

# **CLUSTERING AND VISUALIZING SOLUTION VARIATION IN MASSIVE PROGRAMMING CLASSES**

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# MASSIVE PROGRAMMING CLASSES

- Introductory class sizes
  - ~1500 at UC Berkeley
  - hundreds at MIT
  - Many more complete online programming exercises  
(edX, Coursera, Khan Academy)



Margaret Hamilton, NASA  
software developer



Israeli & Palestinian students  
writing apps and websites  
and founding businesses  
together (MIT MEET)

# STUDENTS WRITE MULTIPLE SHORT SOLUTIONS PER WEEK

## Problem

1. exponentiate a number

## One student solution

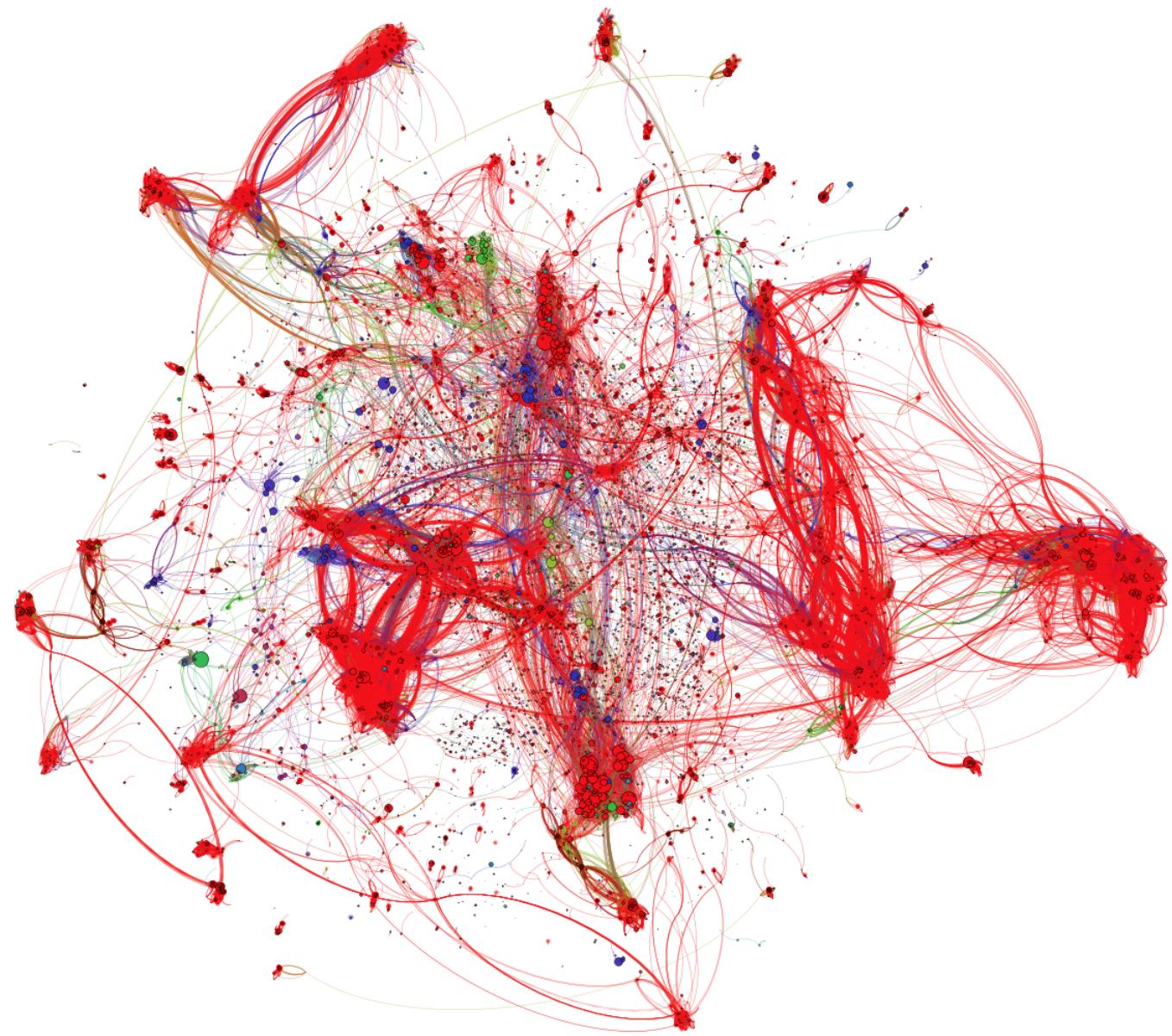
```
def power(base,exp):  
    result=1  
    while exp>0:  
        result*=base  
        exp-=1  
    return result
```

2. compute a derivative

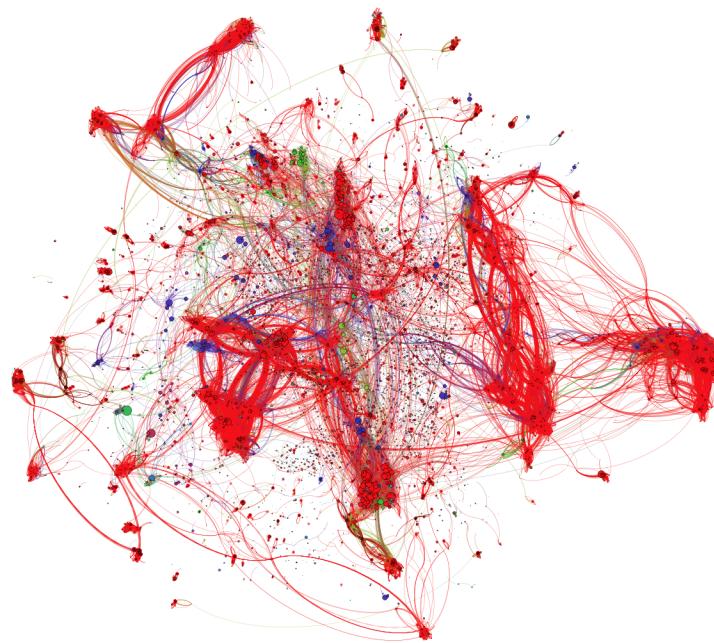
```
def computeDeriv(poly):  
    result=[]  
    for i in range(1,len(poly)):  
        result.append(float(poly[i]*i))  
    return result
```

3. compute a logarithm

```
def myLog(x,b):  
    power=0  
    while b**power<=x:  
        power+=1  
    return power-1
```







- "Codewebs" by Huang et. al. (WWW '14)
  - ~40,000 student submissions to the same problem
  - Source: Coursera's Machine Learning course
  - Ran on a computing cluster

# THESIS CONTRIBUTION 1:

## CLUSTER AND VISUALIZE IN A HUMAN-READABLE WAY

```
def iterPower(base,exp):
    result=1
    while exp>0:
        result*=base
        exp-=1
    return result
```

This synthesized solution represents 1538 solutions

# OUTLINE

- Solution Variation (**SV**)
- Research Questions
  - (R1) understand **SV**
  - (R2) feedback on **SV** at scale
  - (R3) personalized feedback on **SV** at scale
  - (R4) collect and distribute student advice, given **SV**
- Discussion

# SOLUTION VARIATION

- Correctness
- Approach
- Readability

## CORRECTNESS WITH RESPECT TO TEST CASES

1. `power(5, 3)` should return 125
2. `power(3, 4)` should return 81
3. `power(2, 5)` should return 32
4. . . .

(automated with an "autograder")

# AUTOGRADERS CAN ONLY DO SO MUCH

These are all "correct":

```
def power(base,exp):  
    result=1  
    while exp>0:  
        result*=base  
        exp-=1  
    return result  
  
def power(base,exp):  
    if exp == 0:  
        return 1  
    else:  
        return base * power(base,  
exp-1)
```

```
def power(base, exp):  
    tempBase=base  
    result = base  
  
    if type(base)==int:  
        while exp==0:  
            result = 1  
            print(result)  
            break  
        exp=exp-1  
        while exp >0:  
            tempCal=abs(tempBase)  
            exp=exp-1  
            while exp<0:  
                break  
            for i in range (1,tem
```

# APPROACH

- Disregards teacher's request to write it themselves

```
def power(base, exp):  
    return base**exp
```

- Reveals possible misconceptions, e.g., unnecessary statements

```
def power(base,exp):  
    result=1  
    while exp>0:  
        result=result*base  
        exp-=1  
        continue #keyword here does not change execution  
    return result
```

# APPROACH

- Common

```
def power(base,exp):  
    result=1  
    while exp>0:  
        result*=base  
        exp-=1  
    return result
```

- Unusual, possibly innovative

```
def power(base,exp):  
    if exp == 0:  
        return 1  
    else:  
        return base * power(base, exp-1)
```

# READABILITY

- Correct w.r.t. test cases
- Difficult to read

```
def power(base, exp):  
    tempBase=base  
    result = base  
  
    if type(base)==int:  
        while exp==0:  
            result = 1  
            print(result)  
            break  
        exp=exp-1  
        while exp >0:  
            tempCal=abs(tempBase)  
            exp=exp-1  
            while exp<0:  
                break  
            for i in range (1,tempCal):
```

INCOMPLETE IMPLEMENTATION OF  
STRATEGIZED PROGRAMMATICS DESIGNATED  
TO MAXIMIZE ACQUISITION OF AWARENESS  
AND UTILIZATION OF COMMUNICATIONS SKILLS  
PURSUANT TO STANDARDIZED REVIEW AND  
ASSESSMENT OF LANGUAGINAL DEVELOPMENT.



The reason Verbal SAT scores are at an all-time low

ANY INTERROGATORY  
VERBALIZATIONS? —



**READABILITY MATTERS**

- **Student design choices** affect correctness, approach and readability
- Examples:
  - `for` vs. `while`
  - `a *= b` vs. `a = a*b`
  - recursion vs. iteration

*Solution variation is a result of these choices*

# SOLUTION VARIATION

- Different comments, statement order, variable names

```
def iterPower(base, exp):  
    '''  
    base: int or float.  
    exp: int >= 0  
  
    returns: int or float, base^exp  
    '''  
    result = 1  
    while exp > 0:  
        result *= base  
        exp -= 1  
    return result  
  
  
def iterPower(base, exp):  
    wynik = 1  
    while exp > 0:  
        exp -= 1 #using exp argument as counter  
        wynik *= base  
    return wynik
```

April

answer.py ✓

2014

215.py ✓

2140.py ✓

2145.py ✓

2156.py ✓

21372.py ✓

21376.py ✓

21384.py ✓

21389.py ✓

21400.py ✓

21404.py ✓

21409.py ✓

21425.py ✓

21432.py ✓

21440.py ✓

21461.py ✓

21465.py ✓

```
def iterPower(base, exp):
    """
    base: int or float.
    exp: int >= 0

    returns: int or
float, base^exp
    """

    # Your code here
    res=1.
    while exp>0:
        exp-=1
        res=res*base
    return res
```

 21465.py	
 21470.py	
 21472.py	
 21474.py	
 21480.py	
 21489.py	
 21500.py	
 21506.py	
 21519.py	
 21522.py	
 21524.py	
 21527.py	
 21532.py	
 21533.py	
 21552.py	
 21553.py	

## 215.py

235 bytes

Created 5/20/14, 11:36 AM  
Modified 5/20/14, 11:36 AM  
Last opened 5/20/14, 11:36 AM  
[Add Tags...](#)

## CHALLENGE

How do you understand  
(1) what students wrote  
(2) give feedback at scale?

## OPPORTUNITY

What value *only* exists in a  
massive programming class?

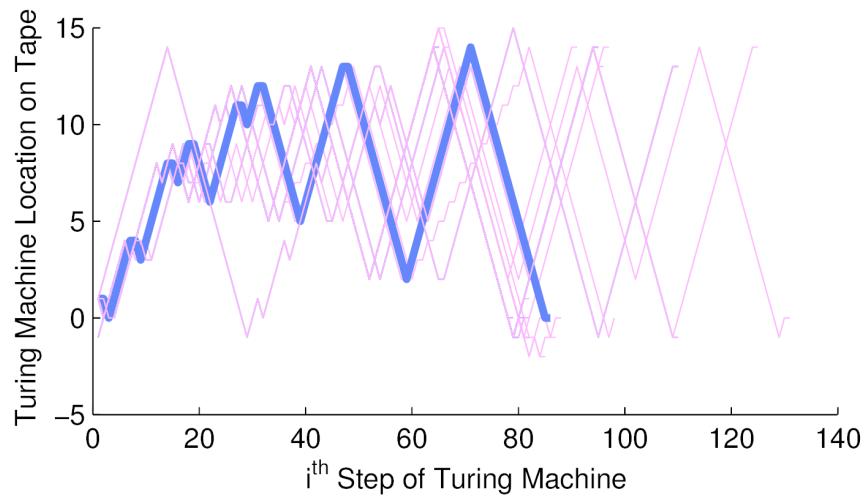
# OPPORTUNITY: EXPLOITING SOLUTION VARIATION WITHIN LARGE DATASETS

- Teachers could
  - learn about new solutions from students
  - find better examples for discussion
- Teachers could write better feedback, test cases, evaluation rubrics
- Students could be tapped as experts on their solutions (and bugs they fix)

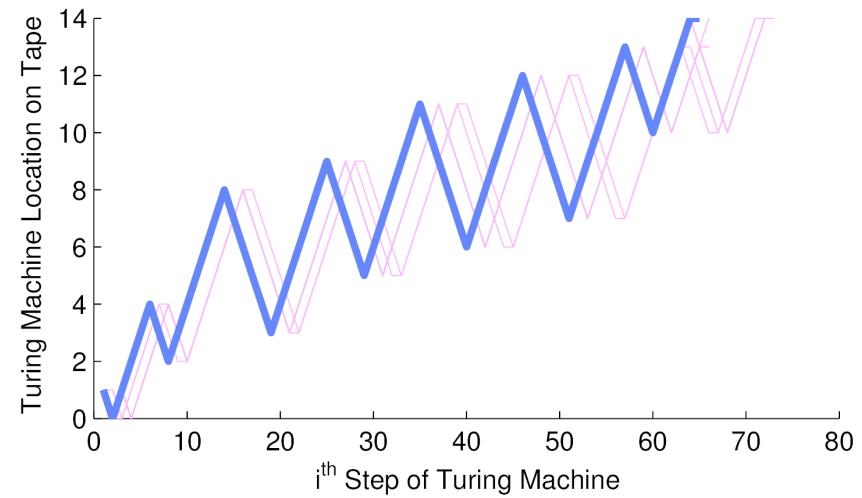
## A Turing Machine - Overview



# TWO COMMON STRATEGIES



**Strategy A**  
(~50% of correct solutions)



**Strategy B**  
(~40% of correct solutions)

2 solutions passed all test cases  
but subverted teacher instructions

- Fellow teachers were not aware
  - of multiple solutions
  - that the test suite was insufficient

# OUTLINE

- Solution Variation (SV)
- Research Questions
  - (R1) understand SV
  - (R2) feedback on SV at scale
  - (R3) personalized feedback on SV at scale
  - (R4) collect and distribute student advice, given SV
- Discussion

## RESEARCH QUESTIONS

When the teacher cannot read all the solutions in a collection,

- (R1) ... how can the teacher understand the common and uncommon variation in their students' solutions?
- (R2) ... how can the teacher give feedback on the approach & readability at scale?
- (R3) ... in a personalized way?
- (R4) How can students do the same?

# OUTLINE

- Solution Variation (SV)
- Research Questions
  - ⇒ (R1) understand **SV**
  - (R2) feedback on **SV** at scale
  - (R3) personalized feedback on **SV** at scale
  - (R4) collect and distribute student advice, given **SV**
- Discussion

## def power(base, exp):

```
'''iterative solution
result=1 #initialize
while exp>0:
    exp-=1 #input as counter
    result=result\ *base
return result

res=1
while exp>0:
    res=res*base
    exp-=1
return res
```

```
result=1
while exp>0:
    exp-=1
    result=result\ *base
return result
```

```
result = 1
while(exp>0):
    exp-=1
    result=result\ *base
return result
```

```
myans=1
while exp>0:
    myans=myans\ *base
    exp-=1
return myans
```

```
ans = base
if (exp == 0):
    return round(base/base, 4)
else:
    for n in range(exp-1):
        ans *= base
    return round(ans, 4)
```

```
result = base
if exp==0:
    return 1
if exp==1:
    return result
while exp > 1:
    result *= base
    exp -= 1
return result
```

**HOW DOES A TEACHER READ  
THOUSANDS OF SOLUTIONS?  
(WITHOUT ACTUALLY READING ALL OF THEM)**

## SYNTHESIZE SOLUTIONS THAT REPRESENT MANY

```
def iterPower(base,exp):
    result=1
    while exp>0:
        result*=base
        exp-=1
    return result
```

represents 1538/3852 solutions

# PIPELINE

1. Remove comments
2. Standardize formatting
3. Normalize variable names *using student-chosen names across all solutions*

The set of unique solutions (ignoring statement order) at the end of this process are our representatives.

```
def power(base, exp):  
  
    '''iterative solution  
    result=1 #initialize  
    while exp>0:  
        exp-=1 #input as counter  
        result=result*\n                 base  
    return result  
  
    result=1  
    while exp>0:  
        exp-=1  
        result=result*\n                 base  
    return result = 1  
    while(exp>0):  
        exp-=1  
        result=result*\n                 base  
    return result
```

```
def power(base, exp):  
  
    result=1  
    while exp>0:  
        exp-=1  
        result=result\  
            *base  
    return result
```

```
def power(base, exp):
```

3

```
result=1
while exp>0:
    exp-=1
    result=result\
        *base
return result
```

```
def power(base, exp):
```

3

```
result=1
while exp>0:
    exp-=1
    result=result\
        *base
return result
```

```
res=1
while exp>0:
    res=res*base
    exp-=1
return res
```

# NORMALIZE VARIABLE NAMES WITH PASSIVE CROWDSOURCING

- Give variables their most popular name across all solutions

# PROBLEM: IDENTIFYING VARIABLES ACROSS SOLUTIONS

```
def power(base,exp):  
    result=1  
    while exp>0:  
        exp-=1  
        result=result*base  
    return result
```

```
def power(base,exp):  
    res=1  
    while exp>0:  
        res=res*base  
        exp-=1  
    return res
```

1. How do we tell that the variable 'res' (left) is the “same” as the variable 'result' (right)?
2. How do we tell if two students voted for the same variable name?
3. What does the “same variable in two different solutions” even mean?

```
def power(base,exp):  
    result=1  
    while exp>0:  
        exp-=1  
        result=result*base  
    return result
```

```
base: 5  
exp: 3, 2, 1, 0  
result: 1, 5, 25, 125
```

```
def power(base,exp):  
    res=1  
    while exp>0:  
        res=res*base  
        exp-=1  
    return res
```

```
base: 5  
exp: 3, 2, 1, 0  
res: 1, 5, 25, 125
```

Run all on test case(s):

`iterPower(5,3)`

# VARIABLES ACROSS ALL SOLUTIONS

- Variable that takes on sequence

1, 5, 25, 125

- Occurs in 3081/3842 solutions
- Most common name

result

- Other names

wynik, out, total, ans, acum, num, mult

- Refer to it as the '**result common variable**'

# VARIABLES ACROSS ALL SOLUTIONS

- Variable that takes on sequence

3, 2, 1, 0

- Occurs in 2744/3842 solutions
- Most common name

exp

- Other names

count, temp, exp3, exp2, exp1, inexp, old  
\_exp

- Refer to it as the '**exp common variable**'

## PRESERVE 1-TO-1 MAPPING BETWEEN NAME AND BEHAVIOR

Common Variable	Found in	Most common name	Renamed
1, 5, 25, 125	3081 solutions	result	result
5, 25, 125	< 3081 solutions	result	<i>result</i> <sub>2</sub>

```
def power(base, exp):
```

3

```
result=1
while exp>0:
    exp-=1
    result=result\
        *base
return result
```

```
result=1
while exp>0:
    result=result\
        *base
    exp-=1
return result
```

```
result2 = base
if (exp2 == 0):
    return round(base/base, 4)
else:
    for n in range(exp2-1):
        result2 *= base
    return round(result2, 4)
```

```
result=1
while exp>0:
    result=result\
        *base
    exp-=1
return result
```

```
result2 = base
if exp==0:
    return 1
if exp==1:
    return result
while exp > 1:
    result2 *= bas
e
    exp -= 1
return result2
```

```
def power(base, exp):  
  
    3  
    result=1  
    while exp>0:  
        exp-=1  
        result=result\  
            *base  
    return result  
  
  
result=1  
while exp>0:  
    result=result\  
        *base  
    exp-=1  
return result
```

```
def power(base, exp):
```

5

```
result=1
while exp>0:
    exp-=1
    result=result\
        *base
return result
```

```
result2 = base
if (exp2 == 0):
    return round(base/base, 4)
else:
    for n in range(exp2-1):
        result2 *= base
    return round(result2, 4)
```

```
result2 = base
if exp==0:
    return 1
if exp==1:
    return result
while exp > 1:
    result2 *= bas
e
    exp -= 1
return result2
```

## SYNTHESIZED REPRESENTATIVE SOLUTIONS

```
def iterPower(base,exp):
    result=1
    while exp>0:
        result*=base
        exp-=1
    return result
```

represents 1538 solutions

# SYNTHESIZED REPRESENTATIVE SOLUTIONS

1538

```
def iterPower(base,exp):  
    result=1  
    while exp>0:  
        result*=base  
        exp-=1  
    return result
```

374

```
def iterPower(base,exp):  
    result=1  
    while exp>0:  
        result=result*base  
        exp-=1  
    return result
```

153

```
def iterPower(base,exp):  
    result=1  
    while exp>0:  
        result=result*base  
        exp=exp-1  
    return result
```

88

```
def iterPower(base,exp2):  
    result=1
```

```
result=1  
for i in range(exp2):  
    result*=base
```

# SYNTHESIZED REPRESENTATIVE SOLUTIONS

97

```
def getGuessedWord(secretWord,lettersGuessed):
    result=''
    for letter in secretWord:
        if letter in lettersGuessed:
            result+=letter
        else:
            result+='_'
    return result
```

36

```
def getGuessedWord(secretWord,lettersGuessed):
    result=''
    for letter in secretWord:
        if letter in lettersGuessed:
            result=result+letter
        else:
            result=result+'_'
    return result
```

15

```
def getGuessedWord(secretWord,lettersGuessed):
    result=""
    for letter in secretWord:
        if letter in lettersGuessed:
            result+=letter
        else:
            result+=" _ "
    return result
```

14

```
def getGuessedWord(secretWord,lettersGuessed):
    result=''
    for letter in secretWord:
        if letter not in lettersGuessed:
            result+='_'
        else:
```

# **SYNTHESIZED REPRESENTATIVE SOLUTIONS**

22

```
def computeDeriv(poly):
    if len(poly)==1:
        return[0.0]
    result=[]
    for i in range(1,len(poly)):
        result.append(float(poly[i]*i))
    return result
```

21

```
def computeDeriv(poly):
    result=[]
    evaluatedTerm=0
    i2=0
    for i2 in range(len(poly)):
        evaluatedTerm=round(poly[i2]*i2,2)
        if i2>=1:
            result.append(evaluatedTerm)
    return result
```

14

```
def computeDeriv(poly):
    result=[]
    for i in range(1,len(poly)):
        result.append(float(poly[i]*i))
    return result
```

13

```
def computeDeriv(poly):
    result=[]
    i4=0
    for i3 in poly:
        if i4>0:
            result=result+[float(i3*i4)]
```

# **SYNTHESIZED REPRESENTATIVE SOLUTIONS**

37

```
def myLog(x,b):
    power=0
    while b**power<=x:
        power+=1
    return power-1
```

6

```
def myLog(x,b):
    power2=0
    while b**(power2+1)<=x:
        power2+=1
    return power2
```

5

```
def myLog(x,b):
    i3=1
    while b**i3<=x:
        i3+=1
    return i3-1
```

3

```
def myLog(x,b):
    power3=0
    while b**power3<=x:
        power3+=1
    if b**power3>x:
        power3-=1
    return power3
```

# PIPELINE ANALYSIS

- Dataset: solutions collected from 6.00x (edX Fall '12)

Problem	Solutions	Represented by	Running Time
power	3875	862	15.5m
hangman	1118	552	8.1m
derivative	1433	1109	10.3m

- With Stacey Terman, pipeline adapted to "normalize" incorrect programs as well

# HIGHLIGHTING DIFFERENCES

1538

```
def iterPower(base,exp):
    result=1
    while exp>0:
        result*=base
        exp-=1
    return result
```

374

```
def iterPower(base,exp):
    result=1
    while exp>0:
        result=result*base
        exp-=1
    return result
```

- Highlights differences in
  - solution popularity
  - syntax

**USERS CONTINUE SYNTHESIZING  
REPRESENTATIVES INTERACTIVELY**

# ADD NEW EQUIVALENCE RULES

rewrite `result=result*base`

as `result*=base|`

capture `exp2` by typing `exp___2`

**add new rule**

# **OVERCODE**

**DEMO**

showing stacks

602 correct  
1026 total

read

largest stack (matching filters)

1538

```
def iterPower(base,exp):  
    result=1  
    while exp>0:  
        result*=base  
        exp-=1  
    return result
```

representing submissions

3428 correct  
3852 total

filtering by

filter

rewrite

legend

lines that appear in at least 50 submissions

```
2582 def iterPower(base,exp):  
723 def iterPower(base,exp_2):  
334 def iterPower(base,exp_3):  
53 def iterPower(base,exp_4):  
53 elif exp_3==1:  
530 else:  
2464 exp-=1  
273 exp=exp-1  
135 exp=exp_2  
362 exp_3-=1  
59 exp_3=exp_3-1  
63 for i in range(0,exp_2):  
172 for i in range(exp_2):  
65 i_2=0  
187 if exp==0:  
216 if exp_2==0:  
348 if exp_3==0:  
2065 result*=base  
2918 result=1  
127 result=1.0  
103 result=base  
105 result=base*result  
949 result=result*base  
74 result_2*=base  
167 result_2=base  
101 result_2=result_2*base  
53 result+=base
```

remaining stacks (matching filters)

374

```
def iterPower(base,exp):  
    result=1  
    while exp>0:  
        result=result*base  
        exp-=1  
    return result
```

153

```
def iterPower(base,exp):  
    result=1  
    while exp>0:  
        result=result*base  
        exp=exp-1  
    return result
```

88

```
def iterPower(base,exp_2):  
    result=1  
    for i in range(exp_2):  
        result*=base  
    return result
```

55

```
def iterPower(base,exp_2):  
    exp=exp_2
```

(<http://0.0.0.0:8000/?src=iterpower>)

# CAN TEACHERS READ AND UNDERSTAND MORE STUDENT CODE WITH OVERCODE?

- 12 participants (11 male)
- mean age: 25.4 ( $\sigma = 6.9$ )
- 4.9 ( $\sigma = 3.0$ ) years of Python programming experience
- 9 previously graded code
- 5 previously graded Python code

# OVERCODE USER STUDY

- Task: Identify the 5 most frequent strategies used to solve the problem (15 min)
- For each strategy, they wrote:
  - a code example
  - comments
  - confidence

# Control interface

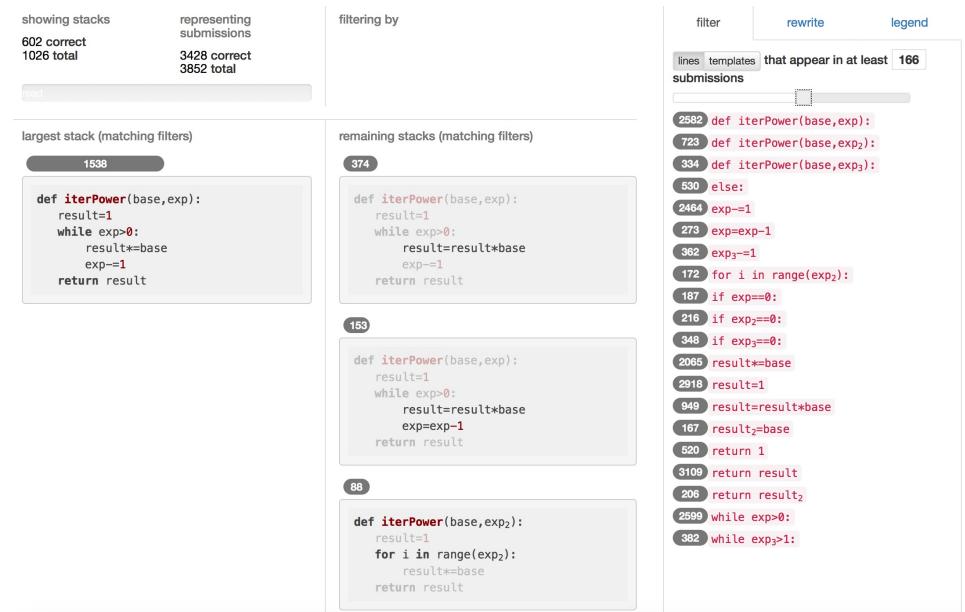
Student submissions file:///Users/ iterPower solution id: 10

```
def iterPower(base, exp):
    result = 1
    for i in range(exp):
        result *= base
    return result
result=1
i=0
while i < exp:
    result *= base
    i += 1
return result
```

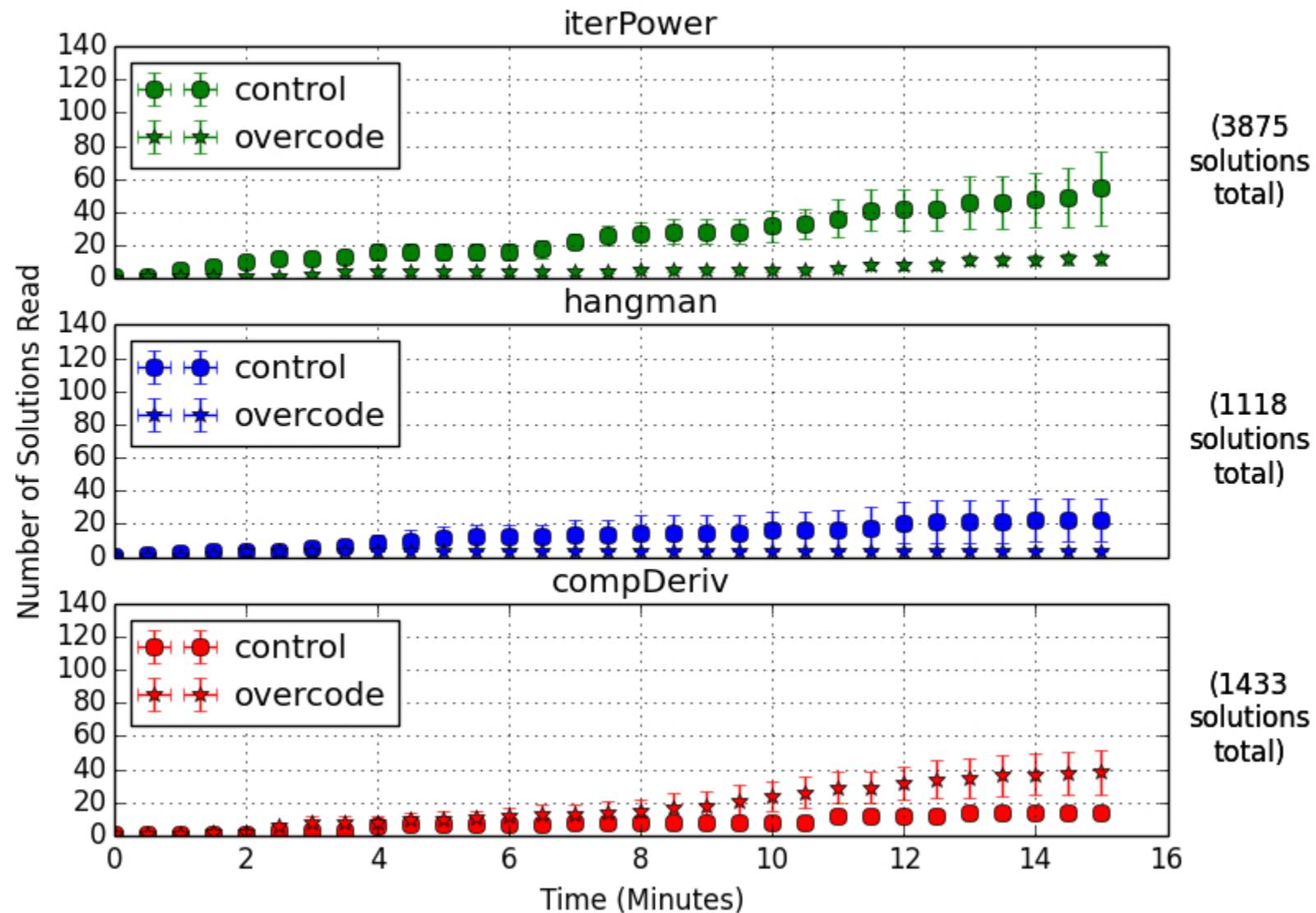
iterPower solution id: 10002

```
def iterPower(base, exp):
    if exp == 0:
        return 1.0
    b = exp
```

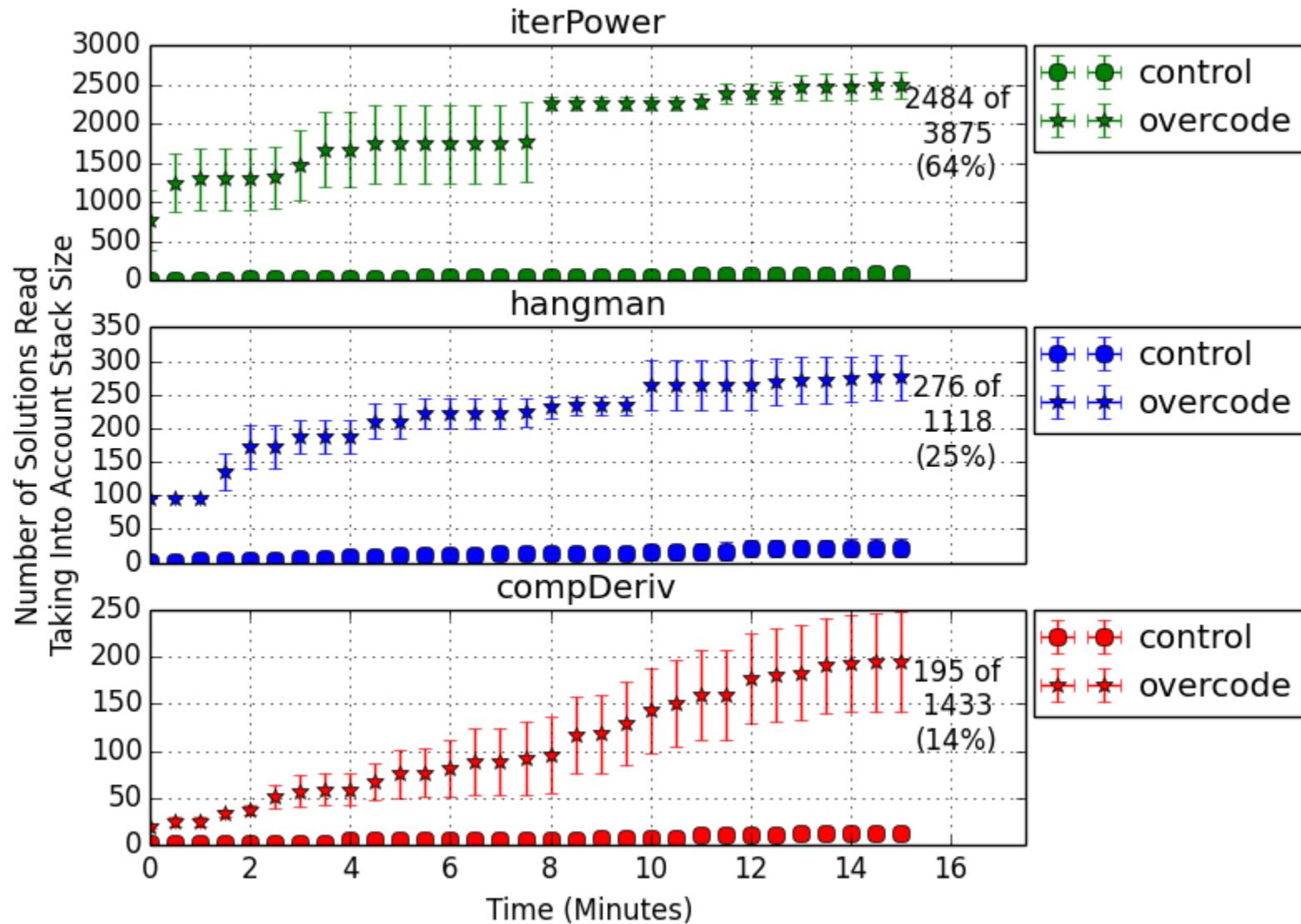
# OverCode



# SOLUTIONS READ

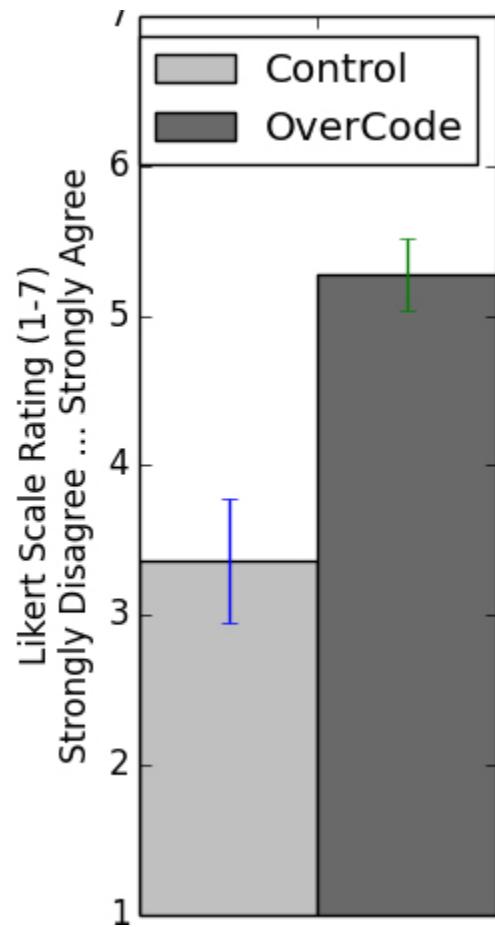


# SOLUTIONS READ



# PERCEIVED UNDERSTANDING

"The interface helped me develop a high-level view of students' understanding and misconceptions."



# WHAT VARIATION DID WE IGNORE?

## VARIABLE NAMING

Common Variable Name	Occur -rence Count	Sequence of Values	Original Variable Names
<b>iterPower</b>			
result	3081	[1,5,0,25,0,125,0]	result, wynik, out, total, ans, acum, num, mult, output, ...
exp	2744	[3,2,1,0]	exp, iterator, app, ii, num, iterations, times, ctr, b, ...
exp	749	[3]	exp, count, temp, exp3, exp2, exp1, inexp, old_exp, ...
i	266	[0,1,2]	i, a, count, c, b, iterValue, iter, n, y, inc, x, times, ...
<b>hangman</b>			
letter	817	['t','i','g','e','r']	letter, char, item, i, letS, ch, c, lett, ...
result	291	['_','_i','_i_','_i_e','_i_e_']	result, guessedWord, ans, str1, anss, guessed, string, ...
i	185	[0,1,2,3,4]	i, x, each, b, n, counter, idx, pos ...
found	76	[0,1,0,1,0]	found, n, letterGuessed, contains, k, checker, test, ...
<b>compDeriv</b>			
result	1186	[[[],[0.0],...,[0.0,35,0.9,0.4,0]]]	result, output, poly_deriv, res, deriv, resultPoly, ...
i	284	[-13.39,0.0,17.5,3.0,1.0]	i, each, a, elem, number, value, num, ...
i	261	[0,1,2,3,4,5]	i, power, index, cm, x, count, pwr, counter, ...
length	104	[5]	length, nmax, polyLen, lpoly, lenpoly, z, l, n, ...

# **EXPAND DIMENSION OF VARIATION**

## **VARIABLE NAMES**

```

def iterPower(base,exp):
    result=1
    while exp>0:
        result*=base
        exp-=1
    return result

```

1538 / 3853 solutions

tag	base	3846	tag	exp	2755	tag	result	3095
	base	3735		exp	2612		result	2495
	a	8	b		8		result	2495
	base	3735		exp	2612		ans	117
	base	3735		exp	2612		res	91
	base	3735		exp	2612		power	32
	base	3735		exp	2612		answer	31
	base	3735		exp	2612	x		28
	base	3735		exp	2612	r		21
	base	3735		exp	2612	a		20
	base	3735		exp	2612	value		17
	base	3735		exp	2612	total		17
	base	3735		exp	2612	resultado		13
	base	3735		exponente	1	resultado		13
	base	3735		exp	2612	ret		8
	base	3735		exp	2612	val		7
	base	3735		exp	2612	results		7
	base	3735		exp	2612	p		7
	base	3735		exp	2612	i		5
	base	3735		exp	2612	out		5

# **EXPAND DIMENSION OF VARIATION**

## **VARIABLE NAMES**

```

def iterPower(base,exp):
    result=1
    while exp>0:
        result*=base
        exp-=1
    return result

```

Synthesized  
representative  
solution

Common variables  
base, exp, and result

1538 / 3853 solutions

tag	base	3846	tag	exp	2755	tag	result	3095
base	3735			exp	2612		result	2495
a	8		b		8		result	2495
base	3735		exp	2612		ans	117	
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base	3735		exp	2612		a	20	
base	3735		exp	2612		value	17	
base	3735		exp	2612		total	17	
base	3735		exp	2612		resultado	13	
base	3735		exponente	1		resultado	13	
base	3735		exp	2612		ret	8	
base	3735		exp	2612		val	7	
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# EXPAND DIMENSION OF VARIATION

## VARIABLE NAMES

```
def iterPower(base,exp):
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    while exp>0:
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        exp-=1
    return result
```

1538 / 3853 solutions

Common variable result  
(1, 5, 25, 125)

tag	base	3846	tag	exp	2755	tag	result	3095
	base	3735		exp	2612		result	2495
	a	8	b	8			result	2495
	base	3735	exp	2612			ans	117
	base	3735	exp	2612			res	91
	base	3735	exp	2612			power	32
	base	3735	exp	2612			answer	31
	base	3735	exp	2612			x	28
	base	3735	exp	2612			r	21
	base	3735	exp	2612			a	20
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	base	3735	exp	2612			total	17
	base	3735	exp	2612			resultado	13
	base	3735	exponente	1			resultado	13
	base	3735	exp	2612			ret	8
	base	3735	exp	2612			val	7
	base	3735	exp	2612			results	7
	base	3735	exp	2612			p	7
	base	3735	exp	2612			i	5
	base	3735	exp	2612			out	5

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	base	3735	exp	2612		x	28	
	base	3735	exp	2612		r	21	
	base	3735	exp	2612		a	20	
	base	3735	exp	2612		value	17	
	base	3735	exp	2612		total	17	
	base	3735	exp	2612		resultado	13	
	base	3735	exponente	1		resultado	13	
	base	3735	exp	2612		ret	8	
	base	3735	exp	2612		val	7	
	base	3735	exp	2612		results	7	
	base	3735	exp	2612		p	7	
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## VARIABLE NAMES

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        exp-=1
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1538 / 3853 solutions

Common variable result  
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	base	3735	exp	2612		r	21	
	base	3735	exp	2612		a	20	
	base	3735	exp	2612		value	17	
	base	3735	exp	2612		total	17	
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	base	3735	exponente	1		resultado	13	
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	base	3735	exp	2612		value	17	
	base	3735	exp	2612		total	17	
	base	3735	exp	2612		resultado	13	
	base	3735	exponente	1		resultado	13	
	base	3735	exp	2612		ret	8	
	base	3735	exp	2612		val	7	
	base	3735	exp	2612		results	7	
	base	3735	exp	2612		p	7	
	base	3735	exp	2612		i	5	
	base	3735	exp	2612		out	5	

# FOOBАЗ

(We'll come back to this system soon, to answer R3.)

# **(R1) UNDERSTAND SOLUTION VARIATION**

- OverCode helps teachers
  - read more complicated solutions
  - "read" more solutions
  - Foobaz is an example of how to expand previously hidden dimensions of variation

# OUTLINE

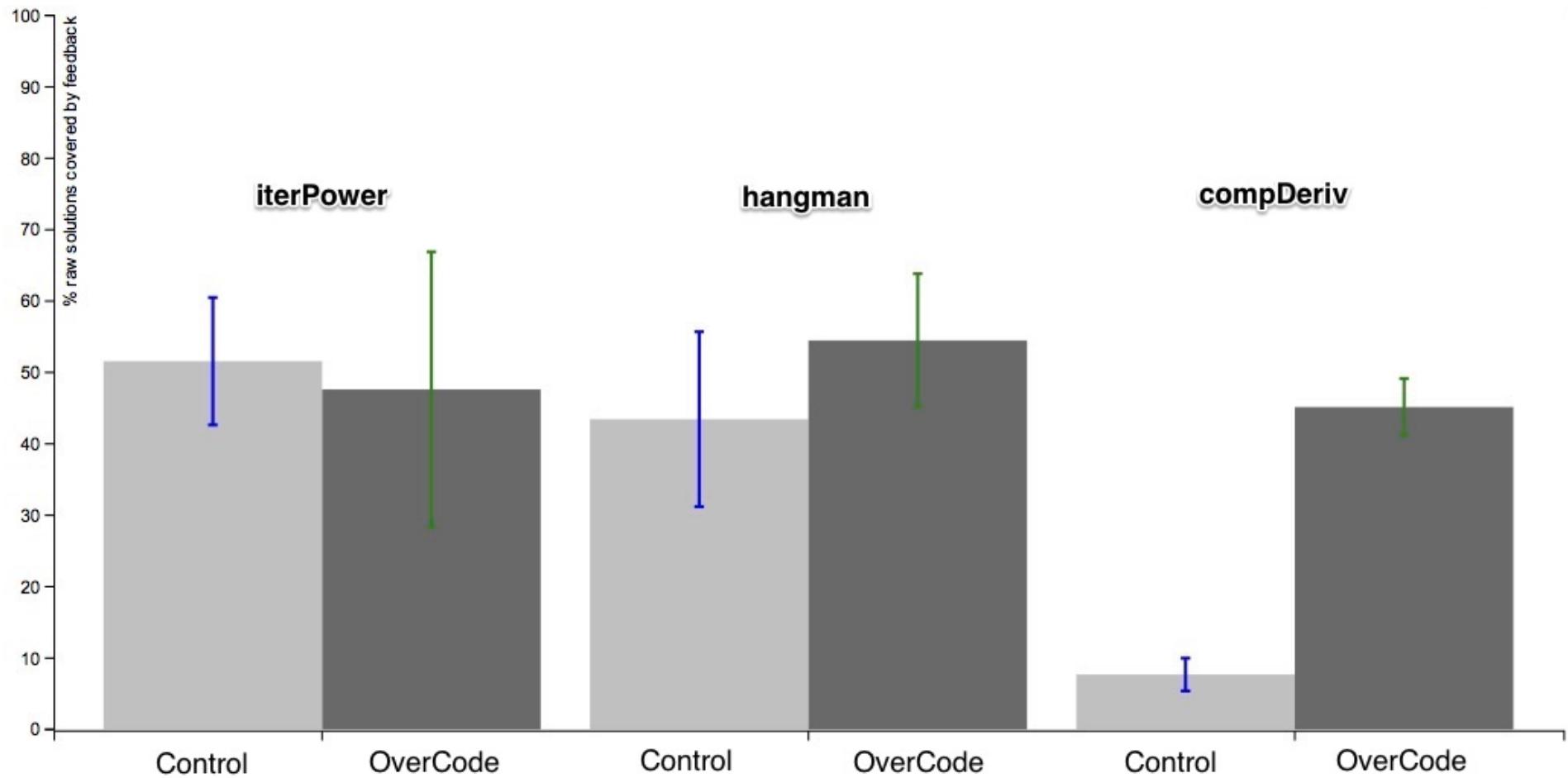
- Solution Variation (SV)
- Research Questions
  - (R1) understand SV
  - ⇒ (R2) feedback on **SV** at scale
  - (R3) personalized feedback on **SV** at scale
  - (R4) collect and distribute student advice, given **SV**
- Discussion

# FEEDBACK ON APPROACH & READABILITY

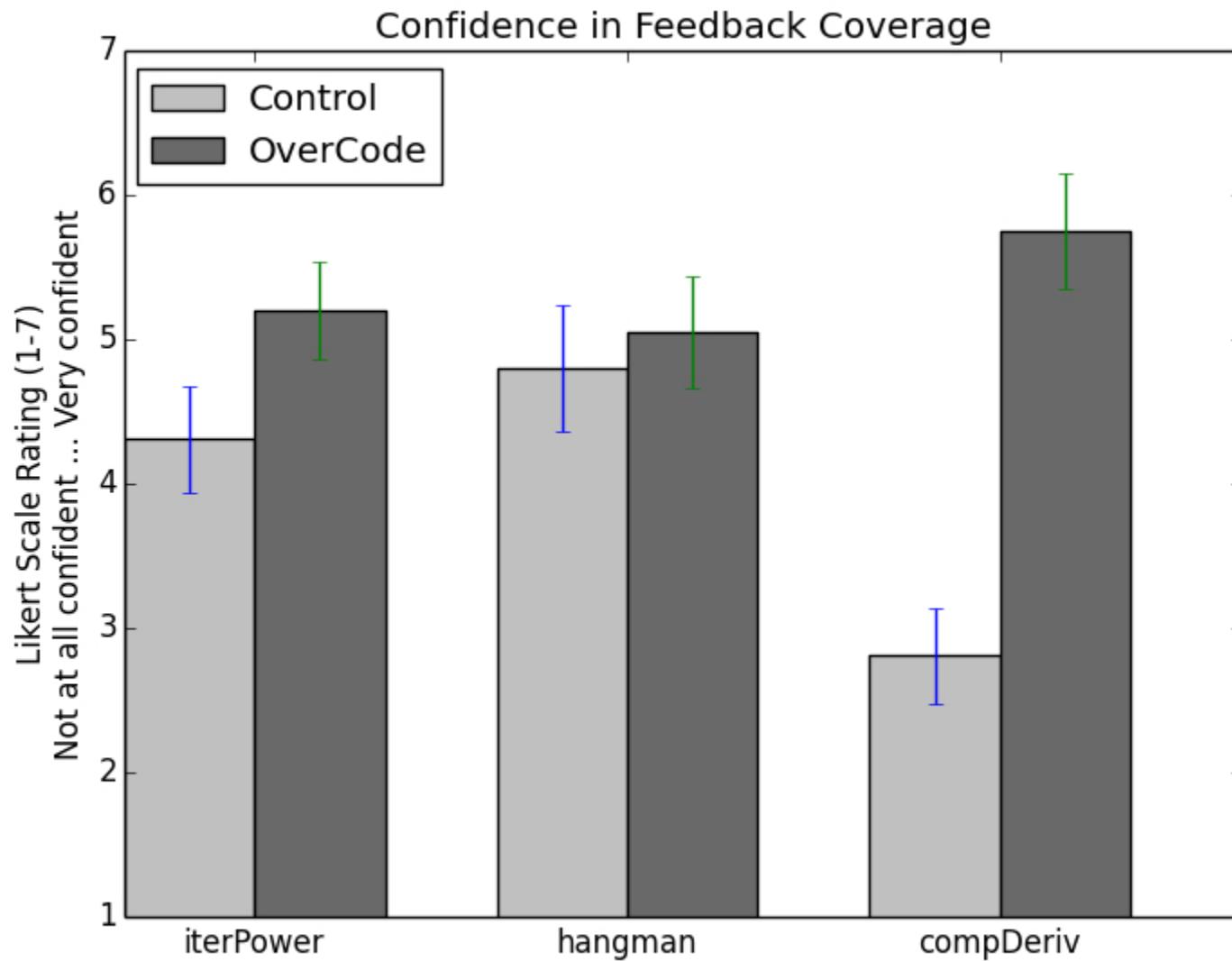
## AT SCALE

- Same subjects and task as before
- Hypotheses for OverCode condition:
  - More feedback coverage
  - More perceived coverage

# % OF RAW SOLUTIONS COVERED BY FEEDBACK



# PERCEIVED FEEDBACK COVERAGE



## **(R2) FEEDBACK ON SOLUTION VARIATION AT SCALE**

- OverCode helps teachers
  - write feedback that is relevant to more solutions

# OUTLINE

- Solution Variation (SV)
- Research Questions
  - (R1) understand SV
  - (R2) feedback on SV at scale
  - ⇒ (R3) personalized feedback on **SV** at scale
  - (R4) collect and distribute student advice, given **SV**
- Discussion

# WHY PERSONALIZE FEEDBACK?

- One-on-one tutoring is a gold standard (*Bloom '84*)
- Good tutors (*Lepper and Wolverton's INSPIRE model*)
  - Ask students to explain their thinking (*Chi '94*)
  - Progressively reveal content
    - Keep students with their zone of proximal development (*Lev Vygotsky*)

**PERSONALIZED FEEDBACK ON  
READABILITY  
VARIABLE NAMES**

**IN THE FORM OF PERSONALIZED ACTIVE LEARNING  
EXERCISES ("QUIZ") ON GOOD AND BAD NAMES**

# WHY VARIABLE NAMES?

- Most basic form of documentation
- Without modifying execution
  - express type and purpose of an object
  - suggest kinds of operators that manipulate it
- Some intro students mix themselves up through naming (Guttag)

```
for i in range(len(inputArray)):  
    a += myFunction(i)
```

i is OK (idiomatic)  
a is not OK (too short)

```
for i in inputArray:  
    result += i
```

i is not OK (misleading)  
result is OK

# QUOTE ABOUT VARIABLE NAMES

- Donald Knuth compares a good programmer to an essayist, who:

*“with thesaurus in hand, chooses the names of variables carefully and explains what each variable means”*

# HOW DO WE GIVE PERSONALIZED FEEDBACK ON VARIABLE NAMES AT SCALE?



# **PERSONALIZED FEEDBACK WORKFLOW**

1. Teacher annotates good and bad variable names in student code (using Foobaz interface)
2. Teacher curates quizzes based on these examples
3. Foobaz analyzes student solutions
4. Foobaz delivers personalized quizzes for each student solution

# PERSONALIZED FEEDBACK WORKFLOW

- (Step 1) Teacher annotates a few good and bad examples of variable names for several **common variables**

Common Variable Name	Occur -rence Count	Sequence of Values	Original Variable Names	fine	too short	misleading or vague
			iterPower			
result	3081	[1,5.0,25.0,125.0]	result, wynik, out, total, ans, acum, num, mult, output, ...			
exp	2744	[3,2,1,0]	exp, iterator, ip, ii, n, iterations, time, ctr, b, ...			
exp	749	[3]	exp, count, temp, exp3, exp, expl, inexp, old_exp, ...			
i	266	[0,1,2]	i, a, count, c, b, iterValue, iter, n, y, inc, x, times, ...			

# PERSONALIZED FEEDBACK WORKFLOW

Teacher Annotations

```
def iterPower(base,exp):
    result=1
    while exp>0:
        result*=base
        exp-=1
    return result
```

1538 / 3853 solutions

tag	base	3846	tag	exp	2755	tag	result	3095
Misleading or vague	base	3735	a	8	2612	Fine	result	2495
base	3735		b	exp	2612	Fine	result	2495
base	3735		exp		ans		117	
base	3735		exp		res		91	
base	3735		exp		power		32	
base	3735		exp		answer		31	
base	3735		exp		x		28	
base	3735		exp		r		21	
base	3735		exp	2612	Too Short	a	20	
base	3735		exp	2612		value	17	
base	3735		exp	2612		total	17	
base	3735		exp	2612		resultado	13	
base	3735		exponente	1		resultado	13	

# PERSONALIZED FEEDBACK WORKFLOW

- (Step 2) Teacher adds commentary, adds or removes choices

Example: quiz template for **common variable result**

Include in quiz?	Local Name	Misleading or vague	Too abrv	Fine	Comments
<input checked="" type="checkbox"/>	a	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="text"/>
<input checked="" type="checkbox"/>	number	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="text"/>
<input checked="" type="checkbox"/>	out	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="text"/>
<input checked="" type="checkbox"/>	result	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="text"/>
		<input type="text"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
					<input type="button" value="Add"/>

# PERSONALIZED FEEDBACK WORKFLOW

- Example student solution:

```
def iterPower(base,exp):  
    myAns=1  
    for j in range(exp):  
        myAns*=base  
    return myAns
```

- (Step 3) Foobaz identifies common variables
  - `myAns` is an instance of **common variable result**
  - `j` is an instance of **common variable i**

# PERSONALIZED FEEDBACK WORKFLOW

- (Step 4) Foobaz delivers personalized variable name quiz

You recently wrote the following solution, and we've replaced one variable's name with A:

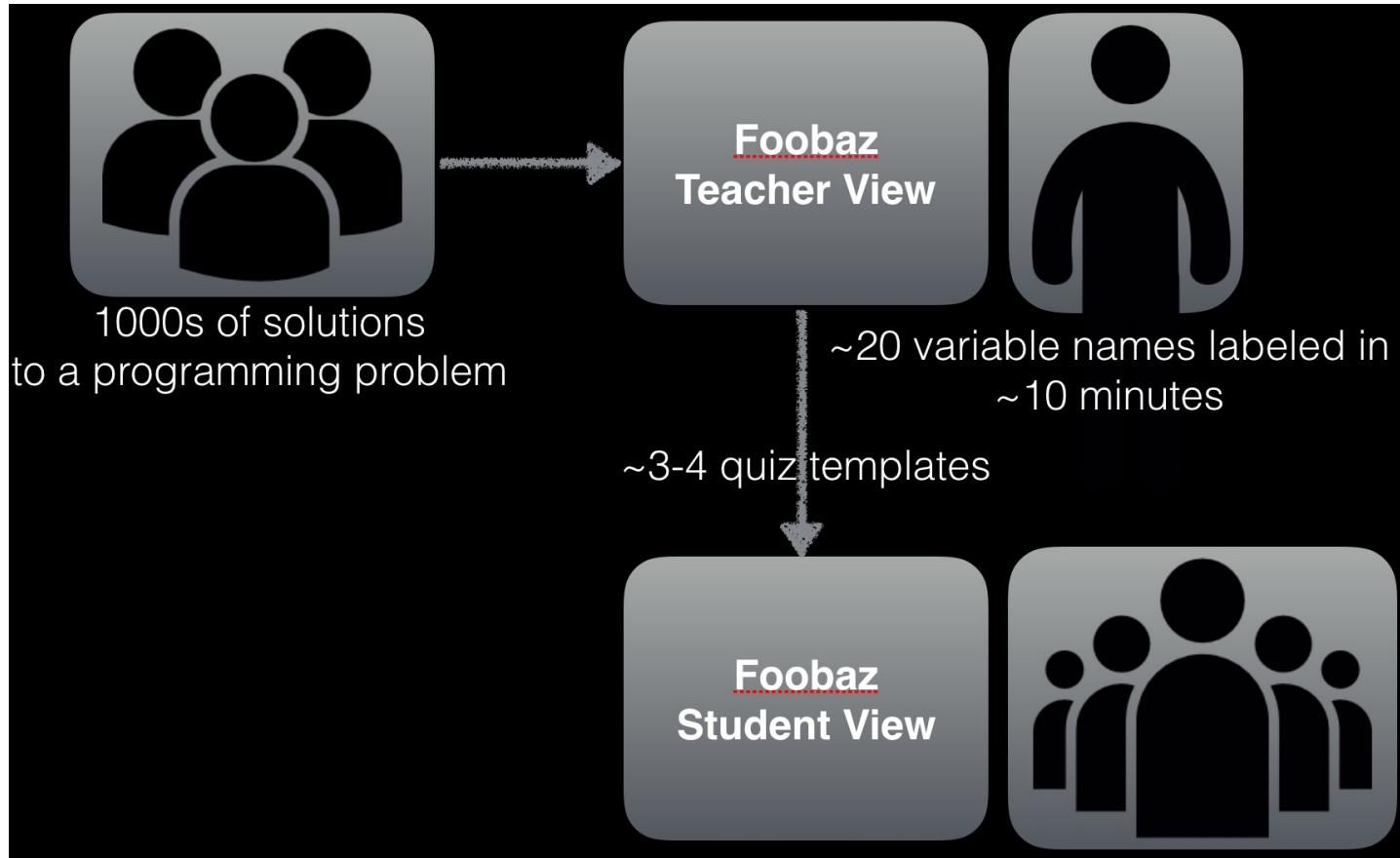
```
def iterPower(base,exp):  
    A=1  
    for j in range(exp):  
        A*=base  
    return A
```

Rate the quality of the following names for the bold symbol A:

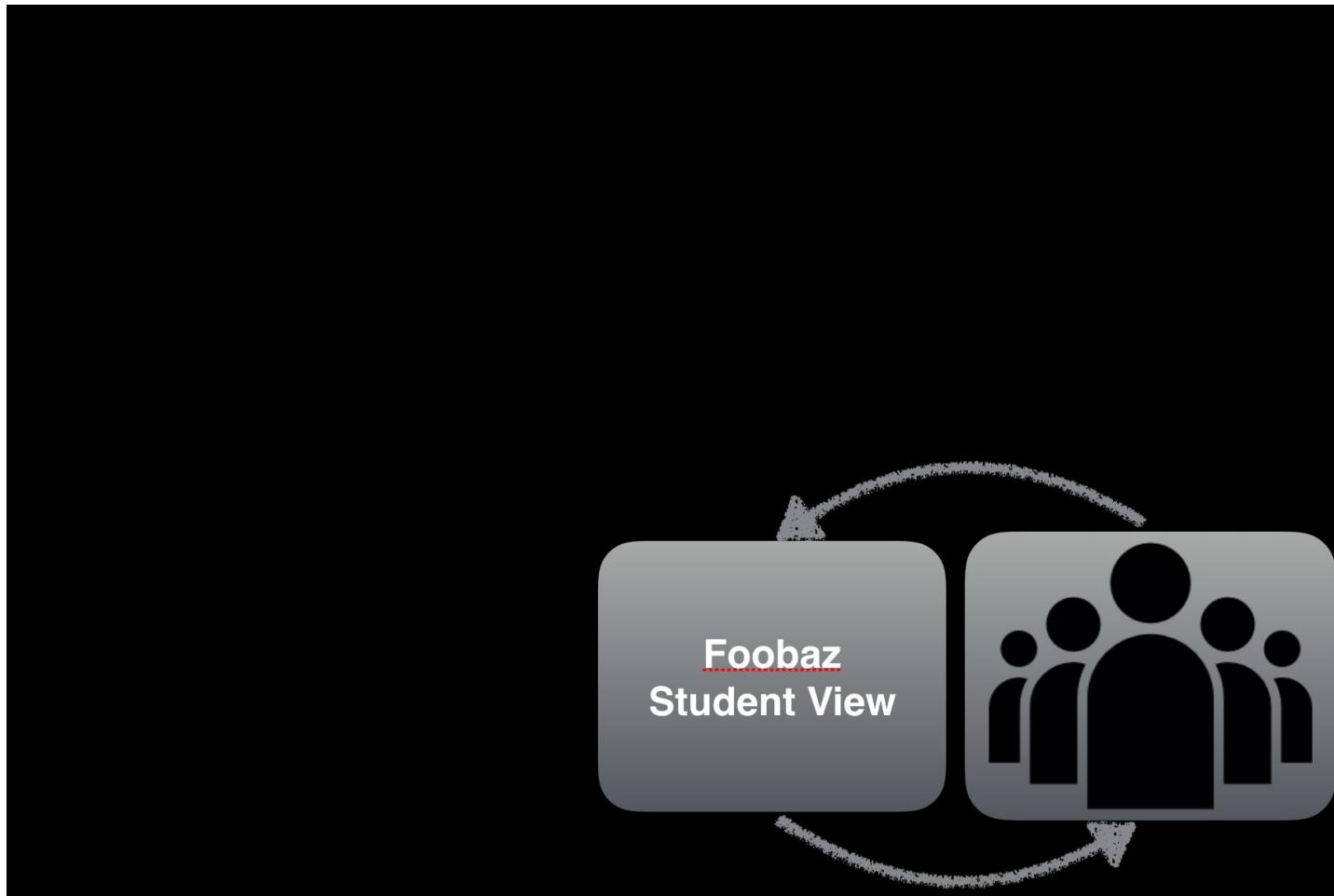
Name	Misleading or vague	Too abbrv	Fine
a	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
number	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
out	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
result	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>

**Compare to teacher**

# PERSONALIZED FEEDBACK WORKFLOW



# PERSONALIZED FEEDBACK WORKFLOW



# USER STUDY FOR TEACHERS

- Participants: 10 teachers
  - Python-course TAs/LAs/graders
  - (6 female, mean age: 23)
- Same datasets as before (`iterPower`, `hangman`, `derivative`)
- Task: Generate personalizable quizzes for as many students as possible

# USER STUDY FOR TEACHERS

## RESULTS

- In 4-11 minutes, each teacher
  - labeled an average of 21 out of 670-929 unique variable names
  - covered at least 75% of student solutions with at least one personalized variable name quiz

## **(R3) PERSONALIZED FEEDBACK ON SOLUTION VARIATION AT SCALE**

- Foobaz workflow helps teachers scale up one-on-one conversations about variable name choices
  - conversations → active learning exercises (quizzes)

# OUTLINE

- Solution Variation (SV)
- Research Questions
  - (R1) understand SV
  - (R2) feedback on SV at scale
  - (R3) personalized feedback on SV at scale
  - ⇒ (R4) collect and distribute student advice, given SV
- Discussion

# LEARNSOURCING PERSONALIZED HINTS

- **Problem:** it's hard to get personalized help in large classes
  - especially when there are many solutions (and bugs)
- **Key Insight:** Students who struggle, then succeed, become experts on particular solutions (and bugs)
- **Approach:** Collect and distribute hints by students who earned the expertise necessary to write them

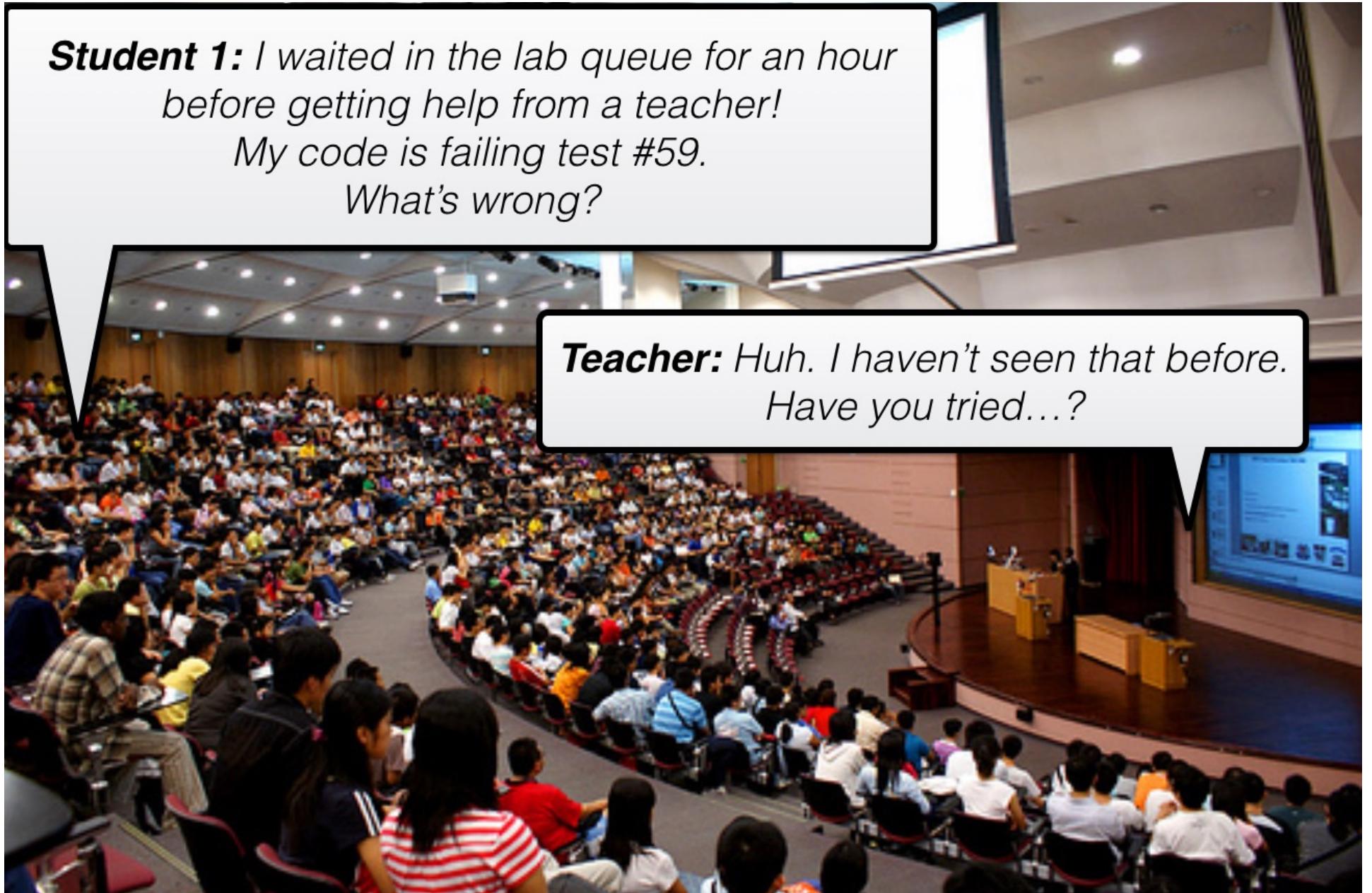
# LEARNSOURCING

- **Prior Art:** *Learnersourcing* puts learners to work while they learn (Kim '13)
- This is *targeted learnersourcing*: hint writers and receivers are not drawn from pool of all students

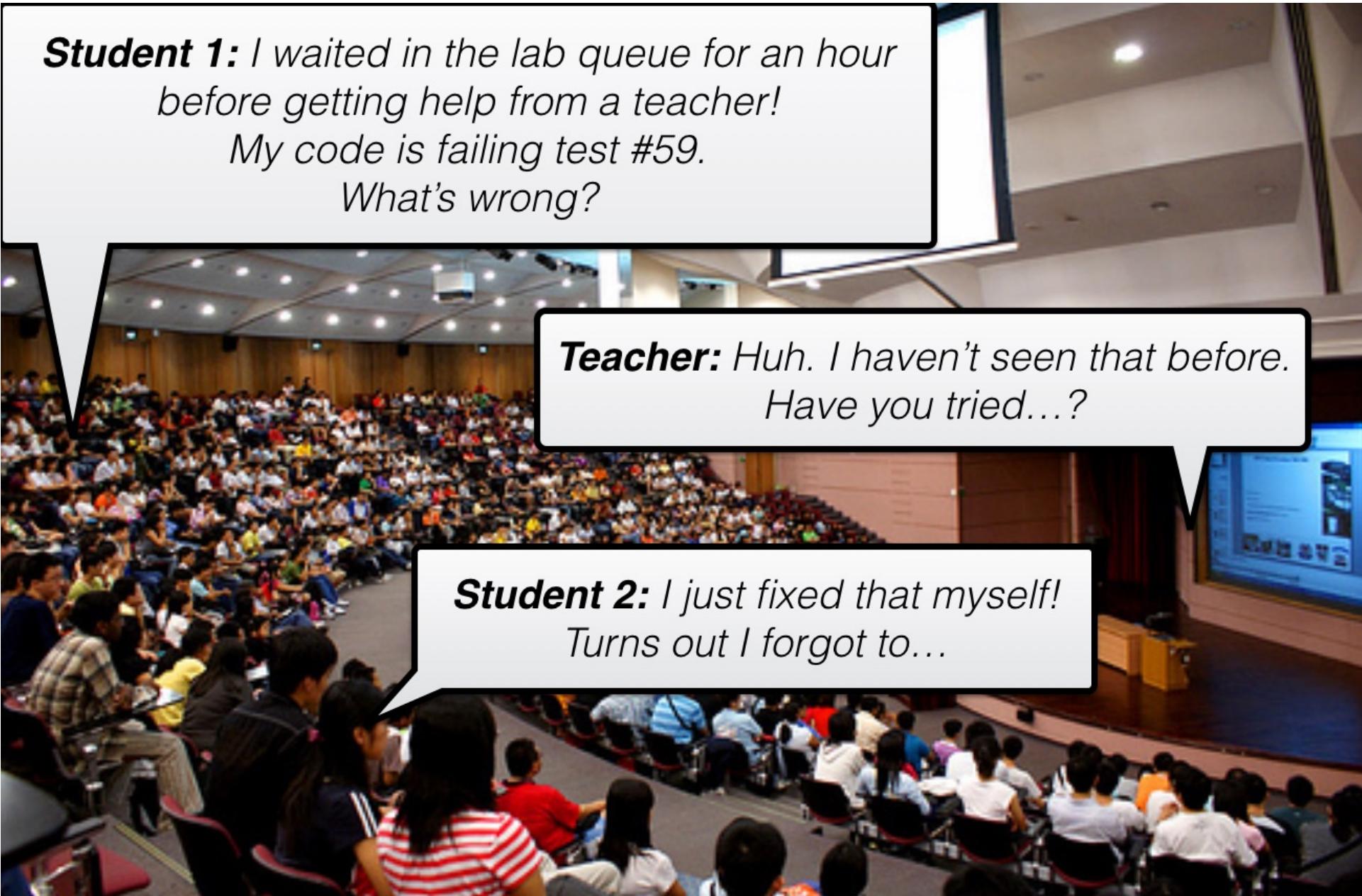
# DEBUGGING

**Student 1:** I waited in the lab queue for an hour before getting help from a teacher!  
My code is failing test #59.  
What's wrong?

**Teacher:** Huh. I haven't seen that before.  
Have you tried...?



# DEBUGGING



**Student 1:** I waited in the lab queue for an hour before getting help from a teacher!  
My code is failing test #59.  
What's wrong?

**Teacher:** Huh. I haven't seen that before.  
Have you tried...?

**Student 2:** I just fixed that myself!  
Turns out I forgot to...

# STUDENTS DON'T ALWAYS DESCRIBE THEIR PROBLEMS IN AN EASILY SEARCHABLE WAY

note ★

A note about using Piazza: search before you post

Hi everyone,

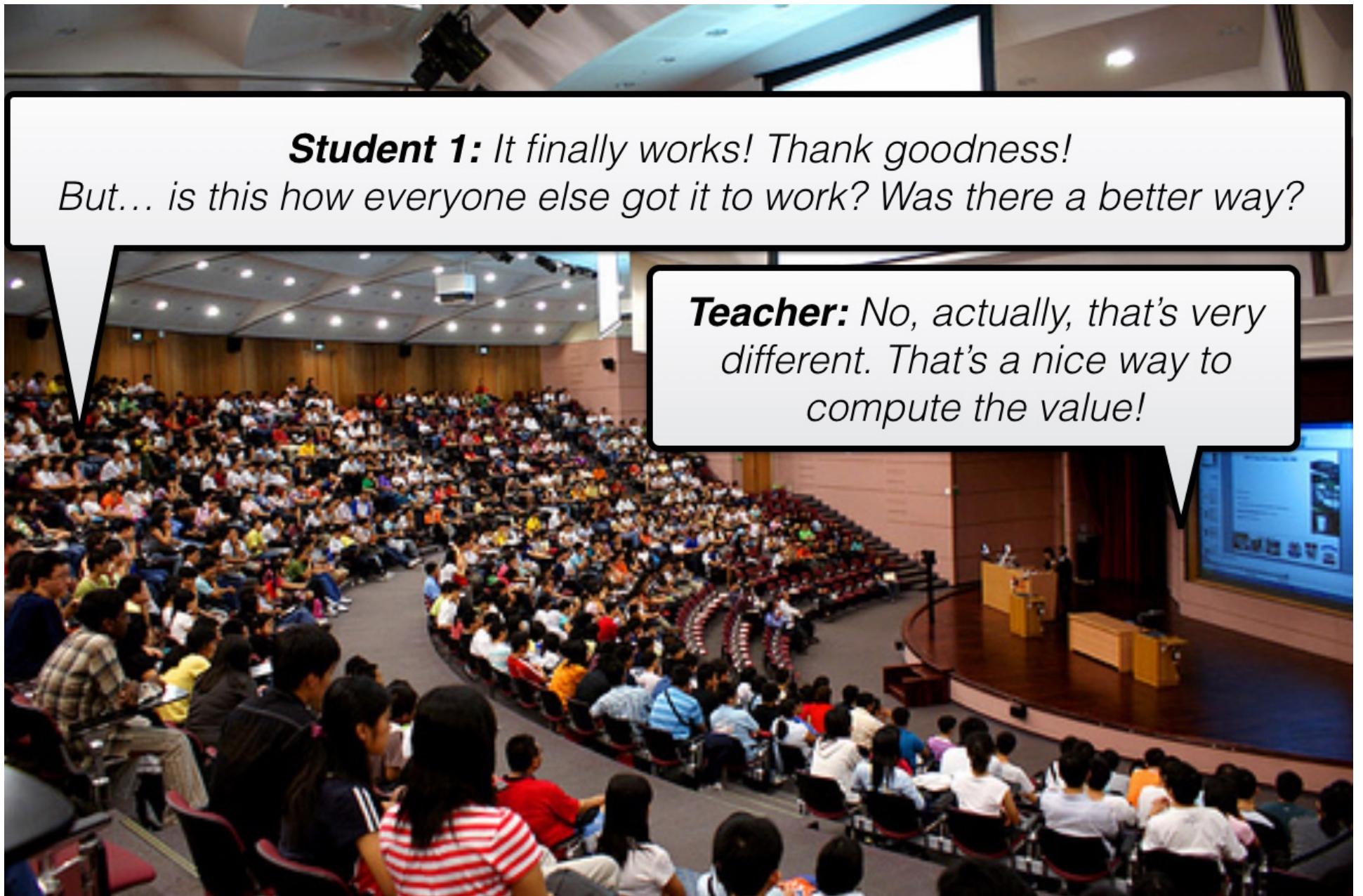
About half of the piazza posts are duplicates. **Please search before you post.**

Thanks!

logistics

edit · good note | 0

# RECOGNIZING GOOD SOLUTIONS

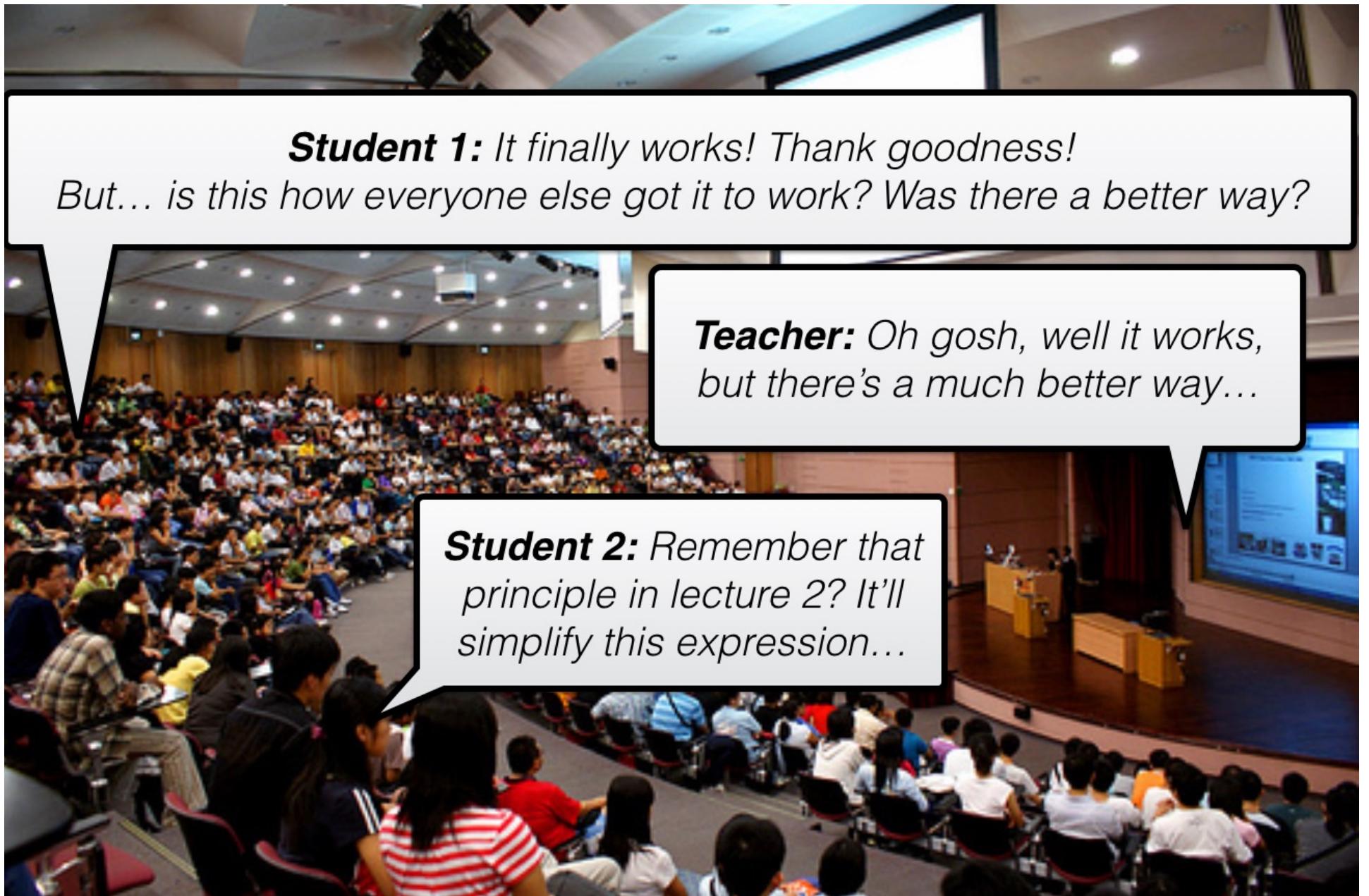


**Student 1:** *It finally works! Thank goodness!*

*But... is this how everyone else got it to work? Was there a better way?*

**Teacher:** *No, actually, that's very different. That's a nice way to compute the value!*

# IMPROVING SOLUTIONS



**Student 1:** It finally works! Thank goodness!

But... is this how everyone else got it to work? Was there a better way?

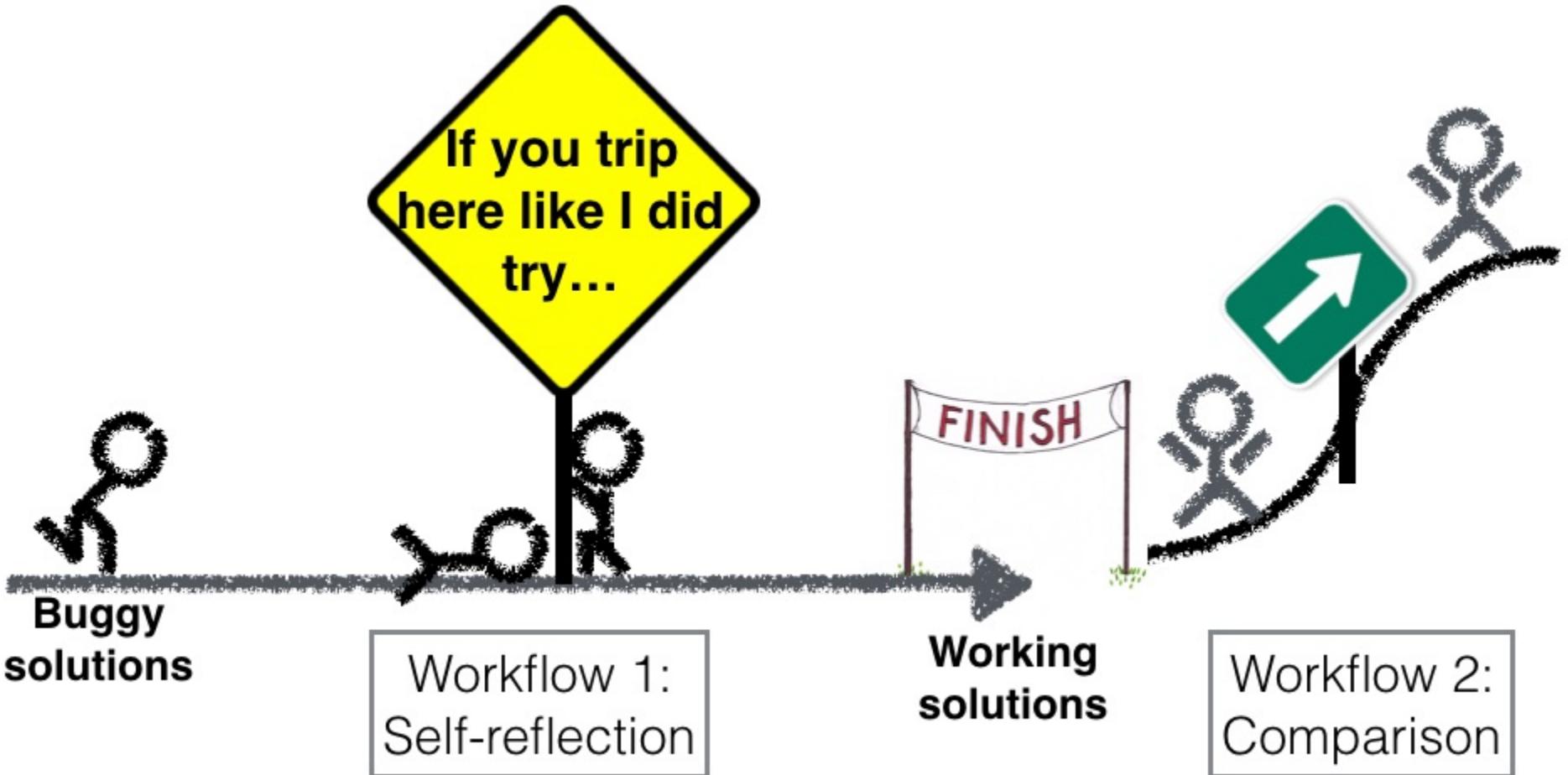
**Teacher:** Oh gosh, well it works, but there's a much better way...

**Student 2:** Remember that principle in lecture 2? It'll simplify this expression...

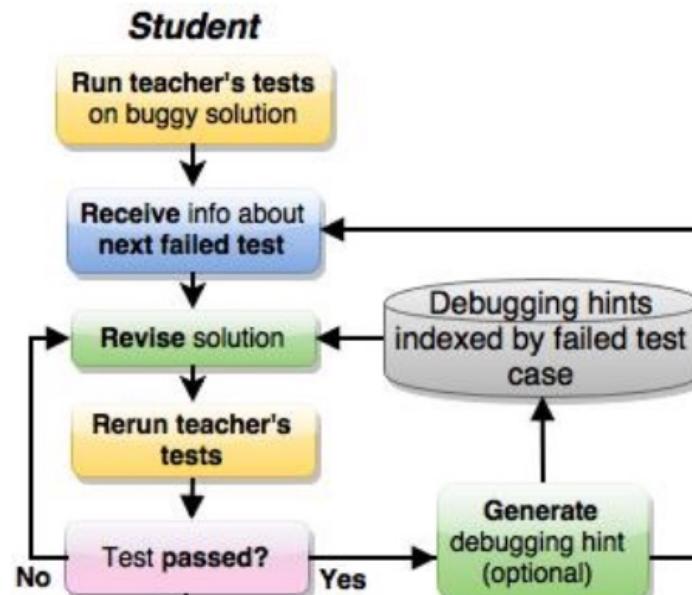
# INSIGHTS

- **Debugging:** Students who fix bug<sub>x</sub> can offer hints for students still stuck on bug<sub>x</sub>
- **Solution Improvement:** Students can
  - compare their solutions to other student solutions
  - write hints to help others improve their own solutions

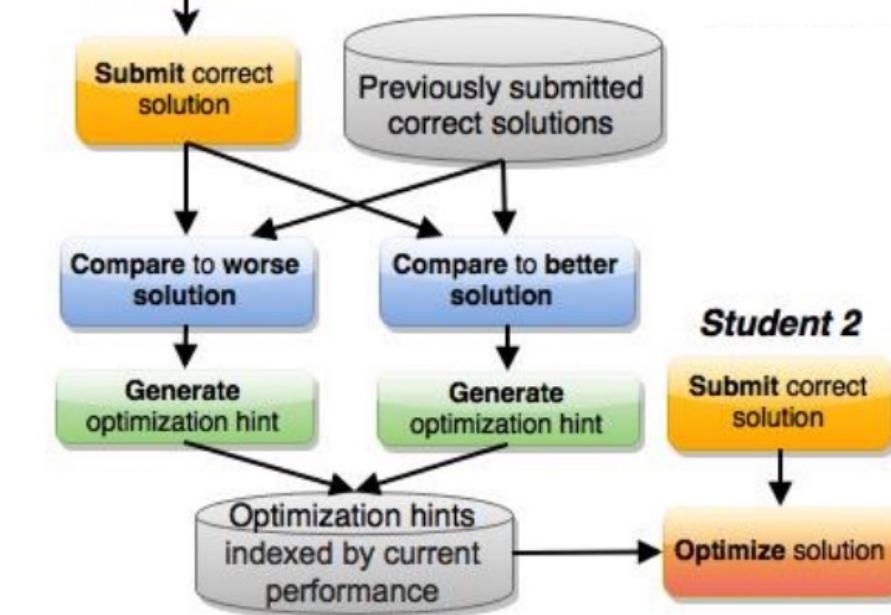
# CONTRIBUTION: TWO TARGETED LEARNERSOURCING WORKFLOWS



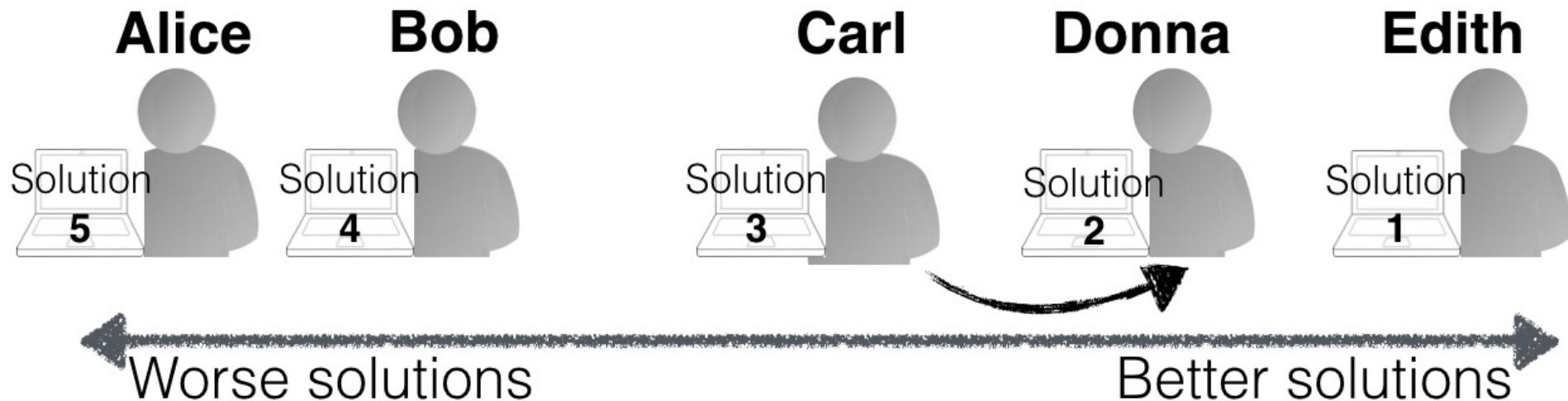
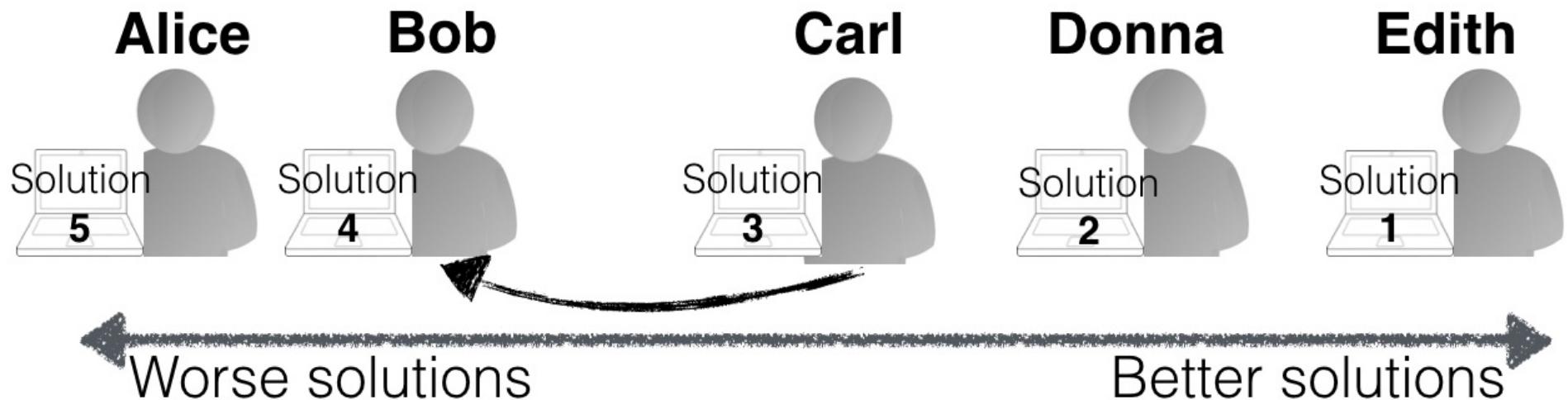
## Workflow 1: Self-reflection



## Workflow 2: Comparison



# COMPARISON WORKFLOW



# EVALUATION IN MIT HARDWARE DESIGN CLASS (>200 STUDENTS)

- Self-reflection workflow
  - deployed over multiple semesters
  - active engagement by students
  - most successful when endorsed by staff
- Comparison workflow
  - solution comparison & hint collection added to lab
  - gave student-written hints to 9 students in 1 hr lab study
  - hints helped students improve solutions

## **(R4) COLLECT AND DISTRIBUTE STUDENT ADVICE, GIVEN SOLUTION VARIATION**

- Demonstrated two targeted learnersourcing workflows that work when there are many different solutions (and bugs)
- Benefits:
  - Opportunities for student reflection & peer teaching
  - Awareness of alternative solutions
  - Reduced dependence on staff

# OUTLINE

- Solution Variation (SV)
- Research Questions
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- Discussion

# THESIS STATEMENT

- *Clustering and visualizing solution variation* collected from programming courses can help teachers
  - gain insights into student design choices
  - enhance test cases
  - give personalized style feedback at scale
  - collect and distribute student-written hints
- Thesis Contributions: systems and workflows that demonstrate these benefits

## RELATED WORK

- Mining patterns in code
  - Huang et al.'s "CodeWebs" @ Stanford (WWW '14)
  - Fast et al.'s "Codex" @ Stanford (CHI '14)
- Mining design choices
  - Kumar et al.'s "Webzeitgeist" (CHI '13)
- Mining variable names
  - Høst and Østvold's data-driven *Programmer English*
- Teacher-written style feedback
  - AutoStyle @ UC Berkeley (L@S '15, ITS '16)
- Prototype-based clustering of solutions
  - Gross et al. (DeLF1 '12)

# CLUSTERING REPRESENTATIVE SOLUTIONS

Interactive Bayesian Case Model Empowering Humans via Intuitive Interaction



# ACKNOWLEDGEMENTS

- MIT CSAIL
- UID group
- Massachusetts Wrestling Community
- Family & Friends

# SUMMARY

- *Clustering and visualizing solution variation* collected from programming courses can help teachers
  - gain insights into student design choices
  - enhance test cases
  - give personalized style feedback at scale
  - collect and distribute student-written hints

# OVERCODE

showing stacks      representing submissions

602 correct  
1026 total

3428 correct  
3852 total

filter      rewrite      legend

lines that appear in at least  submissions

largest stack (matching filters)

1538

```
def iterPower(base,exp):
    result=1
    while exp>0:
        result*=base
        exp-=1
    return result
```

remaining stacks (matching filters)

374

```
def iterPower(base,exp):
    result=1
    while exp>0:
        result=result*base
        exp-=1
    return result
```

153

```
def iterPower(base,exp):
    result=1
    while exp>0:
        result=result*base
        exp=exp-1
    return result
```

88

```
def iterPower(base,exp_2):
    result=1
    for i in range(exp_2):
        result*=base
    return result
```

55

```
def iterPower(base,exp_2):
    exp=exp_2
```

**2582** def iterPower(base,exp):  
**723** def iterPower(base,exp\_2):  
**334** def iterPower(base,exp\_3):  
**53** def iterPower(base,exp\_4):  
**53** elif exp\_3==1:  
**530** else:  
**2464** exp-=1  
**273** exp=exp-1  
**135** exp=exp\_2  
**362** exp\_3-=1  
**59** exp\_3=exp\_3-1  
**63** for i in range(0,exp\_2):  
**172** for i in range(exp\_2):  
**65** i\_2=0  
**187** if exp==0:  
**216** if exp\_2==0:  
**348** if exp\_3==0:  
**2065** result==base  
**2918** result=1  
**127** result=1.0  
**103** result=base  
**105** result=base\*result  
**949** result=result\*base  
**74** result\_2\*=base  
**167** result\_2=base  
**101** result\_2=result\_2\*base  
**53** result+=base

(<http://0.0.0.0:8000/?src=iterpower>)

# OVERCODE

showing stacks  
 1817 correct  
 3478 total  
 read

largest stack (matching filters)

```
22
def computeDeriv(poly):
    if len(poly)==1:
        return[0.0]
    result=[]
    for i in range(1,len(poly)):
        result.append(float(poly[i]*i))
    return result
```

filtering by

remaining stacks (matching filters)

```
21
def computeDeriv(poly):
    result=[]
    evaluatedTerm=0
    i2=0
    for i2 in range(len(poly)):
        evaluatedTerm=round(poly[i2]*i2,2)
        if i2>=1:
            result.append(evaluatedTerm)
    return result
```

```
14
def computeDeriv(poly):
    result=[]
    for i in range(1,len(poly)):
        result.append(float(poly[i]*i))
    return result
```

```
13
def computeDeriv(poly):
    result=[]
    i4=0
    for i3 in poly:
        if i4>0:
            result=result+[float(i3*i4)]
        i4+=1
    if len(result)==0:
        return[0.0]
```

filter

rewrite

legend

lines that appear in at least  submissions

```
3468 def computeDeriv(poly):
78 def computeDeriv(poly3):
81 deriv=0.0
1099 else:
108 evaluatedTerm=0
101 evaluatedTerm=0.0
73 evaluatedTerm=round(poly[i2]*i2,2)
558 for i in range(1,len(poly)):
153 for i2 in range(1,len(poly)):
548 for i2 in range(len(poly)):
453 for i3 in poly:
193 for i6 in poly[1:]:
83 for i7 in range(len(poly)-1):
160 i2+=1
381 i2=0
415 i4+=1
392 i4=0
96 i4=0.0
461 i5+=1
439 i5=1
80 if i2!=0:
118 if i2==0:
88 if i2>0:
219 if i2>=1:
90 if i4!=0:
120 if i4>0:
85 if len(poly)<2:
```

# OVERCODE

showing stacks      representing submissions

134 correct      189 correct  
181 total      236 total

filtering by

filter      rewrite      legend

lines that appear in at least  submissions

read

largest stack (matching filters)

37

```
def myLog(x,b):
    power=0
    while b**power<=x:
        power+=1
    return power-1
```

remaining stacks (matching filters)

6

```
def myLog(x,b):
    power_2=0
    while b**(power_2+1)<=x:
        power_2+=1
    return power_2
```

5

```
def myLog(x,b):
    i_3=1
    while b**i_3<=x:
        i_3+=1
    return i_3-1
```

3

```
def myLog(x,b):
    i=0
    while b**i<x:
        i+=1
    if b**i>x:
        return i-1
    else:
        return i
```

3

```
def myLog(x,b):
```

50 break  
231 def myLog(x,b):  
67 else:  
53 power+=1  
56 power=0  
55 return power-1

(<http://0.0.0.0:8000/?src=mylog>)

# OVERCODE

showing stacks      representing submissions

84 correct      160 correct  
115 total      191 total

filtering by

filter      rewrite      legend

lines that appear in at least  submissions

15

```
def give_and_take(d,L):
    new_dict={}
    for key in d:
        if key in L:
            new_dict[key]=d[key]+1
        else:
            new_dict[key]=d[key]-1
    return new_dict
```

remaining stacks (matching filters)

15

```
def give_and_take(d,L):
    d_copy=d.copy()
    for key in d_copy.keys():
        if key in L:
            d_copy[key]+=1
        else:
            d_copy[key]-=1
    return d_copy
```

12

```
def give_and_take(d,L):
    new_dict={}
    for key in d.keys():
        if key in L:
            new_dict[key]=d[key]+1
        else:
            new_dict[key]=d[key]-1
    return new_dict
```

11

```
def give_and_take(d,L):
    d_copy=d.copy()
    for key in d_copy:
        if key in L:
            d_copy[key]+=1
        else:
            d_copy[key]-=1
```

84    d\_copy=d.copy()  
74    d\_copy[key]+=1  
72    d\_copy[key]-=1  
168    def give\_and\_take(d,L):  
162    else:  
146    if key in L:  
50    new\_dict={}  
103    return d\_copy

(<http://0.0.0.0:8000/?src=giveandtake>)

# OVERCODE

showing stacks      representing submissions      filtering by

40 correct      178 correct  
48 total      186 total

read

largest stack (matching filters)

64

```
def power(base,exp):
    if exp==0:
        return 1
    else:
        return base*power(base,exp-1)
```

remaining stacks (matching filters)

35

```
def power(base,exp2):
    if exp2==0:
        return 1
    elif exp2==1:
        return base
    else:
        return base*power(base,exp2-1)
```

16

```
def power(base,exp):
    if exp==0:
        return 1
    return base*power(base,exp-1)
```

15

```
def power(base,exp2):
    if exp2==0:
        return 1
    if exp2==1:
        return base
    else:
        return base*power(base,exp2-1)
```

4

```
def power(base,exp2):
```

filter      rewrite      legend

lines that appear in at least 50 submissions

102      def power(base,exp):
65      def power(base,exp2):
148      else:
98      if exp==0:
61      if exp2==0:
174      return 1
69      return base
91      return base\*power(base,exp-1)
61      return base\*power(base,exp2-1)

([http://0.0.0.0:8000/?src=q4\\_power](http://0.0.0.0:8000/?src=q4_power))

# OVERCODE

showing stacks      representing submissions

47 correct  
121 total

96 correct  
170 total

filter      rewrite      legend

lines that appear in at least 22 submissions

largest stack (matching filters)

19

```
def deep_reverse(L):
    for i in L:
        i.reverse()
    L.reverse()
```

remaining stacks (matching filters)

15

```
def deep_reverse(L2):
    L2.reverse()
    for i3 in L2:
        i3.reverse()
```

6

```
def deep_reverse(L2):
    L2.reverse()
    for i2 in range(len(L2)):
        L2[i2].reverse()
```

5

```
def deep_reverse(L2):
    L2.reverse()
    for i3 in L2:
        i3.reverse()
    return L2
```

4

```
def deep_reverse(L):
    for i in L:
        i.reverse()
    L.reverse()
    return L
```

The screenshot displays the Overcode interface, which is a tool for visualizing and comparing different implementations of a function. It features a grid of code snippets and various filtering and search tools.

- Metrics:** "showing stacks", "47 correct", "121 total" (left), "representing submissions", "96 correct", "170 total" (top right).
- Filtering:** "filter", "rewrite", "legend".
- Search:** "lines that appear in at least 22 submissions".
- Snippets:** The interface shows six code snippets, each with a snippet ID (19, 15, 6, 5, 4) and a snippet content area. Snippet 19 contains the shortest implementation. Snippet 15 uses nested loops. Snippet 6 uses a range loop. Snippet 5 adds a return statement. Snippet 4 is identical to snippet 19.
- Code Content:** The code snippets use red for function names and black for variable names and operators. The snippets are:
  - def deep\_reverse(L):  
 for i in L:  
 i.reverse()  
 L.reverse()
  - def deep\_reverse(L2):  
 L2.reverse()  
 for i3 in L2:  
 i3.reverse()
  - def deep\_reverse(L2):  
 L2.reverse()  
 for i2 in range(len(L2)):  
 L2[i2].reverse()
  - def deep\_reverse(L2):  
 L2.reverse()  
 for i3 in L2:  
 i3.reverse()  
 return L2
  - def deep\_reverse(L):  
 for i in L:  
 i.reverse()  
 L.reverse()  
 return L
  - def deep\_reverse(L):  
 for i in L:  
 i.reverse()  
 L.reverse()

([http://0.0.0.0:8000/?src=q4\\_deep](http://0.0.0.0:8000/?src=q4_deep))