Chapter 5 - Free energy and chemical thermodynamics

Goal: Apply laws of thermodynamics to non-cyclic processes like chemical reactions, phase changes, and other transformations.

Previously:

All = TdS - pdN + µdN

total U was fixed what if T is fixed but

what if p is fixed but

constant T t Constant p processes

Enthalpy - energy plus the work to make room for a system under constant pressure from the survoundings $H \equiv U + \rho V$

Helmholtz Fre Envoys > total energy to create a system minus the heat you can extract from the curroundings at conestant T.

F = U-TS Sall work done on the system by us and the surroundings.

Gibbs Free Everyy G = U - TS + pV G = H - TS

U, H, F, G -> thermodynamic potentials

What about changes in F + G?

$$dF = dU - TdS$$

$$dF = dQ + dW - TdS$$

$$for a reversible process$$

$$dF = TdS + dW - TdS$$

$$dF = TdS + dW - TdS$$

$$dF = dW$$

$$S amount of work down on the system

$$dF \le dW$$

$$dG = dU - TdS + pdV$$

$$dQ_{ror} = TdS$$

$$dW - TdS + pdV$$

$$dQ_{ror} = TdS$$

$$dW - pdV + dW_{other}$$

$$dG = dW_{other}$$$$

DG is very nestal, how is it measured. First measure DH -> heat absorbed or released for a reaction at constant presence + no other other work Then calculate BS from initial and final Sreed Treed

To Lot IT DS = Sprd - Smut Sprd = Jo Co dt Then $\Delta G = \Delta H - T \cdot \Delta S$

Problem 5.2 T = 298K Calculate SG, from SH +S. P = 1 ber = 105 Pc = late = 1.013.105 Pa DG= DH-TOS $N_1 + 3H_2 \rightarrow 2NH_3$ AH = OKJ AH = -46.11 KJ, mol S=191.61J S=130.68 J S=192.45 J/Kmol DH = Hprof - Hreact = 2mol·(-46.11 kt/mol) = -92.22 kT 15 = Sprod - Screet = 2 mol · 192.45 J (km) - 191.61 J - 2 mol · 130.68 J (km) DS = -198,75 T/ 16= DH- TAS = -92.22 kJ - (298 k)(-198.75 J/k)

Electrolysis, Fuel Cells, Batteries $H_2O \rightarrow H_2 + \frac{1}{2}O_Z$ How much electrical work? NH = 286 kJ -> heat out to run to puch atmospher away PAV = In-R.T = 1,5 mol (8.31 J/kmol) (300 K) = 3.7 kJ ~ 4 kJ 282 kJ will remain in the system in the form of potential energy Is do we wed to do all of this work? heat from the environment?

What is the change in entropy for this cystem? $S_{H_20} = 70 \text{ J/k}$ $S_{H_2} = 131 \text{ J/k}$ $S_0 = 205 \text{ J/k}$ products Hz 20z Spool = 131 J/L + 1.205 J/ = 233,5 J/ DS = 233.51/k - 70 J/k = 163.5 J/k entropy mercago so the most heat that can enter the system will be Q = TSS = 2985/2. 163.55/K Q= 48.7 KJ Go of the 286 KJ that go in, 48.7 kJ come from beat from convroundings. 286KJ-48.7KJ=237.3KJ -> come from electrical work matches 16 from the book 7

In reverse, we can extract 237 kJ of electrical work! H20 -> 16 =- 237.3kJ -> 49 kJ of waste heat to surrounding. H2+202=>H20 -> DN = 282kJ -> from chemical reaching -> PAV = 4kJ ~ from collapen of gas to liquid Compare to chapter 4 S Fred Cell efficiency = what we get = $\frac{273 \, \text{kJ}}{286 \, \text{kJ}} = 83\%$ (car (theoretical) ~50°/ (prectual) 20 - 30% Battery Pb + PbOz + 4H+ + 250 -2 -> 2PbSO4 + 2H20 Start W/ AH -> heat to accomplish this reaction DH =-316 KJ/mol energy out from this reaction at conchant pressure NG = -394 KJ/mol more than DH! dectrical energy out

How? Heat coming into the system from the surroundings

394/bJ/ - 316/bJ/ = 78/bJ/

18/bJ = TAS

Warracal

Warracan in cutopy

was the system can

mas the system can absorb heat from the surroundings

What about the energy = Voltage

Let are given up at the - electron

Let Zet are taken up at the + electron

Voltage = We = 394 kJ

Terol of

Voltage of reaction

Thermodynamic Identity

$$dU = TdS - PdV + \mu dN$$

$$T = \left(\frac{\partial S}{\partial u}\right)_{v, N}$$

$$variables$$

Enthalpry

Helmholtz Fre Enrapy

$$F = U - TS$$

$$dF = JU - TJS - SJT$$

$$\Rightarrow JF = -SJT - PdV + \mu JN$$

Ex.
$$dp = 0$$
 $dN = 0$ for reversible
 $dH = TdS U$ isoberic process
 $dQ = dH$

EX.
$$dT=0$$
 isothermal process

 $dN=0$ | Lyrenerish

 $dF=-pdV$ | $dW=-pdV$
 $dF=dW$

Gibbs Free Everagy

-> dG=-SdT+Vdp+ pdN

-> very natural variables

for experiments

take
$$JF = -SJT - pJV + pJN$$

- hold $V + N$ constant

 $JV = 0$
 $JN = 0$
 $JF = -SJT$

authory is the rate of change of

 $S = -\left(\frac{JF}{JT}\right)V_{,N}$
 $F = v.c.t.$
 $JF = -\left(\frac{JF}{JT}\right)V_{,N}$
 $JF = \left(\frac{JF}{JN}\right)T_{,N}$
 $JF = \left(\frac{JF}{JN}\right)T_{,N}$

$$\leq = -\left(\frac{\partial G}{\partial T}\right)_{P,N} \quad V = \left(\frac{\partial G}{\partial P}\right)_{T,N} \quad M = \left(\frac{\partial G}{\partial N}\right)_{T,P}$$

(mol of $C \Rightarrow 5.3.10^6 \text{ m}^3$)

G = OKJ - most stable elemental

Colobs increasers by 5.3.10° J pur Pa of
present above atmospheri present

(5,665 at 30°C (303K)

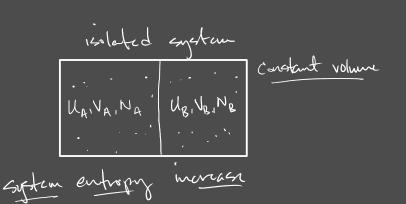
G_{H20} = -237.13 kJ at 288 k + later

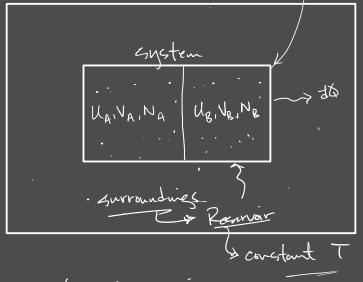
SH20 = 69.91 J/K

>
$$H_{20}$$
 / F = $349.55 J$
 $S = \left(\frac{36}{3T}\right)_{P,N} = > \Delta G = S.\Delta T = \left(\frac{9.91 J}{k}.5k = \frac{349.55 J}{1 - 236.78 kJ}\right)$

5.2 Free Energy as a force toward equilibrium

constant volume





total entropy increases

dStotal = dS + dSR

express in

express i

$$dS_{total} = dS - \frac{1}{T}dU$$

$$= \frac{1}{T}(TdS - dU) = -\frac{1}{T}(dU - TdS)$$

> dStotal = -dF = decrease

Helmholte Fre Energy

System will minimized

its Helmholtz For Everyy

liviting conditions

dT=0

dV=0

dN=0

what about keeping pressure, temperature, number constant?

$$dS_{total} = dS + dS_{R}$$

$$dS_{total} = dS + dS_{R}$$

$$dV = -dV_{R}$$

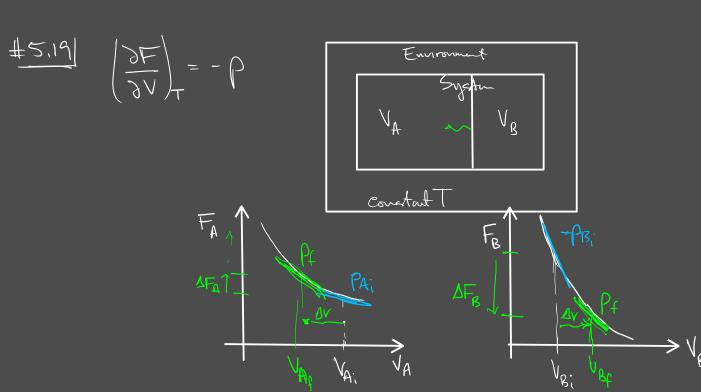
$$dS_{total} = dS - dV - dV$$

$$dS_{total} = dS - dV - dV$$

$$dS_{total} = -dG - dV$$

$$dS_{total} =$$

- * At constant energy and volume, S tends to increase
- * At constant temperature and volume, F tends to decrease
- * At constant temperature and pressure, G tends to decrease



Gibbs Fru Energy & Chemical Potrutial 1G = - SET + V2p + men 2G= pdN $\mu = \left(\frac{36}{3N}\right)_{T_p}$ JG= MN ly is pr constant w/ N. each new perticle

so the Leventy does

not change.

M = (DF)

is a conectant

W/ N here?

No! dencity increases

to keep conectant volume.

How can we wer this? Derive the chemical potential for ideal gas, as a function of presence from earlier $\left(\frac{36}{3p}\right)_{T_1N} = V$ $\frac{3b}{3h} = \frac{N}{1} \frac{3b}{90}$ $\frac{\partial \mu}{\partial \rho} = \frac{V}{N}$ = ideal gas law: $\frac{V}{N} = \frac{K_R T}{\rho}$ $\frac{\partial \mu}{\partial \rho} = \frac{k_R T}{\rho} = \sum_{p} \Delta \mu = \int_{p}^{p} \frac{k_B T}{\rho} d\rho$ $\mu(T,P) - \mu(T,P^{\circ}) = k_{\overline{e}}T \ln(\frac{P}{P^{\circ}})$ $\mu(T,P) = k_B T \ln\left(\frac{P}{P^o}\right) + \mu(T,P^o)$ We as chemical potential at atmospheric pressure $M = -T \left(\frac{35}{3N} \right)_{N,N} = -k_B T \ln \left[\frac{V}{N} \left(\frac{2\pi m k_B T}{h^2} \right)^{3/2} \right] \approx \text{what is } \mu^2 ?$

Phase Transformations of Pure Substances La discontinuous change in properties or state for a small change- variable

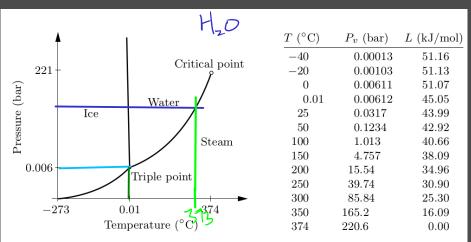


Figure 5.11. Phase diagram for H₂O (not to scale). The table gives the vapor pressure and molar latent heat for the solid-gas transformation (first three entries) and the liquid-gas transformation (remaining entries). Data from Keenan et al. (1978) and Lide (1994). Copyright ©2000, Addison-Wesley.



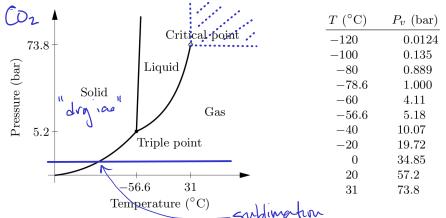


Figure 5.12. Phase diagram for carbon dioxide (not to scale). The table gives the vapor pressure along the solid-gas and liquid-gas equilibrium curves. Data from Lide (1994) and Reynolds (1979). Copyright ©2000, Addison-Wesley.

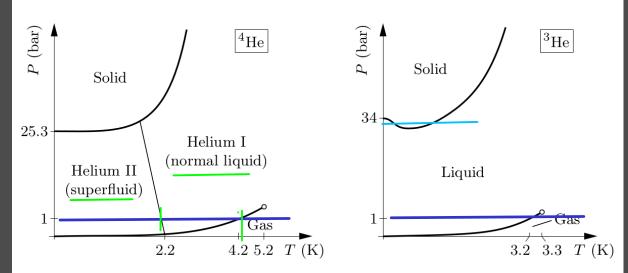


Figure 5.13. Phase diagrams of ⁴He (left) and ³He (right). Neither diagram is to scale, but qualitative relations between the diagrams are shown correctly. Not shown are the three different solid phases (crystal structures) of each isotope, or the superfluid phases of ³He below 3 mK. Copyright ©2000, Addison-Wesley.

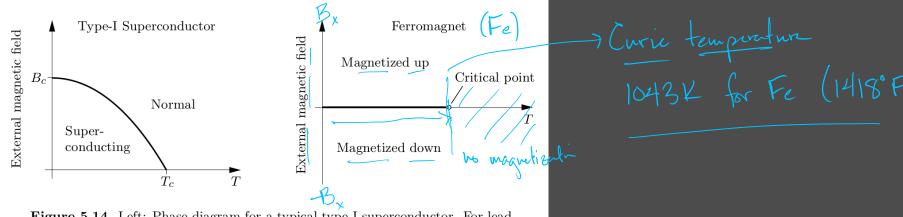


Figure 5.14. Left: Phase diagram for a typical type-I superconductor. For lead, $T_c = 7.2$ K and $B_c = 0.08$ T. Right: Phase diagram for a ferromagnet, assuming that the applied field and magnetization are always along a given axis. Copyright ©2000, Addison-Wesley.

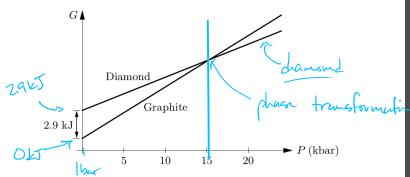


Figure 5.15. Molar Gibbs free energies of diamond and graphite as functions of pressure, at room temperature. These straight-line graphs are extrapolated from low pressures, neglecting the changes in volume as pressure increases. Copyright ©2000, Addison-Wesley.

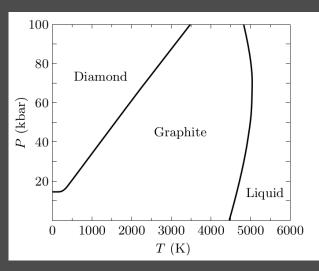


Figure 5.17. The experimental phase diagram of carbon. The stability region of the gas phase is not visible on this scale; the graphite-liquid-gas triple point is at the bottom of the graphite-liquid phase boundary, at 110 bars pressure. From David A. Young, Phase Diagrams of the Elements (University of California Press, Berkeley, 1991). Copyright ©2000, Addison-Wesley.

/H20 10 18/m?

/rack = 3000 kg/m3

what depth on earth would 15 kbar?

What about T dependence?

$$\left(\frac{\partial G}{\partial T}\right)_{P,N} = -S$$

$$S_{graplit} = 5.74 J_{K}$$

$$C = 2.38 J$$

as T is
raical, Gills
goes down,
graphite will
decrease more
quickly

$$h = \frac{1.5 \cdot 10^{9} P_{a}}{3.10^{4} N_{m}^{3}}$$

$$P = \frac{mq}{A}$$

$$P = \frac{p \cdot A \cdot h \cdot q}{A}$$

$$P = \frac{p \cdot A \cdot h \cdot q}{A}$$

$$P = \frac{p \cdot A \cdot h \cdot q}{A}$$

So what about the shape of the phase boundary I'm? on the lime > Ge = Ga incraso p and T so we are still on boundary line dGg = dGg dG = - SdT + Vdp + mdN -Sett + Vedp = -Sett + Vadp Salt-Selt= Vadp-Vedp $\frac{S_{q}-S_{e}}{V_{q}-V_{L}}=\frac{\Delta S}{\Delta V}$ DS = Latent Heat (Enthapy) dP = L Claverius - Clapeyron relation

(any phase)

$$\frac{JP}{JT} = \frac{AS}{AV} = \frac{3.4 \text{ J/k}}{1.9.10^{6} \text{ m}^{3}} = 1.8 \cdot 10^{6} \text{ Pa} = 18^{6} \text{ bar/k}$$

graphits becomes Stable 15kbar at 298K What about 100K higher temp?

mor depth

100 km - 200 km

Lab conditions 1600 K 60 leber