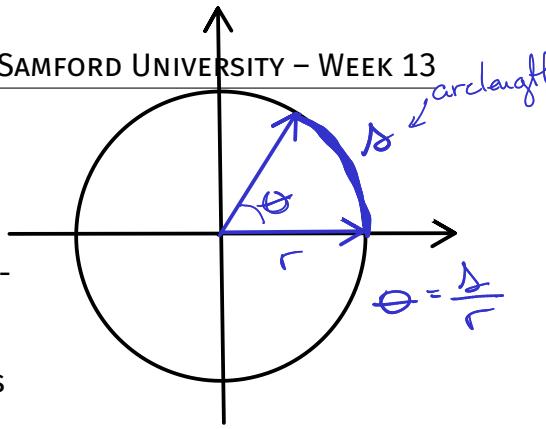
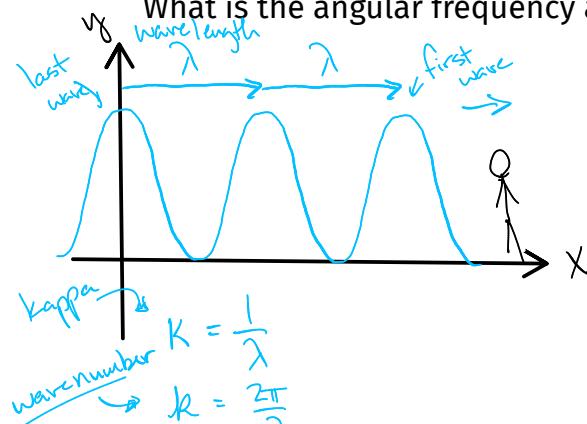


At the end of this worksheet you should be able to

- use the properties of waves to solve for an unknown quantity.
- use the mathematical description of a wave to plot waves motion over time.
- use the conditions of a standing wave on a string to solve for an unknown quantity.



1. A string with a mass density of 10 g/m has a tension of 100 N . A periodic waveform that has a period of 0.1 s is put into this string. What is the frequency? What is the wavelength of this wave? What is the angular frequency and what is the wavenumber?



$$v = \frac{\lambda}{T}$$

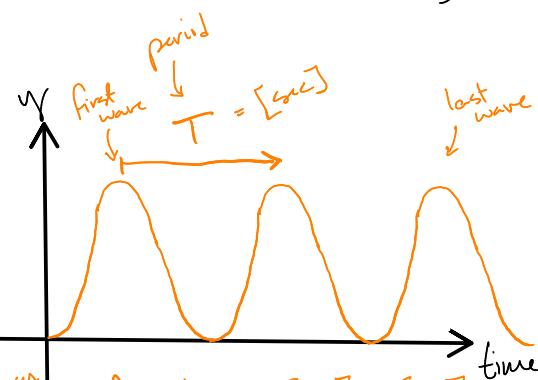
$$v = \lambda \cdot f$$

$$f = \frac{1}{0.1 \text{ s}} = 10 \text{ Hz}$$

$$\lambda = \frac{v}{f} = \frac{100 \text{ m/s}}{10 \text{ Hz}} = 10 \text{ m}$$

2. The wavenumber of a wave is 20 rad/meter , and the period is 0.1 seconds .

- What is the frequency, angular frequency, wavelength, and velocity?



$$f = \frac{1}{T} = [s^{-1}] = [\text{Hz}]$$

$$\omega = \frac{2\pi}{T} \text{ rad} = (2\pi \text{ rad}) \cdot f$$

$$\omega = 2\pi \cdot (10 \text{ Hz}) = 62.8 \frac{\text{rad}}{\text{s}}$$

$$k = \frac{2\pi}{\lambda} = 0.628 \frac{\text{rad}}{\text{m}}$$

[radian]

$$A \cos(k(x - vt) + \phi)$$

↓

$$\underline{A \cos(kx - \omega t + \phi)}$$

- If the force on the string that is carrying this wave is 100 N , then what is the linear mass density?

- If the string is 10 grams then what is the length of the string?

3. A wave has a wavelength of 3 m and an amplitude of 2 m. It travels with a speed of 5 m/s. If the wave has its maximum at the horizontal position of 0 m when $t = 0\text{ s}$, then sketch a plot of the wave at this time below:

know:

$$\lambda, \Delta y_{\text{max}}, v$$

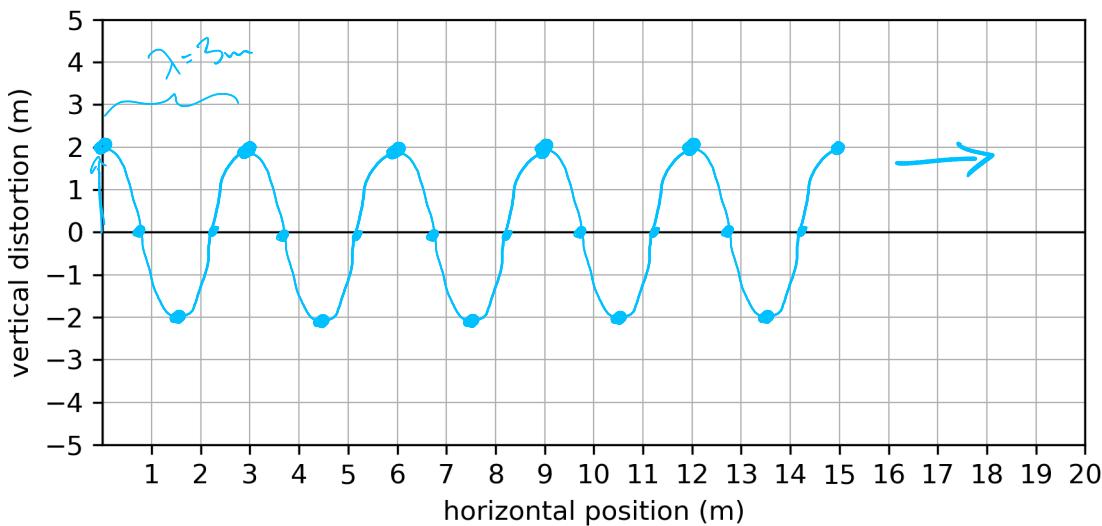
want:

$$k = \frac{2\pi}{\lambda} = \frac{2\pi}{3} \text{ rad/m}$$

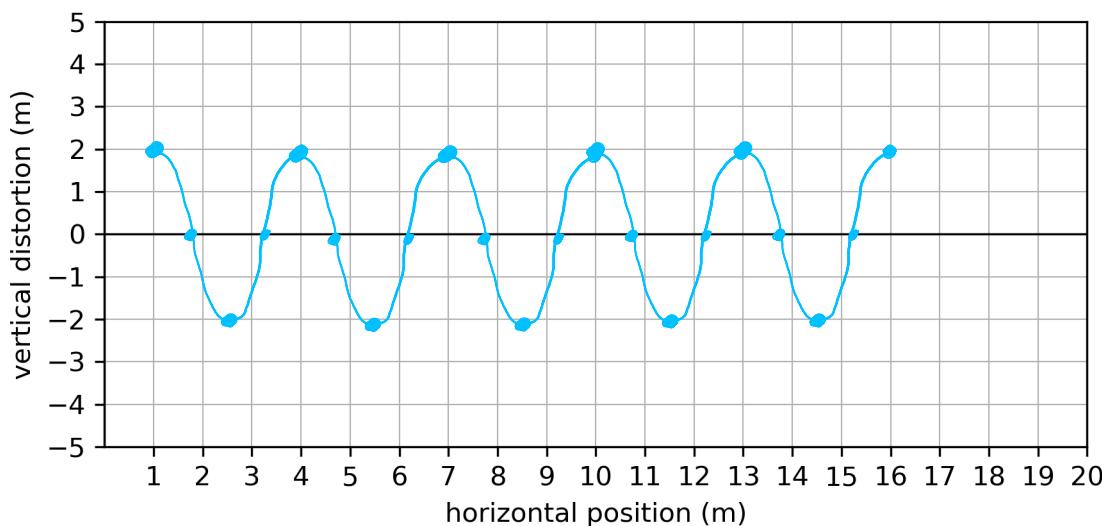
$$f = \frac{v}{\lambda} = \frac{5\text{ m/s}}{3\text{ m}} = 1.67\text{ Hz}$$

$$T = \frac{1}{f} = \frac{3}{5}\text{ s}$$

$$\omega = 2\pi f = \frac{10\pi}{3}\text{ rad/s}$$

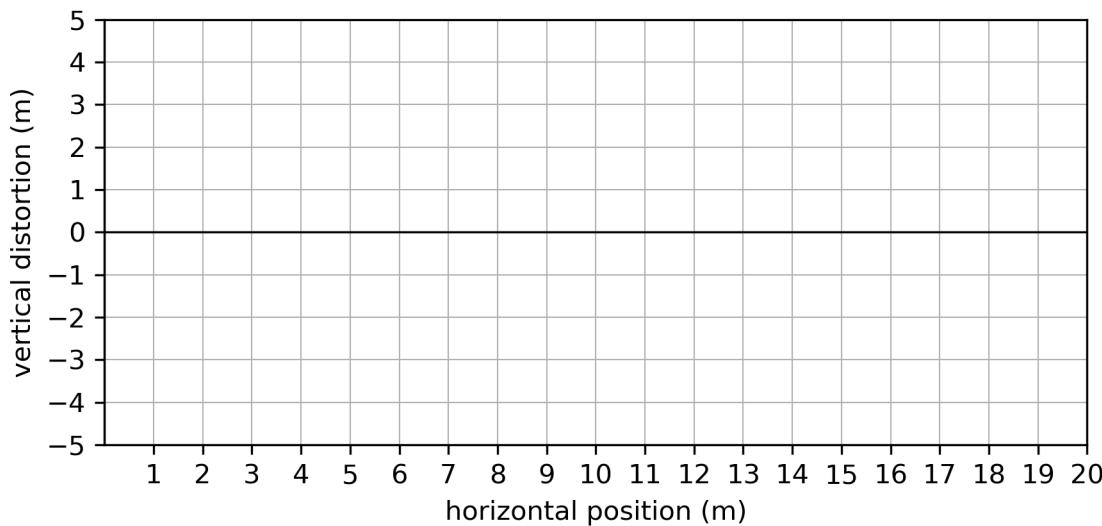


4. Now sketch the wave after 0.2 seconds have gone by.

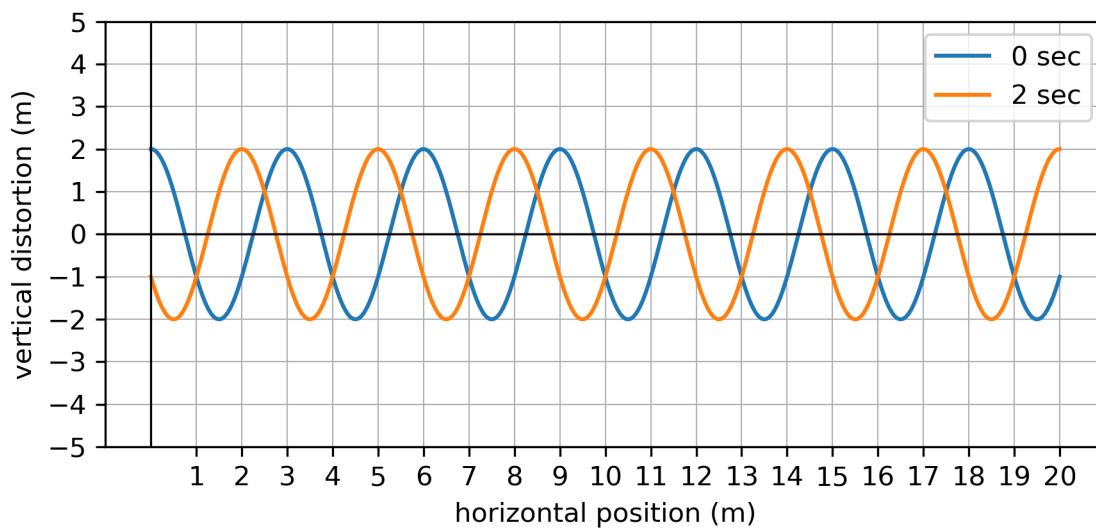


$$\begin{aligned} \Delta x &= v \cdot \Delta t \\ &= 5 \text{ m/s} \cdot (0.2\text{s}) \\ &= 1\text{m} \end{aligned}$$

5. Now sketch the wave 1 second after the beginning.

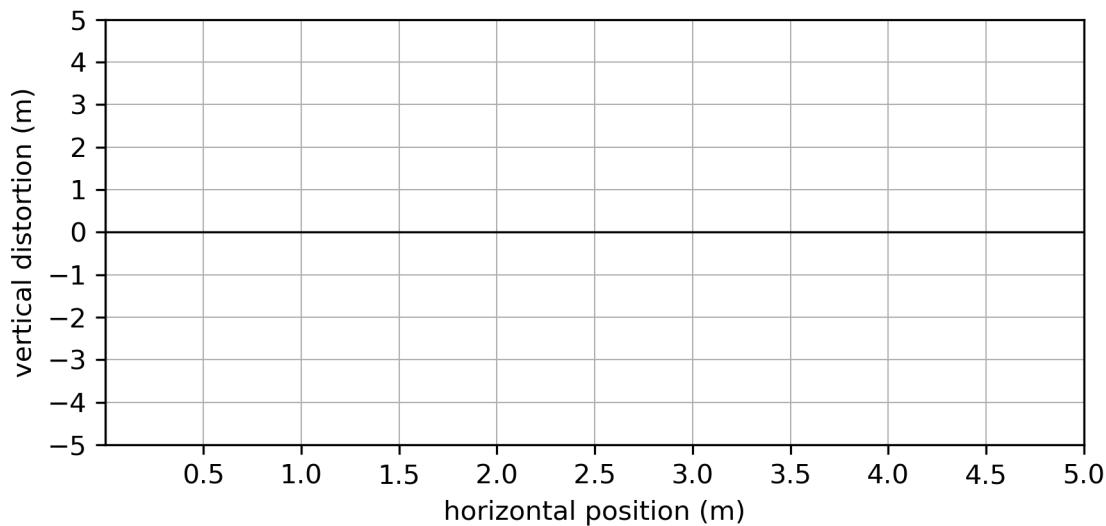


6. The following plot shows a wave at $t = 0\text{ s}$ and then later when $t = 2\text{ s}$. What is the wavelength, amplitude, period, angular frequency, wavenumber, and velocity?



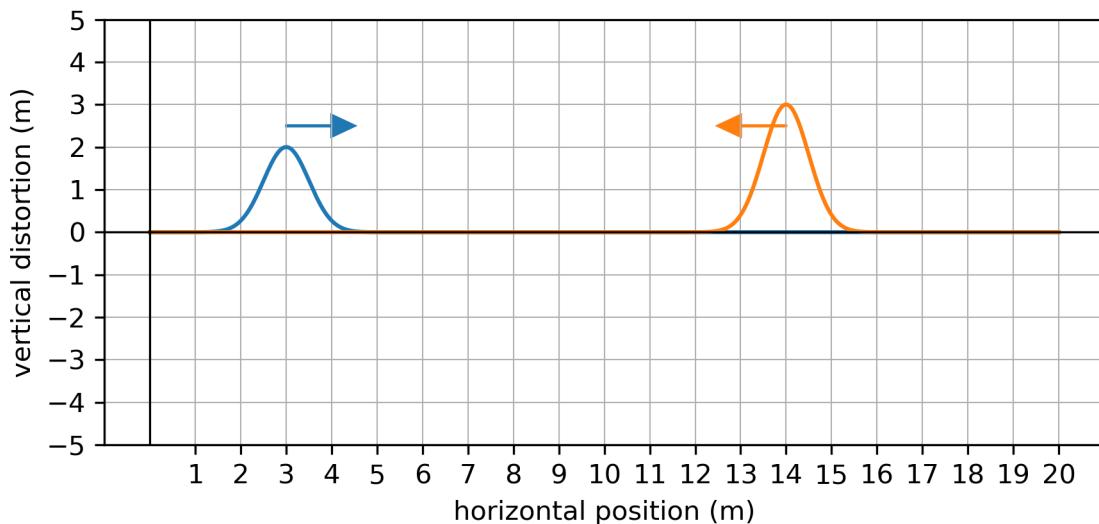
7. A wave on a string is described by the equation below. Plot this function for $t = 0\text{ s}$ and again for $t = 2\text{ s}$.

$$y(x, t) = 3.5 \text{ m} \sin ((6\pi \text{ rad/m})x - (8\pi \text{ rad/s})t)$$

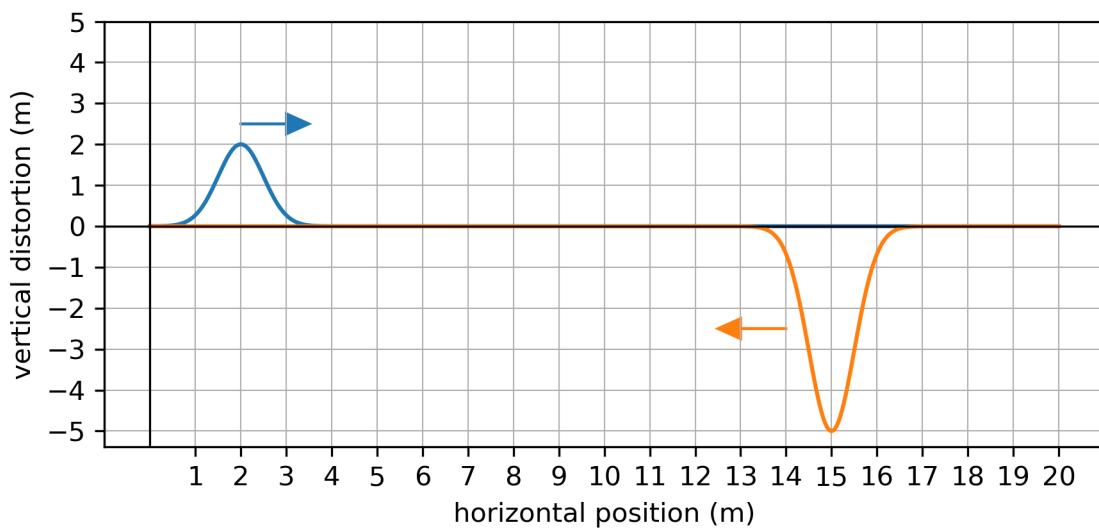


8. A string has a tension of 100 N. But this string has two sections that are knotted together. One side has a linear mass density of 10 g/m and the other side has a linear mass density of 35 g/m. What is the velocity of the wave on the first side of the knot? What is the velocity on the second side? If a wave with a wavelength of 0.2 meters is traveling on the first side, what is its frequency? When the crest of this wave from the first side reaches the knot, this crest simply passes through the knot. But the velocity has changed. So how much time goes by to when the next crest passes the knot? How far has the first crest traveled in the second side of the string? What does this mean about the wavelength on the second side? What is the frequency of wave crests coming into the knot? What is the frequency of crests leaving the knot? On the basis of this analysis, when the speed of a wave changes suddenly at an interface does the wavelength change or does the frequency or do both change?
9. Two waves are approaching each other with speed $v = 4 \text{ m/s}$. At what time and where will these waves fully overlap (their

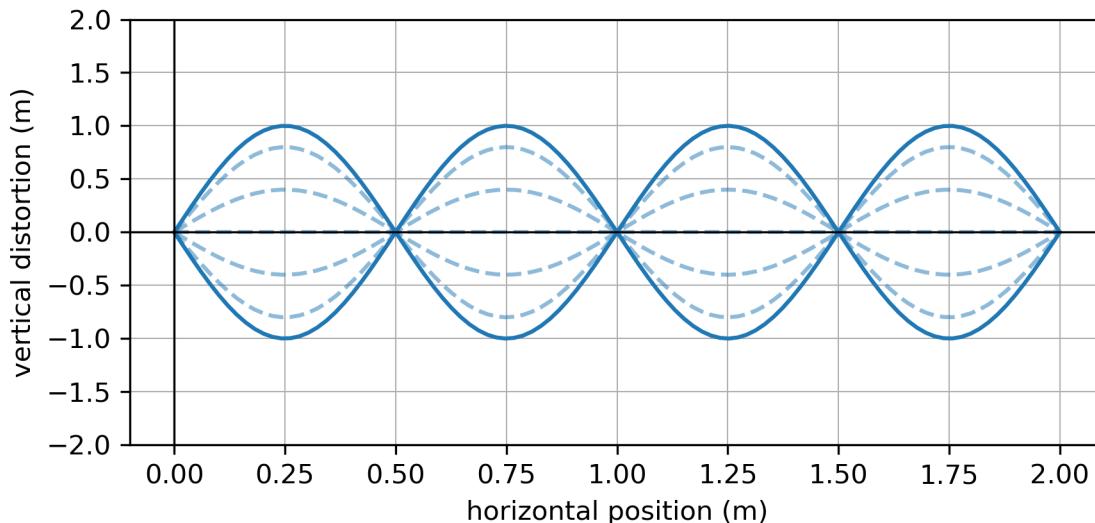
max peaks line up) and what will the wave look like at that time?



10. Again, two waves approach each other with speed $v = 6 \text{ m/s}$. At what time and where will these waves fully overlap and what will the wave look like at that time?



11. The plot below represents a standing wave in a string. How many antinodes are there? How many nodes are there? What is the wavelength of the string. If the speed of the wave on the string is $v = 40 \text{ m/s}$, then what input frequency produces this standing wave? What period of oscillation of the input frequency?



12. If the string from the above problem has three antinodes, then what is the wavelength? If the velocity of the wave is still $v = 40 \text{ m/s}$, then what is the frequency? What is the wavelength and frequency when there are two antinodes? What about when there is one antinode? What is the fundamental frequency? What is the 10th harmonic frequency? What is the 10th harmonic wavelength?

13. Instead of changing the frequency to make a fewer anti-nodes, we could change the velocity instead, and the easiest way to do that is to adjust the force in the string. So if the standing wave goes from 4 antinodes to 3 antinodes, by what ratio does the speed of the wave change? If the speed of the wave changes by this ratio, then by what ratio does the force on the string need to change?

 14. Suppose a wave has a 4th harmonic frequency of 200 Hz then what is the fundamental frequency?

 15. If a standing wave is produced a frequency of 98 Hz and the next standing wave frequency is 112 Hz. What is the fundamental frequency and how many antinodes were there for these two standing waves?

16. If you increase the tension in a string by a factor of 1.3, then by what factor do you change the fundamental frequency of a waves in that string? If you increase the tension in string by 10%, then by what percent do you change the fundamental frequency?

