Squeralize to N coins  $\Omega(N,n) = \frac{N!}{n!(N-n)!}$ # of heads  $\binom{\mathsf{N}}{\mathsf{N}}$ 10 atoms is each atom can have 0 or 1 energy unit So how many posinte arrangements of 4 quanta (10 quanta) 4 energies vs. 10 energies = wacrochats What if atoms can have more then I energy wint at a time 

 $\mathcal{A}(N^d) = \frac{d^d N^{-1}}{d^d N^{-1}}$ paclates of energy macrostate > This model > Einstein Solid that can exchenge energy Two 501:25 Isolated from surroundings Slow evergy transfir

e microcatale macrochabe 9=3 Stated = RA. St.B 9=5 q=1 2p(5) = 21 Qa(1)=3 Itotal = 63 Total number of microchatics possible 7 462 D(6,6) = 462

All microstatis are equally tildy & Fundamental assumption of statistical mechanics. Is But all mucrostates are not equally likely. Itolal (PA) Probability of solid A = \_\_\_\_\_ having of energy S Scholal (Of A)
94 Lorge Numbers, 10 is not important Addition of small numbers 10 + 50 2 10

Very Large Numbers > Multiplication of large

1023 100 numbers is not important

10 10 10 23 10 + 23 10

10 0 10 = 10 \$\alpha \gentleft| 00

Stirling's Approximation N/2 N/e/27N ~ NN JZTN

en JZTN

unt all that

important

In NI ~ N In N - N

$$2(N,q) = \frac{(q+N-1)!}{q!(N-1)!} = \frac{(q+N)!}{q!(N!)!}$$

$$[nQ = \ln(q+N)! - \ln q! - \ln N!]$$

$$[q+N)\ln(q+N) - (q+N)$$

$$[nQ = (q+N)\ln(q+N) - (q+N) - q\ln q + q - N\ln N + N]$$

$$[nQ = (q+N)\ln(q+N) - q\ln q - N\ln N]$$

$$[nQ = (q+N)\ln(q+N) - q\ln q - N\ln N]$$

$$[nq+N] = \frac{(q+N)!}{q!(q+N)} = \frac{(q+N)!}{q!}$$

$$[nq+N] = \frac{(q+N)!}{q!} = \frac{(q+N)!}{q!}$$

$$\Omega(q>>N) \approx e^{N \ln \frac{q}{2} + N} = (\frac{q}{N})^N e^N$$

$$Q(q>7N) = \left(\frac{eq}{N}\right)$$

$$Q(Nq)$$

Now go beek and use this .w/ Einsten solid. Sume # particles Stated = (ega NA (egB) = (egB) (GAGB) NA = NR  $Q_{\text{max}} = \left(\frac{e}{N}\right)^{2N} \left(\frac{q}{2}\right)^{2N}$ 2 max -> 9 A = 9 B = 9 Grandman function
N (2x)

2 = SL Max

Width =  $\frac{91}{100}$  =  $\frac{1}{100}$  =  $\frac{1}{100}$  =  $\frac{1}{100}$  =  $\frac{1}{100}$  =  $\frac{1}{100}$ HW: 9,10,13,18,22 The multiplicity of an ideal gas. > macroctate > volume, total energy, number Ω = distribution of distribution of particles in energy amount the particles a, dV-Vp (conface area of momentum apace) physical volume

Herenburg Uncertainty Principle Lx == # of distinct places to put particle in X-direction LZ LPx LPz DPz DPz

what about two particles?

$$Q_z = Q_A Q_B = \frac{V^2}{(h^3)^2} \cdot V_P^* \cdot \frac{1}{2}$$
 $\stackrel{?}{P_z V_Z}$ 
 $\stackrel{?}{P_z V_Z}$ 
 $\stackrel{?}{P_z V_Z}$ 
 $\stackrel{?}{P_z V_Z}$ 

what about N particles? SLN = 1. VN VP go boek to our particle has everally U U = 1 mu2 = 1 m ( vx + vy + vz)  $U = \frac{1}{2m} \left( p_x^2 + p_y^2 + p_z^2 \right)$  $\rho_x^2 + \rho_y^2 + \rho_z^2 = \left( \sqrt{2} m U \right)^2$ 

$$\chi^{2} + y^{2} + z^{2} = r^{2} \rightarrow 4\pi r^{2} \rightarrow 4\pi (\sqrt{2mn})^{2}$$
87 m U

$$\frac{2 \text{ particles}?}{p_{1x}^{2} + p_{1y}^{2} + p_{1z}^{2} + p_{2x}^{2} + p_{2y}^{2} + p_{2z}^{2} = ([2mU])^{2}}$$

6 dimensional sphere > hyperesphere

Surface area
for an amy
dimensional sphere
3N dimensional hypersphere

$$\Omega_{N} = \frac{1}{N!} \frac{V^{N}}{V^{2N}} \cdot \frac{2\pi^{N/2}}{(3N-1)!} \left(2\pi l_{N}^{N-1}\right)^{2N-1}$$

$$Q_{N} = \frac{1}{N!} \frac{V^{N}}{h^{3N}} \cdot \frac{3N/2}{(3N)!} (2MN)^{\frac{3N}{2}} \frac{3N}{2}$$

1D are 
$$\rightarrow$$
 D

2D area  $\rightarrow$  2TT

3D area  $\rightarrow$   $2TT$ 

D area  $\rightarrow$   $(2T)^{2}$ 
 $(\frac{1}{2}-1)!$ 
 $(\frac{1}{2}-1)!$ 

gamma function

$$Q_N = f(N) \cdot V^N \cdot U^{3N/2}$$

Z ideal gasses interacting

Sentropy

$$g = 2N$$
 $2N$ 
 $2N$ 
 $2N$ 
 $2(N,q)^2 \left(\frac{q+N}{q}\right)^4 \left(\frac{q+N}{N}\right)^N$ 
 $\sqrt{2\pi q} (q+N)/N$ 

26,24,29,30

$$2.22$$
 (a)  $q = 2N$ 

total macroestates = 2N+1

(b) 
$$\Omega = \left(\frac{q+N}{q}\right)^{2} \left(\frac{q+N}{N}\right)^{N} \quad \left(N = 2N\right)^{2}$$

$$= \left(\frac{2\pi q \left(q+N\right)}{N}\right)^{2} \quad \left(q = 2N\right)^{2}$$

$$= a \quad \text{few sho}$$

 $=\frac{2^{4N}}{(8\pi N)^{2}}$ 

(c) 
$$\Omega_{\text{max}} = \Omega_{\Lambda}(N=N, q=N) \Omega_{\mathcal{B}}(N=N, q=N)$$

nidh = 
$$\frac{A}{\text{height}} = \frac{(b)}{(c)} = \dots$$

$$\sqrt{2\pi N} \rightarrow \sqrt{2\pi N} = ... = 2.5.10$$

Any large system in equilibrium will be found in the macrostate, with the greatest multiplicity.

2nd Law of themodynamics

Multiplicity tends to increase

(andropy)

Spontaneous

process

S = Ind

KB

Entropy of an ideal ages

$$S = k_B \ln 2 = \frac{1}{N!} \frac{V^N}{h^{3N}} \cdot \frac{13N/2}{(3N)!} (2mN)^{\frac{3N}{2}}$$

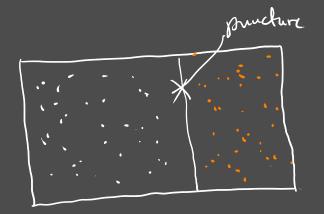
$$S = k_B N \left( ln \left( \frac{V}{N} \left( \frac{4\pi m U}{3N h^2} \right)^{3/2} \right) + \frac{5}{2} \right)$$

What is the entropy of I mol of Nz U=5NKBT at room temp t atm presence?  $\Delta S = S(v_f) - S(v_i) = k_B \ln \left(\frac{S_f}{S_i}\right)$ DS = KBN IN/NE) Explueron Conestant N, U DN = O Q = -W

Economy in entropy

#32

(Free Expansion) Joule Expansion 1 1 1 1 mentated no mesh or pull M=Q+W DN=0 mg no change in temp



BA = NKBINYI

NSA = NSB

15total = DSA + 15g

I for equal volumes Vp = ZV;

15total = 2Nkglu2

La entury of mixing