

Introduction to High Performance Scientific Computing

Autumn, 2016

Lecture 5

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24 October, 2016

Basic data input/output

To open a file for reading or writing:

```
outfile = open("output.txt","w") #open file with flag "w" for writing
infile = open("input.txt","r") #open file with flag "r" for reading
```

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Basic data input/output: write to file

Write two numbers to file, *output.txt*:

```
outfile = open("output.txt","w") #open file with flag "w" for writing
outfile.write("This is a header for output.txt \n \n") #header
```

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Basic data input/output: write to file

Write two numbers to file, *output.txt*:

```
outfile = open("output.txt","w") #open file with flag "w" for writing
outfile.write("This is a header for output.txt \n \n") #header
x = 2.0 #some data to be written
y = 1.0
outfile.write("x = %6.3f, y = %6.3f \n" %(x,y)) #write data
outfile.close() #close file
```

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Basic data input/output: write to file

Write two numbers to file, *output.txt*:

```
outfile = open("output.txt","w") #open file with flag "w" for writing
outfile.write("This is a header for output.txt \n \n") #header
x = 2.0 #some data to be written
y = 1.0
outfile.write("x = %6.3f, y = %6.3f \n" %(x,y)) #write data
outfile.close() #close file
```

If we run this code and look at *output.txt*:

```
$ cat output.txt
This is a header for output.txt
x = 2.000, y = 1.000
```

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Basic data input/output: read from file

Read from file, *input.txt*, separate out numbers

```
infile = open("input.txt","r") #open file with flag "r" for reading
temp = infile.readline() #first read header
temp = infile.readline()
#loop through lines in file
for line in infile:
    print line
```

Output:

```
x = 2.000, y = 1.000
x = 3.000, y = 10.000
x = 4.000, y = 100.000
x = 5.000, y = 1000.000
```

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Basic data input/output: read from file

Read from file, *input.txt*, separate out numbers

```
infile = open("input.txt","r") #open file with flag "r" for reading
temp = infile.readline() #first read header
temp = infile.readline()

#loop through lines in file
for line in infile:
    print line

words = line.split() #separate last line into words
print "words=",words

Output: words= ['x', '=', '5.000,', 'y', '=', '1000.000']
```

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Basic data input/output: read from file

Use *line.split* to break line into words

```
infile = open("input.txt","r") #open file with flag "r" for reading
temp = infile.readline() #first read header
temp = infile.readline()

#loop through lines in file
for line in infile:
    print line

words = line.split() #separate last line into words
print "words=",words

Output: words= ['x', '=', '5.000,', 'y', '=', '1000.000']
```

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Basic data input/output: read from file

And then the last word is y

```
infile = open("input.txt","r") #open file with flag "r" for reading
temp = infile.readline() #first read header
temp = infile.readline()

#loop through lines in file
for line in infile:
    print line

words = line.split() #separate last line into words
print "words=",words

y = float(words[-1]) #pick out y, convert from string to float
print "y=",y

Output: y= 1000.0
```

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Numpy: scientific computing with Python

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Numpy overview

- *Numpy* is an add-on package which introduces arrays into Python
- It has to be imported into codes, usually:
`import numpy as np`

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Numpy overview

- *Numpy* is an add-on package which introduces arrays into Python
- It has to be imported into codes, usually:
`import numpy as np`
- *Numpy* provides Matlab-like linear algebra capabilities
- With *matplotlib*, *numpy* provides Matlab-like visualization
- With *scipy*, *numpy* provides tools for differential equations, optimization, and much more...

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Building arrays

Three methods:

1. **Make a list:**

```
In [112]: x = np.array([3., 5, 7, 9, 11, 13])
In [113]: print x
[ 3.  5.  7.  9. 11. 13.]
In [114]: type(x)
Out[114]: numpy.ndarray
```

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Building arrays

Three methods:

1. **Make a list:**

```
In [112]: x = np.array([3., 5, 7, 9, 11, 13])
In [113]: print x
[ 3.  5.  7.  9. 11. 13.]
In [114]: type(x)
Out[114]: numpy.ndarray
```

2. **Use np.linspace(start, stop, N) -- same as matlab:**

```
In [115]: y=np.linspace(3,13,6)
In [116]: print y
[ 3.  5.  7.  9. 11. 13.]
```

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Building arrays

Three methods:

1. **Make a list:**

```
In [112]: x = np.array([3., 5, 7, 9, 11, 13])
In [113]: print x
[ 3.  5.  7.  9. 11. 13.]
In [114]: type(x)
Out[114]: numpy.ndarray
```

2. **Use np.linspace(start, stop, N) -- same as matlab:**

```
In [115]: y=np.linspace(3,13,6)
In [116]: print y
[ 3.  5.  7.  9. 11. 13.]
```

3. **Use np.arange(start, stop, step) -- same as range, generates array instead of a list; does not include "stop" value:**

```
In [121]: z=np.arange(3,14,2)
```

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```
In [122]: print z
[ 3  5  7  9 11 13]
```

Math with arrays

- Math works basically as you would expect. A few examples:

```
In [128]: print x
[ 3.  5.  7.  9. 11. 13.]

In [129]: y=x+3

In [130]: print y
[ 6.  8. 10. 12. 14. 16.]

In [131]: print x**3
[ 9. 15. 21. 27. 33. 39.]

In [132]: print x**2
[ 9. 25. 49. 81. 121. 169.]

In [133]: print sin(x)
[ 0.14112001 -0.95892427  0.6569866  0.41211849 -0.99999021  0.42016704]
```

(What would happen if x was a list?)

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Math with arrays

- But be careful when making a copy:

```
print x
[ 3  5  7  9 11 13]

In [91]: y=x

In [92]: id(x),id(y)
Out[92]: (4504682688, 4504682688)
```

x and y occupy the same location in memory so changing x can also change y!

```
In [109]: x[3]=100
```

```
In [110]: print x
[ 3  5  7 100 11 13]
```

```
In [111]: print y
[ 3  5  7 100 11 13]
```

Instead, use `y=x.copy()`

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Analyzing arrays

- Use `<tab>` completion to see your options: `x.<tab>`
- A few examples:

```
In [19]: print x
[ 3.  5.  7.  9. 11. 13.]

In [20]: x.sum()
Out[20]: 48.0

In [21]: sum(x)
Out[21]: 48.0

In [22]: print max(x)
13.0

In [23]: print mean(x)
8.0

In [24]: print var(x)
11.6666666667

In [25]: print cumsum(x)
[ 3.  8. 15. 24. 35. 48.]
```

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Analyzing arrays

- Use conditional statements easily:

```
In [21]: x=linspace(-1,1,11)
```

```
In [22]: print x
[-1. -0.8 -0.6 -0.4 -0.2  0.  0.2  0.4  0.6  0.8
 1.]
```

```
In [23]: print x[x<=0]
[-1. -0.8 -0.6 -0.4 -0.2  0.]
```

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Analyzing arrays

- Use conditional statements easily:

```
In [21]: x=linspace(-1,1,11)
```

```
In [22]: print x
[-1. -0.8 -0.6 -0.4 -0.2  0.  0.2  0.4  0.6  0.8
 1.]
```

```
In [23]: print x[x<=0]
[-1. -0.8 -0.6 -0.4 -0.2  0.]
```

- Example: generate step function

```
In [24]: y=x.copy()
```

```
In [25]: y[x>0]=1.0
```

```
In [26]: y[x<=0]=0.0
```

```
In [27]: print y
[ 0.  0.  0.  0.  0.  0.  1.  1.  1.  1.  1.]
```

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Building matrices

- First approach -- array of arrays:

```
In [45]: row1 = np.array([1, 3, 5])
```

```
In [46]: row2 = np.array([2, 4, 6])
```

```
In [47]: row3 = np.array([3, 5, 7])
```

```
In [48]: M = np.array([row1,row2,row3])
```

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Building matrices

First approach -- array of arrays:

```
In [45]: row1 = np.array([1, 3, 5])
In [46]: row2 = np.array([2, 4, 6])
In [47]: row3 = np.array([3, 5, 7])
In [48]: M = np.array([row1,row2,row3])

In [57]: print M
[[1 3 5]
 [2 4 6]
 [3 5 7]]

In [58]: shape(M)
Out[58]: (3, 3)
```

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Building matrices

Second approach: *meshgrid*

```
In [90]: x=np.linspace(0,1,11)
In [91]: y=np.linspace(0,2,6)
In [92]: [xg,yg]=np.meshgrid(x,y)

In [93]: print xg[0:3,0:3]
[[ 0.  0.1  0.2]
 [ 0.  0.1  0.2]
 [ 0.  0.1  0.2]]

In [94]: print yg[0:3,0:3]
[[ 0.  0.  0.]
 [ 0.4 0.4 0.4]
 [ 0.8 0.8 0.8]]
```

See also *mgrid* and *ogrid*

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Building matrices

A few more useful commands are *zeros*, *ones*, and *eye*:

```
In [108]: np.zeros((3,2))
Out[108]:
array([[ 0.,  0.],
       [ 0.,  0.],
       [ 0.,  0.]])

In [109]: np.ones((3,2))
Out[109]:
array([[ 1.,  1.],
       [ 1.,  1.],
       [ 1.,  1.]])

In [110]: np.eye(3)
Out[110]:
array([[ 1.,  0.,  0.],
       [ 0.,  1.,  0.],
       [ 0.,  0.,  1.]])
```

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Linear algebra

Use *dot* for dot products and matrix multiplications.

- dot product:

```
x
Out[116]: array([ 0.,  1.,  2.,  3.,  4.])

In [117]: y=x*2

In [118]: print y
[ 0.  2.  4.  6.  8.]

In [119]: z=dot(x,y)

In [120]: print z
60.0
```

(what will $x \cdot y$ give?)

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Linear algebra

Use *dot* for dot products and matrix multiplications.

- matrix-vector:

```
In [129]: print M
[[1 3 5]
 [2 4 6]
 [3 5 7]]

In [130]: v=array([1, 2, 1])

In [131]: dot(M,v)
Out[131]: array([12, 16, 20])
```

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Linear algebra

Use *dot* for dot products and matrix multiplications.

- matrix-matrix:

```
In [148]: print M1
[[1 2]
 [3 4]]

In [149]: print M2
[[1 1]
 [2 2]]

In [150]: print dot(M1,M2)
[[ 5  5]
 [11 11]]

In [151]: print dot(M2,M1)
[[ 4  6]
 [ 8 12]]
```

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Linear algebra

For more standard operations, `np.linalg.<tab>`

- Examples for determinant, inverse, and eigenvalues/eigenvectors:

```
In [20]: det(M1)
Out[20]: -2.0000000000000004
```

```
In [21]: inv(M1)
Out[21]:
array([[ -2. ,  1. ],
       [ 1.5, -0.5]])
```

```
In [22]: [l,v]=eig(M1)
```

```
In [23]: print l
[-0.37228132  5.37228132]
```

```
In [24]: print v
[[-0.82456484 -0.41597356]
 [ 0.56576746 -0.90937671]]
```

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Linear algebra

Solve $Ax=b$ using... solve:

```
In [63]: A
Out[63]:
array([[1, 2],
       [3, 4]])
```

```
In [64]: b
Out[64]: array([1, 2])
```

```
In [65]: x=solve(A,b)
```

```
In [66]: print x
[ 0.  0.5]
```

```
In [67]: print dot(A,x)-b
[ 0.  0.]
```

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