Vole Simulations

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To look at the sensitivity of the prey population to the model parameters, we can run the model for a variety of different parameters and look how the curve changes. For this simulation, we will set a variety of r values for population runs for vole populations.

Population growth rates

From the literature review (Sarah this is the average data from the model summary data), we constructed minimum, average, and maximum vole stage structured matrices. It is important to note that survival measurements are from M. townsendii and fertility measurements were from M. californicus because no studies on either species contained both measurements.

```
##          Juvenile   Adult
## Juvenile     0.69 0.07935
## Adult        0.20 0.02300

##          Juvenile Adult
## Juvenile   1.4056 1.757
## Adult      0.2800 0.350

##          Juvenile  Adult
## Juvenile   2.6896 3.3456
## Adult      0.4100 0.5100
```

Because the calculated r-values for voles is for a 10 week period, and the predator model is in a time step of seasons, we have to convert the r-value to a seasonal r. To provide some context, annual r-values are also calculated.

```
r_annual<-r_vole*5
r_annual
```

```
## [1] -1.7  2.8  5.8
```

```
if(r_annual[1] <0){
  r_annual[1]=0.04
}

r_vole<-r_annual/4
r_vole
```

```
## [1] 0.01 0.70 1.45
```

Parameters

We can use the pred_prey function created in our owls r-package, then use an ode solver to solve the derivatives. We will use a type two functional response to model the behavior of the prey population. A type two functional response is the simplest model to use in the wake of low data. The response will capture typical more realistic predator-prey relations. The differential equations are below:

$$\frac{dprey}{dt} = rN(1 - \frac{N}{K_{prey}}) - \frac{k_{max}N}{N + D}P$$

$$\frac{dpredator}{dt} = \beta PN - \delta P$$

The model requires multiple parameters: r = growth rate of prey pop (voles/season) This value is extracted from the population matrices using the popbio package to calculate lambda, then r=ln(lambda)

K_prey = carrying capacity of prey (voles)

alpha = attack rate of predator (or capture efficiency; the larger alpha is, the more the per capita growth rate of the prey population is depressed by the addition of a single predator) (units=1/season) The attack rate was calculated from Derting and Cranford (1989). They found that, on average, it takes 1.1 attacks/vole - for this analysis, we assume the attack rate is the same for gophers as for voles. If there are 11 successful attacks per night the average number observed in observations recorded in Bunn et al (1982), then there should be 12.1 total attacks per night. If there is one foraging event per night, and 90 foraging events per season, then we expect 1089 attacks per season. However, this is if there are a significant amount of gophers across the landscape (scaling up from the Derting and Cranford densities, we get over 3000 voles/ha, an unreasonable number). Therefore, we would expect attack rate to decrease with density of the prey population. In sensitivity analysis if the attack rate is less than three, there is coexistence between gopher and owl populations.

h = handling time The amount of time it takes an owl to kill and eat a single vole (1/k_max) (season/vole)

beta= assimilation efficiency (efficiency of turning voles into per capita growth) This number is calculated from field data and represents the fractional value of one vole to an owl producing 4.33 chicks.

delta = death rate of predator (#predator/season)

k_max = maximum feeding rate the most gophers an owl can eat in a single time unit (voles/season). Calculated from empirical data.

D = half saturation constant (1/(alpha*handling time)) The abundance of prey at which the feeding rate is half maximal (gopher)

State variables: N = starting population of prey P = starting population of predator

For this model, time is in terms of season (3 months), so each time interval is represented by a season and four seasons are equivalent to one year.

```
#Parameters
alpha=0.924
beta = 5.85e-4
delta=0.01
K_prey=1000
k_max=654
h=1/k_max
D=1/(alpha*h)
r=r_vole
parameters <- c(r, alpha, beta, delta, K_prey, k_max, D)


#State variables:
N=c(1000, 1000, 1000, 1000,
    500, 500, 500, 500,
    100, 100, 100, 100,
    50, 50, 50, 50,
    10, 10, 10, 10,
```

```
    2,2,2,2)

P=c(0.2, 0.6, 1.0, 2.0,
    0.2, 0.6, 1.0, 2.0,
    0.2, 0.6, 1.0, 2.0,
    0.2, 0.6, 1.0, 2.0,
    0.2, 0.6, 1.0, 2.0,
    0.2, 0.6, 1.0, 2.0)
state<-cbind(N, P)
times<- seq(0, 20, by=1)
```

Simulations, K=1000

We can then run simulations for these various lists of r values while varying predator density.
Then, plotting the prey density over time by each N.

Table 1: N init= 1000

time	N	P	r	K
20	103.4838525	0.2	0.01	1000
20	0.0758022	0.6	0.01	1000
20	0.0000471	1.0	0.01	1000
20	0.0000000	2.0	0.01	1000
20	882.5026540	0.2	0.70	1000
20	558.0738901	0.6	0.70	1000
20	22.0978975	1.0	0.70	1000
20	0.0000003	2.0	0.70	1000
20	945.4359045	0.2	1.45	1000
20	823.2433694	0.6	1.45	1000
20	673.4597085	1.0	1.45	1000
20	0.7047271	2.0	1.45	1000

Table 2: N init= 500

time	N	P	r	K
20	29.4834972	0.2	0.01	1000
20	0.0189370	0.6	0.01	1000
20	0.0000116	1.0	0.01	1000
20	0.0000000	2.0	0.01	1000
20	882.4941322	0.2	0.70	1000
20	556.2628238	0.6	0.70	1000
20	12.3803347	1.0	0.70	1000
20	0.0000001	2.0	0.70	1000
20	945.4359046	0.2	1.45	1000
20	823.2433702	0.6	1.45	1000
20	673.4595437	1.0	1.45	1000
20	0.4041669	2.0	1.45	1000

Table 3: N init= 100

time	N	P	r	K
20	3.4817734	0.2	0.01	1000
20	0.0021530	0.6	0.01	1000
20	0.0000014	1.0	0.01	1000
20	0.0000000	2.0	0.01	1000
20	882.4148792	0.2	0.70	1000
20	527.3028903	0.6	0.70	1000
20	1.4656075	1.0	0.70	1000
20	0.0000000	2.0	0.70	1000
20	945.4359050	0.2	1.45	1000
20	823.2433674	0.6	1.45	1000
20	673.4576415	1.0	1.45	1000
20	0.0462896	2.0	1.45	1000

Table 4: N init= 50

time	N	P	r	K
20	1.6249005	0.2	0.01	1000
20	0.0010028	0.6	0.01	1000
20	0.0000006	1.0	0.01	1000
20	0.0000000	2.0	0.01	1000
20	882.3040262	0.2	0.70	1000
20	471.8783943	0.6	0.70	1000
20	0.6464220	1.0	0.70	1000
20	0.0000000	2.0	0.70	1000
20	945.4359053	0.2	1.45	1000
20	823.2433580	0.6	1.45	1000
20	673.4538861	1.0	1.45	1000
20	0.0201641	2.0	1.45	1000

Table 5: N init= 10

time	N	P	r	K
20	0.3074352	0.2	0.01	1000
20	0.0001895	0.6	0.01	1000
20	0.0000001	1.0	0.01	1000
20	0.0000000	2.0	0.01	1000
20	881.2755878	0.2	0.70	1000
20	181.9658510	0.6	0.70	1000
20	0.1163967	1.0	0.70	1000
20	0.0000000	2.0	0.70	1000
20	945.4359067	0.2	1.45	1000
20	823.2432767	0.6	1.45	1000
20	673.4025138	1.0	1.45	1000
20	0.0035947	2.0	1.45	1000

Table 6: N init= 2

time	N	P	r	K
20	0.0608062	0.2	0.01	1000
20	0.0000375	0.6	0.01	1000
20	0.0000000	1.0	0.01	1000
20	0.0000000	2.0	0.01	1000
20	875.1766209	0.2	0.70	1000
20	37.3432558	0.6	0.70	1000
20	0.0227883	1.0	0.70	1000
20	0.0000000	2.0	0.70	1000
20	945.4359110	0.2	1.45	1000
20	823.2428164	0.6	1.45	1000
20	672.8986207	1.0	1.45	1000
20	0.0007024	2.0	1.45	1000

N= 1000 , K= 1000

N= 500 , K= 1000

N= 100 , K= 1000

N= 50 , K= 1000

N= 10 , K= 1000
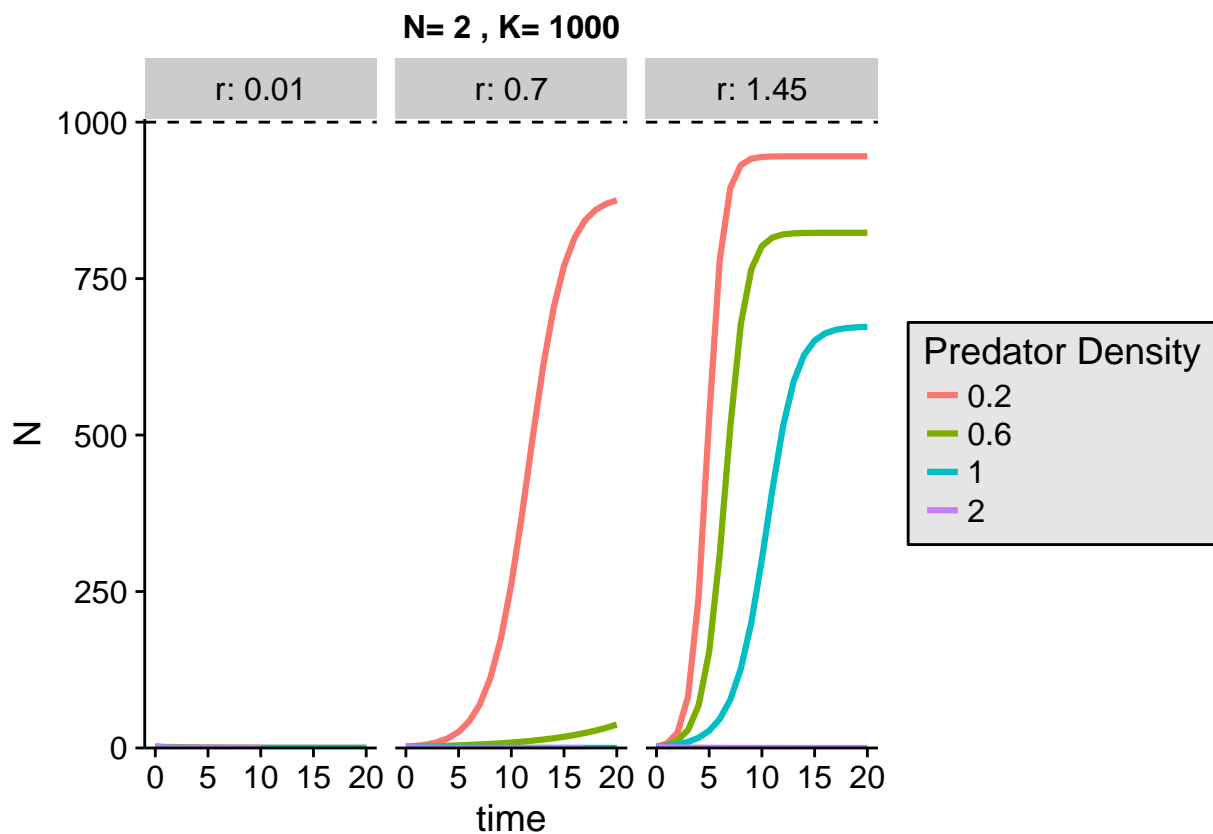
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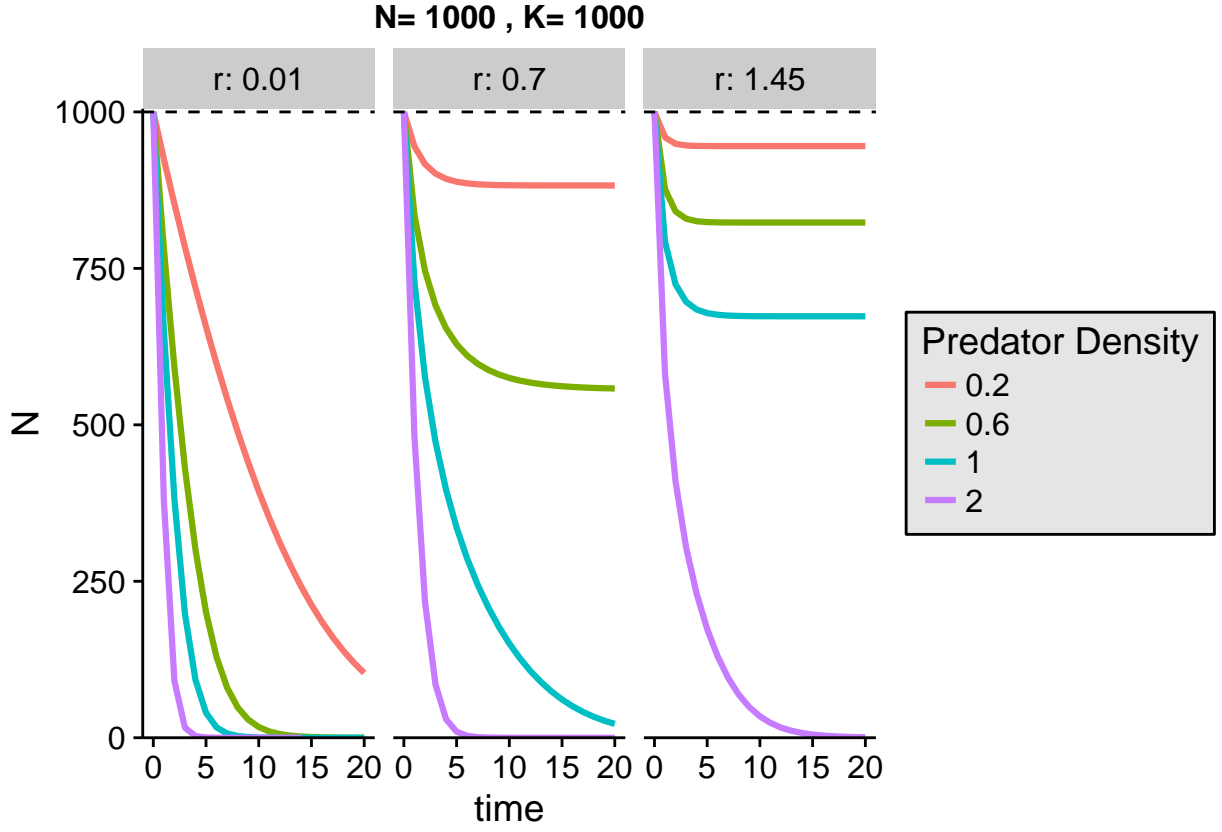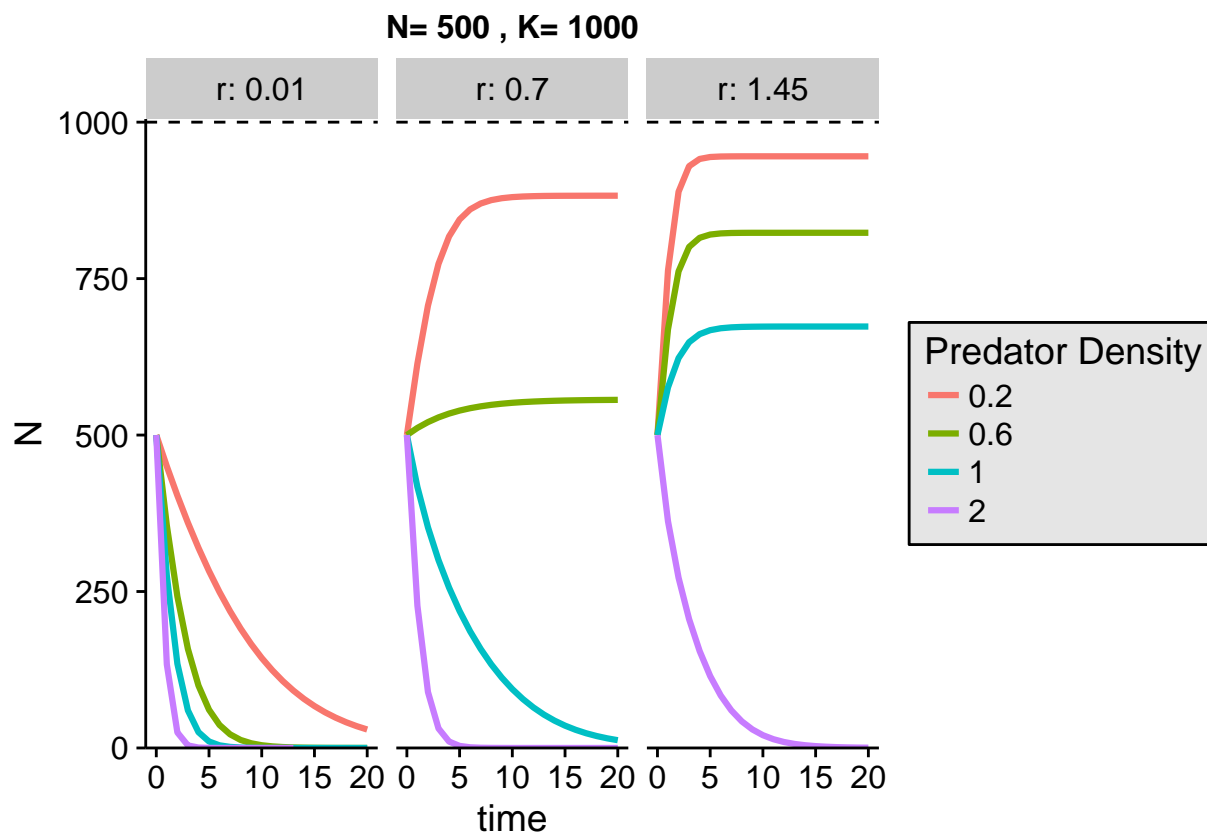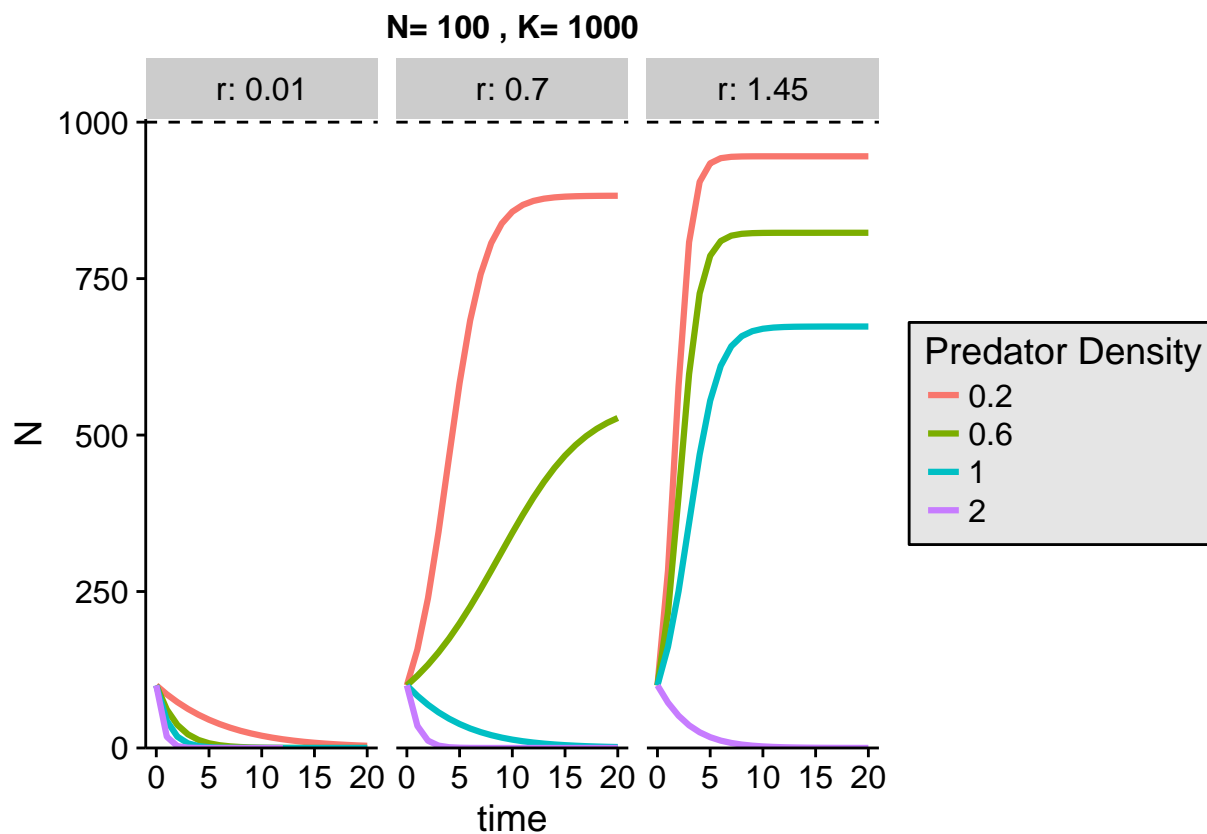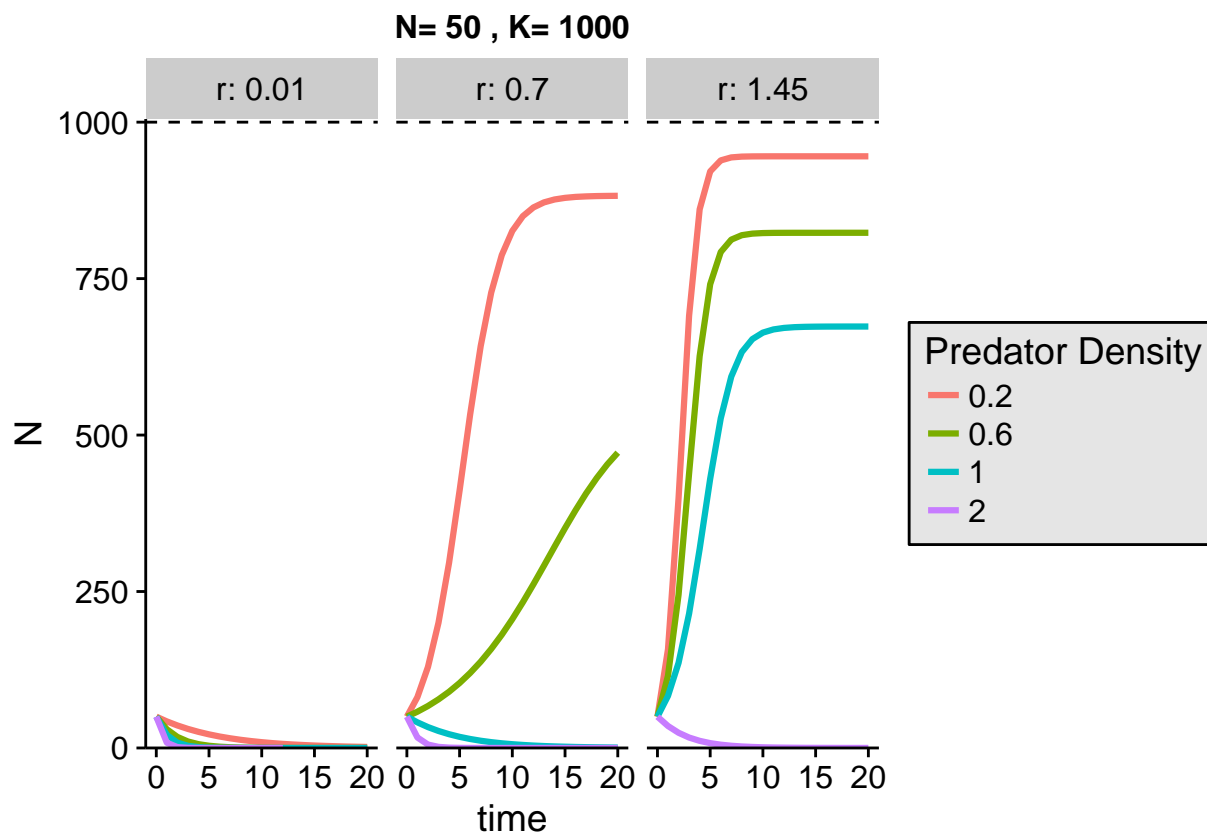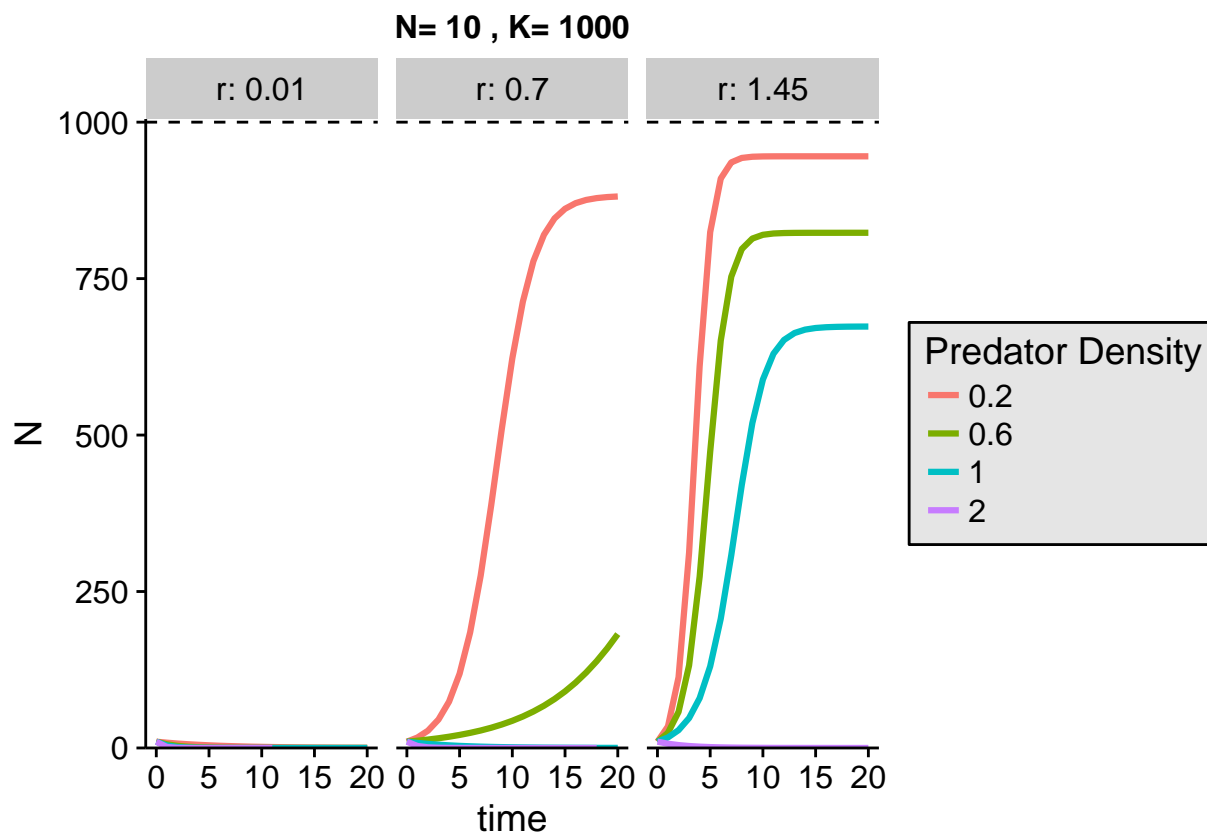
Simulations, K=500

Suppose we want to investigate what happens when the carrying capacity is lower, K=500

Table 7: N init= 1000

time	N	P	r	K
20	90.5719356	0.2	0.01	500
20	0.0717841	0.6	0.01	500
20	0.0000454	1.0	0.01	500
20	0.0000000	2.0	0.01	500
20	416.9368246	0.2	0.70	500
20	191.2085679	0.6	0.70	500
20	3.9433627	1.0	0.70	500
20	0.0000001	2.0	0.70	500
20	461.4242088	0.2	1.45	500
20	375.0403836	0.6	1.45	500
20	269.1644121	1.0	1.45	500
20	0.1063642	2.0	1.45	500

Table 8: N init= 500

time	N	P	r	K
20	28.0897855	0.2	0.01	500
20	0.0186169	0.6	0.01	500
20	0.0000116	1.0	0.01	500
20	0.0000000	2.0	0.01	500
20	416.9333910	0.2	0.70	500
20	190.2868357	0.6	0.70	500
20	3.1974633	1.0	0.70	500
20	0.0000001	2.0	0.70	500
20	461.4242089	0.2	1.45	500
20	375.0403838	0.6	1.45	500
20	269.1640230	1.0	1.45	500
20	0.0885016	2.0	1.45	500

Table 9: N init= 100

time	N	P	r	K
20	3.4598060	0.2	0.01	500
20	0.0021485	0.6	0.01	500
20	0.0000014	1.0	0.01	500
20	0.0000000	2.0	0.01	500
20	416.9039673	0.2	0.70	500
20	180.9699936	0.6	0.70	500
20	1.0510705	1.0	0.70	500
20	0.0000000	2.0	0.70	500
20	461.4242090	0.2	1.45	500
20	375.0403792	0.6	1.45	500
20	269.1598635	1.0	1.45	500
20	0.0313617	2.0	1.45	500

Table 10: N init= 50

time	N	P	r	K
20	1.6200868	0.2	0.01	500
20	0.0010018	0.6	0.01	500
20	0.0000006	1.0	0.01	500
20	0.0000000	2.0	0.01	500
20	416.8650334	0.2	0.70	500
20	168.4652334	0.6	0.70	500
20	0.5498547	1.0	0.70	500
20	0.0000000	2.0	0.70	500
20	461.4242091	0.2	1.45	500
20	375.0403706	0.6	1.45	500
20	269.1538632	1.0	1.45	500
20	0.0166709	2.0	1.45	500

Table 11: N init= 10

time	N	P	r	K
20	0.3072623	0.2	0.01	500
20	0.0001895	0.6	0.01	500
20	0.0000001	1.0	0.01	500
20	0.0000000	2.0	0.01	500
20	416.5312895	0.2	0.70	500
20	101.3697501	0.6	0.70	500
20	0.1128176	1.0	0.70	500
20	0.0000000	2.0	0.70	500
20	461.4242096	0.2	1.45	500
20	375.0403039	0.6	1.45	500
20	269.0953945	1.0	1.45	500
20	0.0034648	2.0	1.45	500

Table 12: N init= 2

time	N	P	r	K
20	0.0607995	0.2	0.01	500
20	0.0000375	0.6	0.01	500
20	0.0000000	1.0	0.01	500
20	0.0000000	2.0	0.01	500
20	414.7314566	0.2	0.70	500
20	31.9364559	0.6	0.70	500
20	0.0226477	1.0	0.70	500
20	0.0000000	2.0	0.70	500
20	461.4242112	0.2	1.45	500
20	375.0399614	0.6	1.45	500
20	268.7314597	1.0	1.45	500
20	0.0006973	2.0	1.45	500

N= 1000 , K= 500

N= 500 , K= 500

N= 100 , K= 500

N= 50 , K= 500

N= 10 , K= 500

N= 2 , K= 500
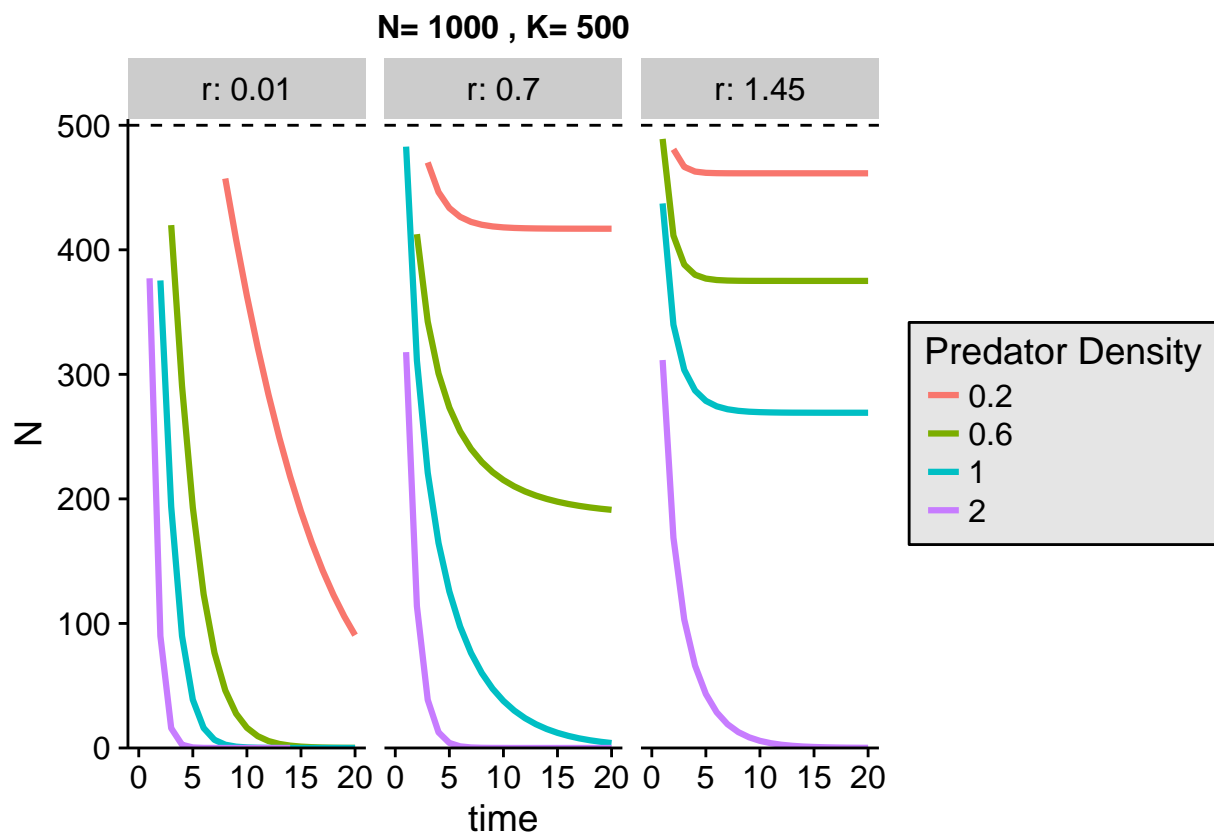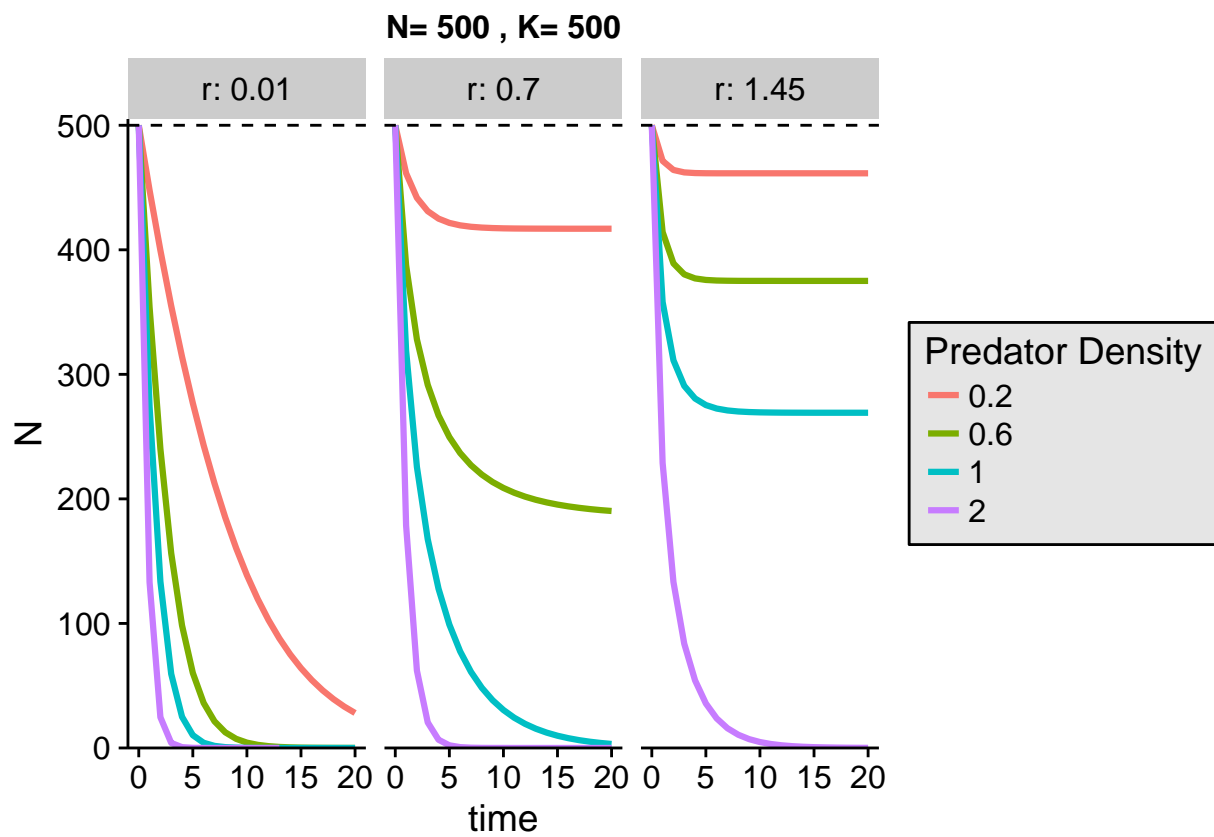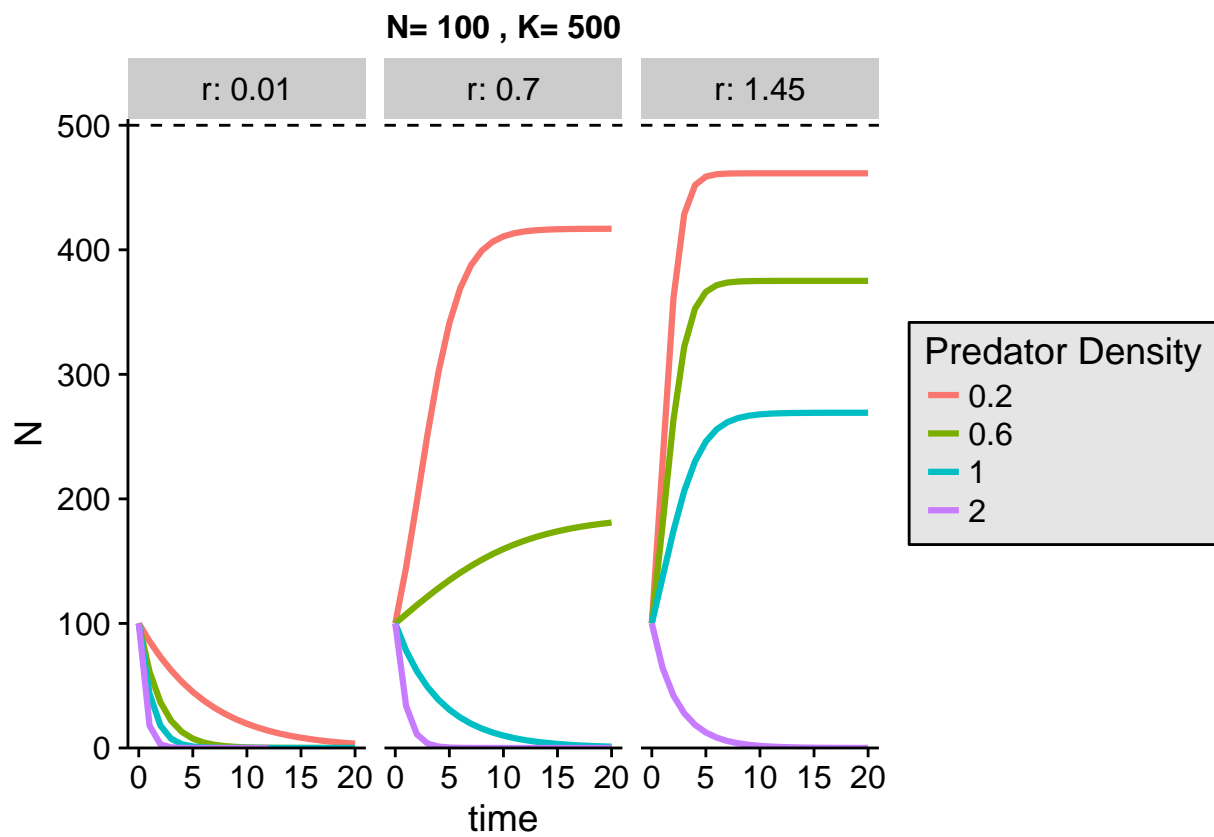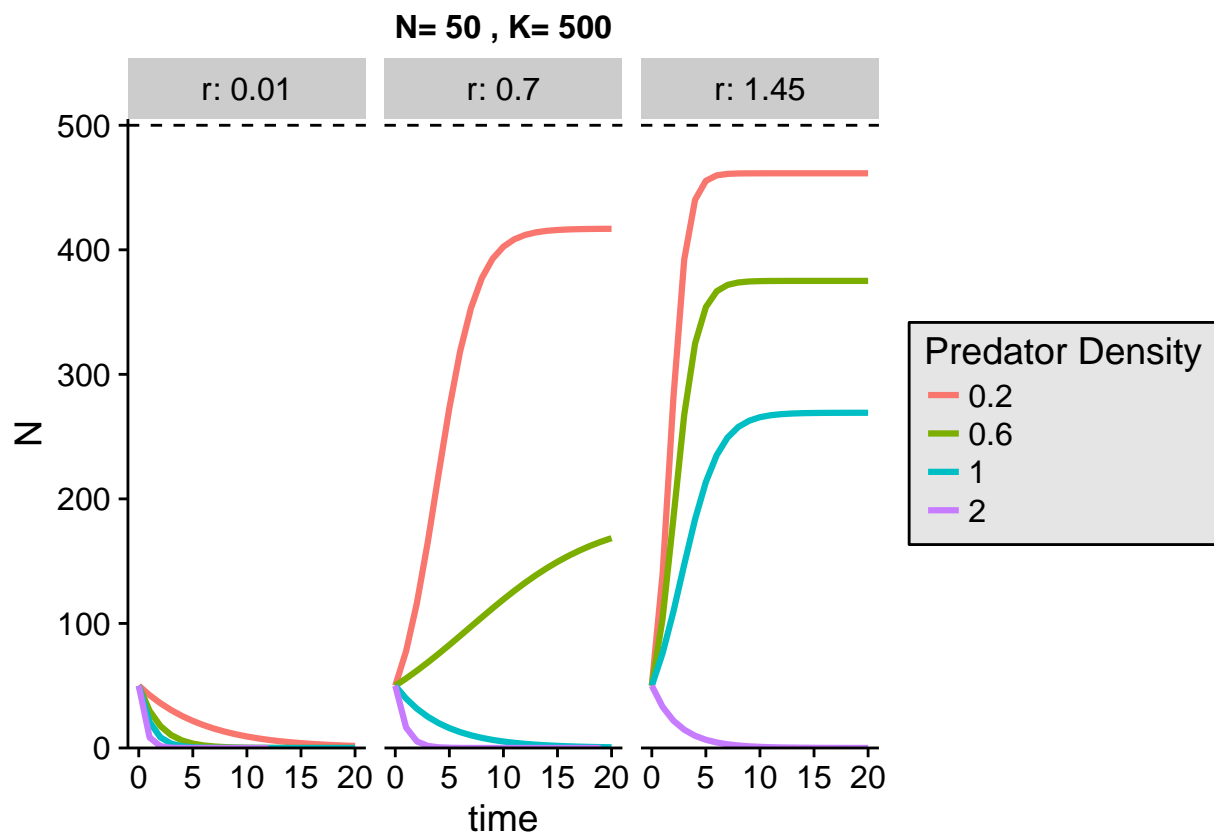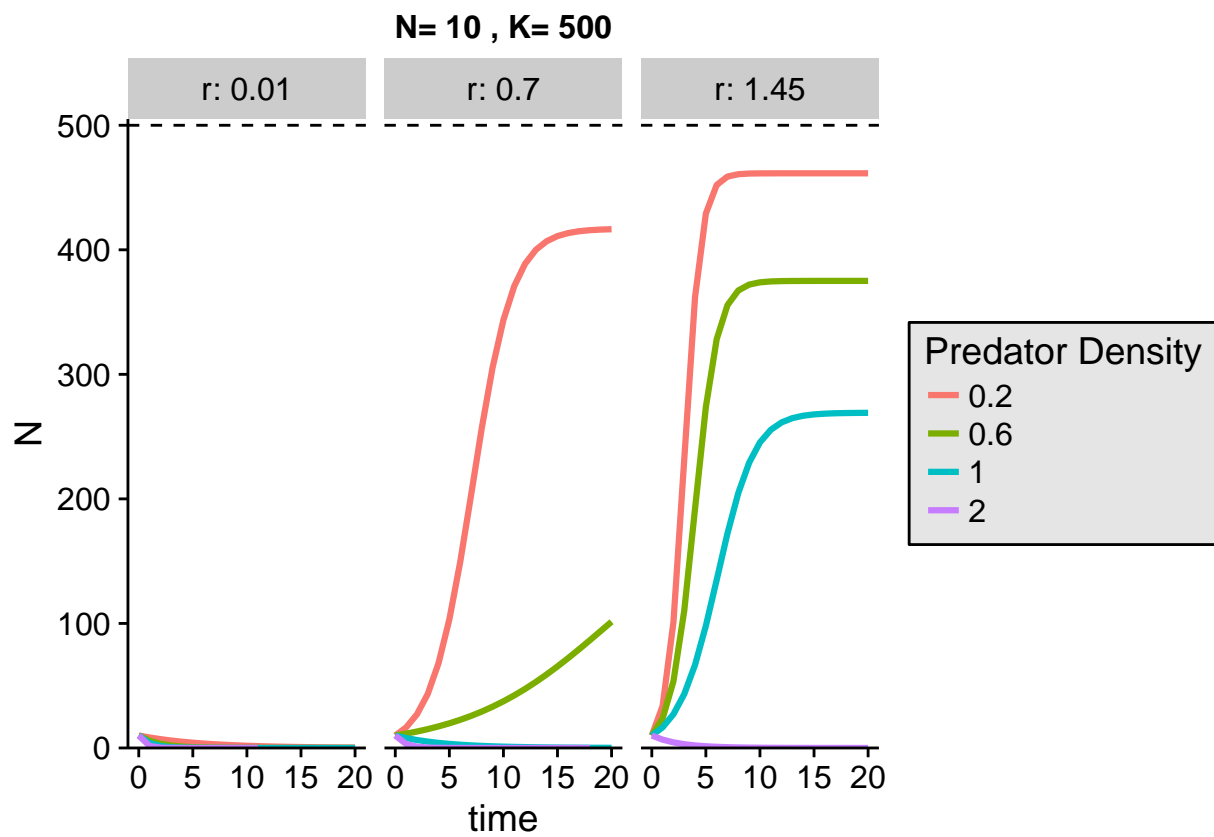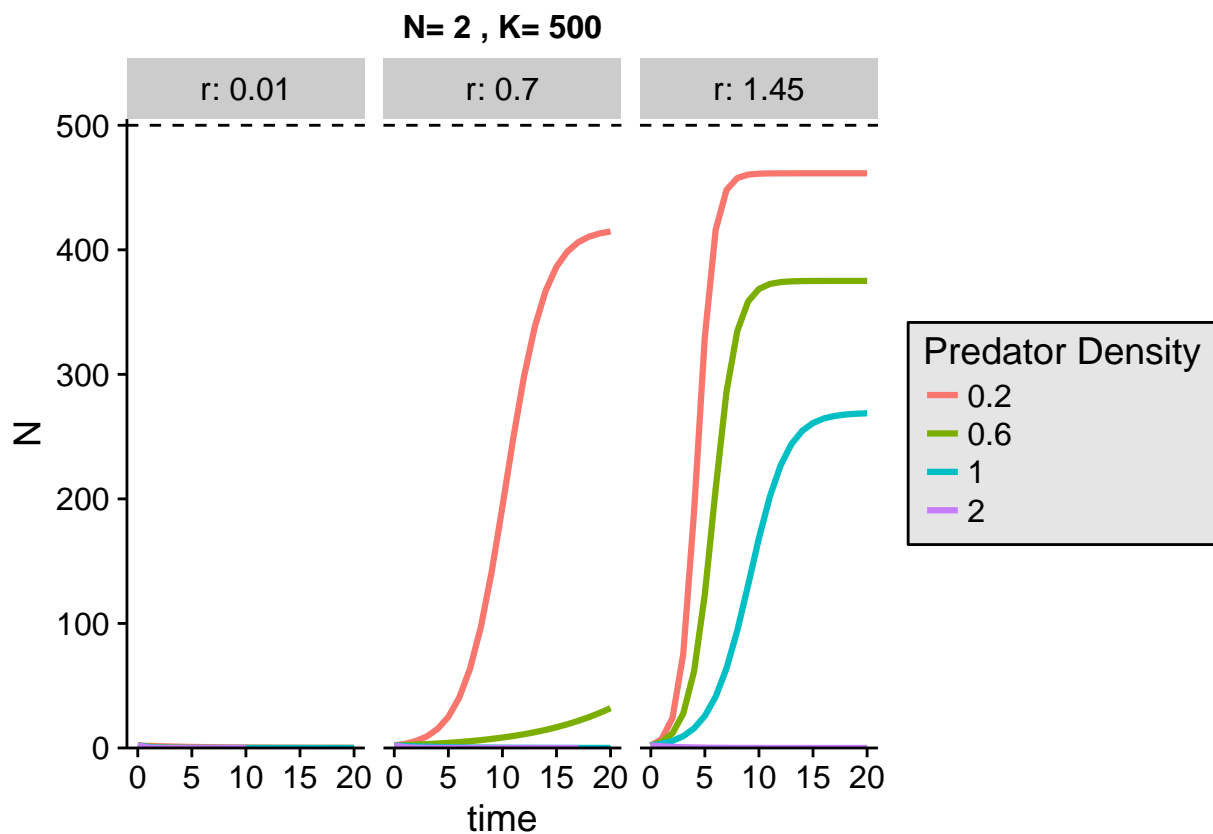
Simulations, K=100

Changing K to 100

Table 13: N init= 1000

time	N	P	r	K
20	43.6190383	0.2	0.01	100
20	0.0498990	0.6	0.01	100
20	0.0000359	1.0	0.01	100
20	0.0000000	2.0	0.01	100
20	76.1671467	0.2	0.70	100
20	24.6048707	0.6	0.70	100
20	0.4248779	1.0	0.70	100
20	0.0000000	2.0	0.70	100
20	88.6741103	0.2	1.45	100
20	64.9805617	0.6	1.45	100
20	39.6577900	1.0	1.45	100
20	0.0111134	2.0	1.45	100

Table 14: N init= 500

time	N	P	r	K
20	20.3139367	0.2	0.01	100
20	0.0163913	0.6	0.01	100
20	0.0000108	1.0	0.01	100
20	0.0000000	2.0	0.01	100
20	76.1669611	0.2	0.70	100
20	24.5743773	0.6	0.70	100
20	0.4107002	1.0	0.70	100
20	0.0000000	2.0	0.70	100
20	88.6741103	0.2	1.45	100
20	64.9805616	0.6	1.45	100
20	39.6577537	1.0	1.45	100
20	0.0107966	2.0	1.45	100

Table 15: N init= 100

time	N	P	r	K
20	3.2936029	0.2	0.01	100
20	0.0021129	0.6	0.01	100
20	0.0000013	1.0	0.01	100
20	0.0000000	2.0	0.01	100
20	76.1654653	0.2	0.70	100
20	24.3244794	0.6	0.70	100
20	0.3204923	1.0	0.70	100
20	0.0000000	2.0	0.70	100
20	88.6741103	0.2	1.45	100
20	64.9805611	0.6	1.45	100
20	39.6574363	1.0	1.45	100
20	0.0087059	2.0	1.45	100

Table 16: N init= 50

time	N	P	r	K
20	1.5825964	0.2	0.01	100
20	0.0009940	0.6	0.01	100
20	0.0000006	1.0	0.01	100
20	0.0000000	2.0	0.01	100
20	76.1635806	0.2	0.70	100
20	24.0137450	0.6	0.70	100
20	0.2503048	1.0	0.70	100
20	0.0000000	2.0	0.70	100
20	88.6741103	0.2	1.45	100
20	64.9805608	0.6	1.45	100
20	39.6570302	1.0	1.45	100
20	0.0069805	2.0	1.45	100

Table 17: N init= 10

time	N	P	r	K
20	0.3058866	0.2	0.01	100
20	0.0001892	0.6	0.01	100
20	0.0000001	1.0	0.01	100
20	0.0000000	2.0	0.01	100
20	76.1484703	0.2	0.70	100
20	21.7632065	0.6	0.70	100
20	0.0905426	1.0	0.70	100
20	0.0000000	2.0	0.70	100
20	88.6741104	0.2	1.45	100
20	64.9805549	0.6	1.45	100
20	39.6537902	1.0	1.45	100
20	0.0026878	2.0	1.45	100

Table 18: N init= 2

time	N	P	r	K
20	0.0607454	0.2	0.01	100
20	0.0000375	0.6	0.01	100
20	0.0000000	1.0	0.01	100
20	0.0000000	2.0	0.01	100
20	76.0725141	0.2	0.70	100
20	14.7858519	0.6	0.70	100
20	0.0215815	1.0	0.70	100
20	0.0000000	2.0	0.70	100
20	88.6741105	0.2	1.45	100
20	64.9805282	0.6	1.45	100
20	39.6374269	1.0	1.45	100
20	0.0006589	2.0	1.45	100

N= 1000 , K= 100

N= 500 , K= 100

N= 100 , K= 100

N= 50 , K= 100

N= 10 , K= 100

N= 2 , K= 100
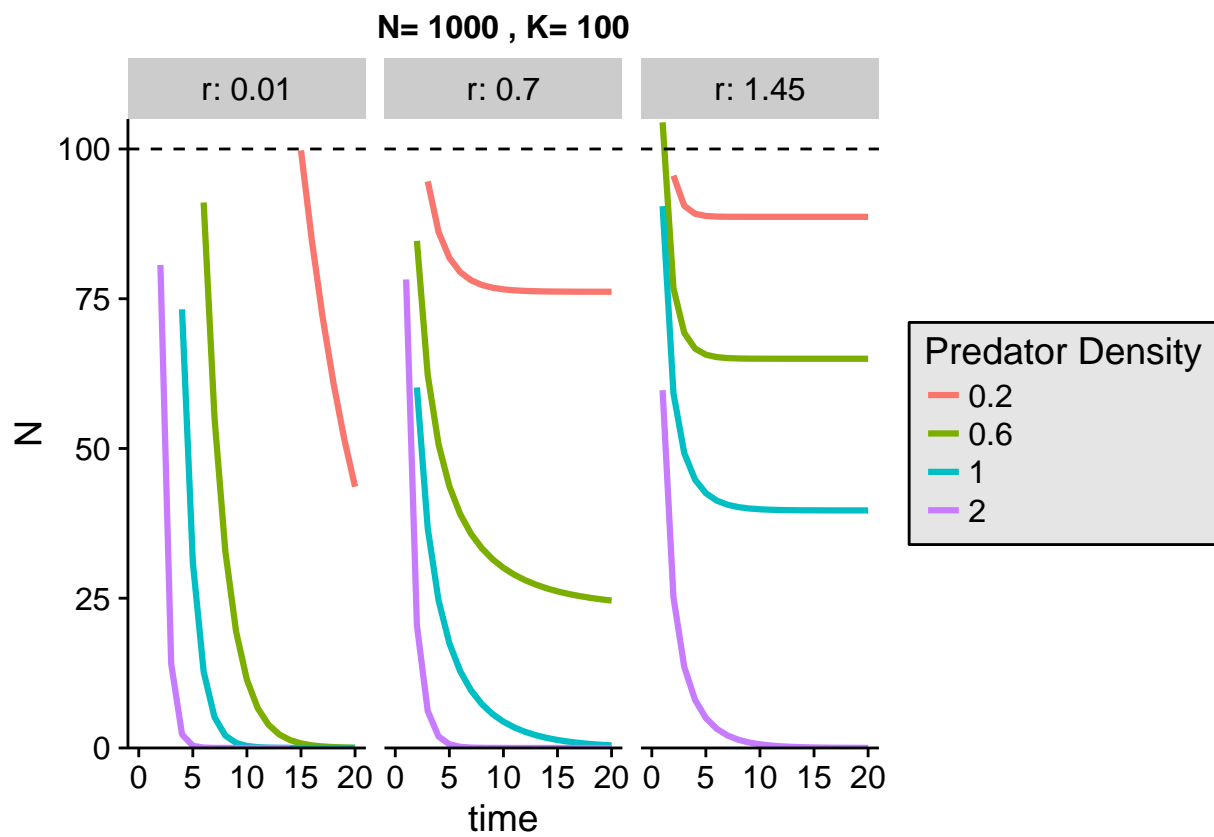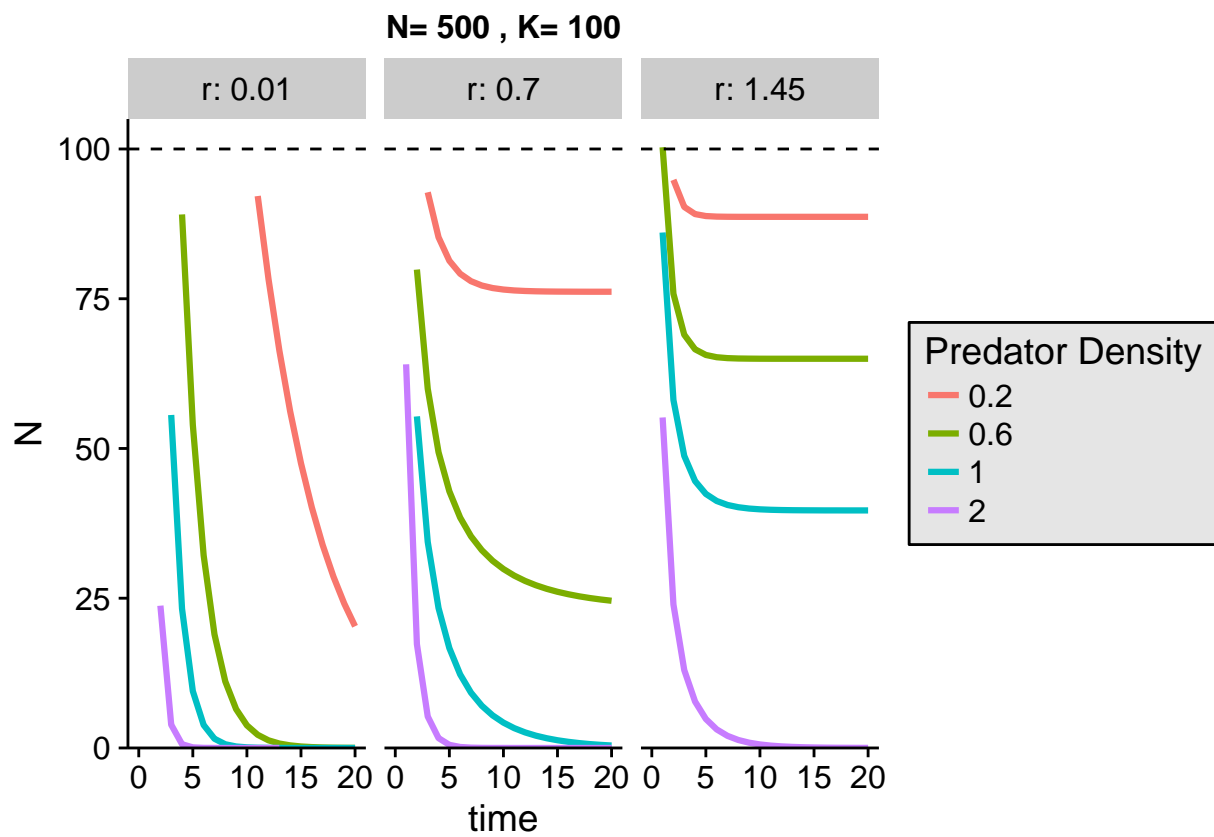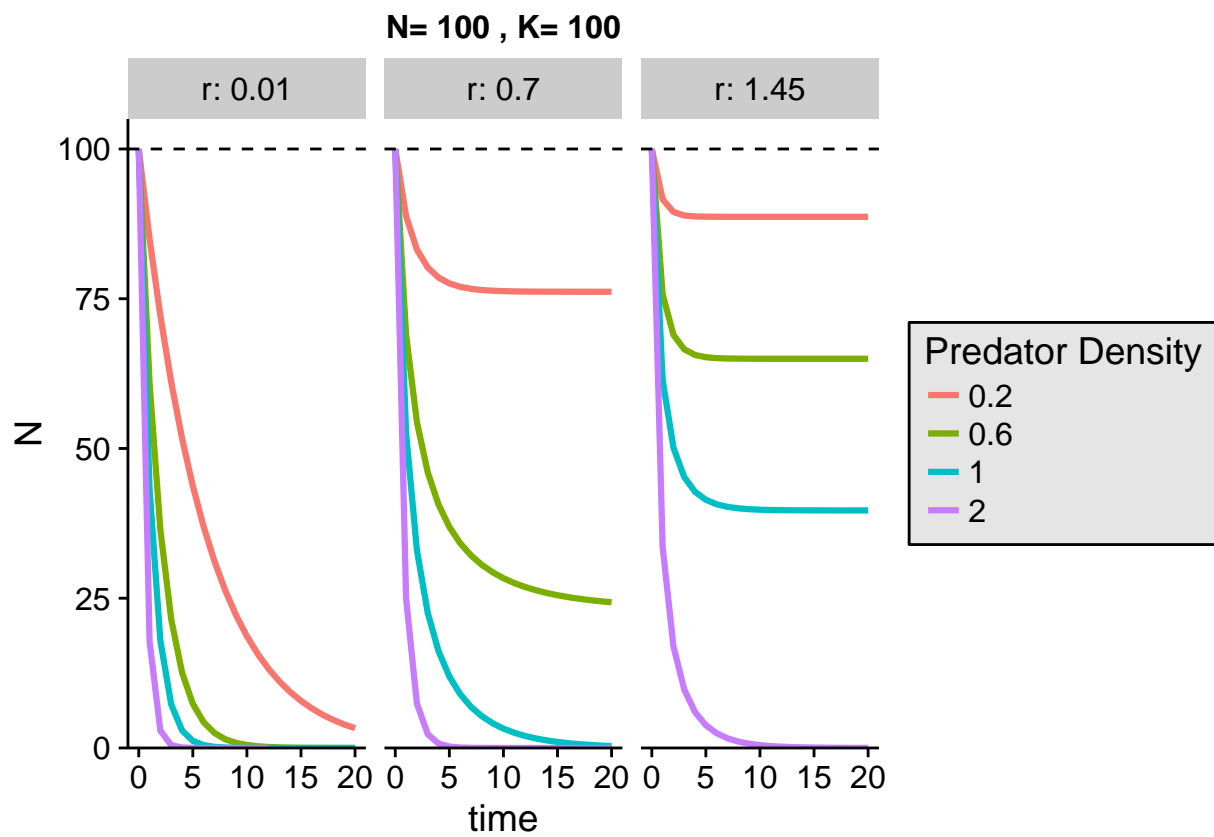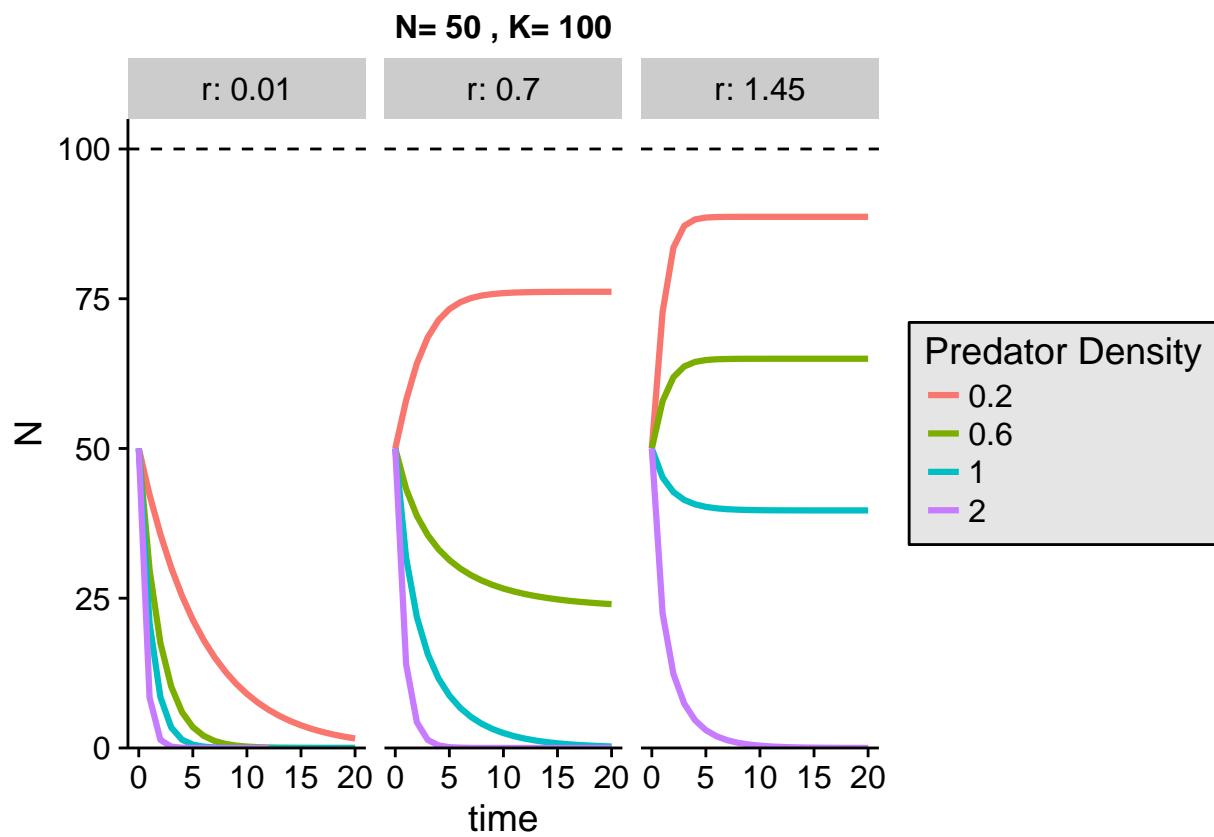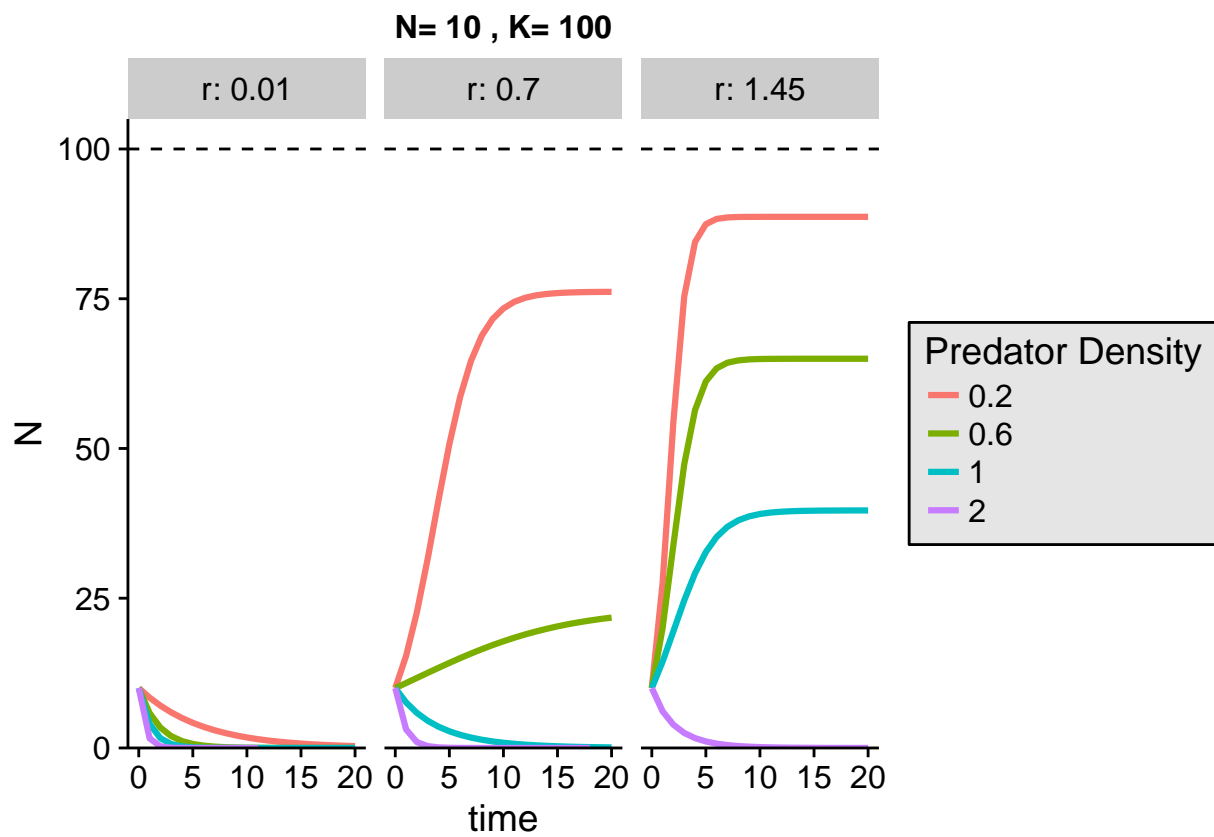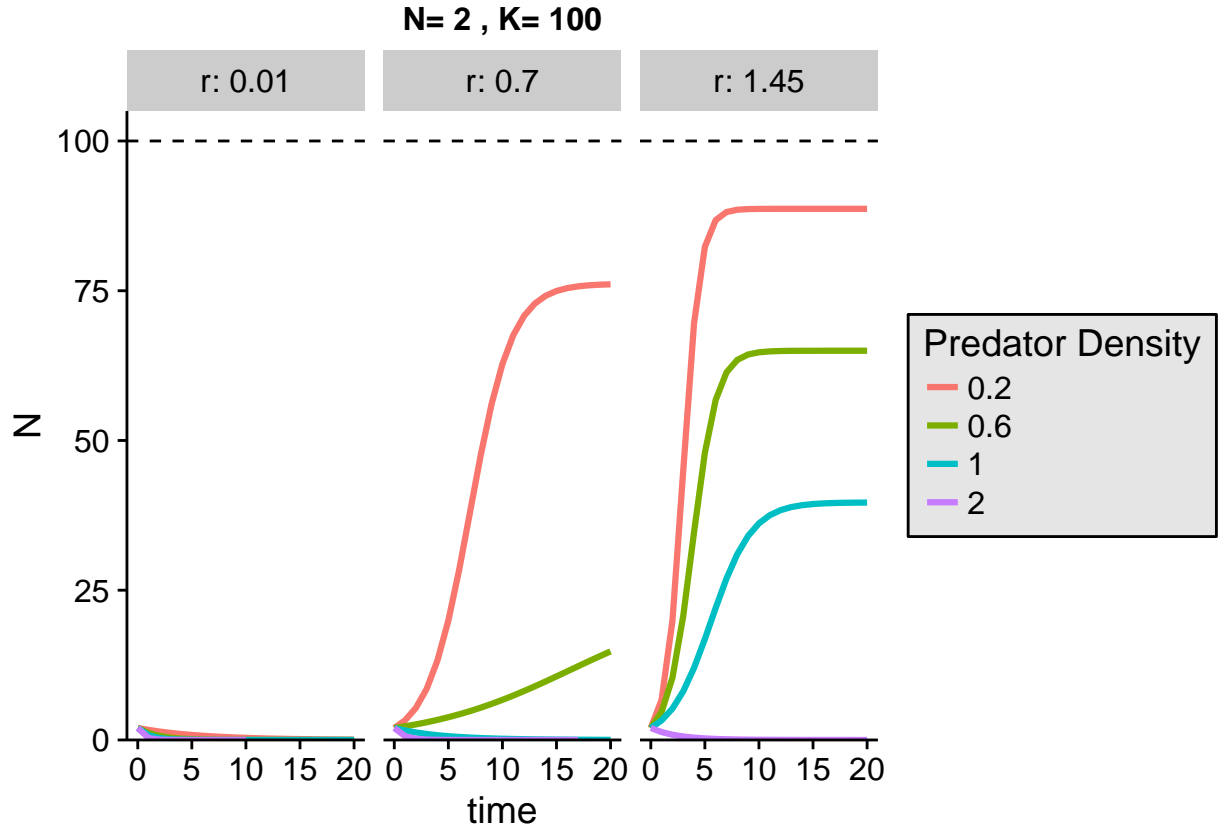
Simulations, K=50

Table 19: N init= 1000

time	N	P	r	K
20	25.6600858	0.2	0.01	50
20	0.0356347	0.6	0.01	50
20	0.0000283	1.0	0.01	50
20	0.0000000	2.0	0.01	50
20	37.4647511	0.2	0.70	50
20	11.6279922	0.6	0.70	50
20	0.1975556	1.0	0.70	50
20	0.0000000	2.0	0.70	50
20	44.0005476	0.2	1.45	50
20	31.7023201	0.6	1.45	50
20	18.9700735	1.0	1.45	50
20	0.0051634	2.0	1.45	50

Table 20: N init= 500

time	N	P	r	K
20	15.0272591	0.2	0.01	50

time	N	P	r	K
20	0.0142466	0.6	0.01	50
20	0.0000098	1.0	0.01	50
20	0.0000000	2.0	0.01	50
20	37.4647082	0.2	0.70	50
20	11.6208827	0.6	0.70	50
20	0.1943095	1.0	0.70	50
20	0.0000000	2.0	0.70	50
20	44.0005476	0.2	1.45	50
20	31.7023201	0.6	1.45	50
20	18.9700646	1.0	1.45	50
20	0.0050911	2.0	1.45	50

Table 21: N init= 100

time	N	P	r	K
20	3.1069813	0.2	0.01	50
20	0.0020701	0.6	0.01	50
20	0.0000013	1.0	0.01	50
20	0.0000000	2.0	0.01	50
20	37.4643360	0.2	0.70	50
20	11.5633775	0.6	0.70	50
20	0.1712082	1.0	0.70	50
20	0.0000000	2.0	0.70	50
20	44.0005476	0.2	1.45	50
20	31.7023200	0.6	1.45	50
20	18.9699905	1.0	1.45	50
20	0.0045670	2.0	1.45	50

Table 22: N init= 50

time	N	P	r	K
20	1.5380988	0.2	0.01	50
20	0.0009844	0.6	0.01	50
20	0.0000006	1.0	0.01	50
20	0.0000000	2.0	0.01	50
20	37.4638693	0.2	0.70	50
20	11.4917324	0.6	0.70	50
20	0.1488432	1.0	0.70	50
20	0.0000000	2.0	0.70	50
20	44.0005476	0.2	1.45	50
20	31.7023196	0.6	1.45	50
20	18.9698940	1.0	1.45	50
20	0.0040412	2.0	1.45	50

Table 23: N init= 10

time	N	P	r	K
20	0.3041842	0.2	0.01	50

time	N	P	r	K
20	0.0001887	0.6	0.01	50
20	0.0000001	1.0	0.01	50
20	0.0000000	2.0	0.01	50
20	37.4601412	0.2	0.70	50
20	10.9466196	0.6	0.70	50
20	0.0726197	1.0	0.70	50
20	0.0000000	2.0	0.70	50
20	44.0005477	0.2	1.45	50
20	31.7023183	0.6	1.45	50
20	18.9691239	1.0	1.45	50
20	0.0020994	2.0	1.45	50

Table 24: N init= 2

time	N	P	r	K
20	0.0606780	0.2	0.01	50
20	0.0000375	0.6	0.01	50
20	0.0000000	1.0	0.01	50
20	0.0000000	2.0	0.01	50
20	37.4414663	0.2	0.70	50
20	8.8439530	0.6	0.70	50
20	0.0203824	1.0	0.70	50
20	0.0000000	2.0	0.70	50
20	44.0005477	0.2	1.45	50
20	31.7023115	0.6	1.45	50
20	18.9652788	1.0	1.45	50
20	0.0006166	2.0	1.45	50

N= 1000 , K= 50

N= 500 , K= 50

N= 100 , K= 50

N= 50 , K= 50

N= 10 , K= 50

N= 2 , K= 50