

Chapter 4ish - 5ish

wavelength - distance of an oscillation
- one electric field max to another max
- λ , meters, cm, nm

period - time for one oscillation to pass a point as the wave goes by
- T , seconds
 κ ← cursor key

wavenumber - $\frac{1}{\lambda} \kappa, k$

propagation constant $\frac{2\pi}{\lambda} = k$

frequency - $\nu = \frac{1}{T} = \text{Hz}$
 ω

angular frequency $\frac{2\pi}{T} = 2\pi\nu$

speed $\rightarrow v = \frac{\lambda}{T} = \lambda \cdot f = \lambda \nu$

in materials, light slows down

$C \rightarrow$ speed of light in vacuum
 $\rightarrow v < C$

$$\frac{C}{v} = n \leftarrow \text{index of refraction}$$

conventionally $n \geq 1$

but can be negative (metamaterials)

and can be complex (absorptive materials)

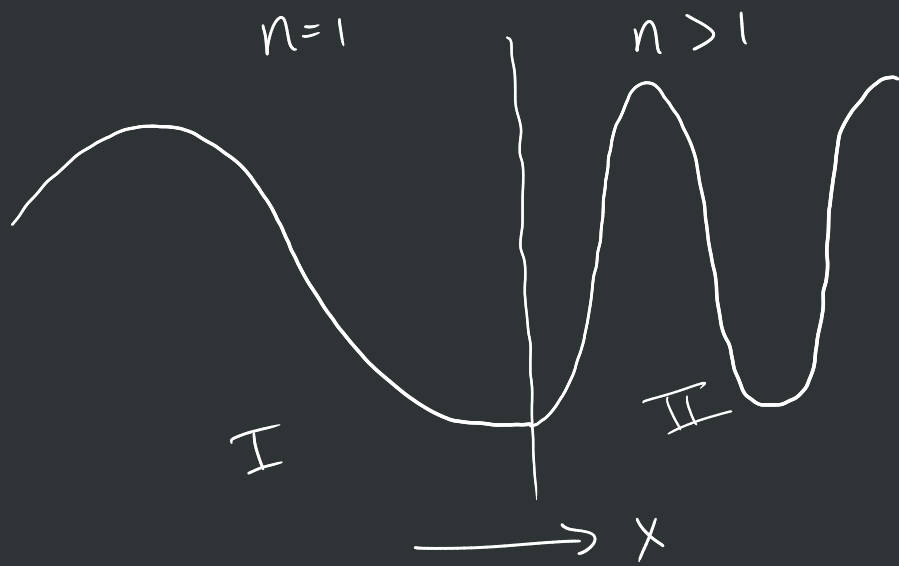
$$v = \frac{C}{n} = \lambda \cdot \nu$$

\rightarrow if n increases at some boundary
 λ decreases, but not ν .

ν is constant

$$E = h \cdot \nu = \frac{hc}{n\lambda}$$

\hookrightarrow Planck's constant



$$v = \frac{c}{n} = \lambda \nu$$

$$\frac{c}{n_1 \lambda_1} = \nu = \frac{c}{n_2 \lambda_2}$$

$$\frac{c}{n_1 \lambda_1} = \frac{c}{n_2 \lambda_2}$$

$$\frac{n_2}{n_1} = \frac{\lambda_1}{\lambda_2}$$

$$\frac{n_2}{n_1} = \left(\frac{\lambda_2}{\lambda_1} \right)^{-1}$$

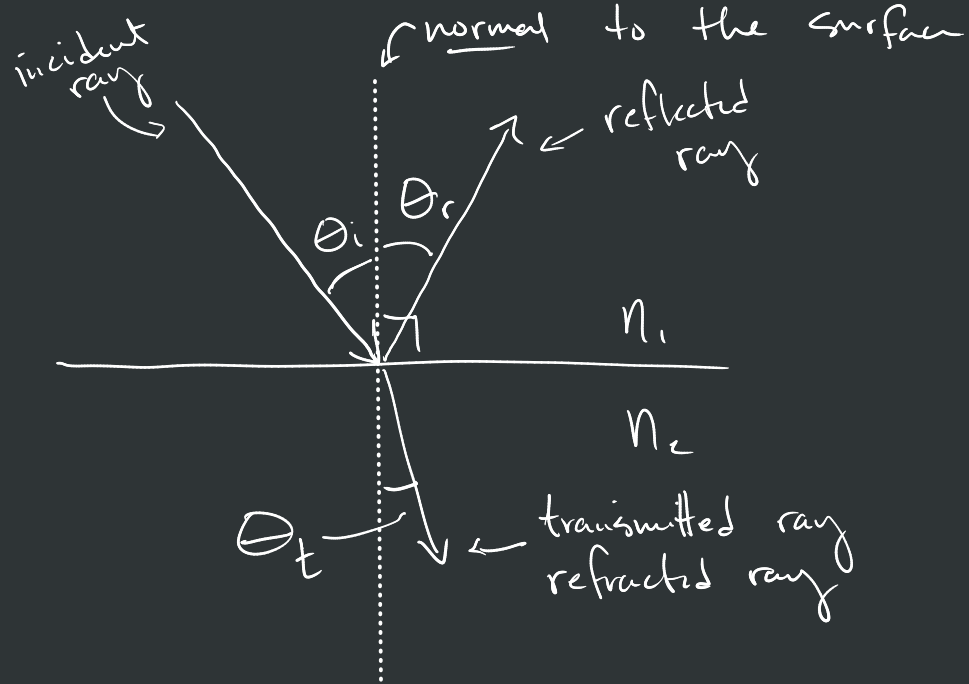
→ I is vacuum

$$\frac{n}{1} = \left(\frac{\lambda_2}{\lambda_0} \right)^{-1}$$

\uparrow \uparrow
 $n=1$ λ_0
 in vacuum in vacuum

$$\lambda_2 = \frac{\lambda_0}{n} \leftarrow n > 1$$

→ so this goes down w/ n



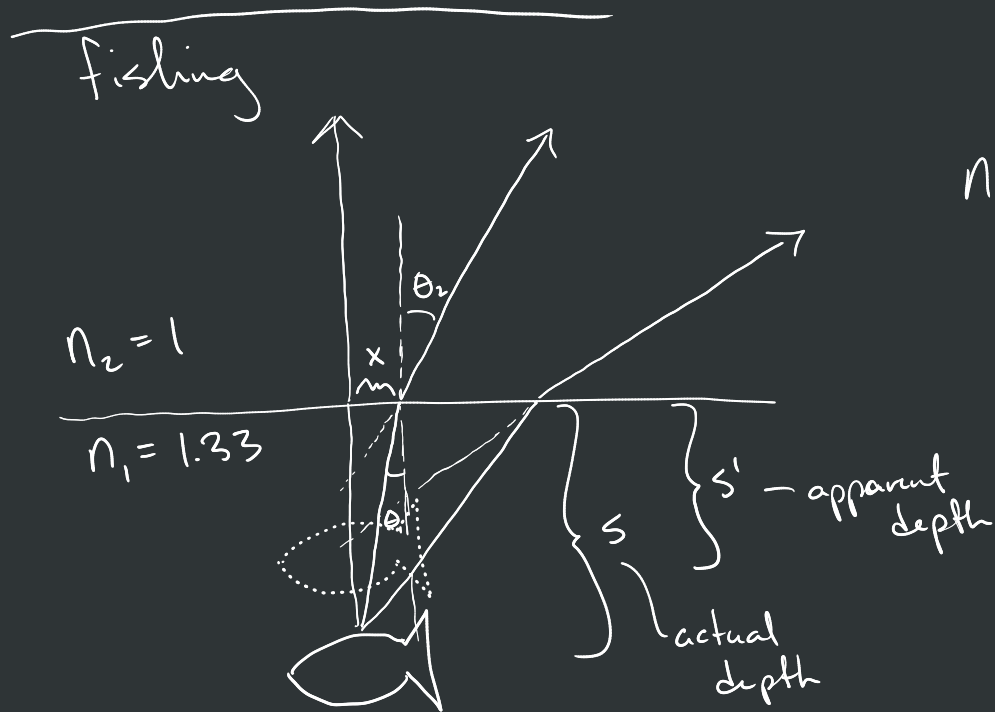
Law of Reflection

$$\rightarrow \theta_i = \theta_r$$

Law of Refraction (Snell's Law)

$$n_1 \sin \theta_i = n_2 \sin \theta_t$$

$$\hookrightarrow n_1 \sin \theta_1 = n_2 \sin \theta_2$$



$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

for small θ , $\sin \theta \approx \tan \theta \approx \theta$

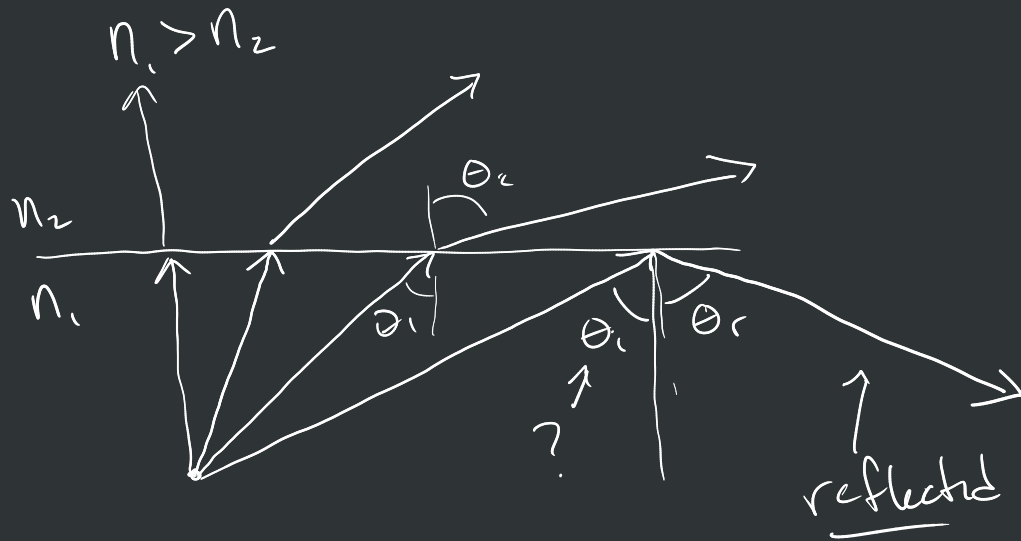
$$n_1 \tan \theta_1 = n_2 \tan \theta_2$$

$$\frac{n_1 \cancel{x}}{s} = \frac{n_2 \cancel{x}}{s'}$$

$$\frac{s'}{s} = \frac{n_2}{n_1} = \frac{1}{1.33} \approx 0.752$$

$$s' = 0.752 \cdot s$$

critical angle



$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$\sin \theta_2 = \frac{n_1}{n_2} \sin \theta_1$$

$$\theta_2 = \sin^{-1} \left(\frac{n_1}{n_2} \sin \theta_1 \right)$$

What θ_1 causes θ_2 to be 90°

$$\sin \theta_2 = \frac{n_1}{n_2} \sin \theta_1$$

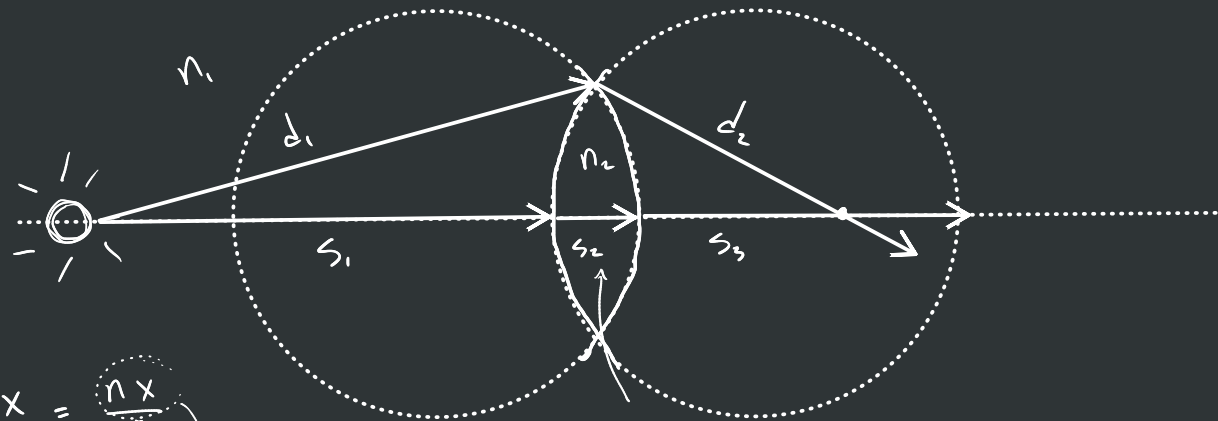
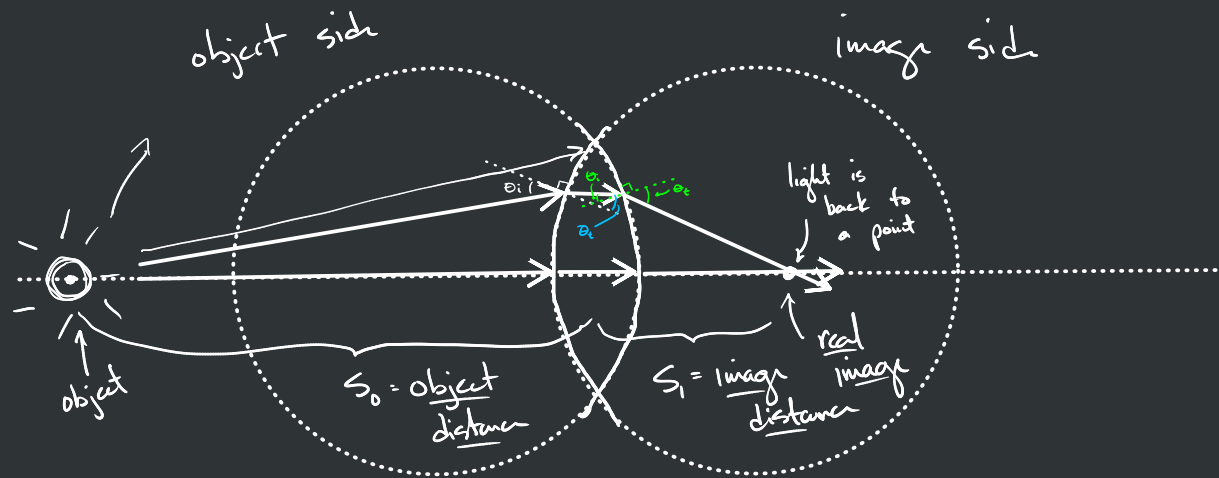
when this is ≥ 1

$$1 = \frac{n_1}{n_2} \sin \theta_1$$

critical angle $\rightarrow \theta_1 = \theta_c = \sin^{-1} \left(\frac{n_2}{n_1} \right)$

$\leftarrow < 1$

HW: Chapter 4: 6, 7, 8, 21, 24



$$t = \frac{x}{v} = \frac{n x}{c}$$

$v = \frac{c}{n}$

optical path length

$$\frac{n_1 d_1}{c} + \frac{n_1 d_2}{c} = \frac{n_1 s_1}{c} + \frac{n_2 s_2}{c} + \frac{n_1 s_3}{c}$$

$$n_1 d_1 + n_1 d_2 = n_1 s_1 + n_2 s_2 + n_1 s_3$$

} optical path lengths are the same!

perfect images

reflection

- ellipse
- hyperboloid
- parabola

refraction

- ellipse
- hyperboloid
- cartesian oval

Refraction



Thin lens

$$\frac{n_1}{s_o} + \frac{n_2}{s_i} = \frac{n_2 - n_1}{R}$$

↑ object distance

↑ image distance

thin lens (Lens Makers Equation)

$$\frac{1}{s_o} + \frac{1}{s_i} = (n_2 - 1) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$\frac{1}{f} = (n_2 - 1) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

↑ focal length

(Thin Lens Equation)

$$\frac{1}{s_o} + \frac{1}{s_i} = \frac{1}{f}$$



	+	-
s_o	real object	virtual object
s_i	real image	virtual image
f	converging lens	diverging lens
y_o	upright object	inverted object
y_i	upright image	inverted image

Optics Lab:

Conjugate Points: $\frac{1}{s_o} + \frac{1}{s_i} = \frac{1}{f}$

Focal length Exp: $\frac{1}{s_o} + \frac{1}{s_i} = \frac{1}{f}$
 ~~$\frac{1}{s_o} \rightarrow \infty$~~
 $\frac{1}{s_i} = \frac{1}{f} \Rightarrow s_i = f$ for $s_o \rightarrow \infty$

Diverging Lens: $\frac{1}{s_o} + \frac{1}{s_i} = \frac{1}{-f}$

$$\frac{1}{s_i} = \frac{1}{-f} - \frac{1}{s_o}$$

$$s_i = \frac{1}{\frac{1}{-f} - \frac{1}{s_o}}$$

Finding a virtual image:

$$\frac{1}{s_o} + \frac{1}{s_i} = \frac{1}{f}$$

$$\left(\frac{1}{s_i} = \frac{1s_o}{fs_o} - \frac{1f}{s_o f} = \frac{s_o - f}{fs_o} \right)$$

$$s_i = \frac{s_o \cdot f}{s_o - f}$$

NINE: $s_o = 27 \text{ cm}$

$$f = -15 \text{ cm}$$

$$s_i = \frac{27(-15)}{27 + 15} = -9.60 \text{ cm}$$

Now for the check:

$$\frac{1}{s_o} + \frac{1}{s_i} = \frac{1}{f}$$

$$s_i = 16.2 \text{ cm}$$

$$f = 10 \text{ cm}$$

$$s_o = 26.13$$

$$s_o = \frac{s_i \cdot f}{s_i - f}$$

$$s_o = \frac{16.2 \cdot 10}{16.2 - 10}$$

$$s_o = 26.13$$

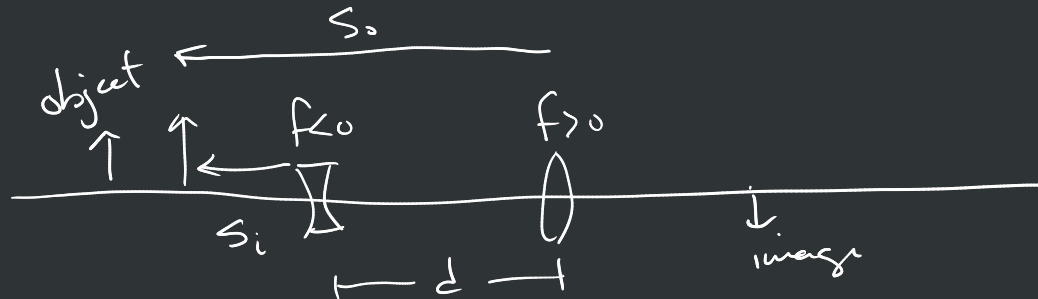
s_o now we need to compare

$$s_o = d - s_i$$

$$26.13 = d - (-9.6)$$

$$16.53 = d$$

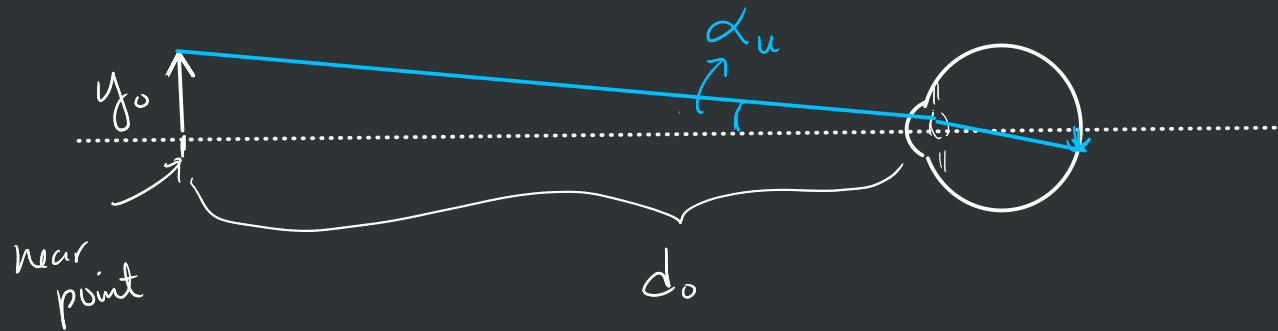
↖ 17.3 measured



Optical Devices

Magnifying Glass

Unaided Eye



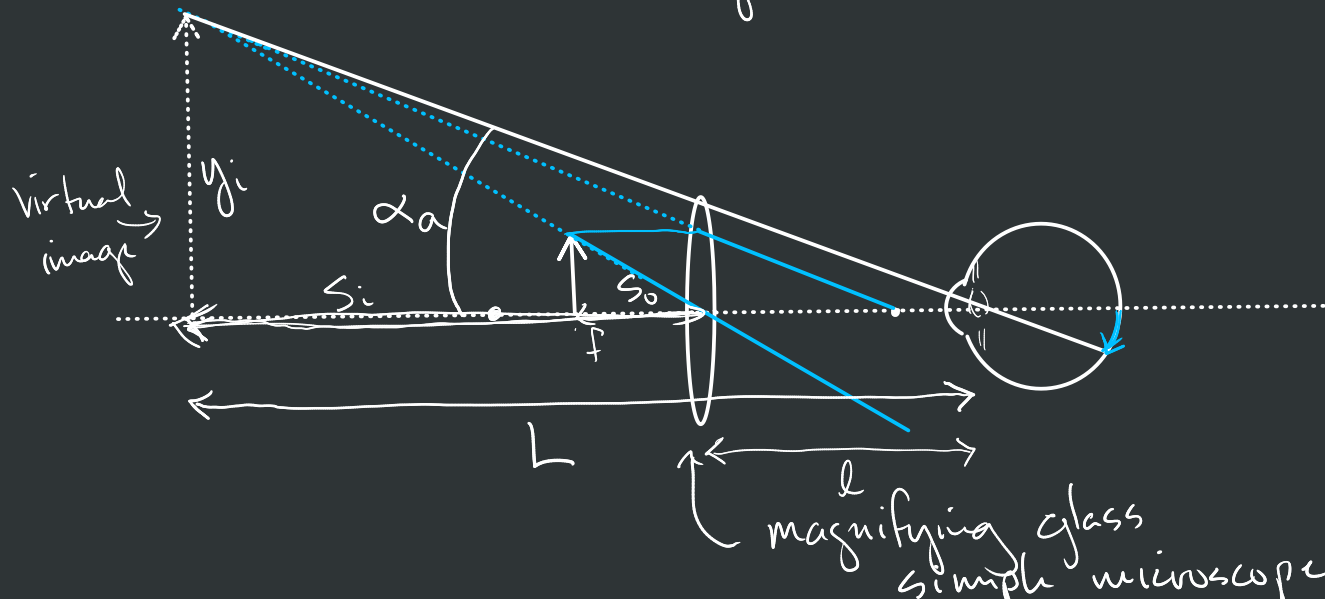
magnifying power
angular magnification

$$MP = M_A = \frac{\alpha_a}{\alpha_u}$$

radius
↓

$$\tan \alpha_u = \frac{y_o}{d_o} \approx \sin \alpha_u \approx \alpha_u$$

Aided Eye



$$\tan \alpha_a = \frac{y_i}{L} \approx \alpha_a$$

$$MP = \frac{y_i}{L} \cdot \frac{d_o}{y_o}$$

↑ this is positive

$$M_t = \frac{y_i}{y_o} = -\frac{s_i}{s_o}$$

$$\rightarrow 57.3^\circ \leftarrow 1 \text{ rad} \cdot \frac{180}{\pi} = 57.3^\circ$$

$$\tan 1 \text{ rad} = 1.557$$

$$\tan 0.1 \text{ rad} = 0.10033$$

$$\hookrightarrow 5.73^\circ$$

$$\frac{1}{s_o} + \frac{1}{s_i} = \frac{1}{f}$$

$$s_i \left[\frac{1}{s_o} = \frac{1}{f} - \frac{1}{s_i} \right] s_i$$

$$\frac{s_i}{s_o} = \frac{s_i}{f} - 1$$

$$-\frac{s_i}{s_o} = \left[1 - \frac{s_i}{f} \right]$$

$$MP = - \frac{s_i}{s_o} \cdot \frac{d_o}{L}$$

$$MP = \left(1 - \frac{s_i}{f} \right) \frac{d_o}{L}$$

$$s_i = -(L - l)$$

$$MP = \left(1 + \frac{L - l}{f} \right) \cdot \frac{d_o}{L}$$

$$\frac{1}{f} = \mathcal{D} \leftarrow \text{dioptric power}$$

$$\boxed{MP = (1 + (L - l)\mathcal{D}) \cdot \frac{d_o}{L}} \text{ eq. 5.16}$$

\mathcal{D}

\mathcal{D}

Case 1: $l = f$

$$\begin{aligned} [MP]_{l=f} &= \left(1 + (L - l) \frac{1}{f} \right) \cdot \frac{d_o}{L} \\ &= \left(\cancel{1} + \frac{\cancel{L}}{f} - \frac{\cancel{L}}{\cancel{f}} \right) \cdot \frac{d_o}{\cancel{L}} \end{aligned}$$

$$[MP]_{l=f} = \frac{d_o}{f} = d_o \mathcal{D}$$

Case 2: $l = 0$

$$\begin{aligned} [MP]_{l=0} &= \left(1 + (L - \vec{l}) \mathcal{D} \right) \cdot \frac{d_o}{L} \\ &= \left(1 + L \mathcal{D} \right) \frac{d_o}{L} \end{aligned}$$

$$[MP]_{l=0} = \left(\frac{1}{L} + \mathcal{D} \right) \cdot d_o$$

if we shrink L to d_o ,

$$[MP]_{\substack{l=0 \\ L=d_o}} = \left(\frac{1}{d_o} + \mathcal{D} \right) \cdot d_o$$

$$[MP]_{\substack{l=0 \\ L=d_o}} = 1 + \mathcal{D} \cdot d_o$$

Case 3: We put the object at the focal point, $s_o = f$.
The image is formed

$$\frac{1}{s_o} + \frac{1}{s_i} = \frac{1}{f}$$

$$\frac{1}{f} + \frac{1}{s_i} = \frac{1}{f}$$

$\xrightarrow{\quad}$

$$\frac{1}{s_i} = 0$$

$$s_i \rightarrow \infty$$

$$MP = (1 + (L - l)\mathcal{D}) \cdot \frac{d_o}{L}$$

$$[MP]_{L \rightarrow \infty} = \cancel{\frac{d_o}{L}} + \frac{K \cdot \mathcal{D} \cdot d_o}{\cancel{L}} - \frac{l \mathcal{D} \cdot d_o}{\cancel{L}}$$

$$[MP]_{L \rightarrow \infty} = \mathcal{D} \cdot d_o = \frac{d_o}{f}$$

