

Minimize $f(X) = x_1^2 - x_1x_2 + x_2^2 + 2x_1 + 4x_2 + 3$
 where $-5 \leq x_1, x_2 \leq 5$

The movement of the bees is recorded in three phases

Employed Phase-

- Generate a new solution.
- Calculate new fitness.
- Apply greedy selection.

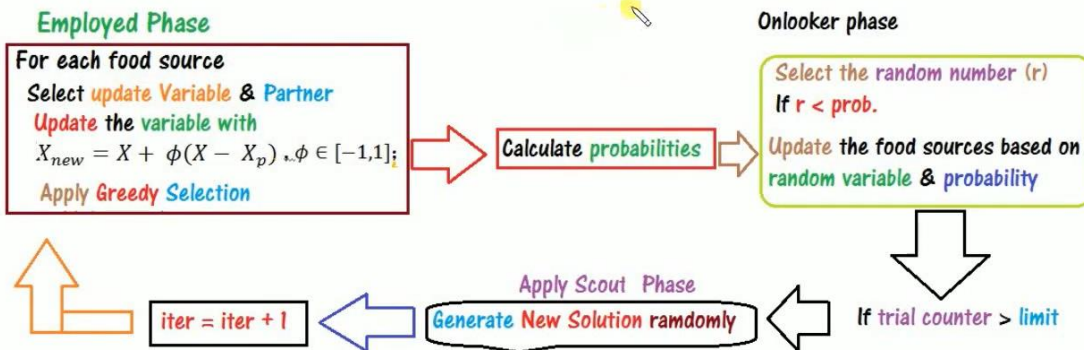
Onlooker Phase-

- Calculate the probabilities.
- Produce a new solution depending on probability.
- Calculate new fitness.
- Apply greedy selection.

Scout Phase-

- Find the abandoned solution (based on the value of limit)
- Generate a new solution randomly to replace them.

Working Rule (Algorithm)



Phases of the MATLAB Code:

Phase 1: Input parameter

Phase 2: Defining Objective & Fitness Function

Phase 3: Generate Initial Population

ABC Main ITERATION Loop Start

Phase 4: Perform Employed & Onlooker Phases

Select variable & Partner

Generate New Solution

Perform Greedy Selection

Phase 5: Memorize the Best Solution

Phase 6: Perform Scout Phase

Phase 7: Plot the result

Illustrative Example

Minimize $f(X)$

$$= x_1^2 - x_1 x_2 + x_2^2 + 2x_1 + 4x_2 + 3$$

where $-5 \leq x_1, x_2 \leq 5$

MATLAB CODE: EXPLANATION

Phase 1: Input parameter

```
%% Phase 1: Input parameters
FoodSource = 100; % Food Sources Bees
D = 2; % Dimension of the problem
lb = [-5 -5]; % Lower bound of the variables
ub = [5 5]; % Upper bound of the variables
max_iter = 100; % Maximum number of iteration
N = FoodSource./2; % Population Size
limit = (N.*D); % Used for Scoutt Phase
trial=zeros(N,1); % Initialize to ZERO
```

Illustrative Example

Minimize $f(X)$

$$= x_1^2 - x_1 x_2 + x_2^2 + 2x_1 + 4x_2 + 3$$

where $-5 \leq x_1, x_2 \leq 5$

MATLAB CODE: EXPLANATION

%% Phase 2: Defining the objective function
& Fitness function

Defining Objective Function

```
function out = fns1(X)
    x1 = X(:,1);
    x2 = X(:,2);
    out = x1.^2-x1.*x2+x2.^2+2.*x1+4.*x2+3;
end
```

Illustrative Example

Minimize $f(X)$

$$= x_1^2 - x_1 x_2 + x_2^2 + 2x_1 + 4x_2 + 3$$

where $-5 \leq x_1, x_2 \leq 5$

Maximize

$$\text{fit} = \begin{cases} \frac{1}{1+f} & ; f \geq 0 \\ 1 + |f| & ; f < 0 \end{cases}$$

MATLAB CODE: EXPLANATION

%%% Calculate fitness

```
function out = fns(X)
    x1 = X(:,1);
    x2 = X(:,2);
    fx = x1.^2-x1.*x2+x2.^2+2.*x1+4.*x2+3;
    for i=1:size(fx,1)
        if fx(i,:) >= 0
            fit(i,:) = 1./(1+fx(i,:));
        elseif fx(i,:) < 0
            fit(i,:) = 1+abs(fx(i,:));
        end
    end
    out = fit;
```

Illustrative Example

Minimize $f(X)$

$$= x_1^2 - x_1 x_2 + x_2^2 + 2x_1 + 4x_2 + 3$$

$$\text{where } -5 \leq x_1, x_2 \leq 5$$

Use $x = L + \text{rand.} * (U - L)$

MATLAB CODE: EXPLANATION

Phase 3: Generate Initial Population

%% Phase 3: Generate Initial Population randomly

```
for i=1:N
    for j = 1:D
        pos(i,j) = lb(:,j) + rand.*(ub(:,j)-lb(:,j));
    end
end
```

position

Illustrative Example

Minimize $f(X)$

fns1

$$= x_1^2 - x_1 x_2 + x_2^2 + 2x_1 + 4x_2 + 3$$

$$\text{where } -5 \leq x_1, x_2 \leq 5$$

Use $x = L + \text{rand.} * (U - L)$

fns

MATLAB CODE: EXPLANATION

Phase 3: Generate Initial Population

%% Phase 3: Generate Initial Population randomly

```
for i=1:N
    for j = 1:D
        pos(i,j) = lb(:,j) + rand.*(ub(:,j)-lb(:,j));
    end
end
```

fx = fns1(pos); %% Minimize Objective Function

fx1 = fns(pos); %% Maximize Fitness Function



Illustrative Example

Minimize $f(X)$

$$= x_1^2 - x_1 x_2 + x_2^2 + 2x_1 + 4x_2 + 3$$

$$\text{where } -5 \leq x_1, x_2 \leq 5$$

Use $x = L + \text{rand.} * (U - L)$

MATLAB CODE: EXPLANATION

Phase 3: Generate Initial Population

%% Phase 3: Generate Initial Population randomly

```
for i=1:N
    for j = 1:D
        pos(i,j) = lb(:,j) + rand.*(ub(:,j)-lb(:,j));
    end
end
```

fx = fns1(pos); %% Minimize Objective Function

fx1 = fns(pos); %% Maximize Fitness Function

Select **update Variable** & **Partner**

- **Generate** a new solution

$$X_{new} = X + \phi(X - X_p)$$

$$\phi \in [-1,1];$$

- **Calculate** new fitness.

- Apply **greedy selection**
(accept **new solution** if it is **better**).

$$f_{new} < f_{old};$$



Employed bee Phase:

Employed bee Phase:

Select the random variable to change:

Select the random partner:

Create a new food location:

Perform greedy selection:

Trial Value:

food Source

.....
.....
.....
.....
.....

Employed bee Phase:

1st employed bee: [3.1472 -4.0246]

Select the random variable to change:

Let it be 1 : [3.1472 -4.0246]

Select the random partner:

Let partner be 4: [4.1338 4.5751]

food Source

Maximize
 $f(x)$

3.1472	-4.0246	31.9645
4.0579	-2.2150	32.6168
-3.7301	0.4688	13.2971
4.1338	4.5751	48.6753
1.3236	4.6489	41.4537

Employed bee Phase:

Select the random variable to change:

Select the random partner:

Create a new food location:

Perform greedy selection:

Trial Value:

MATLAB CODE: EXPLANATION

Phase 4: Employed bee Phase:

```
for i=1:N
```

```
    p2c = ceil(rand*D); % Choose the Variable to change  
    partner = ceil(rand*N); % Choose the Partner
```


Employed bee Phase:

Select the random variable to change:

Select the random partner:

$$l = 1$$

Create a new food location:

Perform greedy selection:

Trial Value:

MATLAB CODE: EXPLANATION

Phase 4: Employed bee Phase:

```
for i=1:N
    p2c = ceil(rand*D); % Choose the Variable to change
    partner = ceil(rand*N); % Choose the Partner
    while(partner==i)
        partner = ceil(rand*N);
    end
```

Employed bee Phase:

Select the random variable to change:

Select the random partner:

Create a new food location:

$$X_{new} = X + \phi(X - X_p)$$

$\phi \in [-1,1];$

Perform greedy selection:

Trial Value:

MATLAB CODE: EXPLANATION

Phase 4: Employed bee Phase:

```
for i=1:N
    Xnew = pos(i,:); % For new solution "i" FoodSource
    p2c = ceil(rand*D); % Choose the Variable to change
    partner = ceil(rand*N); % Choose the Partner
    while(partner==i)
        partner = ceil(rand*N);
    end
```

Employed bee Phase:

1st employed bee: [3.1472 -4.0246]

Select the random variable to change:

Let it be 1: [3.1472 -4.0246] \times

Select the random partner

Let partner be 4: [4.1338 4.5751] \times_p

Create a new food location:

Let $\phi = 0.71$

$$X_{new} = X + \phi(X - X_p)$$

$$X_{new} = 3.1472 + 0.71(3.1472 - 4.1338) \\ = 2.4467 \in (-5, 5)$$

Thus, $X_1 = [2.4467 -4.0246]$

food Source	Maximize $f(x)$	Minimize fit	trial
$\times \rightarrow$ $\begin{bmatrix} 3.1472 & -4.0246 \\ 4.0579 & -2.2150 \\ -3.7301 & 0.4688 \\ 4.1338 & 4.5751 \\ 1.3236 & 4.6489 \end{bmatrix}$	$\begin{bmatrix} 31.9645 \\ 32.6168 \\ 13.2971 \\ 48.6753 \\ 41.4537 \end{bmatrix}$	$\begin{bmatrix} 0.0303 \\ 0.0297 \\ 0.0699 \\ 0.0201 \\ 0.0236 \end{bmatrix}$	$\begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$

food Source	Maximize $f(x)$	Minimize fit	trial
$\begin{bmatrix} \\ \\ \\ \\ \end{bmatrix}$	$\begin{bmatrix} \\ \\ \\ \\ \end{bmatrix}$	$\begin{bmatrix} \\ \\ \\ \\ \end{bmatrix}$	$\begin{bmatrix} \\ \\ \\ \\ \end{bmatrix}$

Employed bee Phase:

Select the random variable to change:

Select the random partner:

Create a new food location:

$$X_{new} = X + \phi(X - X_p) \\ \phi \in [-1, 1];$$

Perform greedy selection:

Trial Value:

MATLAB CODE: EXPLANATION

Phase 4: Employed bee Phase:

```
for i=1:N
    Xnew = pos(i,:); % For new solution "i" FoodSource
    p2c = ceil(rand*D); % Choose the Variable to change
    partner = ceil(rand*N); % Choose the Partner

    while(partner==i)
        partner = ceil(rand*N);
    end

    X = pos(i,p2c);
    Xp = pos(partner,p2c);
    Xnew(p2c) = X + (rand-0.5).*2.*(X-Xp);
```

Employed bee Phase:

Select the random variable to change:

Select the random partner:

Create a new food location:

$$X_{new} = X + \phi(X - X_p) \\ \phi \in [-1, 1];$$

Perform greedy selection:

Trial Value:

MATLAB CODE: EXPLANATION

Phase 4: Employed bee Phase:

```
Xnew(p2c) = X + (rand-0.5).*2.*(X-Xp);

%%% Check the bounds
for j = 1:D
    if Xnew(j) > ub(j)
        Xnew(j) = ub(j);
    elseif Xnew(j) < lb(j)
        Xnew(j) = lb(j);
    end
end
```

Employed bee Phase:

Select the random variable to change:

Select the random partner:

Create a new food location:

$$X_{new} = X + \phi(X - X_p)$$

$$\phi \in [-1, 1];$$

Perform greedy selection:

$$f_{new} < f_{old};$$

Minimization

Trial Value:

MATLAB CODE: EXPLANATION

Phase 4: Employed bee Phase:

```

Xnew(p2c) = X + (rand-0.5).*2.*(X-Xp);

%%% Perform Greedy Selection
fnew = fns1(Xnew);    fns1 → Min
if fnew < fx(i,:)
    pos(i,:) = Xnew;
    fx(i,:) = fnew;
    trial(i)=0;
else
    trial(i)=trial(i) + 1;
end

```

● Calculate probabilities

Select the random number (r)

If $r < \text{prob.}$

● New solution is generated with the help of partner solution (X_p) by

$$X_{new} = X + \phi(X - X_p)$$

$$\phi \in [-1, 1];$$

● Perform greedy selection:

$$f_{new} < f_{old};$$

then Update the solution, otherwise NOT

Onlooker phase



MATLAB CODE: EXPLANATION

%%%%% ONLOOKER BEE PHASE START %%%%%%%%%

Calculate probabilities

Select the random number (r)

If $r < \text{prob.}$ ⇒

```

prob = fx./sum(fx);

for i=1:N
    if (rand < prob(i))

```


MATLAB CODE: EXPLANATION

Calculate **probabilities**

Select the random number (r)

If $r < \text{prob.}$

- New solution is generated with the help of partner solution (X_p) by

$$X_{\text{new}} = X + \phi(X - X_p)$$

$$\phi \in [-1, 1];$$

```
%%%%% ONLOOKER BEE PHASE START %%%%%%%%%
```

```
prob = fx./sum(fx);

for i=1:N
    if(rand<prob(i))
        Xnew = pos(i,:);
        p2c = ceil(rand*D);
        partner = ceil(rand*N);
        while(partner==i)
            partner=ceil(rand*N);
        end
        X = pos(i,p2c);
        Xp = pos(partner,p2c);
        Xnew(p2c) = X + (rand-0.5).*2.*(X-Xp);
```

MATLAB CODE: EXPLANATION

Calculate **probabilities**

Select the random number (r)

If $r < \text{prob.}$

- New solution is generated with the help of partner solution (X_p) by

$$X_{\text{new}} = X + \phi(X - X_p)$$

$$\phi \in [-1, 1];$$

- Perform **greedy selection**:

$$f_{\text{new}} < f_{\text{old}};$$

then Update the solution, otherwise NOT

```
%%% Check the bounds
```

```
for j = 1:D
    if Xnew(j)>ub(j)
        Xnew(j) = ub(j);
    elseif Xnew(j)<lb(j)
        Xnew(j) = lb(j);
    end
end
```

```
%%% Perform Greedy Selection
```

```
fnew = fns1(Xnew);
if fnew < fx(i,:)
    pos(i,:) = Xnew;
    fx(i,:) = fnew;
    trial(i)=0;
else
    trial(i)=trial(i)+1;
end
```

Memorize the best answer

Display Output

MATLAB CODE: EXPLANATION

```
%% MEMORIZE THE BEST SOLUTION SO FAR
```

```
[fxval, fxind] = min(fx);
```

```
Gbest = pos(fxind,:);
```

```
Xbest(iter,:) = Gbest;
```

```
Fbest(iter) = fxval;
```

```
Fbest1(iter) = fns1(Gbest);
```

```
% Show Iteration Information
```

```
disp(['Iteration ' num2str(iter) ':  
Best Cost = ' num2str(Fbest(iter))]);
```

Scout Phase-

Find the abandoned solution
(based on the value of limit)

- Generate a new solution
randomly to replace them.

MATLAB CODE: EXPLANATION

```
H = find(trial>limit);
```

```
if length(H)>0
```

```
%%% Generate Population randomly for such "H"
```

```
for j = 1:D
```

```
pos(H,j) = lb(:,j) + rand.*(ub(:,j)-lb(:,j));
```

```
end
```

```
fx(H,:)=fns1(pos(H,:));
```

```
end
```

MATLAB CODE: EXPLANATION

Phase 7: Plot the result

```
plot(Fbest1, 'r','LineWidth', 2);
```

```
xlabel('Iteration');
```

```
ylabel('Fitness Value');
```

```
grid on;
```