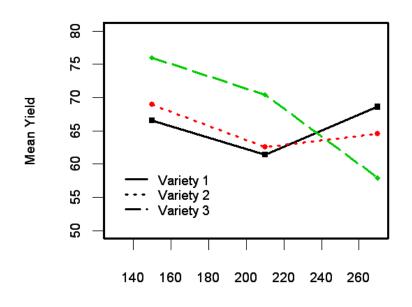
```
> # This file is stored as cane.r
                                                                  10
                                                                         1
                                                                               270 72.8 1 270
                                                                               270 64.8 1 270
>
                                                                  11
> # Enter the data. Note that the first
                                                                               270 86.3 1 270
                                                                 12
                                                                         1
> # line of this file is a line of data.
                                                                               150 58.6 2 150
                                                                  13
> # not a line of variable names.
                                                                               150 65.2 2 150
                                                                  14
                                                                         2
>
                                                                  15
                                                                               150 70.2 2 150
> cane <- read.table("cane.dat",</pre>
                                                                               150 51.8 2 150
                                                                  16
     col.names=c("Variety","Nitrogen",
                                                                               210 64.3 2 210
                                                                  17
              "Yield"))
                                                                  18
                                                                          2
                                                                                210 48.3 2 210
+
>
                                                                  19
                                                                                210 74.0 2 210
> # Create factors
                                                                  20
                                                                               210 63.6 2 210
                                                                               270 64.4 2 270
>
                                                                  21
                                                                               270 67.3 2 270
> cane$V <- as.factor(cane$Variety)</pre>
                                                                  22
> cane$N <- as.factor(cane$Nitrogen)</pre>
                                                                               270 78.0 2 270
                                                                  23
                                                                  24
                                                                                270 72.0 2 270
>
>
                                                                  25
                                                                          3
                                                                               150 65.8 3 150
> # Print the data frame
                                                                               150 68.3 3 150
                                                                  26
>
                                                                  27
                                                                          3
                                                                               150 72.7 3 150
                                                                               150 67.6 3 150
> cane
                                                                  28
                                                                               210 64.1 3 210
  Variety Nitrogen Yield V N
                                                                  29
1
            150 70.5 1 150
                                                                  30
                                                                               210 64.8 3 210
             150 67.5 1 150
                                                                               210 70.9 3 210
2
                                                                  31
3
       1
             150 63.9 1 150
                                                                  32
                                                                                210 58.3 3 210
             150 64.2 1 150
4
       1
                                                                  33
                                                                          3
                                                                                270 56.3 3 270
5
             210 67.3 1 210
                                                                  34
                                                                          3
                                                                                270 54.7 3 270
6
             210 75.9 1 210
                                                                               270 66.2 3 270
       1
                                                                  35
                                                                          3
             210 72.2 1 210
7
       1
                                                                  36
                                                                         3
                                                                                270 54.4 3 270
             210 60.5 1 210
8
       1
                                                                  >
       1
             270 79.9 1 270
9
                                                                  >
```

```
> # Compute mean yields for all combinations
> # of nitrogen levels and varieties and
> # Make a profile plot.
>
> means <- tapply(cane$Yield,</pre>
          list(cane$Variety,cane$Nitrogen),
            mean)
> means
                 270
    150
           210
1 66.525 68.975 75.950
2 61.450 62.550 70.425
3 68.600 64.525 57.900
>
> # Set up the profile plot
>
> par(cex=1.2,1wd=3,mex=1.5,mkh=.20)
> x.axis <- unique (cane$Nitrogen)</pre>
> matplot(c(130,270), c(50,80),
      type="n", xlab="Nitrogen(lb/acre)",
      ylab="Mean Yield",
      main= "Sugar Cane Yields")
>
    Add a profile for each soil type
>
> matlines(x.axis,means,type='l',
              lty=c(1,3,5),lwd=3)
>
> # Plot symbols for the sample means
>
```

### **Sugar Cane Yields**



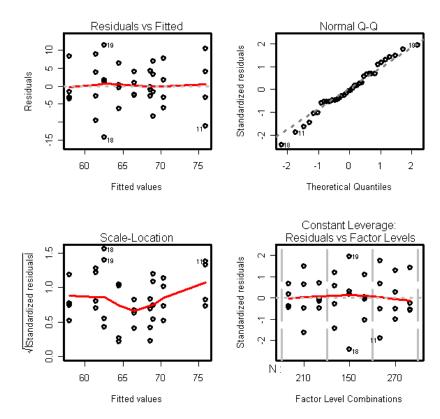
Nitrogen(lb/acre)

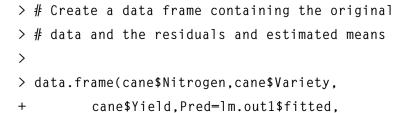
```
> # Fit a model with main effects and
> # interaction effects. Compute both
> # sets of Type I sums of squares.
>
```

```
> options(contrasts=c('contr.sum','contr.ploy'))
                                                             Call:
                                                             lm(formula = Yield ~ V * N, data = cane)
> lm.out1 <- lm(Yield~N*V, data=cane)</pre>
> anova(lm.out1)
                                                             Residuals:
Analysis of Variance Table
                                                                 Min
                                                                         10 Median
                                                                                        30
                                                                                              Max
                                                             -14.2500 -3.1313 -0.3625 3.9562 11.4500
Response: Yield
                                                             Coefficients:
       Df Sum Sq Mean Sq F value Pr(>F)
N
        2 56.54 28.27 0.6085 0.55148
                                                                      Estimate Std. Error t value Pr(>|t|)
        2 319.37 159.69 3.4370 0.04680 *
                                                             (Intercept) 66.3222 1.1360 58.380 <2e-16 ***
        4 559.79 139.95 3.0121 0.03547 *
                                                                      4.1611
                                                                                 1.6066 2.590 0.0153 *
N:V
                                                             ٧1
Residuals 27 1254.46 46.46
                                                             ٧2
                                                                       -1.5139
                                                                                 1.6066 -0.942 0.3544
                                                             N 1
                                                                       -0.7972
                                                                                 1.6066 -0.496 0.6238
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
                                                                       -0.9722
                                                             N2
                                                                                 1.6066 -0.605 0.5501
>
                                                             V1:N1
                                                                      -3.1611
                                                                                 2.2721 -1.391 0.1755
> lm.out2 <- lm(Yield~V*N, data=cane)</pre>
                                                             V2:N1 -2.5611
                                                                                 2.2721 -1.127 0.2696
> anova(lm.out2)
                                                             V1:N2
                                                                      -0.5361
                                                                                 2.2721 -0.236 0.8152
Analysis of Variance Table
                                                             V2:N2 -1.2861
                                                                                 2.2721 -0.566 0.5760
                                                             Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Response: Yield
       Df Sum Sq Mean Sq F value Pr(>F)
                                                             Residual standard error: 6.816 on 27 degrees of freedom
        2 319.37 159.69 3.4370 0.04680 *
                                                             Multiple R-Squared: 0.4272, Adjusted R-squared: 0.2575
        2 56.54 28.27 0.6085 0.55148
N
     4 559.79 139.95 3.0121 0.03547 *
                                                             F-statistic: 2.517 on 8 and 27 DF, p-value: 0.03462
V:N
Residuals 27 1254.46 46.46
                                                             > model.matrix(lm.out2)
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
                                                               (Intercept) V1 V2 N1 N2 V1:N1 V2:N1 V1:N2 V2:N2
> summary(lm.out2, correlation=F)
                                                             1
                                                                      1 \ 1 \ 0 \ 1 \ 0 \ 1
                                                                       1 1 0 1 0 1 0 0
```

```
1 1 0 1 0
3
                         1
                              0
                                   0
                                        0
          1 1 0 1 0
4
                              0
                                   0
                                        0
          1 1 0 0 1
5
                              0
                                   1
                                        0
          1 1 0 0 1
6
                              0
                                   1
                                        0
7
          1 1 0 0 1
                              0
                                   1
                                        0
          1 1 0 0 1
                                   1
8
                              0
                                        0
          1 1 0 -1 -1
9
                          - 1
                                   - 1
                                         0
10
          1 1 0 -1 -1
                                    - 1
                                         0
                          - 1
          1 1 0 -1 -1
11
                                    - 1
                          - 1
                               0
                                         0
12
          1 1 0 -1 -1
                                    - 1
                                         0
                          - 1
                               0
13
          1 0 1 1 0
                               1
                                    0
                                        0
14
          1 0 1 1 0
                              1
                                    0
                                        0
15
          1 0 1 1 0
                              1
                                    0
                                        0
16
          1 0 1 1 0
                                   0
                                        0
                              1
17
          1 0 1 0 1
                               0
                                    0
                                        1
18
          1 0 1 0 1
                               0
                                    0
                                        1
          1 0 1 0 1
19
                               0
                                    0
                                        1
20
          1 0 1 0 1
                               0
                                    0
                                        1
21
          1 0 1 -1 -1
                                        - 1
                               - 1
                                    0
22
          1 0 1 -1 -1
                              - 1
                                        - 1
                                    0
23
          1 0 1 -1 -1
                              - 1
                                    0
                                        - 1
24
          1 0 1 -1 -1
                                         - 1
                               - 1
25
          1 -1 -1 1 0
                                         0
                          - 1
                               - 1
26
          1 -1 -1 1 0
                          - 1
                               - 1
                                     0
                                         0
27
          1 -1 -1 1 0
                               -1
                                          0
                          - 1
                                     0
28
          1 -1 -1 1 0
                          - 1
                               - 1
                                     0
                                         0
29
          1 -1 -1 0 1
                                    - 1
                                        - 1
                          0
30
          1 -1 -1 0 1
                                   - 1
                          0
                                        - 1
31
          1 -1 -1 0 1
                                   - 1
                                        - 1
                          0
```

```
32
          1 -1 -1 0 1
                               0
                                   -1 -1
                          0
33
          1 -1 -1 -1 -1
                          1
                                    1
                                1
                                         1
34
          1 -1 -1 -1 -1
                           1
                                1
                                     1
                                          1
          1 -1 -1 -1 -1
35
                           1
                                1
                                     1
                                          1
36
          1 -1 -1 -1 -1
                                          1
                           1
                                1
                                     1
attr(,"assign")
[1] 0 1 1 2 2 3 3 3 3
attr(,"contrasts")
attr(,"contrasts")$V
[1] "contr.sum"
attr(,"contrasts")$N
[1] "contr.sum"
>
> # Create diagnostic plots
> par(mfrow=c(2,2))
> plot(lm.out1)
```





+	Resid=r	ound(lm.out1\$	resid,3))
cane.	Nitrogen	cane.Variety	cane.Yield Pred Resid
1	150	1	70.5 66.525 3.975
2	150	1	67.5 66.525 0.975
3	150	1	63.9 66.525 -2.625
4	150	1	64.2 66.525 -2.325
5	210	1	67.3 68.975 -1.675
6	210	1	75.9 68.975 6.925
7	210	1	72.2 68.975 3.225
8	210	1	60.5 68.975 -8.475
9	270	1	79.9 75.950 3.950
10	270	1	72.8 75.950 -3.150
11	270	1	64.8 75.950 -11.150
12	270	1	86.3 75.950 10.350
13	150	2	58.6 61.450 -2.850
14	150	2	65.2 61.450 3.750
15	150	2	70.2 61.450 8.750
16	150	2	51.8 61.450 -9.650
17	210	2	64.3 62.550 1.750
18	210	2	48.3 62.550 -14.250
19	210	2	74.0 62.550 11.450
20	210	2	63.6 62.550 1.050
21	270	2	64.4 70.425 -6.025
22	270	2	67.3 70.425 -3.125
23	270	2	78.0 70.425 7.575
24	270	2	72.0 70.425 1.575
25	150	3	65.8 68.600 -2.800
26	150	3	68.3 68.600 -0.300
27	150	3	72.7 68.600 4.100

```
28
           150
                         3
                                67.6 68.600 -1.000
                                                                     >
                                                                     > y <- matrix(cane$Yield.ncol=1)</pre>
29
           210
                                64.1 64.525 -0.425
                         3
                                64.8 64.525 0.275
                                                                     > b <- solve(crossprod(D)) %*% crossprod(D.y)</pre>
30
           210
           210
                                70.9 64.525 6.375
31
                         3
                                                                     > yhat <- D %*% b
                                                                     > sse <- crossprod(y-yhat)</pre>
32
           210
                         3
                                58.3 64.525 -6.225
33
           270
                                56.3 57.900 -1.600
                                                                     > df2 < -nrow(y) - st
34
           270
                         3
                                54.7 57.900 -3.200
                                                                     >
                                                                     > c1 <- kronecker( cbind(Iden(s-1),-one(s-1)),</pre>
35
           270
                            66.2 57.900 8.300
                                                                                     t(one(t)) )
36
           270
                         3
                                54.4 57.900 -3.500
                                                                     > q1 <- t(b) %*% t(c1)%*% solve( c1 %*%
>
                                                                              solve(crossprod(D)) %*% t(c1))%*%
> # Compute Type III sums of squares and
                                                                     +
> # corresponding F-tests.
                                                                                c1 %*% b
>
                                                                     \rightarrow df1<- s-1
> # Generate an identity matrix and a
                                                                     > f <- (q1/df1)/(sse/df2)
> # vector of ones
                                                                     > p <- 1-pf(f,df1,df2)
>
                                                                     > c1
> Iden <- function(n) diag(rep(1,n))</pre>
                                                                          [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9]
> one <- function(n) matrix(rep(1,n),ncol=1)</pre>
                                                                      \lceil 1. \rceil \quad 1 \quad 1 \quad 1 \quad 0 \quad 0 \quad 0 \quad -1 \quad -1 \quad -1
>
                                                                     [2.] 0 0 0 1 1 1 -1 -1 -1
> # Compute the transpose of the model
                                                                     > data.frame(SS=q1,df=df1,F.stat=f,p.value=p)
> # matrix for the cell means model
                                                                            SS df F.stat p.value
>
                                                                     1 319.3739 2 3.436975 0.04679743
> s <- length(unique(cane$Nitrogen))</pre>
                                                                     > c2 <- kronecker( t(one(s)).
> t <- length(unique(cane$Variety))</pre>
> st <- s*t
                                                                                  cbind(Iden(t-1), -one(t-1))
> r <- length(cane$Yield)/(st)</pre>
                                                                     > q2 <- t(b) %*% t(c2)%*%solve( c2 %*%
> D <- t(kronecker(Iden(st), t(one(r))))</pre>
                                                                              solve(crossprod(D)) %*% t(c2))%*%
>
                                                                                 c2 %*% b
> # Least squares estimation
                                                                     > df1<- t-1
```

```
> f <- (q2/df1)/(sse/df2)
> p < -1-pf(f,df1,df2)
> c2
   [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9]
[1,] 1 0 -1 1 0 -1 1 0 -1
[2.] 0 1 -1 0 1 -1 0 1 -1
> data.frame(SS=q2,df=df1,F.stat=f,p.value=p)
      SS df F.stat p.value
1 56.54056 2 0.608467 0.551478
>
>
> c3 <- kronecker( cbind(Iden(s-1),-one(s-1)),</pre>
             cbind(Iden(t-1), -one(t-1)) )
> q3 <- t(b) %*% t(c3)%*% solve( c3 %*%
       solve(crossprod(D)) %*% t(c3))%*%
         c3 %*% b
> df1 <- (s-1)*(t-1)
> f <- (q3/df1)/(sse/df2)
> p <- 1-pf(f,df1,df2)
> c3
   [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9]
[1,] 1 0 -1
[2,] 0
                        0 0 -1
          1 -1 0
[3.] 0
          0
            0 1
                     0 -1 -1 0
[4.] 0 0 0 0 1 -1 0 -1 1
> data.frame(SS=q3,df=df1,F.stat=f,p.value=p)
      SS df F.stat p.value
1 559.7878 4 3.012107 0.03547072
```

#### Conclusion:

- Variety 3 exhibits a linear decrease in yield as nitrogen increases from 150 lb/acre to 270 lb/acre.
- Varieties 1 and 2 exhibit parallel linear increasing trends in yield as nitrogen increases from 150 lb/acre to 270 lb/acre.
- Variety 1 appears to provide a consistently higher yield than Variety 2, but the difference in these two varieties is not ``significant'' at the .05 level.
- Variety 3 seems to do as well as Variety 1 at 150 lb/acre of nitrogen.

```
data set1:
                                                                    contrast (.5(v1+v2)-v3)*(n-lin)'
 infile 'D:\temp\cane.dat ':
                                                                                variety*nitrogen
 input variety nitrogen yield:
                                                                               -.5 0 .5 -.5 0 .5 1 0 -1:
                                                                    contrast (.5(v1+v2)-v3)*(n-quad)'
run;
                                                                                variety*nitrogen
/* Print the data */
                                                                              -.5 1 -.5 -.5 1 -.5 1 -2 1:
                                                                    estimate 'n-linear' nitrogen -1 0 1;
proc print data=set1;
                                                                    estimate 'n-quad' nitrogen -1 2 -1;
  var yield;
                                                                    estimate 'v1-v2' variety 1 -1 0;
                                                                    estimate (v1+v2)-v3 variety .5 .5 -1:
run:
                                                                   estimate '(v1-v2)*(n-lin)' variety*nitrogen
/* Compute an ANOVA table */
                                                                                    -1 0 1 1 0 -1 0 0 0;
                                                                    estimate '(v1-v2)*(n-quad)' variety*nitrogen
proc glm data=set1;
                                                                                    -1 2 -1 1 -2 1 0 0 0:
                                                                   estimate '(.5(v1+v2)-v3)*(n-lin)' variety*nitrogen
 class variety nitrogen;
 model yield = variety|nitrogen /
                                                                                    -.5 0 .5 -.5 0 .5 1 0 -1:
        p clm alpha=.05 ss1 ss2
                                                                   estimate '(.5(v1+v2)-v3)*(n-quad)' variety*nitrogen
        ss3 ss4 e e1 e2 e3 e4:
                                                                                    -.5 1 -.5 -.5 1 -.5 1 -2 1:
 output out=setr r=resid p=yhat;
                                                                    run;
 lsmeans variety*nitrogen / stderr pdiff;
 means variety nitrogen / tukey:
                                                                  /* Make a profile plots for the interaction
 contrast 'n-linear' nitrogen -1 0 1;
 contrast 'n-quad' nitrogen -1 2 -1;
                                                                    between varieties and nitrogen levels */
 contrast 'v1-v2' variety 1 -1 0;
 contrast (v1+v2)-v3 variety .5 .5 -1:
                                                                  proc sort data=set1; by variety nitrogen;
 contrast '(v1-v2)*(n-lin)' variety*nitrogen
                                                                  proc means data=set1 noprint;
                  -1 0 1 1 0 -1 0 0 0;
                                                                   by variety nitrogen;
 contrast '(v1-v2)*(n-quad)' variety*nitrogen
                                                                   var vield:
                                                                   output out=means mean=my;
                  -1 2 -1 1 -2 1 0 0 0:
```

```
run;
axis1 label=(f=swiss h=2.5)
     ORDER = 120 \text{ to } 300 \text{ by } 30
     value=(f=swiss h=2.0) w=3.0;
axis2 label=(f=swiss h=2.0)
     order = 50 to 80 by 10
     value=(f=swiss h=2.0) w= 3.0;
SYMBOL1 V=CIRCLE H=2.0 w=3 1=1 i=join;
SYMBOL2 V=DIAMOND H=2.0 w=3 1=3 i=join;
SYMBOL3 V=square H=2.0 w=3 1=9 i=join;
PROC GPLOT DATA=means;
  PLOT my*nitrogen=variety /
          vaxis=axis2 haxis=axis1;
  TITLE1 H=3.0 F=swiss "Sugar Cane Yields";
     LABEL my='Mean Yield';
     LABEL nitrogen = 'Nitrogen (lb/acre)';
RUN:
```

# **General Form of Estimable Functions**

Effect		Coefficients
Intercept		L1
variety	1	L2
variety	2	L3
variety	3	L1-L2-L3
nitrogen	150	L5
nitrogen	210	L6
nitrogen	270	L1-L5-L6
variety*nitroge	n 1 150	L8
variety*nitroge	n 1 210	L9
variety*nitroge	n 1 270	L2-L8-L9
variety*nitroge	n <b>2 150</b>	L11
variety*nitroge	n 2 210	L12
variety*nitroge	n 2 270	L3-L11-L12
variety*nitroge	n 3 150	L5-L8-L11
variety*nitroge	n 3 210	L6-L9-L12
variety*nitroge	n 3 270	L1-L2-L3-L5-L6+L8+L9+L11+L12
· · · · · · · · · · · . ·		_: _=

**Type I Estimable Functions** 

		Coefficients				
Effect		variety	nitrogen	variety*nitrogen		
		_	_			
Intercept		0	0	0		
variety	1	L2	0	0		
variety	2	L3	0	0		
variety	3	-L2-L3	0	0		
nitrogen	150	0	L5	0		
nitrogen	210	0	L6	0		
nitrogen	270	0	-L5-L6	0		
variety*nitrogen	1 150	0.3333*L2	0.3333*L5	L8		
variety*nitrogen	1 210	0.3333*L2	0.3333*L6	L9		
variety*nitrogen	1 270	0.3333*L2	-0.3333*L5-0.3333*L6	-L8-L9		
variety*nitrogen	2 150	0.3333*L3	0.3333*L5	L11		
variety*nitrogen	2 210	0.3333*L3	0.3333*L6	L12		
variety*nitrogen	2 270	0.3333*L3	-0.3333*L5-0.3333*L6	-L11-L12		
variety*nitrogen	3 150	-0.3333*L2-0.3333*L3	0.3333*L5	-L8-L11		
variety*nitrogen	3 210	-0.3333*L2-0.3333*L3	0.3333*L6	-L9-L12		
variety*nitrogen	3 270	-0.3333*L2-0.3333*L3	-0.3333*L5-0.3333*L6	L8+L9+L11+L12		

**Type II Estimable Functions** 

-----Coefficients-----

Effect		variety	nitrogen	variety*nitrogen
Intercept		0	0	0
variety	1	L2	0	0
variety	2	L3	0	0
variety	3	-L2-L3	0	0
nitrogen	150	0	L5	0
nitrogen	210	0	L6	0
nitrogen	270	0	-L5-L6	0
variety*nitroger	1 150	0.3333*L2	0.3333*L5	L8
variety*nitroger	1 210	0.3333*L2	0.3333*L6	L9
variety*nitroger	1 270	0.3333*L2	-0.3333*L5-0.3333*L6	-L8-L9

0.3333\*L5

0.3333\*L6

0.3333\*L5

0.3333\*L6

-0.3333\*L5-0.3333\*L6

-0.3333\*L5-0.3333\*L6

L11

L12

-L11-L12

-L8-L11

-L9-L12

L8+L9+L11+L12

0.3333\*L3

0.3333\*L3

0.3333\*L3

-0.3333\*L2-0.3333\*L3

-0.3333\*L2-0.3333\*L3

-0.3333\*L2-0.3333\*L3

variety\*nitrogen 2 150

variety\*nitrogen 2 210

variety\*nitrogen 2 270

variety\*nitrogen 3 150

variety\*nitrogen 3 210

variety\*nitrogen 3 270

# **Type III Estimable Functions**

		Coefficients					
Effect		variety	nitrogen	variety*nitrogen			
Intercept		0	0	0			
variety	1	L2	0	0			
variety	2	L3	0	0			
variety	3	-L2-L3	0	0			
nitrogen	150	0	L5	0			
nitrogen	210	0	L6	0			
nitrogen	270	0	-L5-L6	0			
variety*nitrogen	1 150	0.3333*L2	0.3333*L5	L8			
variety*nitrogen	1 210	0.3333*L2	0.3333*L6	L9			
variety*nitrogen	1 270	0.3333*L2	-0.3333*L5-0.3333*L6	-L8-L9			
variety*nitrogen	2 150	0.3333*L3	0.3333*L5	L11			
variety*nitrogen	2 210	0.3333*L3	0.3333*L6	L12			
variety*nitrogen	2 270	0.3333*L3	-0.3333*L5-0.3333*L6	-L11-L12			
variety*nitrogen	3 150	-0.3333*L2-0.3333*L3	0.3333*L5	-L8-L11			

 variety\*nitrogen 3 210
 -0.3333\*L2-0.3333\*L3
 0.3333\*L6
 -L9-L12

 variety\*nitrogen 3 270
 -0.3333\*L2-0.3333\*L3
 -0.3333\*L5-0.3333\*L6
 L8+L9+L11+L12

**Type IV Estimable Functions** 

	Coefficients					
Effect		variety	nitrogen	variety*nitrogen		
Intercept		0	0	0		
variety	1	L2	0	0		
•	2	L3	0	0		
variety		-	-			
variety	3	-L2-L3	0	0		
nitrogen	150	0	L5	0		
nitrogen	210	0	L6	0		
nitrogen	270	0	-L5-L6	0		
variety*nitroge	n 1 150	0.3333*L2	0.3333*L5	L8		
variety*nitroge	n 1 210	0.3333*L2	0.3333*L6	L9		
variety*nitroge	n 1 270	0.3333*L2	-0.3333*L5-0.3333*L6	-L8-L9		
variety*nitroge	n 2 150	0.3333*L3	0.3333*L5	L11		
variety*nitroge	n 2 210	0.3333*L3	0.3333*L6	L12		
variety*nitroge	n 2 270	0.3333*L3	-0.3333*L5-0.3333*L6	-L11-L12		
variety*nitroge	n 3 150	-0.3333*L2-0.3333*L3	0.3333*L5	-L8-L11		
variety*nitroge	n 3 210	-0.3333*L2-0.3333*L3	0.3333*L6	-L9-L12		
variety*nitroge	n 3 270	-0.3333*L2-0.3333*L3	-0.3333*L5-0.3333*L6	L8+L9+L11+L12		

			Sum of			
Source		DF	Squares	Mean Square	F Value	Pr > F
Model		8	935.702222	116.962778	2.52	0.0346
Error		27	1254.460000	46.461481		
Corrected Total		35	2190.162222			
	R-Square	Co	peff Var Roo	ot MSE yield M	ean	
	0.427230	10	0.27750 6.8°	16266 66.322	22	
Source		DF	Type I SS	Mean Square	F Value	Pr > F
variety		2	319.3738889	159.6869444	3.44	0.0468
nitrogen		2	56.5405556	28.2702778	0.61	0.5515
variety*nitrogen		4	559.7877778	139.9469444	3.01	0.0355
Source		DF	Type II SS	Mean Square	F Value	Pr > F
variety		2	319.3738889	159.6869444	3.44	0.0468
nitrogen		2	56.5405556	28.2702778	0.61	0.5515
variety*nitrogen		4	559.7877778	139.9469444	3.01	0.0355
Source		DF	Type III SS	Mean Square	F Value	Pr > F
variety		2	319.3738889	159.6869444	3.44	0.0468
nitrogen		2	56.5405556	28.2702778	0.61	0.5515
variety*nitrogen		4	559.7877778	139.9469444	3.01	0.0355
Source		DF	Type IV SS	Mean Square	F Value	Pr > F
variety		2	319.3738889	159.6869444	3.44	0.0468
nitrogen		2	56.5405556	28.2702778	0.61	0.5515
variety*nitrogen		4	559.7877778	139.9469444	3.01	0.0355

#### **Least Squares Means**

			Standard		LSMEAN
variety	nitrogen	yield LSMEAN	Error	Pr >  t	Number
1	150	66.5250000	3.4081330	<.0001	1
1	210	68.9750000	3.4081330	<.0001	2
1	270	75.9500000	3.4081330	<.0001	3
2	150	61.4500000	3.4081330	<.0001	4
2	210	62.5500000	3.4081330	<.0001	5
2	270	70.4250000	3.4081330	<.0001	6
3	150	68.6000000	3.4081330	<.0001	7
3	210	64.5250000	3.4081330	<.0001	8
3	270	57.9000000	3.4081330	<.0001	9

# Least Squares Means for effect variety\*nitrogen Pr > |t| for H0: LSMean(i)=LSMean(j)

Dependent Variable: yield

i/j	1	2	3	4	5	6	7	8	9
1		0.6154	0.0610	0.3017	0.4168	0.4255	0.6702	0.6815	0.0848
2	0.6154		0.1594	0.1301	0.1937	0.7658	0.9386	0.3640	0.0296
3	0.0610	0.1594		0.0056	0.0098	0.2617	0.1389	0.0252	0.0009
4	0.3017	0.1301	0.0056		0.8212	0.0735	0.1495	0.5289	0.4678
5	0.4168	0.1937	0.0098	0.8212		0.1139	0.2202	0.6852	0.3432
6	0.4255	0.7658	0.2617	0.0735	0.1139		0.7079	0.2315	0.0150
7	0.6702	0.9386	0.1389	0.1495	0.2202	0.7079		0.4053	0.0350
8	0.6815	0.3640	0.0252	0.5289	0.6852	0.2315	0.4053		0.1806
9	0.0848	0.0296	0.0009	0.4678	0.3432	0.0150	0.0350	0.1806	

NOTE: To ensure overall protection level, only probabilities associated with pre-planned comparisons should be used.

Dependent Variable: yield

Contrast	DF	Contrast SS	Mean Square	F Value	Pr > F
n-linear	1	39.5266667	39.5266667	0.85	0.3645
n-quad	1	17.0138889	17.0138889	0.37	0.5501
v1-v2	1	193.2337500	193.2337500	4.16	0.0513
(v1+v2)-v3	1	126.1401389	126.1401389	2.71	0.1110
(v1-v2)*(n-lin)	1	0.2025000	0.2025000	0.00	0.9478
(v1-v2)*(n-quad)	1	1.6875000	1.6875000	0.04	0.8503
(.5(v1+v2)-v3)*(n-lin)	1	528.0133333	528.0133333	11.36	0.0023
(.5(v1+v2)-v3)*(n-quad)	1	29.8844444	29.8844444	0.64	0.4296

		Standard		
Parameter	Estimate	Error	t Value	Pr >  t
n-linear	2.5666667	2.7827289	0.92	0.3645
n-quad	-2.9166667	4.8198279	-0.61	0.5501
v1-v2	5.6750000	2.7827289	2.04	0.0513
(v1+v2)-v3	3.9708333	2.4099139	1.65	0.1110
(v1-v2)*(n-lin)	0.4500000	6.8162659	0.07	0.9478
(v1-v2)*(n-quad)	2.2500000	11.8061189	0.19	0.8503
(.5(v1+v2)-v3)*(n-lin)	19.9000000	5.9030595	3.37	0.0023
(.5(v1+v2)-v3)*(n-quad)	-8.2000000	10.2243989	-0.80	0.4296