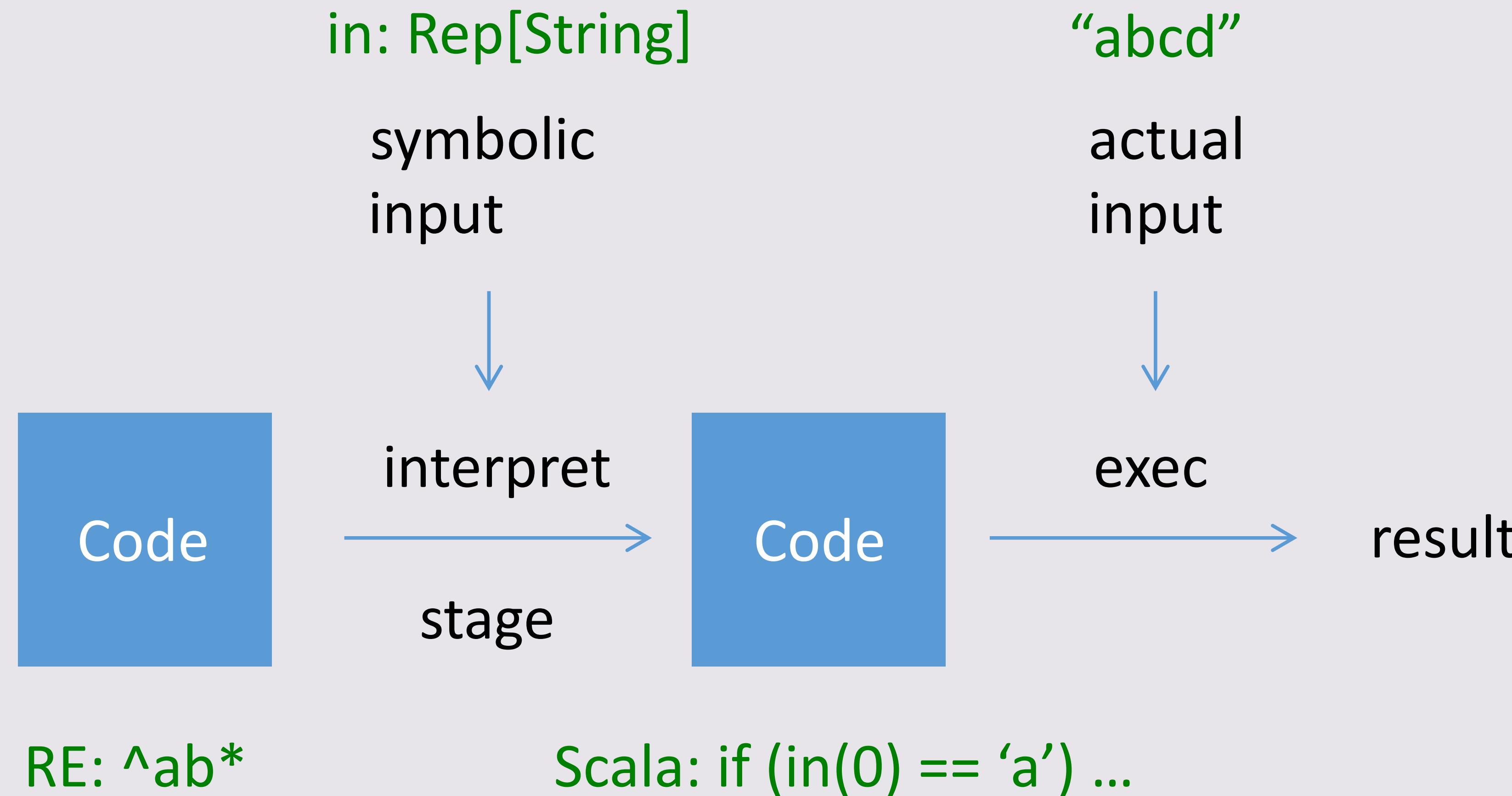
# Turning Interpreters into Compilers







# Turning interpreters into compilers



# Usability Issues

- cognitive overhead of multi-level language
- notational overhead?
- multi-stage errors

puzzler 4  
*synthesis*

# Programming by Example

- $f(1)=2, f(2)=3, \dots$
- $g(1)=2, g(2)=4, \dots$
- $h(1)=3, h(2)=5, \dots$

# SMT solver underspecified

- (assert (and (= (f 1) 2) (= (f 2) 3)))
- Model:  
 $f(x) = \text{if } x=2 \text{ then } 3 \text{ else if } x=2 \text{ then } 3 \text{ else } 2$
- Try it: <https://rise4fun.com/Z3/bpMYx>

# SMT solver overspecified

- (assert (forall ((x Int) (y Int))  
  ( $\Rightarrow$  (or (and (= x 1) (= y 2))  
              (and (= x 2) (= y 3))))  
              (= y (+ (\* a x) b))))))
- Solution: a=1, b=1, so f(x)=x+1.
- Try it: <https://rise4fun.com/Z3/HcJY>

# SMT solver full program

```
(declare-const a Int)
(declare-const b Int)
(define-fun f ((x Int)) Int (+ (* a x) b))
(assert (and (= (f 1) 2) (= (f 2) 3)))
(check-sat)
(get-model)
```

- Try it: <https://rise4fun.com/Z3/jhr8>

# Usability Issues

- Trade-offs, e.g. between expressivity and decidability.
- Need to be precise induces cognitive overhead.
- Precision is brittle.
- Many ways to encode.

# why evaluation is hard

- Many conflicting dimensions: faster, safer, easier
- Does a new toolkit enable new ways
  - of thinking?
  - of programming?
  - of creating?

# Discussion

What is particularly hard about evaluating methods for communicating with computers?

# Group Projects

- Systems HCI requiring heavy-duty PL
  - Humans modifying DSLs for PBD (programming by demonstration)
  - Explore with interactively defined templates
- Generic human-centered PL
  - Pick language feature, design it in a human-friendly way
  - Pick a language, describe how—and to what extent—its features are being used in the wild
- Usable + X (PL technique)
  - Usable Generative Programming
  - Usable Probabilistic Programming
  - Usable Type System / Verification
  - Usable Synthesis
    - inductive bias alignment between human and machine
    - ranking function improvements
    - DSL improvements
    - expressing constraints on intermediate states, i.e., equivalence values or types

Thank you !