

Chapter 4ish - 5ish

wavelength - distance of an oscillation
- one electric field max to another max
- λ , meters, cm, nm

period - time for one oscillation to pass a point as the wave goes by
- T , seconds

wavenumber - $\frac{1}{\lambda}$ κ, k

propagation constant $\frac{2\pi}{\lambda} = k$

frequency - $\nu = \frac{1}{T} = \text{Hz}$

angular frequency $\frac{2\pi}{T} = 2\pi\nu$

speed $\rightarrow v = \frac{\lambda}{T} = \lambda \cdot f = \lambda \nu$

in materials, light slows down

$C \rightarrow$ speed of light in vacuum
 $\rightarrow v < C$

$$\frac{C}{v} = n \leftarrow \text{index of refraction}$$

conventionally $n \geq 1$

but can be negative (metamaterials)

and can be complex (absorptive materials)

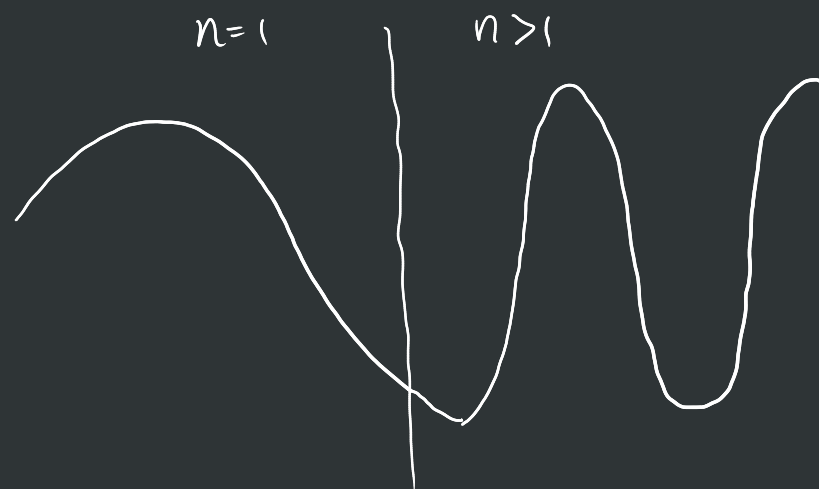
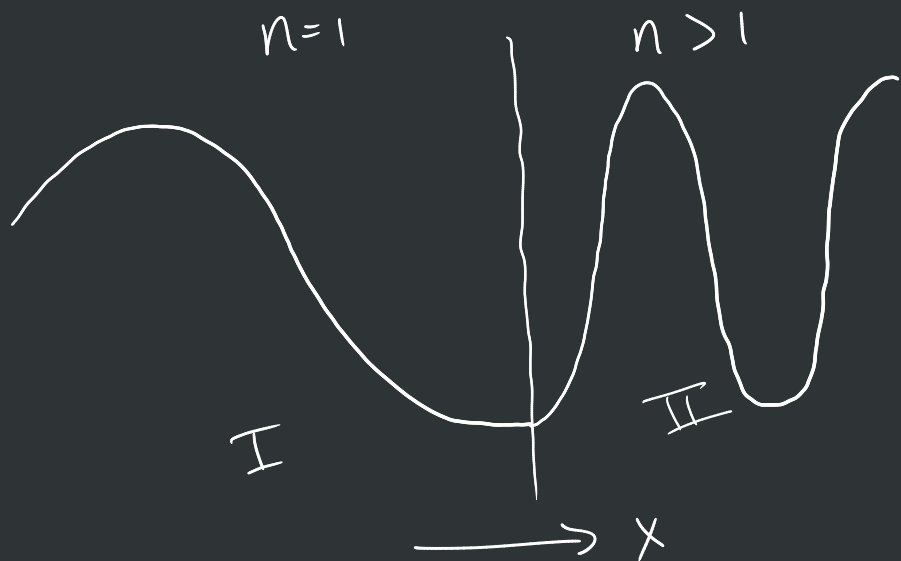
$$v = \frac{C}{n} = \lambda \cdot \nu$$

\rightarrow if n increases at some boundary
 λ decreases, but not ν .

ν is constant

$$E = h \cdot \nu = \frac{hc}{n\lambda}$$

\hookrightarrow Planck's constant



$$v = \frac{c}{n} = \lambda \nu$$

$$\frac{c}{n_1 \lambda_1} = \nu = \frac{c}{n_2 \lambda_2}$$

$$\frac{c}{n_1 \lambda_1} = \frac{c}{n_2 \lambda_2}$$

$$\frac{n_2}{n_1} = \frac{\lambda_1}{\lambda_2}$$

$$\frac{n_2}{n_1} = \left(\frac{\lambda_2}{\lambda_1} \right)^{-1}$$

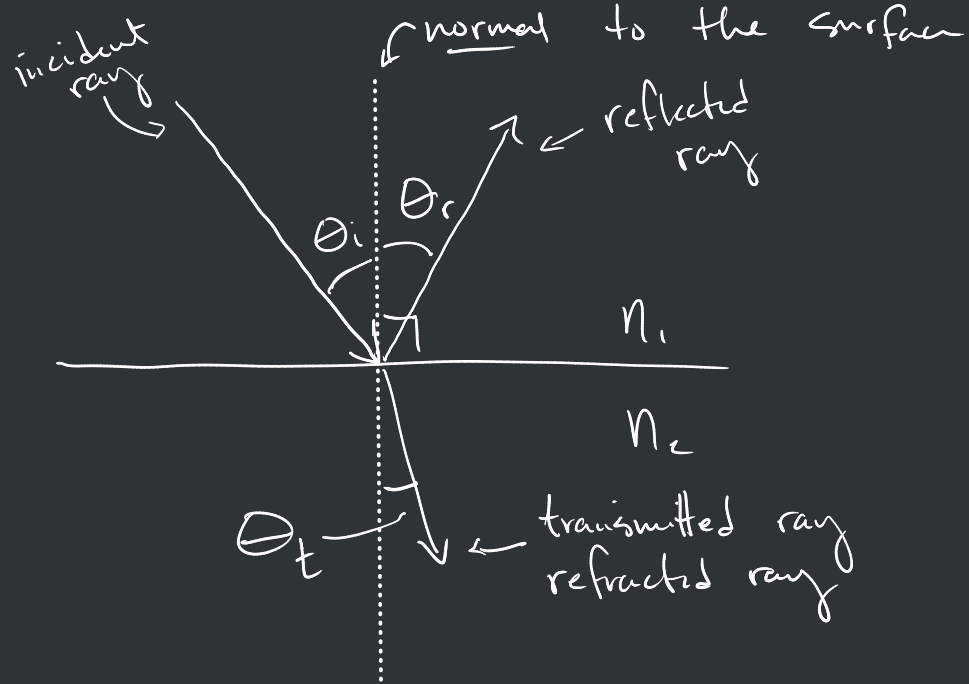
→ I is vacuum

$$\frac{n}{1} = \left(\frac{\lambda_2}{\lambda_0} \right)^{-1}$$

\uparrow \uparrow
 $n=1$ λ_0
 in vacuum in vacuum

$$\lambda_2 = \frac{\lambda_0}{n} \leftarrow n > 1$$

→ so this goes down w/ n



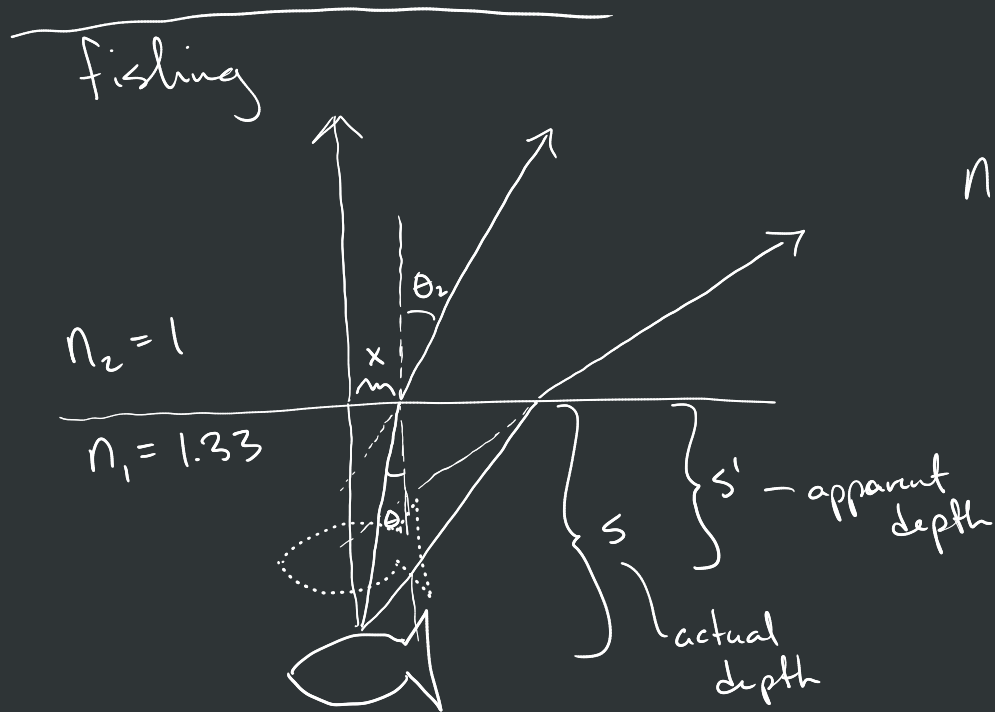
Law of Reflection

$$\rightarrow \theta_i = \theta_r$$

Law of Refraction (Snell's Law)

$$n_1 \sin \theta_i = n_2 \sin \theta_t$$

$$\hookrightarrow n_1 \sin \theta_1 = n_2 \sin \theta_2$$



$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

for small θ , $\sin \theta \approx \tan \theta \approx \theta$

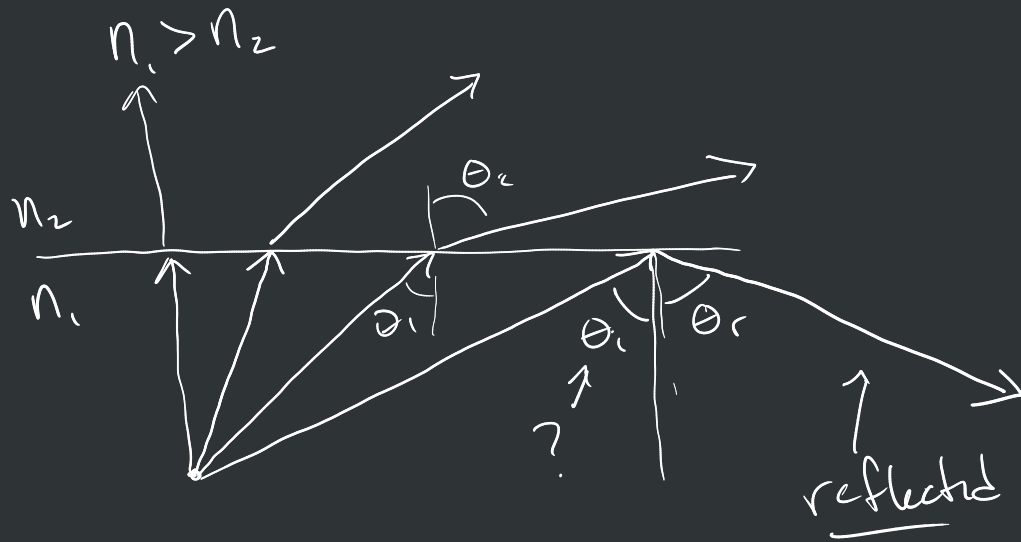
$$n_1 \tan \theta_1 = n_2 \tan \theta_2$$

$$\frac{n_1 \cancel{X}}{s} = \frac{n_2 \cancel{X}}{s'}$$

$$\frac{s'}{s} = \frac{n_2}{n_1} = \frac{1}{1.33} \approx 0.752$$

$$s' = 0.752 \cdot s$$

critical angle



$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$\sin \theta_2 = \frac{n_1}{n_2} \sin \theta_1$$

$$\theta_2 = \sin^{-1} \left(\frac{n_1}{n_2} \sin \theta_1 \right)$$

What θ_1 causes θ_2 to be 90°

$$\underbrace{\sin \theta_2}_{\text{when this is } \geq 1} = \frac{n_1}{n_2} \sin \theta_1$$

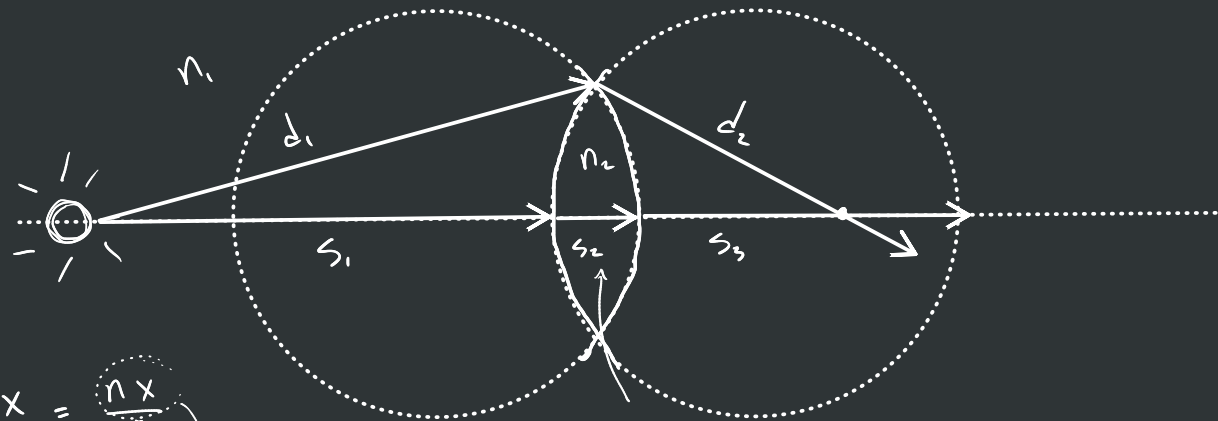
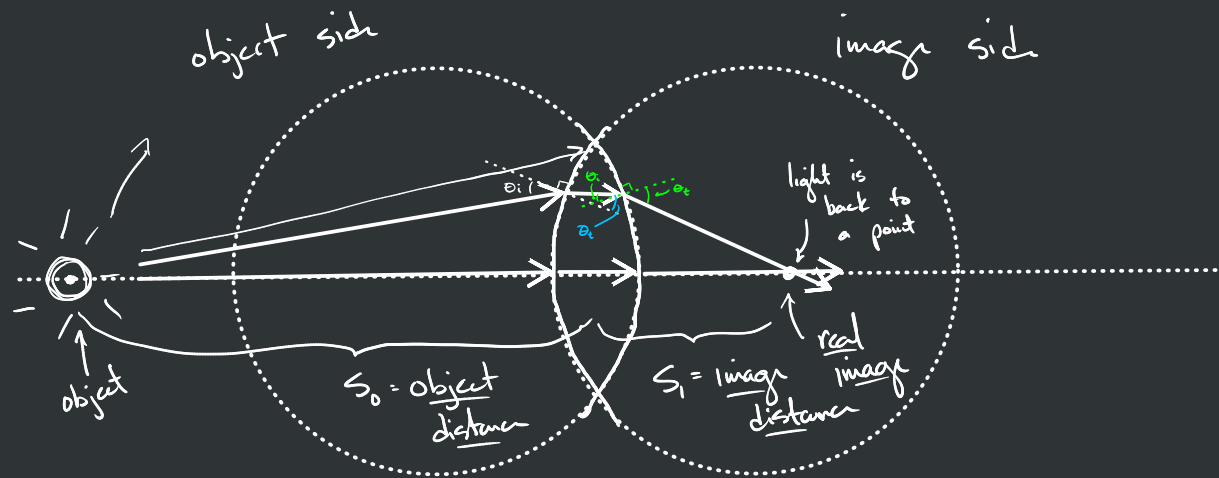
when this is ≥ 1

$$1 = \frac{n_1}{n_2} \sin \theta_1$$

critical angle $\rightarrow \theta_1 = \theta_c = \sin^{-1} \left(\frac{n_2}{n_1} \right)$

$\leftarrow < 1$

HW: Chapter 4: 6, 7, 8, 21, 24



$$t = \frac{x}{v} = \frac{n x}{c}$$

optical path length

$$\frac{n_1 d_1}{c} + \frac{n_1 d_2}{c} = \frac{n_1 s_1}{c} + \frac{n_2 s_2}{c} + \frac{n_1 s_3}{c}$$

$$n_1 d_1 + n_1 d_2 = n_1 s_1 + n_2 s_2 + n_1 s_3$$

} optical path lengths are the same!

perfect images

reflection

- ellipse
- hyperboloid
- parabola

refraction

- ellipse
- hyperboloid
- cartesian oval

Refraction



Thin lens

$$\frac{n_1}{s_o} + \frac{n_2}{s_i} = \frac{n_2 - n_1}{R}$$

↑ object distance

↑ image distance

thin lens (Lens Makers Equation)

$$\frac{1}{s_o} + \frac{1}{s_i} = (n_2 - 1) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$\frac{1}{f} = (n_2 - 1) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

↑ focal length

(Thin Lens Equation)

$$\frac{1}{s_o} + \frac{1}{s_i} = \frac{1}{f}$$



	+	-
s_o	real object	virtual object
s_i	real image	virtual image
f	converging lens	diverging lens
y_o	upright object	inverted object
y_i	upright image	inverted image

