

Titel

Namen



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## Distortion example



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$$\begin{aligned}x &= x_d + (x_d - x_c)(1 + K_1 r^2 + K_2 r^4) + P_1 (r^2 + 2(x_d - x_c)^2) + 2P_2(x_d - x_c)(y_d - y_c) \\y &= y_d + (y_d - y_c)(1 + K_1 r^2 + K_2 r^4) + 2P_1(x_d - x_c)(y_d - y_c) + P_2 (r^2 + 2((y_d - y_c)^2))\end{aligned}$$

**Abbildung:** Formula to correct tangential and radial distortion

**Radial distortion:**

**Tangential distortion:**

$K_n = n^{th}$  radial distortion coefficient

$P_n = n^{th}$  tangential distortion coefficient

$(x_d, y_d)$  = distorted image point as projected on image plane,

$(x, y)$  = undistorted image point as projected on image plane,

$(x_c, y_c)$  = distortion center,

$$r = \sqrt{(x_d - x_c)^2 + (y_d - y_c)^2},$$

coefficients bigger 2 were not considered.

# Distortion example

$$x = x_d + (x_d - x_c)(1 + K_1 r^2 + K_2 r^4) + P_1 (r^2 + 2(x_d - x_c)^2) + 2P_2(x_d - x_c)(y_d - y_c)$$
$$y = y_d + (y_d - y_c)(1 + K_1 r^2 + K_2 r^4) + 2P_1(x_d - x_c)(y_d - y_c) + P_2 (r^2 + 2((y_d - y_c)^2))$$

## Radial distortion:

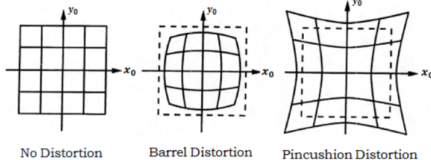


Abbildung: radial distortions

## Tangential distortion:

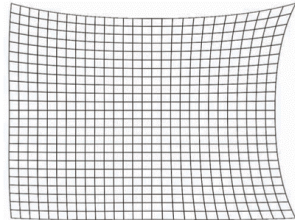


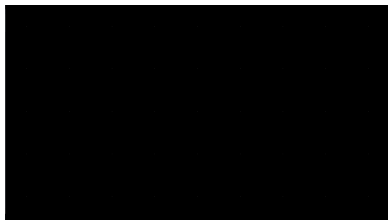
Abbildung: first order tangential distortion

# pixel size detection



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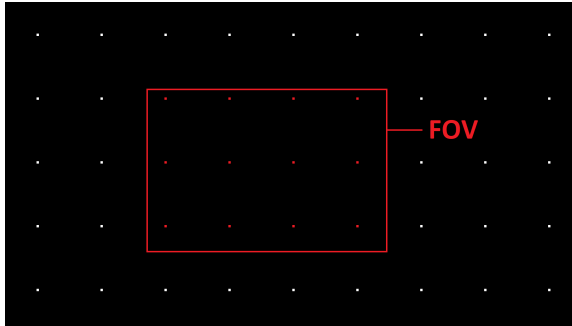
pixelSize = 1:



pixelSize = 8:



# Center point estimation



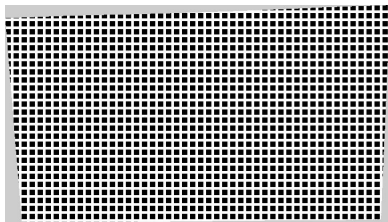
$$\mathbf{x}_c = \frac{\sum_{k=1}^n \mathbf{x}_k}{n}$$

$n$  : number of seen pixels

$\mathbf{x}_k$  : position of seen pixel

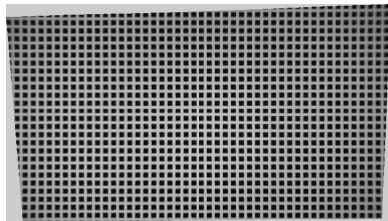
# Results

## Ground truth:



**Abbildung:** all white lines that we're drawn and seen on the screen

## Mapped Image:



**Abbildung:** the seen lines after they were mapped by the algorithm

# Comparison

## Substraction of ground truth and mapped image



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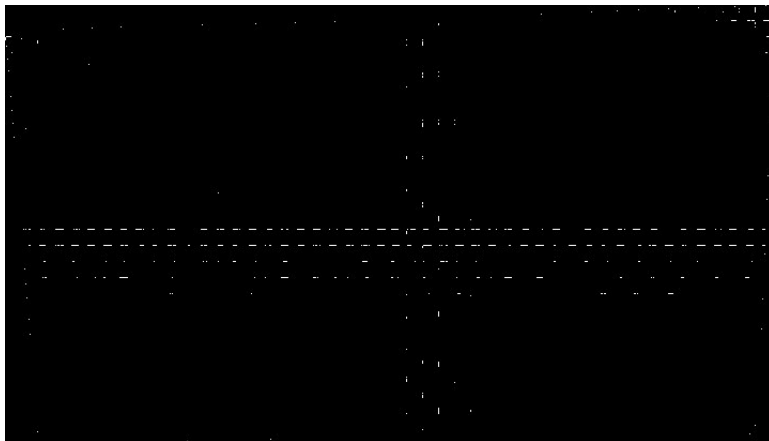
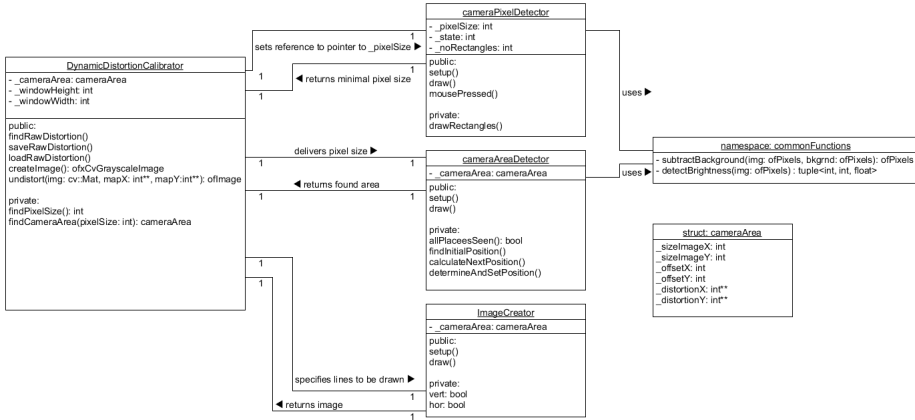


Abbildung: difference of both images

824 of 290,191 pixels do not fit

# Overview implementation

## UML diagramm







- ▶ Map gaining:
  - ▶ Depends on approach used
  - ▶ Usual dependencies
    - ▶ # images
    - ▶ Field of View (FOV)
    - ▶ Turnover rate of images (3 images per seconds)
    - ▶ Framerate (21 frames per second)
- ▶ Interpolate Map  $< 100\text{ ms}$
- ▶ Correct distortion  $< 100\text{ ms}$

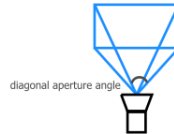
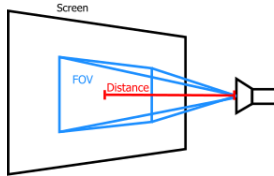
# Runtime FOV



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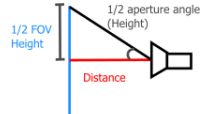
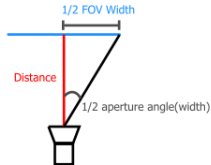
## Received Info:

- ▶  $\alpha_{width||height}$
- ▶  $\alpha_{diag}$



## Our FOV:

- ▶ 670x395 pixels
- ▶  $\alpha_{diag} = 68.46^\circ$
- ▶ camera specs:  
 $\alpha_{diag,s} = 68.5^\circ$





naive:

$$rt(w_s, h_s) = \frac{1}{3}(w_s + h_s) = 790 \text{ sec}$$

$w_s$  : width of screen

$h_s$  : height of screen

$w_{FOV}$  : width of FOV

$h_{FOV}$  : height of FOV



Center point & FOV based:

$$1. \quad rt_{cp}(w_s, h_s, s) = \frac{w_s \cdot h_s}{3s^2}$$

$$2. \quad rt_{map}(w_{FOV}, h_{FOV}, s, m, j) = \frac{1}{3j} (w_{FOV} + 2s + 2m + h_{FOV} + 2s + 2m)$$

$$3. \quad rt(w_s, h_s, w_{FOV}, h_{FOV}, s, m, j) = \frac{1}{3} \left( (w_{FOV} + 4s + 4m + h_{FOV}) \frac{1}{j} + \frac{w_s \cdot h_s}{s^2} \right)$$

$s$  : space between lit pixels in center point estimation

$m$  : safety margin

$j$  : skip range

## Find optimum

$$rt'(s) = -\frac{w_s h_s}{3s^3} + \frac{4}{3j} \stackrel{!}{=} 0$$

$$s = \sqrt[3]{\frac{w_s \cdot h_s \cdot j}{4}}$$

For our Setup

$j = 1:$

$s = 70$

$\Rightarrow$

$rt = 550$

$j = 3:$

$s = 101$

$\Rightarrow$

$rt = 211$

# Future Work



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- ▶ Run mapping in one step with *openframeworks*-version
- ▶ detect white threshold
- ▶ improvement of line detection  $\Rightarrow$  line counting?
- ▶ solve flipping problems seen in substracted picture
- ▶ unplausable found mappings
- ▶ undo statemachine if internal *openframeworks*-timing works