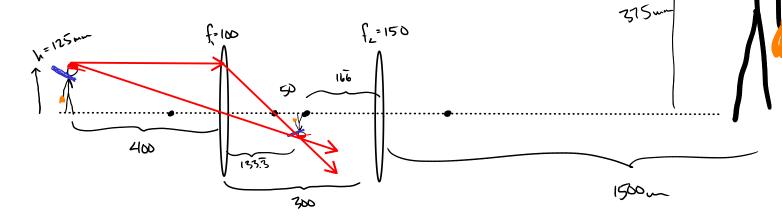
Week 14 covers sections of chapter 24 in the textbook. Topics include:

- · compound systems of lenses
- · the optics of the eye and corrective lenses
- 1. When two or more thin lenses are used in series, an image is formed by the system as a whole, but predicting where based on the geometry of the system can seem daunting. The key to understanding how to approach such a system is to know that each lens forms an image, and that images formed from a previous lens serve as the object for the next lens. This can obviously become a very tedious problem with many lenses since you have to work a separate image/object problem for each lens, but lets just stick with two for the moment. Lets use two converging lenses of focal lengths $f_1 = +100$ mm and $f_2 = +150$ mm and space them 300 mm apart (s = 300 mm). An object that is 125 mm tall and upright is located 400 mm from the first lens. Let's start a ray tracing first:



(a) Where is the image formed from the first lens only?

$$\frac{1}{P_1} + \frac{1}{q_1} = \frac{1}{f_1} = \frac{1}{P_1} = 133.3 \text{ mm}$$

- (b) Is this a real or virtual image and is it upright or inverted?
- (c) How far away is this image from the second lens? Is there a *general* equation you can use to find this? Is this a <u>real</u> or virtual object? Is it upright or inverted?

to find this? Is this a real or virtual object? Is it upright
$$P_2 = S - q_1 = 300 mm - 133.3 mm = 166.6 mm$$
Separation
blt levers

(d) Where is the image formed as a result of the second lens acting on the first image as an object?

$$\frac{1}{P_2} + \frac{1}{g_2} = \frac{1}{f_2} = \frac{1}{f_2} = \frac{1}{\frac{1}{f_2} - \frac{1}{150}} = \frac{1500 \text{ mm}}{150 - 11675}$$

(e) Is this a real image? Is it upright or inverted?

h,=125mm

b/c (weat disk is printive a) o

(f) What is the magnification from each of these stages and what are the image heights?

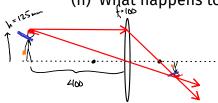
$$M_{2} = -\frac{9z}{P^{2}} = -\frac{1500}{166.6} = -\frac{9}{9}$$

$$h'_{2} = -\frac{9}{166.6} \cdot (-41.6) = 375 \text{ mm}$$

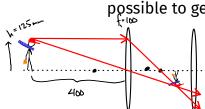
(g) What is the overall magnification? Compare this to the product of the individual magnifications.

$$M_t = \frac{h_2'}{h_1} = \frac{375m}{(25m)} = +3 = M_1 \cdot M_2 = \frac{k_1'}{h_1} \cdot \frac{h_2'}{h_2'} = \frac{h_2'}{h_1'}$$

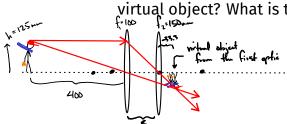
(h) What happens to the final image distance as the lenses get farther apart? $P_z = \frac{1}{2} - \frac{1}{2}$



- (i) What happens to the final image distance as the lenses get closer together? Is it possible to get a virtual final image?



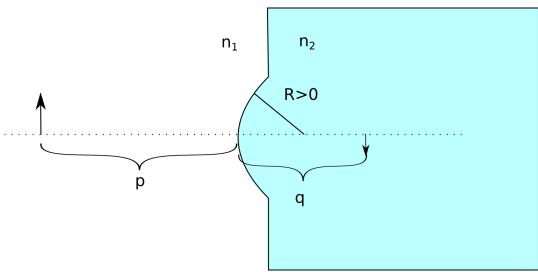
(j) What happens if you get the lenses even closer together? Is it possible to get a virtual object? What is the image when you have a virtual object? S = 100 mm



$$Q_z = \frac{100 \text{ mm} - 133.\overline{3} = -33.\overline{3}}{\frac{1}{f_z} - \frac{1}{f_z}} = \frac{1}{\frac{1}{70} - \frac{1}{-33.\overline{3}}} = \frac{27.3 \text{ ms}}{\frac{1}{70} - \frac{1}{-33.\overline{3}}}$$

2. Let's apply some of what we have learned to a model of the eye. The typical eye is around 22.5 mm in diameter. We will draw a picture of the eye with an object very far away and to the left so that the light is traveling right from the object and into the eye. The cornea and lens of the eye work together to form an image on the retina (which is the inside surface on the right in our drawing). The cornea is a spherical bulge on the surface of the eye that has a radius of curvature of about 8 mm.

Much of the convergence of light from an object to the retina is actually accomplished by the cornea, rather than the lens, which is for fine adjustment and close objects. In order to model the focusing power of the cornea, we need a slightly different equation that handles images formed by only one spherical surface (in other words half of a lens) where the image is formed *inside the material of the lens*. Here is a picture of what I mean:



This equation for this:

$$\frac{n_1}{p} + \frac{n_2}{q} = \frac{n_2 - n_1}{R}$$

where p and q have their usual meaning but $n_1 = 1$ since in this case it is air and $n_2 = 1.33$ since the inside of the eye is mostly waterish.

Now assume that the object is very far away.

(a) Where would the image be formed if only the cornea is doing any refracting?

(b) Does this image form on the retina of the eye? ($D_{\rm eye}=22.5\,{\rm mm}$) What else needs to be in the eye?

So we need additional convergence to make the image be formed exactly on the retina, but the cornea has done a lot of work.

(c) What focal length would we need from a thin lens that is positioned 5.4 mm away from the cornea in order to take the image formed by the cornea alone and instead form the image on the retina?

The lens in the eye is not symmetric but has a different radius of curvature on each side, and it has an index of refraction n=1.45 but it is immersed in the waterishness of the eye and not air, so we need to use the *lens makers equation* to see what focal length of a relaxed lens is:

$$\frac{1}{f} = \frac{(n_2 - n_1)}{n_2} \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

But note that a convex radius is positive and a concave radius is negative when approached from the left to the right. The left side of the lens has a radius of curvature of +10 mm and the right side of the lens has a radius of curvature of -6 mm. Update your drawing with this info and then work the following problem.

(d) What is the focal length of a lens with this particular geometry?

3. Now all of that was for an object very far away. The *closest* that people with normal vision can see an object clearly is about 25 cm. The cornea's shape does not change but

the lens can, so what does the focal length of the lens need to be in order to form and image from this very close object?