

1. Express the wave function for one-dimensional harmonic waves in terms of the following parameters:

- Frequency and wavelength
- Period and wavelength
- Angular frequency and wave vector

$$1) \eta(x) = A \cos\left(\frac{2\pi x}{\lambda} - 2\pi \nu t + \phi\right)$$

$$2) \eta(x) = A \cos\left(\frac{2\pi x}{\lambda} - \frac{2\pi t}{T} + \phi\right)$$

3)

starting place \rightarrow

$$\eta(x) = A \cos(k(x - vt) + \phi)$$

$$\text{or } \eta(x) = A \cos(kx - \omega t + \phi)$$

2. Consider the plane electromagnetic wave in vacuum (in SI units) given by the expressions:

$$E_x = 0$$

$$E_y = 4 \cos[2\pi \cdot 10^{14}(t - x/c) + \pi/2]$$

$$E_z = 0$$

- 4 \leftarrow Calculate the frequency, wavelength, direction of motion, amplitude, initial phase angle, and polarization of the wave.

- Write an expression for the magnetic flux density.

$$\omega \left(t - \frac{x}{c}\right) = \omega t - \underbrace{\frac{\omega x}{c}}_k$$

not sure about

$$\text{but } k \cdot v = \omega$$

$$\text{and } v = \frac{\omega}{k} = \lambda \cdot \nu$$

$\rho \rightarrow \pi?$

so since

$$\omega = 2\pi \cdot 10^{14}$$

$$\omega = 2\pi \nu$$

$$\text{then } \nu = 10^{14} \text{ Hz}$$

$$\lambda = \frac{2\pi}{k} = \frac{2\pi c}{\omega}$$

$$\text{but also } \lambda = \frac{v}{\nu}$$

$$\begin{aligned} \text{so } \lambda &= \frac{c}{10^{14}} = \frac{3 \cdot 10^8}{10^{14}} \\ &= 3 \cdot 10^{-6} \\ &= 3 \mu\text{m} \end{aligned}$$

3. Write an expression for the \vec{E} and \vec{B} fields that constitute a plane harmonic wave traveling in the $+z$ -direction. The wave is linearly polarized with its plane of vibration at 45° to the yz -plane.
4. A 500-nm harmonic EM wave, whose electric field is in the z -direction, is traveling in the y -direction in vacuum.
- What is the frequency of the wave?
 - Determine both v and k for this wave.
 - If the electric field amplitude is 700 V/m, what is the amplitude of the magnetic field?
 - Write an expression for both $E(t)$ and $B(t)$ given that each is zero at $x = 0$ and $t = 0$. Put in all the appropriate units.

5. Consider a linearly polarized plane electromagnetic wave traveling in the $+x$ -direction in free space having as its plane of vibration the xy -plane. Given that its frequency is 5 MHz and its amplitude is $E_0 = 0.05 \text{ V/m}$
- Find the period and wavelength of the wave.
 - Write an expression for $E(t)$ and $B(t)$.
 - Find the flux density, $\langle S \rangle$, of the wave.
6. A light wave travels from point A to point B in vacuum. Suppose we introduce into its path a flat glass plate ($n = 1.50$) of thickness $L = 1.00 \text{ mm}$. If the vacuum wavelength is 500 nm, how many waves span the space from A to B with and without the glass in place? What phase shift is introduced with the insertion of the plate?

