# Collatz Conjecture

#### Emily Howard

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## 1 Conjecture 1

If you take x, some number, and double x, so  $x^2$  it will take it one more term to reach 1. Example: Take x to be 100, it takes 26 terms to reach 1. So  $x^2$  would be 200 and it takes 200, 27 terms to reach 1.

#### 2 Conjecture 2

If you start with  $2^n$  it will take n+1 terms to reach 1. Example: If you start with n=1  $2^1$  would be 2 and it takes 2 terms to reach 1. And if you take n=2 it would take 3 terms to reach 1.

## 3 Conjecture 3 and proof

If you start with the equation  $a^*2^n = x$  If we start with know a and know what x if knowing a, we know that every time that you increase n by 1 x also goes up by 1. This is true because if you say that your a=100 and you know that 100 takes 26 terms to reach one. Take a=100 then x=26. So now you know a bunch of patterns that are infinitely long and there are infinitely many of them.