

Thermal Equilibrium - when objects have been in contact
and macroscopic coordinates have stopped changing

↳ involves an exchange of energy between two objects, or an object + its surroundings

↳ volume (constant pressure) → mercury/alcohol

- pressure

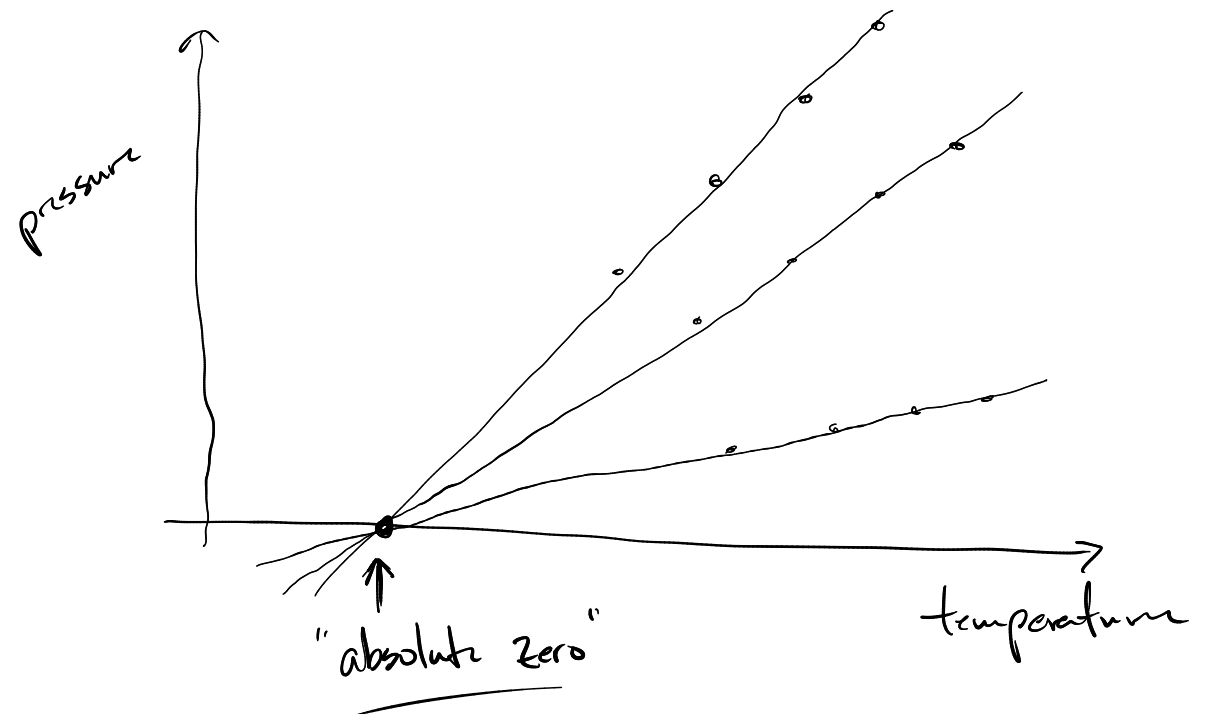
- electrical resistance

- radiation / thermal emf

$$1) \quad C_1 = 0^\circ\text{C} \quad C_2 = 100^\circ\text{C}$$

$$F_1 = 32^\circ\text{F} \quad F_2 = 212^\circ\text{F}$$

$$C = mF + b$$



$$0\text{K} = -273.15^\circ\text{C}$$

1.2 Ideal Gas Law \rightarrow Equation of State \rightarrow relates all of the state variables together

$$pV = N k_B T$$

$p = \frac{F}{\text{Area}}$
 $[Pa] = \left[\frac{N}{m^2} \right]$

N \rightarrow number of particles
 k_B Boltzmann's constant
 $k_B = 1.38 \cdot 10^{-23} \frac{J}{K}$

$$pV = nRT$$

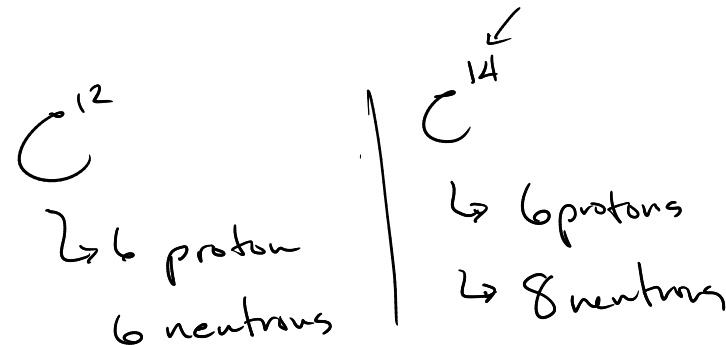
n \rightarrow number of moles
universal gas constant
 $R = 8.31 \frac{J}{mol \cdot K} ?$

$$N k_B = nR$$
$$6.022 \cdot 10^{23} \cdot 1.38 \cdot 10^{-23} = R$$
$$8.31 \frac{J}{mol K} = R$$

Number, moles, molar, density

$$1 \text{ mole of things} = 6.022 \cdot 10^{23} \text{ things}$$

particle
atom
molecule



1 mole is 1 gram of protons + neutrons

Ex: mass of one proton in kg?

mass of one proton \times number of proton = mass of the collection

$$m \times N = M$$

$$m = \frac{1g}{N_A} = \frac{1}{6.022 \cdot 10^{23}} = 1.7 \cdot 10^{-24} \text{ grams} = \underline{1.7 \cdot 10^{-27} \text{ kg}}$$

What about N_2 ?

$$1 \text{ mole of } N_2 = 2 \left(14 \frac{g}{\text{mol}} \right) = 28 \frac{g}{\text{mol}}$$

Volume of 1 mole of air at room temp and atmospheric pressure?

$$\hookrightarrow 1 \text{ atm} = \underline{1.013 \cdot 10^5 \text{ Pa}}$$

$$V = \frac{nRT}{P} = \frac{1 \text{ mol} \cdot 8.31 \frac{J}{K \cdot \text{mol}} \cdot 300K}{10^5 \text{ Pa}} = 0.0249 \text{ m}^3$$

$$V_{\text{cube}} = \Delta^3$$

$$\Delta = 0.292 \text{ m} \sim 30 \text{ cm} \sim 1 \text{ ft}$$

1.17] $PV = nRT \left(1 + \frac{B(T)}{V/n} \right)$

a) $PV = nRT \left(1 + \frac{n}{V} \cdot B(T) \right)$

at atmospheric pressure $P = 10^5 \text{ Pa}$

→ solve for $\frac{n}{V}$

$$P = \frac{n}{V} RT \left(1 + \frac{n}{V} B(T) \right)$$

$$0 = \frac{n}{V} RT + \left(\frac{n}{V} \right)^2 \cdot RT \cdot B(T) - P$$

T	B(T)	$\frac{n}{V}$	$\frac{n}{V} \cdot B(T)$
100	-16.0		
200	-3.5		
300	-4.2		
400	9.0		
500	16.9		
600	21.3		

$$b) \quad PV = nRT \left(1 + \frac{B(T)}{V/n} \right) \quad \text{if}$$

$$c) \rightarrow PV = nRT \left(1 + \frac{B(T)}{V/n} + \frac{C(T)}{(V/n)^2} \right) \quad \left. \vphantom{PV = nRT} \right\} \text{ want: } B + C \text{ in terms of } a + b$$

$$\left(P + \frac{an^2}{V^2} \right) \left(V - nb \frac{V}{V} \right) = nRT$$

$$\left(P + \frac{an^2}{V^2} \right) V \left(1 - \frac{nb}{V} \right) = nRT$$

$$\left(P + \frac{an^2}{V^2} \right) V = nRT \left(1 - \frac{nb}{V} \right)^{-1}$$

$$PV + \frac{an^2}{V} = nRT \left(1 - \frac{nb}{V} \right)^{-1}$$

$$PV = nRT \left(1 - \frac{nb}{V} \right)^{-1} - \frac{an^2}{V}$$

use our approx.

$$(1+x)^p \approx 1 + px + \frac{1}{2}p(p-1)x^2 \quad px \ll 1$$

$$\left(1 + \left(-\frac{nb}{V} \right) \right)^{-1} \approx 1 + (-1) \left(-\frac{nb}{V} \right) + \frac{1}{2}(-1)(-1-1) \left(-\frac{nb}{V} \right)^2$$

$$\approx 1 + \frac{nb}{V} + \left(\frac{nb}{V} \right)^2$$

$$PV = nRT \left(1 + \frac{nb}{V} + \left(\frac{nb}{V} \right)^2 \right) - \frac{an^2}{V} \begin{matrix} nRT \\ nRT \end{matrix} \longleftrightarrow PV = nRT \left(1 + \frac{n}{V} \cdot B(T) + \left(\frac{n}{V} \right)^2 \cdot C(T) \right)$$

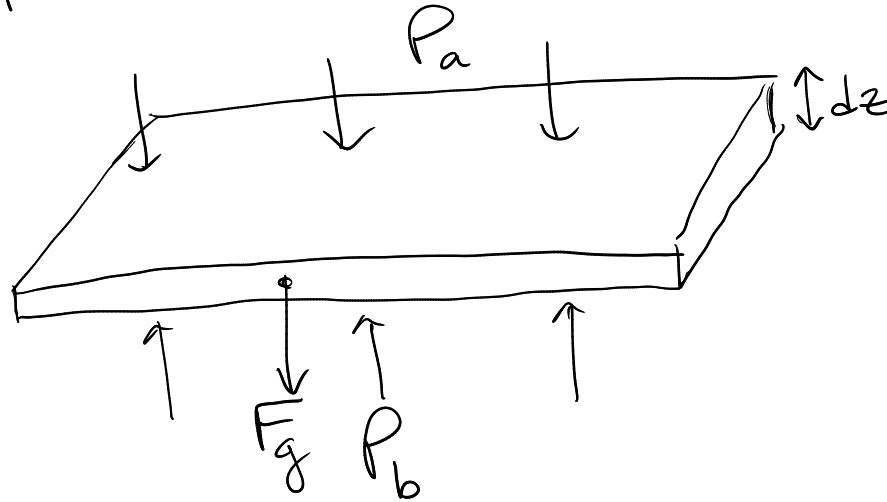
$$PV = nRT \left(1 + \frac{nb}{V} + \left(\frac{nb}{V} \right)^2 - \frac{an^2}{V \cdot nRT} \right) = nRT \left[1 + \underbrace{\frac{n}{V} \left(b - \frac{a}{RT} \right)}_{B(T)} + \underbrace{\left(\frac{n}{V} \right)^2 \cdot b^2}_{C(T)} \right]$$

d) → plot data from that table ←

→ plot $B(T) = b - \frac{a}{RT}$ choose b, a

1.16 | $\rho = \frac{M}{V}$

↑
"rho"
volumetric
mass
density



$$P = \frac{F}{A}$$

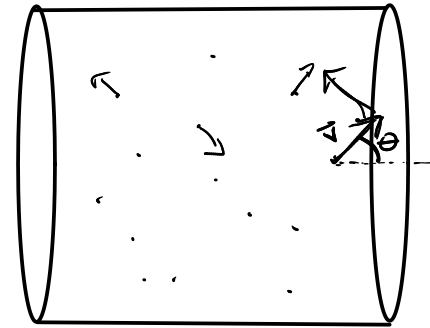
$$+ P_b \cdot A - P_a \cdot A - M \cdot g = 0$$

$$\frac{dP}{dz} = \underbrace{\quad}_{\rho}$$

1.2b | Kinetic Theory and Equipartition of Energy

pressure \longleftrightarrow kinetic energy \longleftrightarrow temperature

$$\text{pressure}_{\text{collision}} = \frac{F}{A} = \frac{\Delta p}{A \Delta t} \quad \leftarrow \underbrace{2mv \cos \theta}$$



$$d(\text{pressure}) = \frac{2mv \cos \theta}{dA \cdot dt} \cdot \left. \begin{array}{l} \text{number of particles hitting area } dA \\ \text{w/ velocity } v \text{ in } dt \text{ amount of time} \end{array} \right\} \begin{array}{l} \text{integrate over all velocities} \\ \text{and over } \theta \end{array}$$

number of atoms
traveling in a particular
direction w/ a particular
speed

• fraction of them
that are within
striking distance
of the surface dA

Probability

$$P(x) = \frac{\text{desired outcomes}}{\text{total outcomes}}$$

$N(x) \leftarrow$ number of desired outcomes

\nearrow
total outcomes

$$N = \sum_{x=0}^{\infty} N(x)$$

\nwarrow
rearrange

$$P(x) = \frac{N(x)}{N}$$

$$N(x) = P(x) \cdot N$$

normalized probabilities

$$\sum_{x=0}^{\infty} P(x) = 1$$

$$\langle x \rangle = \sum_{x=0}^{\infty} x \cdot P(x)$$

\uparrow
• average value
• expectation value

$\underbrace{\hspace{10em}}_{\rightarrow \text{weighted average by probability}}$

$$\langle x^2 \rangle = \sum_{x=0}^{\infty} x^2 \cdot P(x)$$

$$\langle f(x) \rangle = \sum_{x=0}^{\infty} f(x) \cdot P(x)$$

Example (Blundell 3.3)

$$P(x) = \frac{e^{-m} m^x}{x!}; \text{ show } \sum_{x=0}^{\infty} P(x) = 1$$

Looked up Taylor Series:

$$e^x = \sum_{n=0}^{\infty} \frac{x^n}{n!}$$

$$\sum_{x=0}^{\infty} \frac{e^{-m} m^x}{x!} = 1$$

$$e^{-m} \cdot \sum_{x=0}^{\infty} \frac{m^x}{x!} = 1$$

$$\sum_{x=0}^{\infty} \frac{m^x}{x!} = e^m \checkmark$$

$$\text{Show } \langle x \rangle = \sum_{x=0}^{\infty} x \cdot P(x) = m$$

$$= \sum_{x=0}^{\infty} x \cdot \frac{e^{-m} m^x}{x!} = m$$

$$= e^{-m} \sum_{x=0}^{\infty} \frac{x \cdot m^x}{x!} = m$$

