

1. Select a starting prior $\Pi_0 = \mathcal{N}(\bar{\mathbf{v}}_0, G_0^{-2})$; Set $k = 0$;
2. Draw an independent sample $\mathbf{v}_1^{(k)}, \dots, \mathbf{v}_M^{(k)}$ from the prior $\mathcal{N}(\bar{\mathbf{v}}_k, G_k^{-2})$. For each $\mathbf{v}_m^{(k)}$, compute the corresponding weight

$$w_m^{(k)} = \exp L(\mathbf{v}_m^{(k)}).$$

3. Use the collection $(\mathbf{v}_m^{(k)}, w_m^{(k)})$ for $m \leq M$ (posterior) to build the next prior distribution $\Pi_{k+1} = \mathcal{N}(\bar{\mathbf{v}}_{k+1}, G_{k+1}^{-2})$.
4. Increase $k \rightarrow k + 1$ and repeat pp. 2 and 3 until convergence.

A prior is called **conjugated** if the corresponding posterior belongs to the same family of measures as prior. This reduces the step of computing the posterior to parameter update.

Our **main result** claims that the Gaussian prior for a regular parametric family yields a **nearly Gaussian posterior** (**nearly conjugated**).

Therefore, it suffices to recompute the parameters of normal law.

It is natural and standard to use the **posterior mean**

$$\overline{\mathbf{v}}_{k+1} = \hat{\mathbf{v}}_k = \frac{1}{N_k} \sum_m w_m^{(k)} \mathbf{v}_m^{(k)}, \quad N_k = \sum_m w_m^{(k)}.$$

Alternatively, a robust (trimmed) mean could be used.