

CH 13

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1e.

This distribution $\alpha_{\text{tank}} \sim \text{Normal}(0, 1)$ has more shrinkage.

2e.

$y_i \sim \text{Binomial}(1, \pi_i)$ $\text{logit}(\pi_i) = \alpha_{\text{group}[i]} + \beta x_i$ $\alpha_{\text{group}} \sim \text{Normal}(\alpha_{\text{bar}}, \sigma_\alpha)$ $\alpha_{\text{bar}} \sim \text{Normal}(0, 1.5)$ $\sigma_\alpha \sim \text{Exponential}(1)$ $\beta \sim \text{Normal}(0, 0.5)$

3e.

$y_i \sim \text{Normal}(\mu_i, \sigma)$ $\mu_i = \alpha_{\text{group}[i]} + \beta x_i$ $\alpha_{\text{group}[i]} \sim \text{Normal}(\alpha_{\text{bar}}, \sigma_\alpha)$ $\beta \sim \text{Normal}(0, 1)$ $\sigma \sim \text{Exponential}(1)$ $\alpha_{\text{bar}} \sim \text{Normal}(0, 1)$ $\sigma_\alpha \sim \text{Exponential}(1)$

4e.

$y_i \sim \text{Poisson}(\pi_i)$ $\log(\pi_i) = \alpha_{\text{group}[i]} + \beta x_i$ $\alpha_{\text{group}} \sim \text{Normal}(\alpha_{\text{bar}}, \sigma_\alpha)$ $\alpha_{\text{bar}} \sim \text{Normal}(0, 1)$ $\sigma_\alpha \sim \text{Exponential}(1)$ $\beta \sim \text{Normal}(0, 1)$

5e.

$y_i \sim \text{Poisson}(\pi_i)$ $\log(\pi_i) = \alpha_{\text{group}[i]} + \alpha_{\text{groupb}[i]} + \beta x_i$ $\alpha_{\text{group}} \sim \text{Normal}(\alpha_{\text{bar}}, \sigma_{\text{group}})$ $\alpha_{\text{groupb}} \sim \text{Normal}(0, \sigma_{\text{groupb}})$ $\alpha_{\text{bar}} \sim \text{Normal}(0, 1)$ $\sigma_{\text{group}} \sim \text{Exponential}(1)$ $\sigma_{\text{groupb}} \sim \text{Exponential}(1)$ $\beta \sim \text{Normal}(0, 1)$

1m. Revisit the Reed frog survival data, `data(reedfrogs)`, and add the predation and size treatment variables to the varying intercepts model. Consider models with either main effect alone, both main effects, as well as a model including both and their interaction. Instead of focusing on inferences about these two predictor variables, focus on the inferred variation across tanks. Explain why it changes as it does across models.

```
library(rethinking)
```

```
## Loading required package: rstan
```

```
## Loading required package: StanHeaders
```

```
##  
## rstan version 2.26.13 (Stan version 2.26.1)
```

```
## For execution on a local, multicore CPU with excess RAM we recommend calling
## options(mc.cores = parallel::detectCores()).
## To avoid recompilation of unchanged Stan programs, we recommend calling
## rstan_options(auto_write = TRUE)
## For within-chain threading using `reduce_sum()` or `map_rect()` Stan functions,
## change `threads_per_chain` option:
## rstan_options(threads_per_chain = 1)
```

```
## Do not specify '-march=native' in 'LOCAL_CPPFLAGS' or a Makevars file
```

```
## Loading required package: parallel
```

```
## Loading required package: dagitty
```

```
## rethinking (Version 2.01)
```

```
##
## Attaching package: 'rethinking'
```

```
## The following object is masked from 'package:stats':
##
##      rstudent
```

```
library(tidyr)
```

```
##
## Attaching package: 'tidyr'
```

```
## The following object is masked from 'package:rstan':
##
##      extract
```

```
library(rstan)
data(reedfrogs)
d <- reedfrogs
str(d)
```

```
## 'data.frame':   48 obs. of  5 variables:
## $ density : int  10 10 10 10 10 10 10 10 10 10 ...
## $ pred    : Factor w/ 2 levels "no","pred": 1 1 1 1 1 1 1 1 2 2 ...
## $ size    : Factor w/ 2 levels "big","small": 1 1 1 1 2 2 2 2 1 1 ...
## $ surv    : int   9 10 7 10 9 9 10 9 4 9 ...
## $ propsurv: num   0.9 1 0.7 1 0.9 0.9 1 0.9 0.4 0.9 ...
```

$dtank < -1 : nrow(d)dat < -list(S = dsurv, P = dpred, Z = dsize, tank = d$tank)$

approximate posterior

```
m13.1 <- ulam( alist( S ~ dbinom( Z, p ), S ~ dbinom( P, p ), logit(p) <- a[tank], a[tank] ~ dnorm( 0, 1.5 ) ),  
data=dat, chains=4, log_lik=TRUE )
```

$dtank < -1 : nrow(d)dat < -list(S = dsurv, P = dpred, Z = dsize, tank = d$tank)$

```
m13.2 <- ulam( alist( S ~ dbinom( Z, p ), S ~ dbinom( P, p ) logit(p) <- a[tank], a[tank] ~ dnorm( a_bar, sigma ),  
a_bar ~ dnorm( 0, 1.5 ) sigma ~ dexp( 1 ) ), data=dat, chains=4, log_lik=TRUE )
```

I think this is what the code would look like, but I can't get it to run without an error message.

2m.

I would just do:

WAIC(m13.1)

WAIC(m13.2)

3m. Cauchy distribution in place of the Gaussian distribution. Cauchy has a higher peak.

I can't figure this out, and have run out of time.