

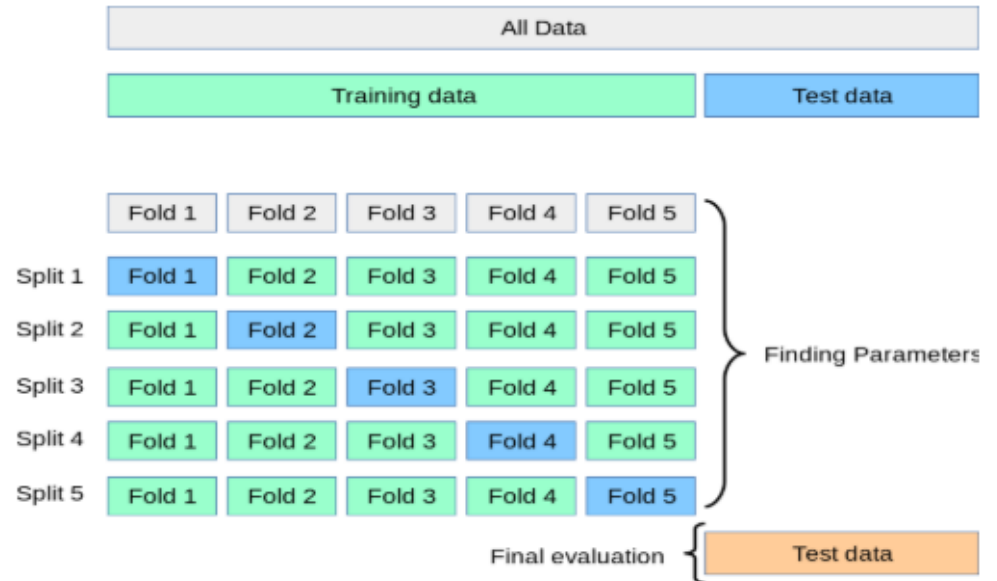
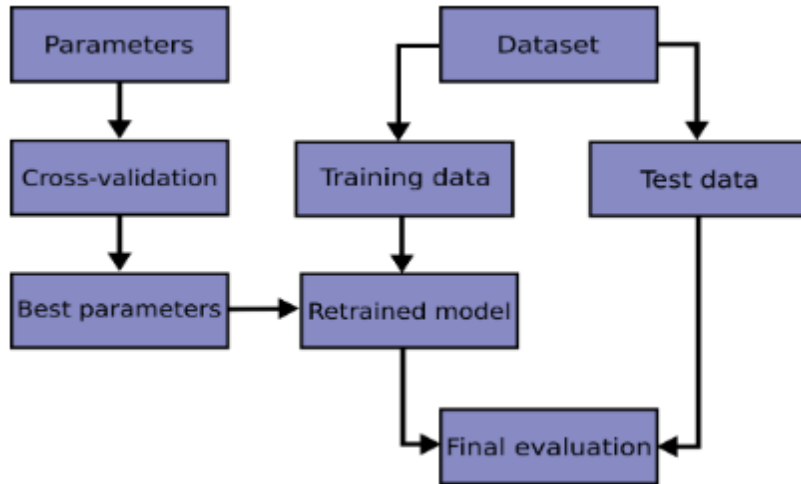
Machine Learning & Scikit-Learn

Day6. 파이프라인

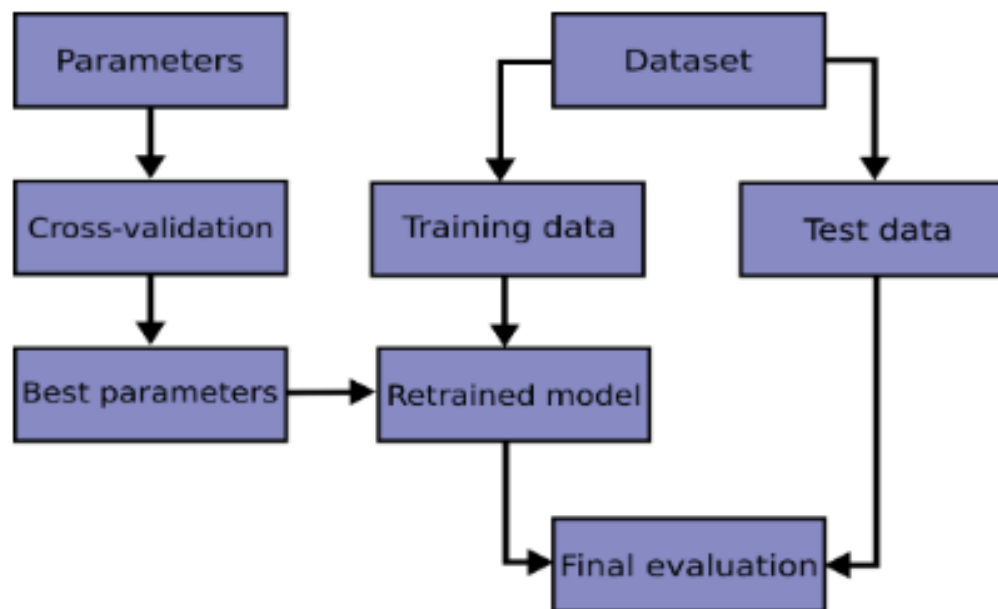
#1

파이프라인

- cross_val_score(Estimator, X, y) 함수

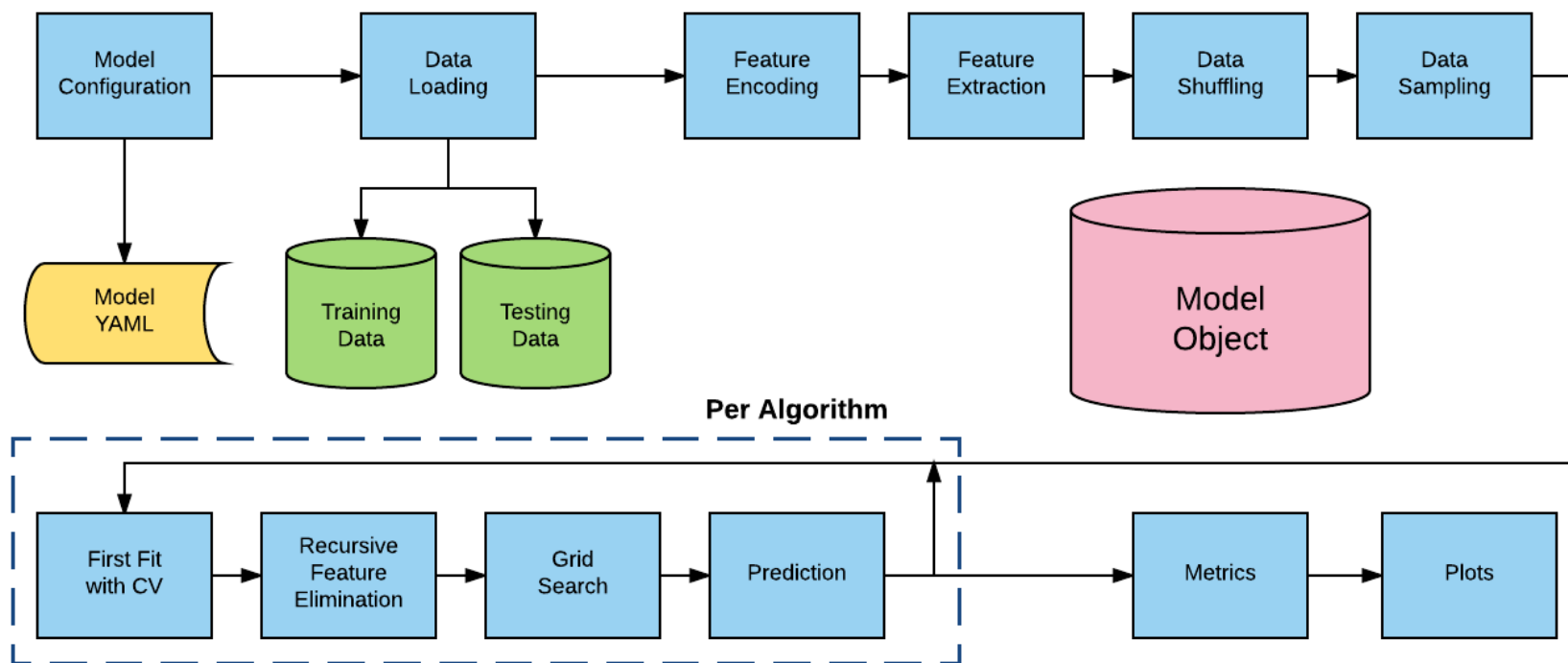


- GridSearchCV(Estimator, param_grid) 함수
 - Estimator에 param_grid의 값을 적용하여 성능 평가하여 가장 성능이 우수한 파라미터를 가지는 estimator를 선택함



■ 파이프 라인

- 문제 해결에 가장 적합한 알고리즘과 파라미터를 찾는 과정



Iterator	Arguments	Results	Example
<code>chain()</code>	<code>p, q, ...</code>	<code>p0, p1, ... plast, q0, q1, ...</code>	<code>chain('ABC', 'DEF') --> A B C D E F</code>

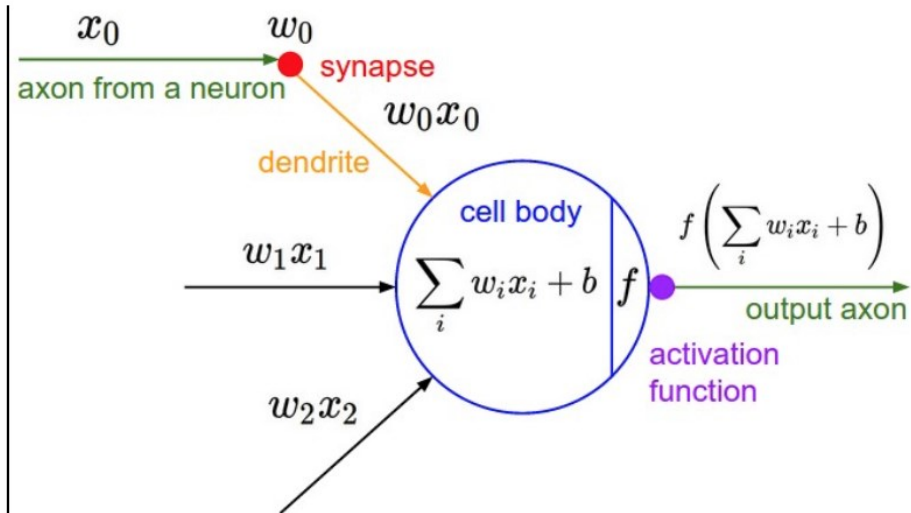
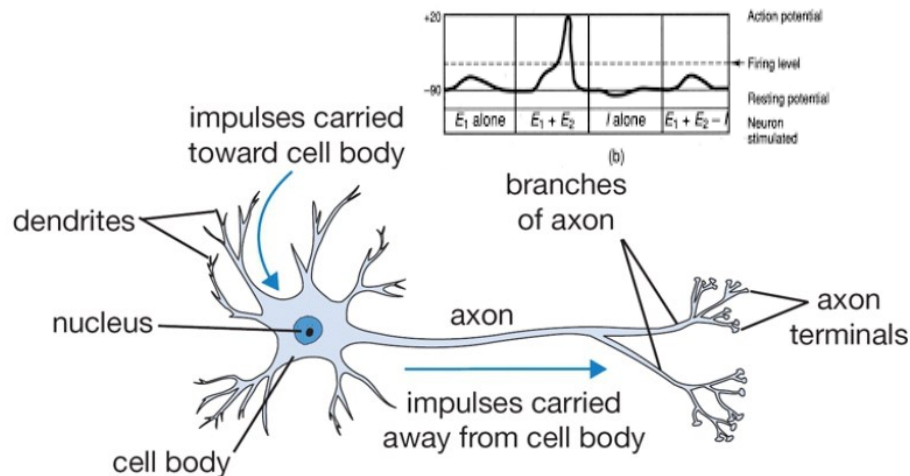
#2

Artificial Neural Network

추천 링크

<https://youtu.be/aircAruvnKk>

■ Artificial Neuron



A cartoon drawing of a biological neuron (left) and its mathematical model (right).

	Unit step	$g(z) = \begin{cases} 1 & \text{if } z \geq 0 \\ -1 & \text{otherwise.} \end{cases}$
		$g(z) = \begin{cases} 1 & \text{if } z \geq 0 \\ 0 & \text{otherwise.} \end{cases}$
	Linear	$g(z) = z$
	Logistic (sigmoid)	$g(z) = 1 / (1 + \exp(-z))$
	Hyperbolic tangent (sigmoid)	$g(z) = \frac{\exp(2z) - 1}{\exp(2z) + 1}$
...		

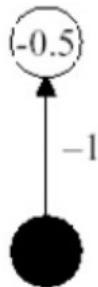
Perceptron

- Perceptron

✓ 논리 연산

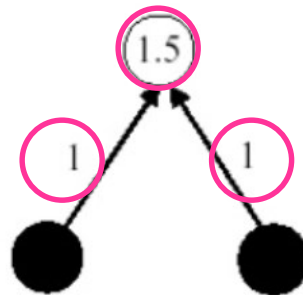
NOT

<i>in</i>	<i>out</i>
0	1
1	0



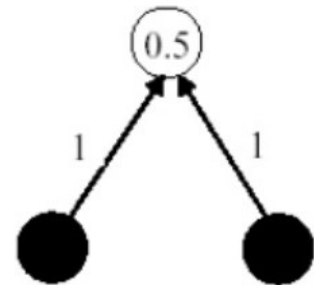
AND

<i>in</i> ₁	<i>in</i> ₂	<i>out</i>
0	0	0
0	1	0
1	0	0
1	1	1



OR

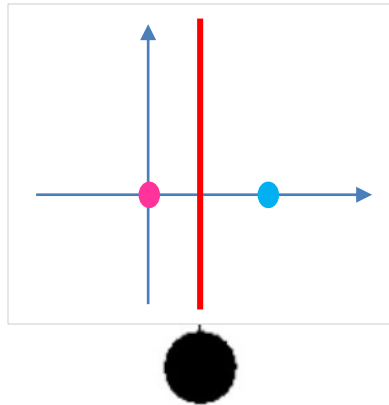
<i>in</i> ₁	<i>in</i> ₂	<i>out</i>
0	0	0
0	1	1
1	0	1
1	1	1



- Perceptron은 선형 분류기

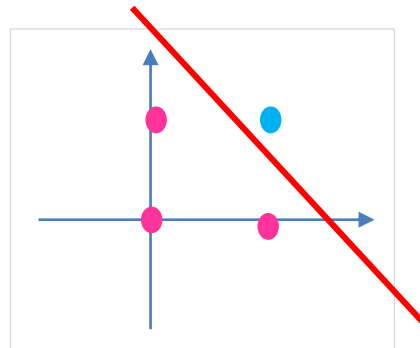
NOT

in	out
0	1
1	0



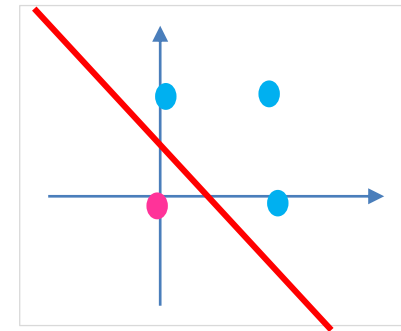
AND

in_1	in_2	out
0	0	0
0	1	0
1	0	0
1	1	1

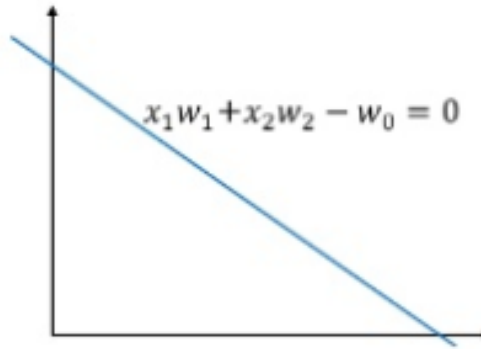
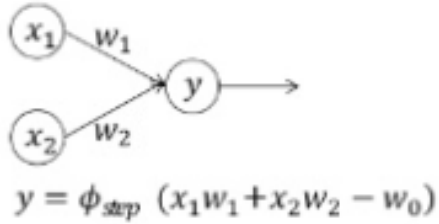


OR

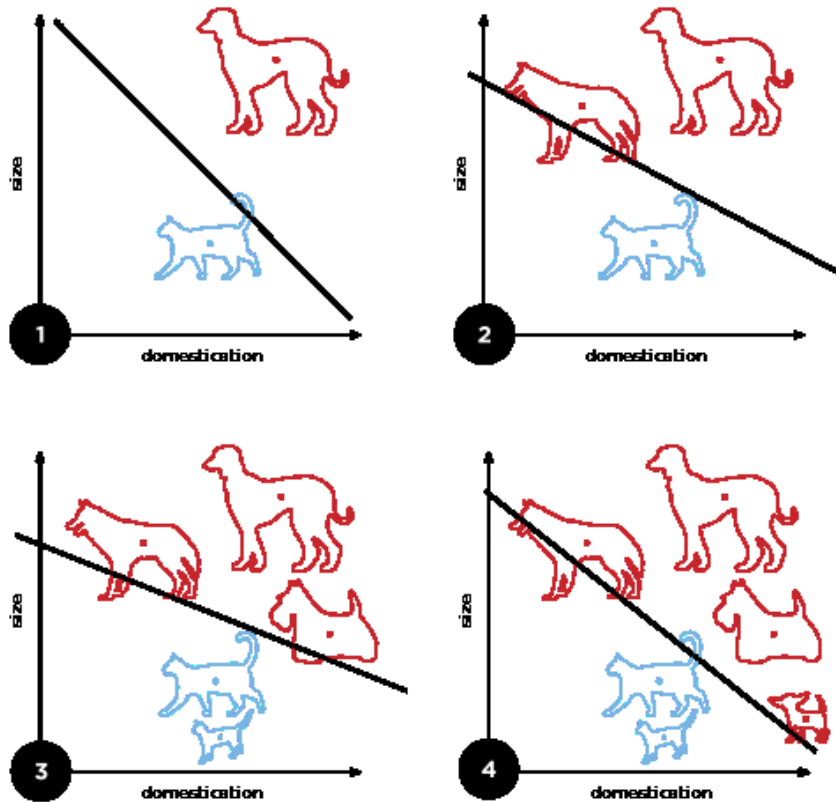
in_1	in_2	out
0	0	0
0	1	1
1	0	1
1	1	1



■ Perceptron



■ Perceptron 학습의 목표



A 2D plot showing a blue line representing the decision boundary. The equation $x_1w_1 + x_2w_2 - w_0 = 0$ is written next to the line. A large red **W** is positioned above the equation.

■ Perceptron 학습 규칙(= delta rule)

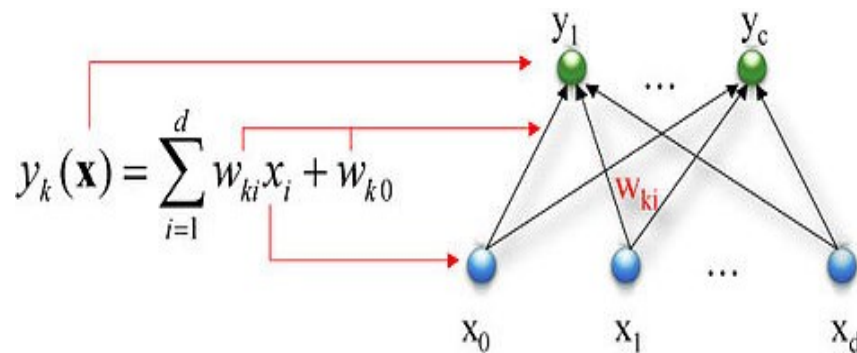
- 에러가 최소가 되는 w 를 구함
- Cost function

$$E = \sum_j \frac{1}{2} (t_j - y_j)^2.$$

- Weight update between input neuron i and output neuron j

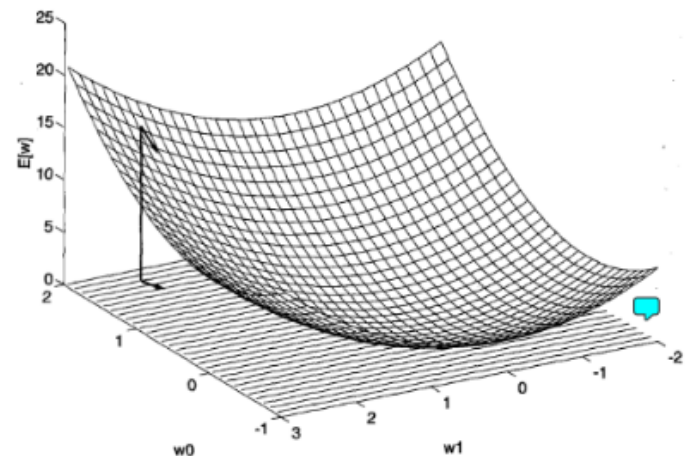
$$W_{ji}(t+1) = W_{ji}(t) - \eta \Delta W_{ji}(t)$$

$$= W_{ji}(t) + \eta (t_j - y_j) x_i$$

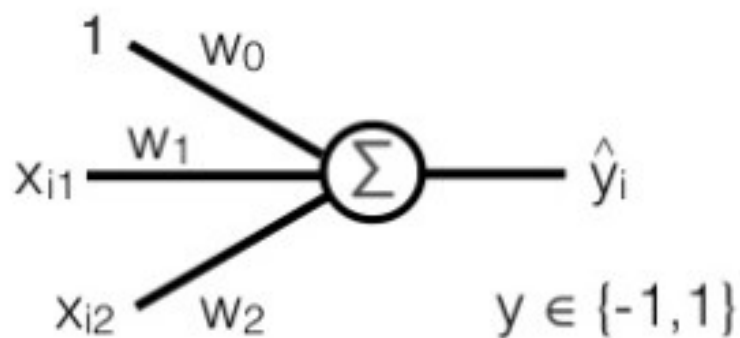


$$\begin{aligned} \frac{\partial E}{\partial w_{ji}} &= \frac{\partial \left(\frac{1}{2} (t_j - y_j)^2 \right)}{\partial w_{ji}} = \frac{\partial \left(\frac{1}{2} (t_j - y_j)^2 \right)}{\partial y_j} \frac{\partial y_j}{\partial w_{ji}} \\ &= -(t_j - y_j) \frac{\partial y_j}{\partial w_{ji}} = -(t_j - y_j) x_i, \end{aligned}$$

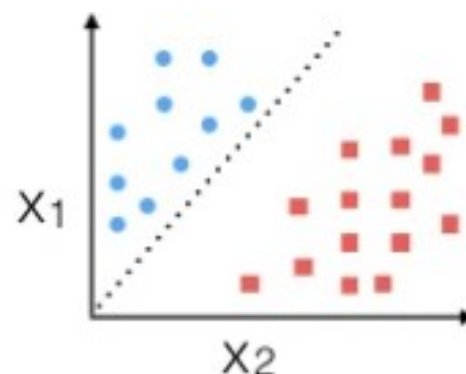
$$\frac{\partial x_i w_{ji}}{\partial w_{ji}} = x_i,$$



■ Perceptron 학습 규칙



$$\hat{y} = \mathbf{w}^T \mathbf{x} = w_0 + w_1 x_1 + w_2 x_2$$



$$\hat{y}_i \begin{cases} 1 & \text{if } \mathbf{w}^T \mathbf{x}_i \geq \theta \\ -1 & \text{otherwise} \end{cases}$$

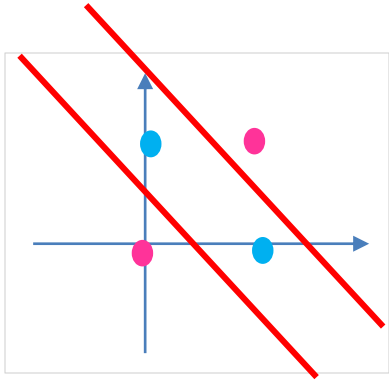
w_j = weight
 x_i = training sample
 y_i = desired output
 \hat{y}_i = actual output
 t = iteration step
 η = learning rate
 θ = threshold (here 0)

update rule:

$$w_j(t+1) = w_j(t) + \eta(y_i - \hat{y}_i)x_i$$

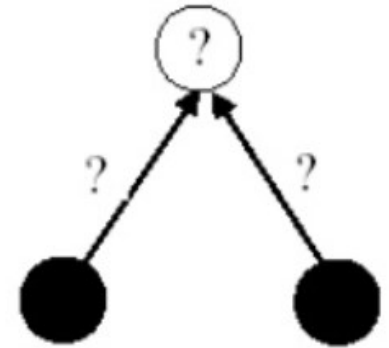
until
 $t+1 = \text{max iter}$
 or error = 0

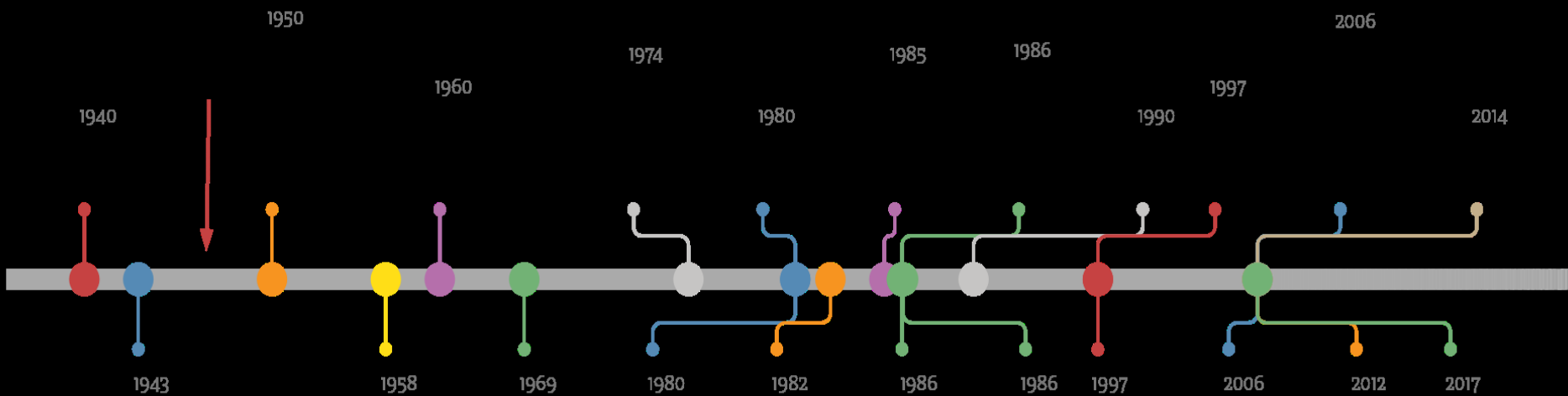
- Perceptron의 문제점: OXR 연산



XOR

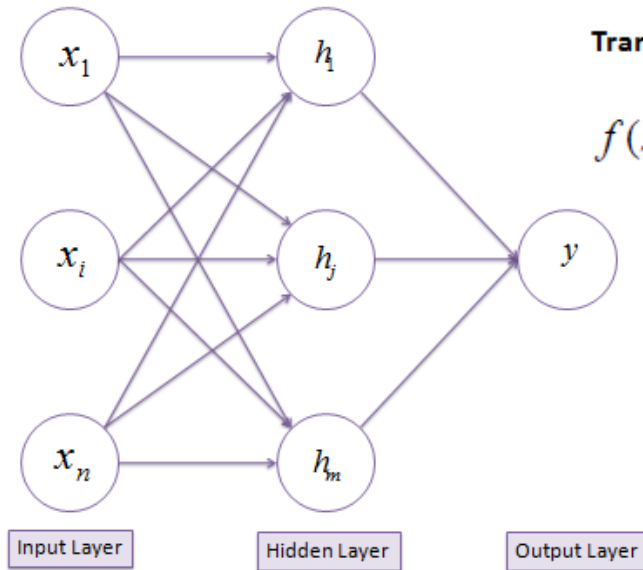
in_1	in_2	out
0	0	0
0	1	1
1	0	1
1	1	0





Multi layered Perceptron

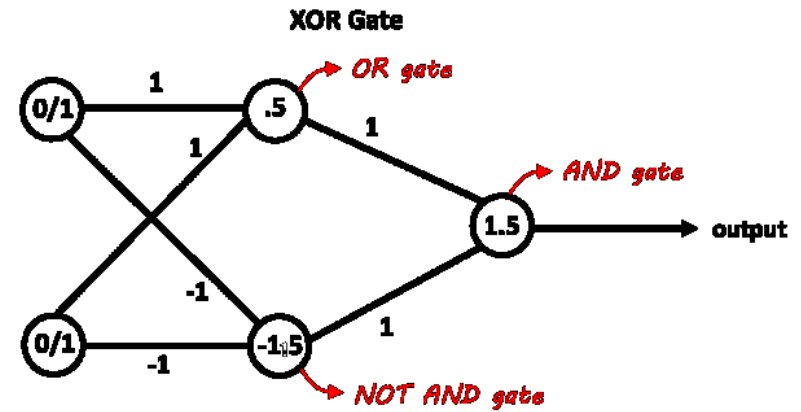
■ MLP 구조



Transformation

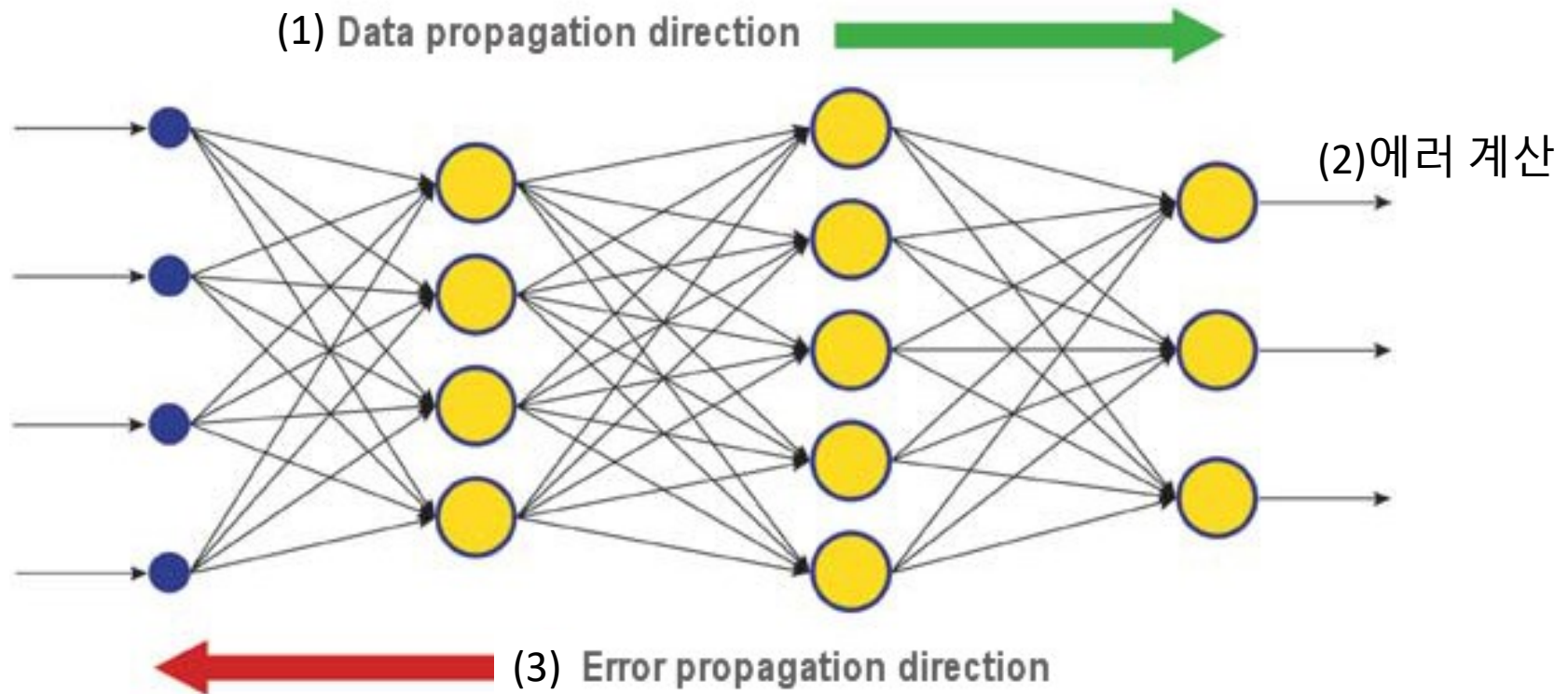
$$f(s) = \frac{1}{1 + e^{-s}}$$

$$s = \sum w \cdot x$$

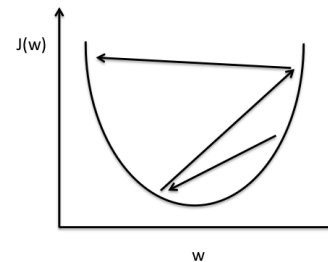
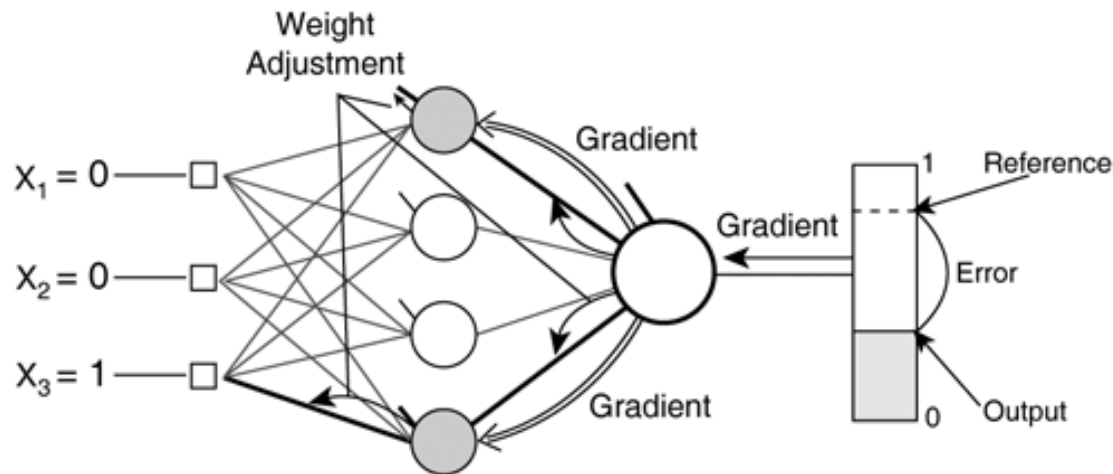


X1	X2	Y
0	0	0
0	1	1
1	0	1
1	1	0

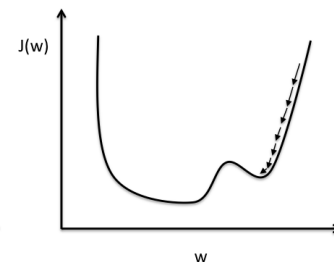
■ MLP의 학습



- 학습 규칙: 오류 역전파 학습(EBP, Error Back Propagation)



Large learning rate: Overshooting.



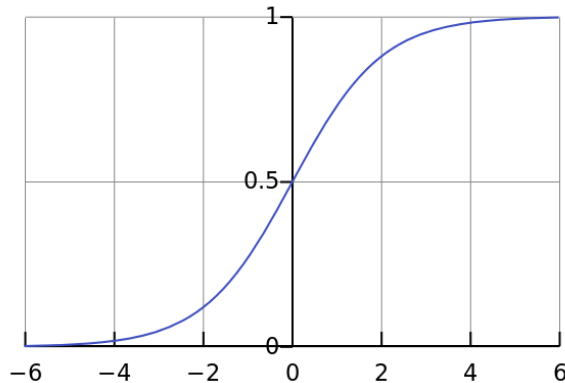
Small learning rate: Many iterations until convergence and trapping in local minima.

$$\delta_j = \begin{cases} \sigma'(\zeta_j)(t_j - y_j) & \text{if } j \text{ is an output unit} \\ \sigma'(\zeta_j) \sum_k \delta_k w_{jk} & \text{if } j \text{ is a hidden unit} \end{cases}$$

■ Activation functions

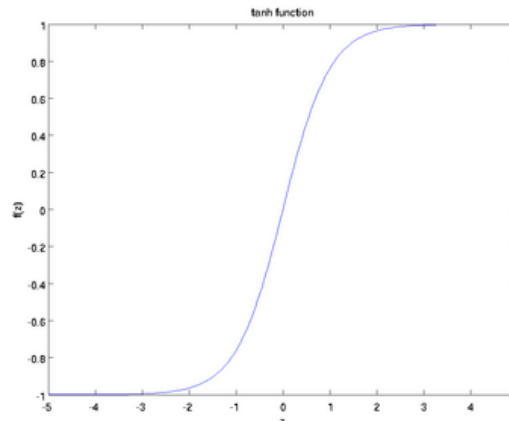
Sigmoid function

$$A = \frac{1}{1+e^{-x}}$$



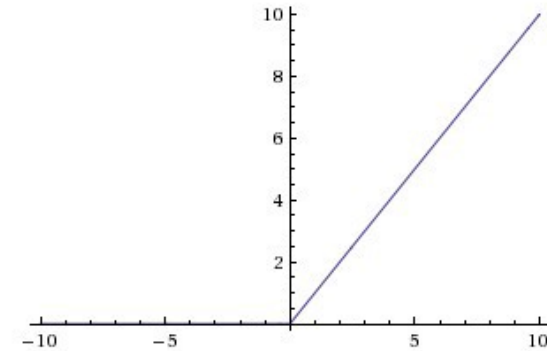
tanh function

$$\tanh(x) = \frac{2}{1+e^{-2x}} - 1$$



ReLu function

$$A(x) = \max(0, x)$$



필기체 숫자 인식에 적용

(1) 자료 준비

```
from sklearn.datasets import load_digits
```

```
X, y = load_digits(return_X_y=True)
print(len(X))
from sklearn.model_selection import train_test_split
X_train, X_test, y_train, y_test = train_test_split(X,
                                                    y,
                                                    test_size = 0.33)
```

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- 필기체 숫자 인식에 적용

- (2) 모델 import와 인스턴스화

```
from sklearn.neural_network import MLPClassifier
```

```
mlp = MLPClassifier(solver='sgd', activation='logistic',  
                    hidden_layer_sizes=(30, 10),  
                    random_state=1, max_iter=2000)
```

- 필기체 숫자 인식에 적용

- (3) 학습 데이터로 학습

```
mlp.fit(X_train,y_train)
```

```
C:\Users\user\Anaconda3\lib\site-packages\sklearn\neural_network\multilayer_perceptron.py:347: ConvergenceWarning: Stochastic Optimizer: Maximum iterations (2000) reached and the optimization was not converged.
% self.max_iter, ConvergenceWarning)
```

```
MLPClassifier(activation='logistic', alpha=0.0001, batch_size='auto',
              beta_1=0.9, beta_2=0.999, early_stopping=False, epsilon=1e-08,
              hidden_layer_sizes=(30, 10), learning_rate='constant',
              learning_rate_init=0.001, max_iter=2000, momentum=0.9,
              n_iter_no_change=10, nesterovs_momentum=True, power_t=0.5,
              random_state=1, shuffle=True, solver='sgd', tol=0.0001,
              validation_fraction=0.1, verbose=False, warm_start=False)
```

- 필기체 숫자 인식에 적용


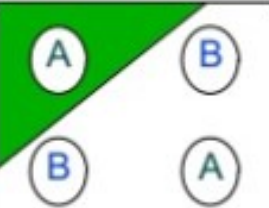


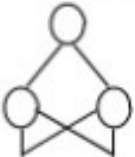
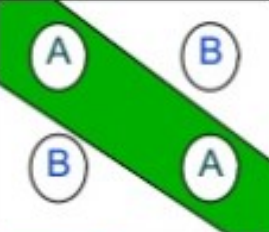


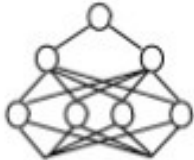
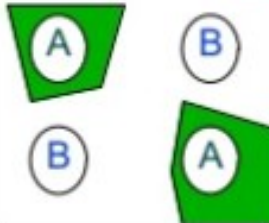


- (4) 성능 평가

```
mlp.score(X_train, y_train)
```

```
0.9891936824605154
```

```
mlp.score(X_test, y_test)
```

```
0.9579124579124579
```

Structure	Types of Decision Regions	Exclusive-OR Problem	Classes with Meshed regions	Most General Region Shape.
Single-Layer 	Half Plane Bounded By Hyperplane			
Two-Layer 	Convex Open Or Closed Regions			
Three-Layer 	Arbitrary (Complexity Limited by No. of Nodes)			

Q & A