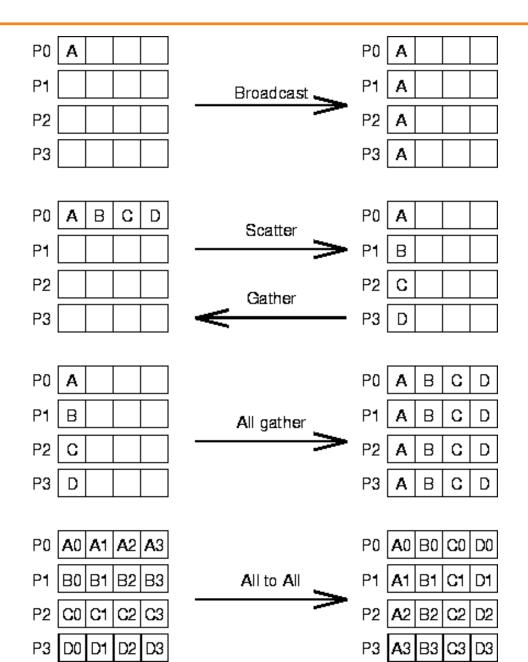
Introduction to High Performance Scientific Computing

Autumn, 2016

Lecture 16

Last time: MPI collective data movement

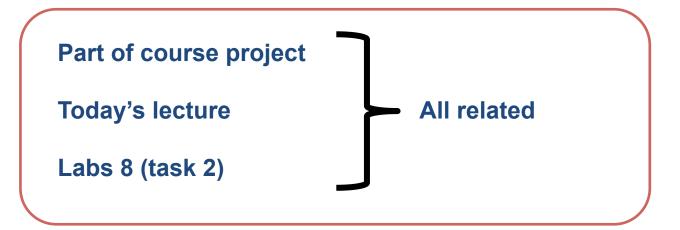


Today

- Coarse grain parallelization
- Send and Receive
- Domain Decomposition
- Using gather and gatherv

Today

- Coarse grain parallelization
- Send and Receive
- Domain Decomposition
- Using gather and gatherv



Coarse-grain vs fine-grain parallelism

- With OpenMP, we've used fine-grain approach
 - Look for a code segment (e.g. a loop) that can be parallelized
 - Let OpenMP do the rest (just for that segment)

Coarse-grain vs fine-grain parallelism

- With OpenMP, we've used fine-grain approach
 - Look for a code segment (e.g. a loop) that can be parallelized
 - Let OpenMP do the rest (just for that segment)
- With MPI, typically take a coarse-grain approach
 - At beginning of simulation, distribute data and tasks to processes
 - Each process works on its own problem
 - Occasionally communicating when necessary
- Can also use coarse-grain approach in OpenMP! (Project part 3.2)

We have already seen a "sort-of" coarse grain approach with quadrature:

```
!set number of intervals per processor
Nper_proc = (N + numprocs - 1)/numprocs
!starting and ending points for processor
   istart = myid * Nper_proc + 1
   iend = (myid+1) * Nper_proc
   if (iend>N) iend = N
```

We have already seen a "sort-of" coarse grain approach with quadrature:

```
!set number of intervals per processor
   Nper proc = (N + numprocs - 1)/numprocs
!starting and ending points for processor
    istart = myid * Nper proc + 1
    iend = (myid+1) * Nper proc
    if (iend>N) iend = N
!loop over intervals computing each interval's contribution to
integral
    do i1 = istart,iend
        xm = dx*(i1-0.5) !midpoint of interval i1
        call integrand(xm,f)
        sum i = dx*f
        sum_proc = sum_proc + sum_i !add contribution from interval
to total integral
   end do
```

- More generally, at start of program we will:
 - 1. Obtain myid and total number of processes, numprocs:

```
call MPI_COMM_RANK(MPI_COMM_WORLD, myid, ierr)
call MPI_COMM_SIZE(MPI_COMM_WORLD, numprocs, ierr)
```

2. Use this information to distribute *Ntotal* points (or pieces of data) across *numprocs* processors

- More generally, at start of program we will:
 - 1. Obtain myid and total number of processes, numprocs:

```
call MPI_COMM_RANK(MPI_COMM_WORLD, myid, ierr)
call MPI_COMM_SIZE(MPI_COMM_WORLD, numprocs, ierr)
```

- 2. Use this information to distribute *Ntotal* points (or pieces of data) across *numprocs* processors
- 3. We will use a simple fortran subroutine, *MPE_DECOMP1D*:

```
call MPE_DECOMP1D( Ntotal, numprocs, myid, istart, iend)
Nlocal = iend - istart + 1
```

- Simple subroutine which assigns istart and iend to each process
- If Ntotal=100, numprocs = 2:
 - $myid = 0 \rightarrow istart = 1, iend = 50$
 - $myid = 1 \rightarrow istart = 51, iend = 100$

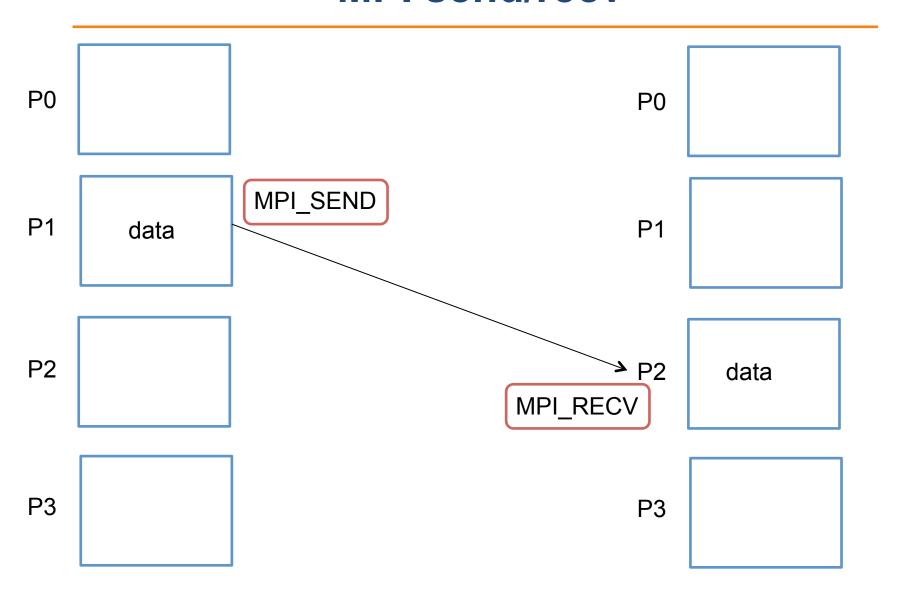
Complex parallelization

- MPE_DECOMP1D partitions data on a 'line'
- What about more complicated topologies or networks?
 - e.g. simulation of 1e7 air molecules?
 - Advanced tools exist to do the partitioning for you
 - E.g. ParMETIS:

ParMETIS is an MPI-based parallel library that implements a variety of algorithms for partitioning unstructured graphs, meshes, and for computing fill-reducing orderings of sparse matrices. ParMETIS extends the functionality provided by METIS and includes routines that are especially suited for parallel AMR computations and large scale numerical simulations. The algorithms implemented in ParMETIS are based on the parallel multilevel k-way graph-partitioning, adaptive repartitioning, and parallel multi-constrained partitioning schemes developed in our lab.

- Bcast and Reduce are examples of collective communication
- Point-to-point communication carried out by send and recv
- Probably the most basic and most important MPI commands

MPI send/recv



- Bcast and Reduce are examples of collective communication
- Point-to-point communication carried out by send and recv
- Probably the most basic and most important MPI commands

- Can send data between any two processors.
- Both send and recy are needed for data transfer.
- E.g. for previous figure need: if myid==1, send data to P2 and If myid==2 receive data from P1

These will send the integer n which has size 1 from processor 1 to processor 0.

```
If (myid==1) call MPI_SEND(n, 1, MPI_INTEGER,0, tag, MPI_COMM_WORLD,ierr)

If (myid==0) call MPI_RECV(n, 1, MPI_INTEGER,1,

tag, MPI_COMM_WORLD, status, ierr)
```

These will send the integer n which has size 1 from processor 1 to processor 0.

tag: an integer label which can contain information about the data (e.g. which molecule the data belongs to or which row in a matrix)

status: provides information about the received message (source, tag, length)

MPI Send/Recv: example

- **f90example2.f90: compute** array1 = sin(i1), i1=1,2,...
- New code: sendExample.f90
- Now, array1 is only computed on P0, and we want to send the 3rd component to P1 and store it in P1's (empty) array1

MPI Send/Recv: example

- **f90example2.f90: compute** array1 = sin(i1), i1=1,2,...
- New code: sendExample.f90
- Now, array1 is only computed on P0, and we want to send the 3rd component to P1 and store it in P1's (empty) array1
- Compute array1 on P0 and send it to P1:

MPI Send/Recv: example

```
Must also have MPI_RECV on P1:
```

Source

Notes:

- MPI_ANY_TAG: The destination will accept a message with any tag
- status(MPI_TAG) = 3; we have used the tag to send/set the array index

Comments on send/recv

- Send/Recv are blocking operations
 - Code waits at send until the data has been received.
 - But what if all processes are trying to send data to each other?
 - Can degrade performance or freeze the code

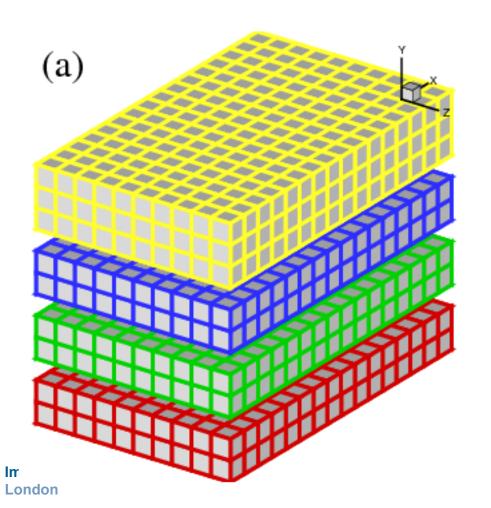
Comments on send/recv

- Send/Recv are blocking operations
 - Code waits at send until the data has been received
 - But what if all processes are trying to send data to each other?
 - Can degrade performance or freeze the code
- Solutions:
 - Combined send/recv: MPI_SENDRECV
 - Non-blocking send/recv: MPI_ISEND, MPI_IRECV
 - Usually used with MPI_WAIT or MPI_TEST
 - Buffered send: MPI_BSEND
 - Sender sends message and moves on
 - Message is stored in buffer until receiver is ready

Send/Recv and domain decomposition

A parallel computation computes a potential field, f(x,y,z,t) on four processors.

P0, P1, P2, P3 solve for f in separate subdomains



How would you compute the gradient?

$$\nabla f = \left(\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}\right)$$

Computation of derivative

Equispaced grid: $x = x_1, x_2, x_3, ...$

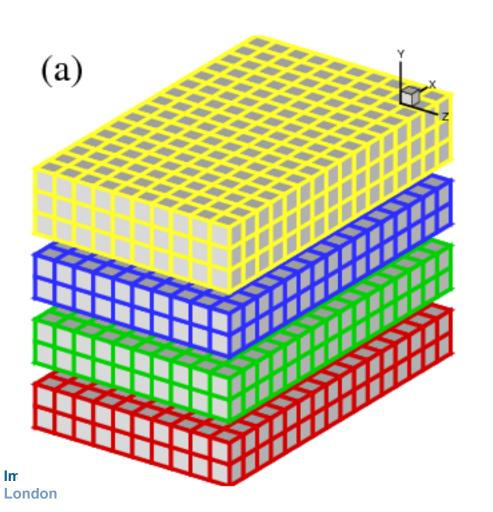
$$x_{i+1} - x_i = h = constant$$

Then,
$$\frac{df_i}{dx} pprox \frac{f_{i+1} - f_{i-1}}{2h}$$

Send/Recv and domain decomposition

A parallel computation computes a potential field, f(x,y,z,t) on four processors.

P0, P1, P2, P3 solve for f in separate subdomains



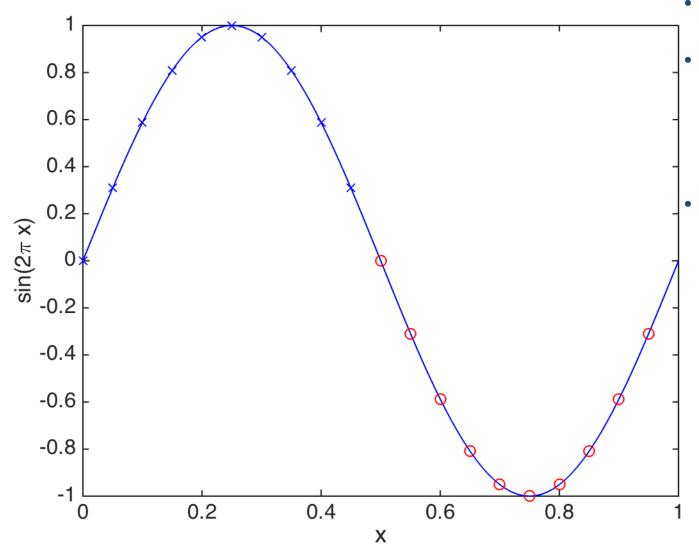
How would you compute the gradient?

$$\nabla f = \left(\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}\right)$$

- No problems with x and z directions
- But what about y?

Send/Recv and domain decomposition

Let's look at a simpler 1-D problem



10 points on P0, 10 points on P1 To compute df/dx for i=10 on P0, need to recv

f(i=11) from P1

- On P0, f will have 12 points:
 - The ten points shown
 - and 2 points received from each neighbor

 gradient_p.f90: compute df/dx given f=sin(2πx) distributed across processors

Code outline:

- 1. Initialize MPI
- 2. Read Ntotal from data.in
- 3. Construct domain decomposition assign Nlocal points from istart to iend to each processor.
- 4. Make grid and field, f=sin(2*pi*x), in the local subdomain
- 5. Compute derivative
- 6. Output error

Key parts:

Domain decomposition (subroutine from MPE library)

```
!construct decomposition
    call MPE_DECOMP1D( Ntotal, numprocs, myid, istart, iend)
    Nlocal = iend - istart + 1
```

Key parts:

 Domain decomposition (subroutine from MPE library) !construct decomposition call MPE_DECOMP1D(Ntotal, numprocs, myid, istart, iend) Nlocal = iend - istart + 1 Make local grid and field !make grid and field call make_grid(Ntotal,Nlocal,istart,iend,x) dx = x(2) - x(1)print *, 'proc', myid, ' has been assigned the interval x=', x(1), x(Nlocal)call make_field(Nlocal,x,f(2:Nlocal+1)) !note: f(1) and f(Nlocal+2) must be obtained from neighboring processors

Key parts:

Domain decomposition (subroutine from MPE library)

```
!construct decomposition
    call MPE_DECOMP1D( Ntotal, numprocs, myid, istart, iend)
    Nlocal = iend - istart + 1
```

Make local grid and field

```
!make grid and field
    call make_grid(Ntotal,Nlocal,istart,iend,x)
    dx = x(2)-x(1)
    print *, 'proc', myid, ' has been assigned the interval x=',
x(1),x(Nlocal)
```

```
call make_field(Nlocal,x,f(2:Nlocal+1)) !note: f(1) and f(Nlocal+2) must be obtained from neighboring processors
```

Compute derivative (with send/recv at subdomain boundaries)...

```
!Send data at top boundary up to next processor
!i.e. send f(nlocal+1) to myid+1 and store it there as f(1)
!data from myid=numprocs-1 is sent to myid=0
    if (myid<numprocs-1) then</pre>
        receiver = myid+1
   else
         receiver = 0
   end if
    if (myid>0) then
        sender = myid-1
   else
        sender = numprocs-1
   end if
   call MPI_SEND(f(Nlocal+1),1,MPI_DOUBLE_PRECISION, receiver,0,
                                             MPI_COMM_WORLD,ierr)
   call MPI_RECV(f(1) 1,MPI_DOUBLE_PRECISION, sender, MPI_ANY_TAG,
                                      MPI COMM WORLD, status, ierr)
```

```
!Send data at top boundary up to next processor
!i.e. send f(nlocal+1) to myid+1 and store it there as f(1)
!data from myid=numprocs-1 is sent to myid=0
    if (myid<numprocs-1) then</pre>
        receiver = myid+1
   else
         receiver = 0
   end if
    if (myid>0) then
        sender = myid-1
   else
        sender = numprocs-1
   end if
   call MPI_SEND(f(Nlocal+1),1,MPI_DOUBLE_PRECISION, receiver,0,
                                             MPI_COMM_WORLD,ierr)
   call MPI_RECV(f(1) 1,MPI_DOUBLE_PRECISION, sender, MPI_ANY_TAG,
                                      MPI COMM WORLD, status, ierr)
```

- At end of computation, each process has it's own part of df/dx
- It is sometimes useful to *gather* the data onto one process (e.g. for writing data to a file)
- Easy to do if gathering ten numbers from ten processors and storing them in an array

- At end of computation, each process has it's own part of df/dx
- It is sometimes useful to *gather* the data onto one process (e.g. for writing data to a file)
- Easy to do if gathering ten numbers from ten processors and storing them in an array

Nlocal (size 1, type int) is sent into Nper_proc (rank 1 array, type int) on
 myid = 0

- At end of computation, each process has it's own part of df/dx
- It is sometimes useful to *gather* the data onto one process (e.g. for writing data to a file)
- Easy to do if gathering ten numbers from ten processors and storing them in an array

- Nlocal (size 1, type int) is sent into Nper_proc (rank 1 array, type int) on
 myid = 0
- Trickier to do when gathering arrays into larger array. Then need array
 of locations where to place sub-arrays
 - e.g., disps = [1, 1+Nper_proc(1), 1+Nper_proc(1)+Nper_proc(2), ...]

- Trickier to do when gathering arrays into larger array. Then need array
 of locations where to place sub-arrays
 - e.g., disps = [1, 1+Nper_proc(1), 1+Nper_proc(1)+Nper_proc(2), ...]
 - Then use mpi_gatherv with disps as input:

 df (size Nlocal) is gathered from each processor and stored in df_total (in locations determined from Nper_proc and disps)

Notes on method of lines

Lecture 14: Solving N ODEs:

$$\frac{dT_i}{dt} = S_i(t) + \frac{T_{i+1} - 2T_i + T_{i-1}}{\Delta x^2}, \ i = 1, 2, ..., N$$

- Can solve ODEs with odeint which adjusts the time step error criteria are satisfied
- Can also use time-step methods (see lab 8)
- Simplest is explicit Euler:

$$\frac{dT_i}{dt} \approx \frac{T_i(t + \Delta t) - T_i(t)}{\Delta t}$$
$$T_i(t + \Delta t) = T_i(t) + \Delta t \left[S_i(t) + \frac{T_{i+1} - 2T_i + T_{i-1}}{\Delta x^2} \right], i = 1, 2, ..., N$$

Notes on method of lines

Simplest is explicit Euler:

$$\frac{dT_i}{dt} \approx \frac{T_i(t + \Delta t) - T_i(t)}{\Delta t}$$

$$T_i(t + \Delta t) = T_i(t) + \Delta t \left[S_i(t) + \frac{T_{i+1} - 2T_i + T_{i-1}}{\Delta x^2} \right], i = 1, 2, ..., N$$

error ~ dt, very poor stability propertis → requires very small time step

- Fourth-order Runge-Kutta (RK4) is a much better fixed-time step method
- In course project, you are provide with routines for both methods
 - Will have to modify euler
 - But will only have to provide appropriate RHS for RK4 (as RHS was provided for odeint)

1. Lazy approach:

```
$ time mpiexec -n 2 midpointpt
real  0m0.073s
user  0m0.081s
sys 0m0.030s
```

1. Lazy approach:

```
$ time mpiexec -n 2 midpointpt
real  0m0.073s
user  0m0.081s
sys 0m0.030s
```

2. Use MPI_WTIME to time particular parts of code:

```
starttime = MPI_WTIME() !***START TIMER***
    !code...
!
endtime = MPI_WTIME() !***STOP TIMER***
print *, 'time= ',endtime - starttime, 'seconds'
```

1. Lazy approach:

```
$ time mpiexec -n 2 midpointpt
real  0m0.073s
user  0m0.081s
sys 0m0.030s
```

2. Use MPI_WTIME to time particular parts of code:

```
starttime = MPI_WTIME() !***START TIMER***
    !code...
!
endtime = MPI_WTIME() !***STOP TIMER***
print *, 'time= ',endtime - starttime, 'seconds'
```

3. But to get detailed information, use a profiler: VampirTrace, IPM, ...

From IPM webpage (http://ipm-hpc.sourceforge.net/):

