

$$\frac{P(S_{z})}{P(S_{1})} = \frac{E_{z}(S_{z})/k_{0}}{E_{z}(S_{z})/k_{0}}$$

$$\frac{P(S_{z})}{P(S_{1})} = \frac{E_{z}(S_{z})-S_{z}(S_{z})}{E_{z}(S_{z})-S_{z}(S_{z})}/k_{0}$$

$$\frac{P(S_{z})}{P(S_{1})} = \frac{E_{z}(S_{z})-S_{z}(S_{z})}{E_{z}(S_{z})-S_{z}(S_{z})} = \frac{1}{2}\left[U_{z}(S_{z})-U_{z}(S_{z})\right]$$

$$\frac{dU_{z}}{dU_{z}} = TdS_{z}$$

$$\frac{dE_{z}}{dU_{z}} = TdS_{z}$$

$$\frac{P(\Delta_{i})}{P(\Delta_{i})} = \frac{-[E(\Delta_{i})]/k_{B}T}{P(\Delta_{i})} = \frac{-E(\Delta_{i})]/k_{B}T}{e} = \frac{-E(\Delta_{i})/k_{B}T}{e} = \frac{-E(\Delta_{i})/k_{B}T}{e}$$

$$\frac{P(\Delta_z)}{P(\Delta_i)} = \frac{-E(\Delta_z)/k_BT}{-E(\Delta_i)/k_BT}$$

$$\frac{P(\lambda_2)}{-E(\lambda_2)/k_BT} = \frac{P(\lambda_1)}{-E(\lambda_1)/k_BT} = \frac{1}{Z}$$

$$\frac{P(A_2)}{P(A_2)} = \frac{P(A_1)}{-E(A_1)/k_BT} = \frac{1}{Z}$$

$$= \frac{P(A_1)}{Z} = \frac{1}{Z}$$

$$= \frac{1}{Z} = \frac{1}{Z} =$$

How do we calculate
$$Z$$
?

$$\sum P(\Delta) = 1 = \sum Z e = 1$$
From probability

$$Z = \sum E e$$

$$Z = E e$$
Function in the probability

$$Z = \sum E e$$
Figure 1.

$$\frac{1}{2} \leq e = 1$$

An example: probability of finding a H in its first example state T=5800K Suis Sheve from the ground state to the first excited state 10.2eV eV -> evergy of one electron accelerated from rest by a potential of 1V. DK=qDV=1.6.159C.1V=1.6.109J 1 eV = 1.6.15 BJ KOT = 1.38.10 J. 5800 K $\frac{P(s_2)}{P(s_1)} = C$ kg = [eV] = 1.38.10²³ J. (eV) $\frac{P(\Delta_z)}{P(\Delta_s)} = e^{-10.2eV/0.5eV} = e^{-70.4}$ = 0.8625 · 10-4 = 8.625.10 eV KRT = 8.625.105 eV .5400K = 0.5 eV $= 14.10^{4}$ X4 degenerate states

6.2 Average Values

Problem 6.6 + 6.12

$$P(\Delta) = \frac{1}{Z} e \Rightarrow P(\Delta) = \frac{1}{Z}$$

$$Z = \underbrace{\sum_{b}^{-E(b)} k_b T}_{b} \longrightarrow Z = \underbrace{\sum_{b}^{-E(b)} k_b T}_{b}$$

What is the average energy?

hat is not accorded to the following fund
$$\langle E \rangle = \sum_{A} E(A) P(A) = \prod_{A} \sum_{B} E(A) e^{2 \pi i \alpha}$$

arcrange fund

expectation value war state we can integrate!

B = T

went

$$\frac{1}{2} \int_{0}^{\infty} dx dx$$

Publem 6.16 Show
$$\langle E \rangle = -\frac{1}{Z} \cdot \frac{\partial Z}{\partial \beta} = -\frac{\partial (\ln Z)}{\partial \beta}$$

$$Z = Se$$

$$\langle E \rangle = SE(A)P(A)$$

$$= \frac{1}{2}SE(A)e$$

$$= \frac{1}{2}SE(A)e$$

$$\langle E \rangle = \frac{2}{\Delta} \frac{1}{Z e^{\beta E(\Delta)}}$$

$$\langle E \rangle = -\frac{3Z}{2B}$$

$$\langle E \rangle = -\frac{1}{Z e^{\beta E(\Delta)}}$$

$$\langle E \rangle$$

$$\langle E \rangle = \frac{\mathcal{E}}{2} \frac{\mathsf{E}(\mathcal{S})}{\mathcal{E}} e^{\beta E(\mathcal{S})}$$

$$\frac{\mathcal{E}}{\mathcal{E}} e^{\beta E(\mathcal{S})}$$

$$\frac{\mathcal{E}}{\mathcal$$

Problems: 6.15, 6.20

Now, let's consider diatomic gases of rotational energy energy levels of hydrogen = quantized (discret) energy levels
$$E(j) = j(j+1) \cdot E$$

$$E(j) =$$

Z =
$$\sum_{j=0}^{10} (2j+1)e^{-j(j+1)} = ket$$

ved to miltiply

by the degeneracy

to count all of the

Boltzmann factors

$$Z = \int_{0}^{\infty} (2j+1) = j(j+1) = k_{R}T dj$$

hard north > ver northerentice
 this integral can be need ble kgT >> E

So now, what about average votational energy $\langle E_{rot} \rangle = -\frac{1}{2} \cdot \frac{\partial Z}{\partial \beta} = -\epsilon \beta \cdot \left(\frac{-1}{\epsilon \beta^2} \right) = k_B T$ $\downarrow^{str} \mathcal{U} = Nk_B T$ f = 2we are rotational degrees of freedom. f = 2 f = 2 f = 2 f = 2 f = 2

. Moleculus I/ vidistinguishable atoms (H2, O2, N2) $Z = \frac{kT}{2t} \implies proceed from here....$

Revesit the Equipartition theorem. $M = \frac{f}{2}Nk_{B}T$ true for all quadratic forms of energy $\frac{1}{2}mV_{x}$, $\frac{1}{2}T\omega_{x}^{2}$, $\frac{1}{2}kx^{2}$

Proof:
$$E(q) = Cq^2$$

Room variable

 $Z = Ze^{-\beta E(q)} = Ze^{-\beta Cq^2}$
 $Z = Ze^{-\beta E(q)} = Ze^{-\beta Cq^2}$

$$Z = \underbrace{\sum_{q} \underbrace{\int_{q} e^{\beta cq^{2}}}_{q} \Delta_{q}}_{q}$$
 as $\Delta_{q} \rightarrow \underbrace{\int_{q} e^{\beta cq^{2}}}_{q}$

$$Z = \int_{-\infty}^{\infty} e^{-\beta cq^{2}} dq \qquad \text{change of variable to evaluate}$$

$$X^{2} = \beta cq^{2}$$

$$X = q \sqrt{\beta c}$$

$$J_{X} = J_{Q} \sqrt{\beta c}$$

$$\langle E \rangle = -\frac{1}{2} \frac{\partial Z}{\partial \beta} = -\frac{\Delta q \sqrt{\beta c}}{\sqrt{\pi}} \cdot \frac{\partial}{\partial \beta} \left(\frac{\sqrt{\pi}}{\sqrt{q \sqrt{\beta c}}} \right) = -\frac{\Delta q \sqrt{\beta c}}{\sqrt{q \sqrt{c}}} \cdot \left(-\frac{1}{2} \right) \cdot \frac{1}{\beta^{3/2}}$$

$$\langle E \rangle = \frac{1}{2}\beta' = \frac{1}{2}kT$$

65) Partition function & Free Everagus Isolated system of fixed energy -> I is fundamental 5 = kB In 2 For a system held a constant T w/ a resorvoir Z is fundamental -> analogous to I Zegnalish to the number of microestates available to the system at some T.

Z = SE = Sum of Boltzman factors Helmholtz Fre Energy - F= kgln Z 1 incornets units -t= kB hZ F=-kBTINZ ?? -> YES, it is true

Recall, when is
$$F$$
 useful?

$$S = -\left(\frac{\partial F}{\partial T}\right)_{V,N}, \quad P = -\left(\frac{\partial F}{\partial V}\right)_{T,N}, \quad \mu = +\left(\frac{\partial F}{\partial N}\right)_{T,N}$$

distinguishability mathers

What can we say about
$$E(x)$$
?

$$E(p) = \frac{p^2}{2m}$$

more when $\frac{h}{2m}$ of Bright wavelengths

$$P_n = \frac{h}{2m}$$

$$P_n = \frac{nh}{2L}$$

$$E_n = \frac{n^2h^2}{8L^2m}$$

$$Z_{10} = \frac{n^2h^2}{n}$$

Seconds on integral

for large $L + T$

$$Z_{10} = L / \frac{2\pi m k_B T}{h^2}$$

so what can we do w/ this partition function? User it to find any of these quantities Problems: 6.6,12,15,20

6.6) I thought we did this one, but not quite. We worked on the ratio of their things in the sun's atmosphere. But this is different

from the good state to the first existed state 10.2eV = E1

 $\frac{P(b_2)}{= e} = e.$

KOT = 8.625.105 eV . 298 K= 6.0257 eV

 $\frac{P(\delta_2)}{P(\delta_2)} = e = 43.10^{-173}$ very few ionized hydroger at room temp.

But what about at 9500 K? LAT = 8.625.105-9500 K = 0.899 eV

A what about at you.

P(dz) = 2.9.10⁻⁶

X4 × degree on to Aucydros number of your will be a road number of ist joined Ht

6.12 CN Dever ground state
47.10 tever 1st executed state 3 - P(Az) - Le Courting For

3 - P(Az) - Le Courting For

-4.7.10 eV/vot Color for T

6.1 - C $\ln (0.1) = -\frac{4.7.10^4}{1.5}$ $T = \frac{-4.7.10^4 \text{ eV}}{1..(0.1)(8.625.10^5 \text{ eV/k})}$ T = 2.36 K