Week 1 covers sections 1-5 of chapter 13 in the textbook. Topics include

- temperature and measurement scales
- · measurements of amount and density
- the ideal gas law
- · kinetic theory of gas
- 1. The Celsius temperature scale is based on the *triple point* of water, but it is more common to think of it as being 0 °C when water freezes and 100 °C when water boils at 1 atm of pressure. But the Fahrenheit scale is more well known to us so lets do some conversion of common Fahrenheit temperatures. 105 °F, 98.6 °F, 72 °F, 32 °F, 0 °F. Keep going down in Fahrenheit, and see if you can find a Fahrenheit temperature that gives you the same number in Celsius. Make sure you can go backwards and convert some Celsius temperatures back to Fahrenheit.

$$T_{F} = \frac{9}{5}T_{c} + 32$$

$$L_{9} \frac{9}{5}T_{c} = T_{F} - 32$$

$$T_{c} = \frac{5}{9}(T_{F} - 32)$$

it.

TE TC

105°F 40.6°C

12°F 22

32 0

$$7$$
°F -18

 -40 °F -40 °C

2. If I only tell you a *change* in Fahrenheit temperature of a substance but not the actual temperature, then you can figure out the corresponding change in Celsius, but still not the actual temp. A change in temperature measured in Fahrenheit is 1.8 times bigger than the change measured in Celsius. So if the temperature increased by 30 °F, then by how much does the temperature change in Celsius? What does this mean about the "size" of a Celsius degree vs. the "size" of a Fahrenheit degree? Which one represents a larger change in temperature?

3. The kelvin temperature scale is designed as an *absolute* temperature scale, meaning the lowest temperature any object could theoretically be is set to 0 K. The size of a Kelvin degree is the same as the size of a Celsius degree, so that a 20 °C change in temperature is the same as a 20 K temperature change. Absolute zero in the Kelvin Scale is set to -273.15 °C. So, what is 0 °C in Kelvin? What is 20 °C in Kelvin. What is 70 K in Celsius? What is normal human body temperature in K?

$$T_{k} = T_{c} + 273.15^{\circ}C$$

$$T_{c} = T_{k} - 273.15^{\circ}C$$

4. What is absolute zero in the Fahrenheit temperature scale? Find this by using $T_C = -273.15$ first if you want, but then try using a substitution for T_C that will give you an expression for finding any Fahrenheit temperature given a Kelvin one.

$$T_{F} = \frac{9}{5}T_{c} + 32$$

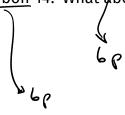
$$T_{E} = T_{K} - 273.15^{\circ}C$$

$$T_{F} = \frac{9}{5}(T_{K} - 273.15) + 32$$

$$T_{F} = \frac{9}{5}T_{K} - 491 + 32$$

$$T_{F} = \frac{9}{5}T_{K} - 459.67 \leftarrow$$

- atomic mass
- 5. What is the molecular weight of Carbon-12? Find a periodic table to help. How many protons are in Carbon-12? How many neutrons? What about the number of protons in Carbon-14? What about the number of neutrons in Carbon-14?



6. How many atoms are in a mole of Helium? How many atoms are in a mole of Carbon-12? What is the mass of a mole of Helium? What is the mass of a mole of Carbon-12?

7. What is the mass of a single CO₂ molecule? What is the mass of a mole of CO₂?

$$M_{CO_2} = \frac{44 \text{ g}}{6.022.18^3} = 7.1.10 \text{ g} = 7.1.10 \text{ kg}$$

8. What is the mass of a mole of dry air which is 78% N_2 , 21% O_2 , and 1% Ar?

9. A balloon is filled with 0.4 mol of helium so that its volume is 0.010 m³.

$$N = 0.4 \text{ mol} \cdot 6.022 \cdot 10^{23} \text{ He atoms}$$

$$N = 2.4 \cdot 10^{23} \text{ He atoms}$$

29 g/mol

• Find the number density.

number density.

Number density =
$$\frac{N}{V} = \frac{2.4 \cdot 10^{23} \text{ atoms}}{0.010 \text{ m}^3} = 2.4 \cdot 10^{25} \text{ He atoms/m}^3$$

· Find the mass density.

the mass density.

M = 4 a. 0.4 mol

Mass density =
$$f = \frac{M}{V}$$

= 1.6 a = 0.0016 kg

 $f = \frac{0.0016 \, \text{kg}}{0.010 \, \text{m}^3} = 0.16 \, \text{kg}$

• Estimate the average distance between atoms. To do this, fine the *volume per particle*, and then treat that volume like a cube and find the side length of the cube. Draw a picture of this model and use that to justify your approximation.

Draw a picture of this model and use that to justify your approximation.

$$\frac{1}{N} = \frac{1}{2 \cdot 4 \cdot 10^{25} \text{ He obs}} = 4.16 \cdot 10^{26} \text{ m}^{3}$$

$$\Delta = 3.46 \cdot 10^{9} \text{ m}$$

$$\Delta = 3.5 \text{ nm} = 35 \text{ A}$$

- 10. You have a pound of feathers and a pound of lead.
 - · Which one weighs more? same
 - · Which one has more mass? sawe
 - · Which one has the greater volume? feathers
 - · Which one contains a larger number of moles? bad question
 - · Which one contains a larger number of atoms? feathers
 - . Which one contains a larger number of protons and neutrons?

11. You check your car tire pressure and see that the pressure is 25 lb/in². What is this in Pascal? (You'll need to look up a conversion factor). This is a gauge pressure, so what is the absolute pressure in the tire?

25 pri .
$$\frac{1}{14.7} \frac{\text{atm}}{\text{pri}} \cdot \frac{1.013 \cdot 10^5 \, \text{Pa}}{1 \, \text{atm}} = 1.7 \cdot 10^5 \, \text{Pa}$$

$$\Rightarrow P_{abs} = P_{gauge} + P_{atm}$$

$$= 1.7 \cdot 10^5 \, \text{Fa}$$

$$P_{abs} = 2.7 \cdot 10^5 \, \text{Fa}$$

12. You check you car tire pressure when it is 15 °C and it is $\frac{25 \text{ lb}}{\text{in}^2}$. By what factor do you increase the number of particles in the tire so that the pressure becomes that 30 lb/in²? (Hint: The volume and temperature do not change.)

$$\frac{P_{2}V_{2}=N_{2}V_{6}V_{2}}{P_{1}V_{1}=N_{1}V_{6}V_{1}} = \sum_{i=1}^{N_{2}} \frac{P_{2}}{P_{1}} = \frac{N_{2}}{N_{1}}$$

$$\frac{N_{2}}{N_{1}} = \frac{44.7 p_{5}i}{39.7 p_{5}i} = 1.13$$

13. The gas pressure inside of a 1 liter sealed container at room temperature is 1 atm. How

many molecules are inside? How many moles of molecules? I deal Gas Law

1 L.
$$\frac{1000 \text{ mL}}{1 \text{ mL}}$$
. $\frac{1 \text{ cm}^3}{100 \text{ cm}^3} = 0.001 \text{ m}^3$
 $\frac{1 \text{ cm}^3}{100 \text{ cm}^3} = \frac{1.013 \cdot 10^5 \text{ Pa}}{100 \text{$

pressure when the temperature rises to 200 K?

PV=NkgT

$$P = (Nkg) T$$
 $P_{2} = \frac{T_{2}}{T_{1}} = \frac{200}{100} = 2$
 $P_{2} = 2 \cdot P_{1}$
 $P_{2} = 2 \cdot latm = 2 \cdot 10^{5} P_{0}$

15. If the pressure inside a tank is 1 atm when the temperature is 100 °C, then what is the pressure when the temperature rises to 200 °C? CAREFUL! >272K

$$\frac{P_{2}}{P_{1}} = \frac{T_{2}}{T_{1}} = \frac{473}{373} = 1.24$$

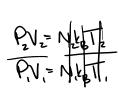
$$\frac{P_{2}}{P_{1}} = 1.24$$

$$\frac{P_{2}}{P_{1}} = 1.24$$

$$\frac{P_{2}}{P_{1}} = 1.26 \text{ atm}$$

$$\frac{P_{2}}{P_{1}} = 1.24 \cdot 10^{5} \text{ Pa}$$
5

16. A gas is in a sealed container. By what factor does the pressure change if



• the volume is doubled?

$$\frac{P_2 V_2}{P_1 V_1} = 1$$

$$\frac{P_2 V_2}{P_1 V_2} = \frac{V_1}{V_2} = \frac{1}{2}$$

$$\frac{V_2}{V_1} = \frac{1}{2}$$

$$P = N k_B T$$

• the temperature is tripled?

$$\frac{P_{i}}{P_{i}} = \frac{T_{2}}{T_{i}} = 3$$

$$PV = Nk_BT$$

$$P = Nk_BT$$

$$V$$

$$P = Nk_BT$$

$$V$$

$$P = Nk_BT$$

$$V$$

$$P = V^{-1}$$

$$P = V^{-1}$$

$$V = (2)^{-1} = \frac{1}{2}$$

• the volume is double and the temperature is tripled?

$$\frac{P_2}{p} = \frac{T_2}{T_1} \cdot \left(\frac{V_2}{V_1}\right)^2 = 3 \cdot (2)^2 = 3 \cdot \frac{1}{2} = \frac{3}{2}$$

• the volume is halved?

$$\frac{P_2}{P_1} = \begin{bmatrix} V_2 \\ V_1 \end{bmatrix}^T = \begin{bmatrix} \frac{1}{2} \end{bmatrix}^T = 2$$

17. You are standing in a room at atmospheric pressure and room temperature. You estimate the room to be 10 m wide by 15 m long by 2 m high. How many moles of gas are in the room?

$$PV = NLT$$

$$R = \frac{PV}{2T} = \frac{1.15 (a.300m^3)}{9.317 \text{ mod}} = 12,300 \text{ mod}$$

18. RT, later, I mol, how big? show me

$$W = nRT = \frac{1 \text{ mol} \cdot 8.31 \cdot 293}{1 \cdot 10^5 P_a} = 0.024 \text{ m}^3$$

V_{rus} =
$$\sqrt{\frac{3k_BT}{m}}$$

mass of an particle in kg

$$V_{\text{rms}} = \sqrt{\frac{3 \cdot 1.38 \cdot 10^{23} \cdot 293 \,\text{k}}{5.31 \cdot 10^{24} \,\text{ks}}}$$

$$= 418 \, \text{m/s}$$

$$V_{rms} = \left(\frac{3k_BT}{m}\right)^{1/2} = \left(3k_B^{1/2}T^{1/2}m^{-1/2}\right)$$

$$V_{rms} \propto T^{1/2} \quad \text{for same } m$$

$$V_{rms} \propto T^{1/2} \quad \text{for conclust } T$$

$$\frac{V_{o_1}}{V_{i_1}} = \left(\frac{T_{i_2}}{T_{i_1}}\right)^{1/2}$$

$$\frac{V_{o_2}}{V_{i_1}} = \left(\frac{M_{o_2}}{M_{N_2}}\right)^{-1/2}$$