

Week 1 covers sections 1-5 of chapter 13 in the textbook. Topics include

- temperature and measurement scales
- measurements of amount and density
- the ideal gas law
- kinetic theory of gas

1. The Celsius temperature scale is based on the *triple point* of water, but it is more common to think of it as being 0 °C when water freezes and 100 °C when water boils at 1 atm of pressure. But the Fahrenheit scale is more well known to us so let's do some conversion of common Fahrenheit temperatures. 105 °F, 98.6 °F, 72 °F, 32 °F, 0 °F. Keep going down in Fahrenheit, and see if you can find a Fahrenheit temperature that gives you the same number in Celsius. Make sure you can go backwards and convert some Celsius temperatures back to Fahrenheit.

$$T_F = \frac{9}{5} T_C + 32$$

$$\hookrightarrow \frac{9}{5} T_C = T_F - 32$$

$$T_C = \frac{5}{9} (T_F - 32)$$

T_F	T_C
105 °F	40.6 °C
98.6 °F	37 °C
72 °F	22
32	0
0 °F	-18
-40 °F	-40 °C

$$T = \frac{9}{5} T + 32$$

$$T = -40$$

2. If I only tell you a *change* in Fahrenheit temperature of a substance but not the actual temperature, then you can figure out the corresponding change in Celsius, but still not the actual temp. A change in temperature measured in Fahrenheit is 1.8 times bigger than the change measured in Celsius. So if the temperature increased by 30 °F, then by how much does the temperature change in Celsius? What does this mean about the "size" of a Celsius degree vs. the "size" of a Fahrenheit degree? Which one represents a larger change in temperature?

$$\Delta T_F = \frac{9}{5} \Delta T_C$$

$$\frac{5}{9} \Delta T_F = \Delta T_C$$

3. The kelvin temperature scale is designed as an *absolute* temperature scale, meaning the lowest temperature any object could theoretically be is set to 0 K. The size of a Kelvin degree is the same as the size of a Celsius degree, so that a 20°C change in temperature is the same as a 20 K temperature change. Absolute zero in the Kelvin Scale is set to -273.15°C . So, what is 0°C in Kelvin? What is 20°C in Kelvin. What is 70 K in Celsius? What is normal human body temperature in K?

$$T_K = T_C + \underline{273.15^\circ\text{C}}$$

$$T_C = T_K - 273.15^\circ\text{C}$$

T_C	T_K
0°C	273.15 K
20°C	293.15 K
-203°C	70 K
37°C	310 K

$$\underline{\Delta T_C = \Delta T_K}$$

4. What is absolute zero in the Fahrenheit temperature scale? Find this by using $T_C = -273.15$ first if you want, but then try using a substitution for T_C that will give you an expression for finding any Fahrenheit temperature given a Kelvin one.

$$T_F = \frac{9}{5}T_C + 32$$

$$T_F = \frac{9}{5}(-273.15) + 32$$

$$= -459^\circ\text{F}$$

$$T_F = \frac{9}{5}T_C + 32$$

$$T_C = T_K - 273.15^\circ\text{C}$$

$$T_F = \frac{9}{5}(T_K - 273.15) + 32$$

$$T_F = \frac{9}{5}T_K - 491 + 32$$

$$T_F = \frac{9}{5}T_K - 459$$

5. What is the ~~molecular weight~~ ^{atomic mass} of Carbon-12? Find a periodic table to help. How many protons are in Carbon-12? How many neutrons? What about the number of protons in Carbon-14? What about the number of neutrons in Carbon-14?

6p

6p

6n

8n

$$\text{atomic mass} - \# \text{ of protons} = \# \text{ of neutrons}$$

$$12 - 6p = 6n$$

6. How many atoms are in a mole of Helium? How many atoms are in a mole of Carbon-12? What is the mass of a mole of Helium? What is the mass of a mole of Carbon-12?

1 mole of things = $6.022 \cdot 10^{23}$ things

4g

12g

7. What is the mass of a single CO_2 molecule? What is the mass of a mole of CO_2 ?

$$12\text{g} + 2(16\text{g}) = 44\text{g/mol} \quad (\text{kg})$$

→ mass of one thing \times number of things = total mass of the collection

$$m_{\text{CO}_2} = \frac{44\text{g}}{6.022 \cdot 10^{23} \text{ molecules}} = 7.1 \cdot 10^{-23} \frac{\text{g}}{\text{molecule}} = 7.1 \cdot 10^{-26} \text{ kg}$$

8. What is the mass of a mole of dry air which is 78% N_2 , 21% O_2 , and 1% Ar?

$$\downarrow 28\text{g/mol} \cdot 0.78 = \underline{\hspace{2cm}}$$

$$32\text{g/mol} \cdot 0.21 = \underline{\hspace{2cm}}$$

$$40\text{g/mol} \cdot 0.01 = \underline{\hspace{2cm}}$$

$$29\text{g/mol}$$

9. A balloon is filled with 0.4 mol of helium so that its volume is 0.010 m^3 .

- Find the number of atoms.

$$\rightarrow N = n \cdot N_A \leftarrow \text{Avogadro's}$$

\uparrow number of particles \uparrow number of moles

$$N = 0.4 \text{ mol} \cdot 6.022 \cdot 10^{23} \text{ He atoms/mol}$$

$$N = 2.4 \cdot 10^{23} \text{ He atoms}$$

- Find the number density.

$$\text{number density} = \frac{N}{V} = \frac{2.4 \cdot 10^{23} \text{ atoms}}{0.010 \text{ m}^3} = 2.4 \cdot 10^{25} \text{ He atoms/m}^3$$

- Find the mass density.

$$\text{mass density} = \rho = \frac{M}{V}$$

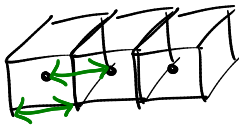
$$M = 4 \frac{\text{g}}{\text{mol}} \cdot 0.4 \text{ mol}$$

$$= 1.6\text{g} = 0.0016 \text{ kg}$$

$$\rho = \frac{0.0016 \text{ kg}}{0.010 \text{ m}^3} = \underline{\underline{0.16 \text{ kg/m}^3}}$$

- Estimate the average distance between atoms. To do this, find the *volume per particle*, and then treat that volume like a cube and find the side length of the cube. Draw a picture of this model and use that to justify your approximation.

$$\frac{N}{V} \rightarrow \frac{V}{N} = \frac{1}{2.4 \cdot 10^{25} \text{ He atoms/m}^3} = 4.16 \cdot 10^{-26} \text{ m}^3/\text{particle} \leftarrow \text{Volume of cube}$$



$$V_{\text{cube}} = \Delta^3$$

$$\Delta = \sqrt[3]{V}$$

$$\Delta = 3.46 \cdot 10^{-9} \text{ m}$$

$$\Delta = 3.5 \text{ nm} = 35 \text{ \AA}$$

10. You have a pound of feathers and a pound of lead.

- Which one weighs more? *same*
- Which one has more mass? *same*
- Which one has the greater volume? *feathers*
- Which one contains a larger number of moles? *bad question*
- Which one contains a larger number of atoms? *feathers*
- Which one contains a larger number of protons and neutrons? *same*

11. You check your car tire pressure and see that the pressure is 25 lb/in². What is this in Pascal? (You'll need to look up a conversion factor). This is a gauge pressure, so what is the absolute pressure in the tire?

$$25 \text{ psi} \cdot \frac{1 \text{ atm}}{14.7 \text{ psi}} \cdot \frac{1.013 \cdot 10^5 \text{ Pa}}{1 \text{ atm}} = 1.7 \cdot 10^5 \text{ Pa}$$

$$\rightarrow P_{\text{abs}} = P_{\text{gauge}} + P_{\text{atm}}$$

$$= 1.7 \cdot 10^5 \text{ Pa} + 1.013 \cdot 10^5 \text{ Pa}$$

$$P_{\text{abs}} = 2.7 \cdot 10^5 \text{ Pa}$$

12. You check your car tire pressure when it is 15 °C and it is 25 lb/in². By what factor do you increase the number of particles in the tire so that the pressure becomes that 30 lb/in²? (Hint: The volume and temperature do not change.)

$$\frac{P_2 V_2 = N_2 k_B T_2}{P_1 V_1 = N_1 k_B T_1} \Rightarrow \frac{P_2}{P_1} = \frac{N_2}{N_1}$$

$$\downarrow$$

$$\frac{N_2}{N_1} = \frac{44.7 \text{ psi}}{39.7 \text{ psi}} = 1.13$$

$$\% \Delta = \left(\frac{N_2 - N_1}{N_1} \right) \times 100$$

$$\% \Delta = \left(\frac{N_2}{N_1} - 1 \right) \times 100$$

$$\% \Delta = +13\%$$

13% increase

$$44.7 \text{ psi}$$

13. The gas pressure inside of a 1 liter sealed container at room temperature is 1 atm. How many molecules are inside? How many moles of molecules? Ideal Gas Law

$$1 \text{ L} \cdot \frac{1000 \text{ mL}}{1 \text{ L}} \cdot \frac{1 \text{ cm}^3}{1 \text{ mL}} \cdot \frac{(1 \text{ m})^3}{(100 \text{ cm})^3} = 0.001 \text{ m}^3$$

$$20^\circ \text{C} + 273.15 = 293.15 \text{ K}$$

$$1 \text{ atm} = 1.013 \cdot 10^5 \text{ Pa}$$

$$N = \frac{PV}{k_B T} = \frac{1.013 \cdot 10^5 \text{ Pa} \cdot 0.001 \text{ m}^3}{1.38 \cdot 10^{-23} \frac{\text{J}}{\text{K}} \cdot 293.15 \text{ K}} = 2.5 \cdot 10^{22} \text{ part.}$$

$$2.5 \cdot 10^{22} \text{ part.} \cdot \frac{1 \text{ mol}}{6.022 \cdot 10^{23} \text{ part.}} = 0.041 \text{ mol}$$

$$n = \frac{PV}{RT} = \frac{1}{0.0821 \cdot 293} = 0.041 \text{ mol}$$

(microscopic)

$$PV = N k_B T$$

$P_a \downarrow m^3 \downarrow \text{Boltzmann} \downarrow K$

$$k_B = 1.38 \cdot 10^{-23} \frac{\text{J}}{\text{K}}$$

(macroscopic)

$$PV = nRT \rightarrow K \rightarrow K$$

$P_a \downarrow m^3 \downarrow \text{mol} \downarrow \text{atm} \downarrow \text{L} \downarrow \text{mol} \downarrow 0.0821 \frac{\text{atm} \cdot \text{L}}{\text{K} \cdot \text{mol}}$

14. If the pressure inside a tank is 1 atm when the temperature is 100 K, then what is the pressure when the temperature rises to 200 K?

$$PV = N k_B T$$

$$P = \left(\frac{N k_B}{V} \right) \cdot T$$

constants

$$\frac{P_2}{P_1} = \frac{T_2}{T_1} = \frac{200}{100} = 2$$

$$P \propto T$$

$$P_2 = 2 \text{ atm}$$

$$P_2 = 2 \cdot 10^5 \text{ Pa}$$

15. If the pressure inside a tank is 1 atm when the temperature is 100 °C, then what is the pressure when the temperature rises to 200 °C? CAREFUL!

$$P \propto T$$

$$\frac{P_2}{P_1} = \frac{T_2}{T_1} = \frac{473}{373} = 1.26$$

16. A gas is in a sealed container. By what factor does the pressure change if

- the volume is doubled?

$$\frac{P_2 V_2}{P_1 V_1} = \frac{\cancel{N_2 k_B T_2}}{\cancel{N_1 k_B T_1}} = 1$$

$$P = \frac{N k_B T}{V} = N k_B T V^{-1}$$

$$P \propto V^{-1}$$

$$\frac{P_2}{P_1} = \left(\frac{V_2}{V_1} \right)^{-1} = \frac{1}{2}$$

$\uparrow \frac{V_2}{V_1} = 2$

- the temperature is tripled?

$$P \propto T \quad \frac{P_2}{P_1} = \frac{T_2}{T_1} = 3$$

- the volume is double and the temperature is tripled?

$$P = \underbrace{N k_B T} V^{-1}$$

$$P \propto T V^{-1}$$

$$\frac{P_2}{P_1} = \frac{T_2}{T_1} \left(\frac{V_2}{V_1} \right)^{-1} = 3 \left(\frac{1}{2} \right) = \frac{3}{2}$$

- the volume is halved?

$$P \propto V^{-1}$$

$$\frac{P_2}{P_1} = \left(\frac{V_2}{V_1} \right)^{-1} = \left(\frac{1}{2} \right)^{-1} = 2$$

17. You are standing in a room at atmospheric pressure and room temperature. You estimate the room to be 10 m wide by 15 m long by 2 m high. How many moles of gas are in the room?

$$10 \times 15 \times 2 = 300 \text{ m}^3$$

$$n = \frac{PV}{RT} = \frac{1.013 \cdot 10^5 \cdot 300 \text{ m}^3}{8.31 \cdot 293} = 12,300 \text{ mol}$$

18. RT , 1 atm , 1 mol , how big? show me

$$V = \frac{nRT}{P} = \frac{1 \text{ mol} \cdot 8.31 \cdot 293}{1.013 \cdot 10^5} = 0.024 \text{ m}^3$$

$$\Delta = \sqrt[3]{V} = 0.3 \text{ m}$$

