

HH

November 27, 2019

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[ ]: import numpy as np
import matplotlib.pyplot as plt
from scipy.signal import find_peaks
%matplotlib inline

[ ]: class Neuron:

    def __init__(self, E_m, C_m, E_na, E_k, E_l, g_na, g_k, g_l):
        self.E_m = E_m
        self.C_m = C_m
        self.E_na = E_na
        self.E_k = E_k
        self.E_l = E_l
        self.g_na = g_na
        self.g_k = g_k
        self.g_l = g_l

    def simulate(self, I_t, dt, time, t_e=None, t_s=None, plot=True,
→save=False):

        num_time_bins = int(time/dt)

        V_t = 0
        V_course = np.zeros(num_time_bins)

        m_t = 0
        m_t1 = np.zeros(num_time_bins)

        h_t = 0
        h_t1 = np.zeros(num_time_bins)

        n_t = 0
        n_t1 = np.zeros(num_time_bins)

        alpha_m = 0
        alpha_h = 0
        alpha_n = 0
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beta_m = 0
beta_h = 0
beta_n = 0

for i in np.arange(0, int(time/dt), 1):

    if t_e:
        if (i*dt) < t_e:
            I = I_t[0]
        elif t_e <= (i*dt) and (i*dt) < t_s:
            I = I_t[1]
        else:
            I = I_t[2]
    else:
        I = I_t

    beta_m = 4*np.exp(-V_t/18)
    beta_h = 1/(1 + np.exp(-(V_t - 30)/10))
    beta_n = 0.125*np.exp(-V_t/80)

    if V_t == 25:
        alpha_m = 1
    else:
        alpha_m = 0.1*((V_t - 25)/(1 - np.exp(-(V_t - 25)/10)))
    alpha_h = 0.07*np.exp(-V_t/20)
    if V_t == 10:
        alpha_n = 0.1
    else:
        alpha_n = 0.01*((V_t - 10)/(1 - np.exp(-(V_t - 10)/10)))

    m_t1[i] = m_t + dt*(alpha_m*(1 - m_t) - beta_m*m_t)
    m_t = m_t1[i]
    h_t1[i] = h_t + dt*(alpha_h*(1 - h_t) - beta_h*h_t)
    h_t = h_t1[i]
    n_t1[i] = n_t + dt*(alpha_n*(1 - n_t) - beta_n*n_t)
    n_t = n_t1[i]

    leak = self.g_l*(V_t - self.E_l)
    sod = self.g_na*(m_t**3)*h_t*(V_t - self.E_na)
    pot = self.g_k*(n_t**4)*(V_t - self.E_k)
    V_course[i] = V_t + (dt/self.C_m)*(I - leak - sod - pot)
    V_t = V_course[i]

if plot:
    figure = plt.figure(figsize=(9, 5))
    plt.grid(alpha=0.4)

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        xi = np.arange(0, len(V_course), 1)*dt
        plt.plot(xi, V_course)
        plt.axhline(y=0, color='k', linestyle='--', alpha=0.4)
#         plt.axvline(x=t_e, color='r', linestyle='--', alpha=0.4)
#         plt.axvline(x=t_s, color='r', linestyle='--', alpha=0.4)
        plt.xlabel('Time / ms', fontsize=15)
        plt.ylabel('Voltage / mV', fontsize=15)
        plt.xticks(fontsize = 10)
        plt.yticks(fontsize = 10)
        plt.title('Hodgkin-Huxley neurite model with %.2f  $\mu$ A current_
→injected'%I, fontsize=17)
        if save:
            plt.savefig('Current_%dA.png'%I_t[1])

    return V_course

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[ ]: E_m = 0
     C_m = 1
     E_na = 115
     E_k = -12
     E_l = 10.6
     g_na = 120
     g_k = 36
     g_l = 0.3

     a = Neuron(E_m, C_m, E_na, E_k, E_l, g_na, g_k, g_l)

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[ ]: I = [0, 8, 0]
     t_e = 50
     t_s = 300
     dt = 0.01 #ms
     time = t_s+100 #ms

     v = a.simulate(I, dt, time, t_e, t_s, save=False)

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[ ]: def threshold_detect(signal):
     peaks, _ = find_peaks(signal, prominence=1)
     return peaks

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[ ]: I = np.arange(0, 20, 0.25)
     dt = 0.01 #ms
     time = 800 #ms

     v = np.zeros((len(I), int(time/dt)))

     for c in range(len(I)):
         v[c, :] = a.simulate(I[c], dt, time, plot=False, save=False)

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[:]: r = []
      for i in range(v.shape[0]):
          trace = v[i, 20000:]
          x = threshold_detect(trace)
          r.append(np.float(len(x))/np.float(0.6))

[:]: figure = plt.figure(figsize=(9, 5))
      plt.grid(alpha=0.4)
      plt.xlabel('Applied current /  $\mu$ A', fontsize=15)
      plt.ylabel('Firing rate /  $s^{-1}$ ', fontsize=15)
      plt.plot(I, r)
      # plt.scatter(I, r, marker='x', alpha=0.6)
      # plt.savefig('Firing_rate.png')

[:]:

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