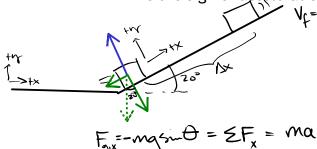
- 1. We have gone through several kinds of equations now and lets sum up some of these as proportions:
  - Fr = ma • acceleration is dir prop net force. a= First
  - assuming constant acceleration and beginning at rest, an object's velocity is proposed the displacement.  $V_{f}^{2} = V_{c}^{2} + \frac{1}{2a\Delta x} \qquad V_{f} = \sqrt{2a\Delta x} \qquad V_{f} = \sqrt{2a\Delta x}$  assuming constant acceleration and beginning at rest, an object's displacement is
  - $\Delta x = \frac{1}{2}at^2 \quad \Delta x \propto t^2$ prop to squarethe elapsed time. sed time.  $\Delta x = 1 + 1 \text{ at}^2$
  - for an object that has been dropped, the distance it has fallen is  $\frac{p_{1}}{p_{1}} + \frac{q_{1}}{q_{2}}$  velocity at that distance.  $\sqrt{1 q_{1}} + \frac{q_{2}}{q_{2}} + \frac{q_{1}}{q_{2}}$
  - assuming constant acceleration and beginning at rest, an object's velocity is  $\frac{dir}{dr} \frac{r}{r} \frac{dr}{dr} \frac{dr}$
- 2. I push a 100 kg box starting at rest along a friction-less floor, with a force of 100 N over a distance of 10 m. How fast is the box going at this point? If I did the same thing to a 200 kg box, then how fast is it going after 10 m? Some starters:
  - What is the net force on the box? | DO N

  - What is the final velocity after 10 m 4 47 ~/~

al velocity after 10 m 4.47 
$$\frac{1}{1}$$
  $\frac{1}{1}$   $\frac{1}{1$ 

- 3. Following up on the previous problem, if I stopped pushing after 10 m and the box continued with its speed, and then at then started sliding up a 20° ramp, then how far along the length of the ramp would the box rise? What height is this above the horizontal? Do the 100 kg and the 200 kg box rise to the same height? Some starters:
  - What is the net force on the box as it goes up the inclined plane?
  - What is the acceleration of the box as it goes up the inclined plane?
  - What is the sign of the displacement of the box going up the plane?
  - Is the sign of acceleration the same or different than displacement?



$$F_{g,x}$$
-mgsn $\theta = \xi F_x = ma_x$ 
-mgsn $\theta = ma_x$ 

$$-mgsn\theta = \Sigma F_x = ma_x$$

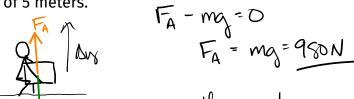
$$-mgsn\theta = ma_x$$

$$-gsn\theta = a_x = -9.85n20 = -3.35m/32$$

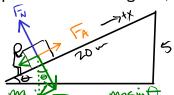
4. We want to examine the idea of mechanical advantage.

X1 = V2 + 2a1x  $-V_i^2 = 2a\Delta x$  $\Delta x = \frac{-v_i^2}{2(-3.35)} = \frac{-(4.47)^2}{2(-3.35)} = 2.98 \text{ m}$ 

• How much force would it take to lift a 100 kg box straight up at constant speed a distance of 5 meters.



• How much force would it take to push X box up an inclined plane that was 20 m long up to the same height? (again at constant speed)



$$F_{A} = mg \cdot n \theta$$

$$= 980N \left(\frac{5}{28}\right)$$

$$= 245 N$$

$$\sin\theta = \frac{5}{20} = \frac{1}{4} = 0.25$$

$$\theta = \sin^{-1}\left(\frac{5}{20}\right)$$

$$\theta = 14.4^{\circ}$$

• What is the ratio of the two forces in these two cases? Which would you rather do? This ratio is known as mechanical advantage

$$\frac{F_{up}}{F_{uchin}} = \frac{980N}{245N} = 4$$

· What is the ratio of the displacement in these two cases?

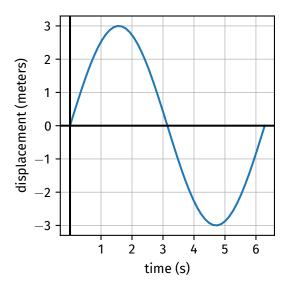
$$\frac{\Delta y_{up}}{\Delta x_{uzlin}} = \frac{5m}{20m} = \frac{1}{4}$$

• How can you use this idea to quickly figure out the force it would take you to push the box up a 100 m ramp that goes up the same height?

(5. Let's talk about springs. Hooke's Law is the relationship between the force exerted by a spring and amount the spring has been stretched or compressed. The amount a spring has been stretched or compressed is the displacement of the end of the spring. Hooke's law says the magnitude of the force exerted is directly proportional to the displacement of the end of the spring. Write this in terms of a proportionality statement and again as an equation with a constant of proportionality. What are the units of the constant of proportionality?

Draw a qualitative plot of the magnitude of this force vs displacement. What is the slope of this graph?

6. Consider the graph below of displacement under condition of not constant acceleration. What would a graph of velocity vs. time look like for this case? What about acceleration vs time.

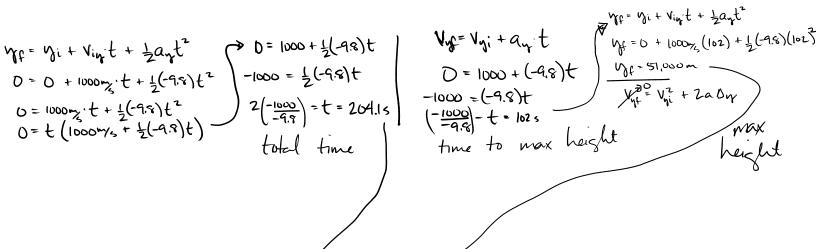


7. I push a 100 kg box starting at rest along a friction-less floor, with a force of 100 N for 10 s. How fast is the box going at this point? If I did the same thing to a 200 kg box, then how fast is it going after 10 s?

First = 
$$100N = Ma$$
 $100N = 100kg.a$ 
 $a = 1 \frac{1}{8}$ 

8. A follow up to the previous question. The momentum of an object is defined as the product of an object's mass and its velocity. In this case the momentum of this object changes because a force external to the object was exerted on it. What is the momentum

of the object initially? What is the momentum of the object at the end? It is said that the change in momentum of an object is equal to the *impulse*, where *impulse* is defined as the product of constant force and the amount of time the force is acting. Is that the case here? How could you use this to quickly find the final velocity of an object if the same force were pushing it for 100 s?



9. If I launch a cannonball from ground level with a speed of 1000 m/s, then there are a variety of angles to choose from. If I fire it at 90°, then how long will it take to come down? How high will it go? How far will it go horizontally? What about 80°? What about 70°? Let's just make a table...

7	0°? Let	i's just m	nake a table		- Vy=U;·CosA
_	Angle (	Time)/	Max Vertical Height	Horizontal Distance	**************************************
Vgi = 1000 · Sin 800	90°	204.15	51,000 m	O	
= 487.873	فر <sup>2</sup> 00 ع	2015	49,500 m	34,900 m	×
Vxi= 1000 20550°	/10°	1917	45,050	65,600	∠ Vx
Vxi=173.6m/4	√60°	176.7	38,300	48,400	
	\50°	1563	29,900	100,500	
Vy= Vyi + ay t	\40°	131.2	21,100	100,500	1000 m/s 1000 m/s
0=984.4+(-9.8)	,t 30°	102	[2,700	88,400	Λ <u>Λ</u>
$t = \frac{994.4}{9.8} = 100.5$	₅ /20°	69.8	5,970	65,600	Vyi=1000 Vyi=984 m/
7' \	/	35.4	1,540	34,900	Ø V <sub>x1</sub> =0
time to	0°	6	<b>D</b>	D	3
Total time 2 (100.5) + 1 (-9.8) (100.5) 2   1 x = Vx · t					
	Jr= 4	19,500 m	x haight	= 24,9005 honz	zontal distance

10. If a soccer ball with a radius of 10 cm is rolls along the ground without slipping at 5 m/s, then how many revolutions does it roll through in 10 s and what distance has a point on the edge of the ball traveled? Some starters:

• How fast is it spinning? By that we mean angular speed. 
$$W = \frac{\sqrt{1 - \frac{5m/5}{5}}}{\sqrt{10m}} = \frac{5m/5}{\sqrt{5}} =$$

- · How many radians does the ball rotate through in this time? What is that in revolutions?
- How far does it roll in this time? Is this the same distance as the distance of a point on the edge of the ball? Why or why not?

$$D = \omega \cdot t \qquad \omega = \Delta \theta$$

$$= 50 \text{ rad} (10 \text{ s})$$

$$\Delta \theta = 500 \text{ rad}$$

$$500 \text{ rad} \cdot \frac{1 \text{ resolution}}{2 \text{ TT rad}} = 79.6 \text{ resolution}$$

$$\Delta T = 50 \text{ rad} \cdot (0.10 \text{ m})$$

$$\Delta T = 50 \text{ rad} \cdot (0.10 \text{ m})$$

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$$\Delta T = 50 \text{ rad} \cdot (0.10 \text{ rad})$$

$$\Delta T = 50 \text{ rad} \cdot (0.10 \text{ rad})$$

$$\Delta T = 50 \text{ rad}$$

11. Following up on the previous problem, how many secon dis does it take for the ball to complete one revolution? This amount of time is referred to as the period of its rotation, and this is a similar characteristic time for the motion of the ball as the period of a pendulum was in the first lab.

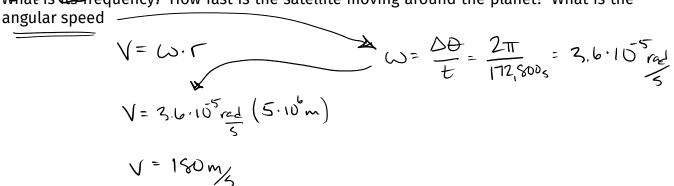
 $\omega = \Delta \theta \Rightarrow t = \Delta \theta$ 

- $t = \frac{2\pi}{50 \text{ red/s}} = 0.1265$ 12. Another follow up. How many revolutions does the ball travel through per second? You dould convert this from angular speed that you would have calculated in the first instance of this problem, but if all you new was the period of the ball's rotation, how could you calculate it from there? (Hint: what is the difference between revolutions per second and seconds per revoution?) This quantity of revolutions per unit of time is sometimes called frequency.
- 13. Suppose a satellite is in orbit around a distant planet. You observe the the satellite to be (5000 km)from the center of the planet, and rotating the planet once every 2 days. What is the mass of the planet you have discovered? What is the period of the satellites motion?

4 time for 1 revolution 6 problem states it takes 2 days

SAMFORD UNIVERSITY - WEEK 6

What is its frequency? How fast is the satellite moving around the planet? What is the



A projectile is launched from the ground with a velocity of 45.0 m/s at an angle of 30.0 degrees above the

horizontal. How far away does it land?  

$$V_{ix} = 45\cos 30 = 39m/s$$

$$V_{iy} = 45\sin 30 = 22.5m/s$$

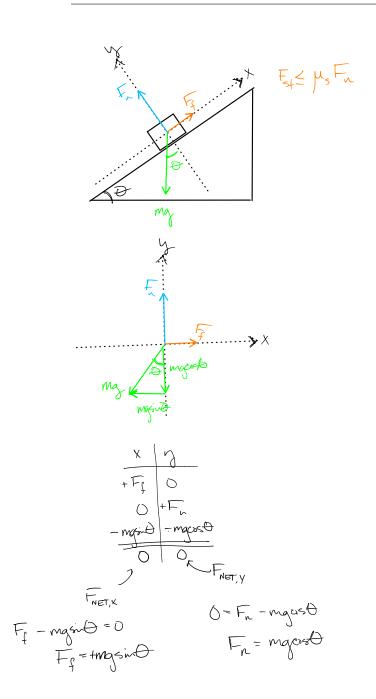
 $\Delta y = V_{1y} + \frac{1}{2}a_{y}^{2}$   $0 = 22.5t + \frac{1}{2}(-98)t^{2}$   $4.9t^{2} = 27.5t$  4.9t = 22.5 4.9t = 22.5 4.9t = 22.5

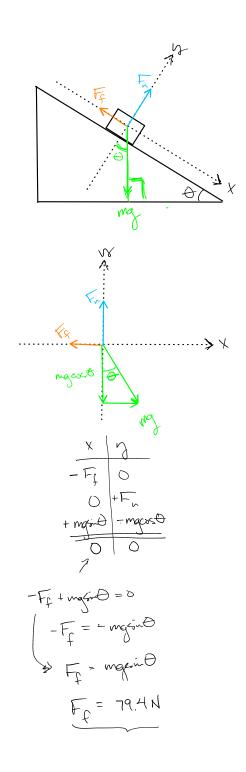
A arrow is released from a bow (ignore the height of the archer, so just assume it starts at ground level) with initial velocity of 700.0 m/s at an angle of 30.0 degrees above the horizontal. How long does it take to land if it was fired over level ground?

$$\mu = \frac{V^2}{g^2}$$

$$\omega = 1.5 \cdot 10^{-4} \text{ rad}_{S} = \frac{\Delta D}{\Delta t}$$

$$t = \frac{2\pi}{\omega} = \frac{121}{\omega}$$





W

$$\omega = \frac{\Delta \Phi}{\Delta t} \qquad = \frac{?}{V}$$

$$(\Delta t) / 45 \cdot 10^{4} = \frac{2\pi}{\Delta t} (\Delta t) = > \Delta t \cdot 1.45 \cdot 10^{4} = \frac{2\pi}{1.45 \cdot 10^{4}}$$

$$\Delta t = \frac{2\tau}{1.45 \cdot 10^{4}} = 43,300 \cdot 5 \cdot \frac{1}{3600} \cdot \frac{hr}{3600} = 12 \cdot hr$$

A cannon is fired with an initial velocity of 1000 m/s at an angle of 30 degrees above the horizontal. The cannon was fired from a 50 meter high cliff. What is the final y-component of velocity at the time the ball reaches the ground?

$$V_f^2 = V_i^2 + 2\alpha_y \Delta i y$$

$$V_f = \sqrt{V_i^2 + 2\alpha_y \Delta i y}$$

$$V_{yi} = 1000\% \sin 20^{\circ}$$

$$V_{F} = V_{i} + V_{yi} + \frac{1}{2}a_{y}t^{2}$$

$$0 = 50 + 500\% + \frac{1}{2}(4.8)t^{2}$$

$$c = 50 \quad B = 500$$

$$t = 102.145$$

$$W_{yf} = V_{yi} + a.t$$

$$V_{yf} = 500\% + (-9.8)(102.14s)$$

$$V_{yf} = -500.9 \text{ m/s}$$

If a soccer ball with a radius of 15 cm rolls along the ground at constant angular speed of 10 radians per second, then how far along the ground does the ball roll in 10 seconds?

$$\omega = 10 \text{ rad}$$

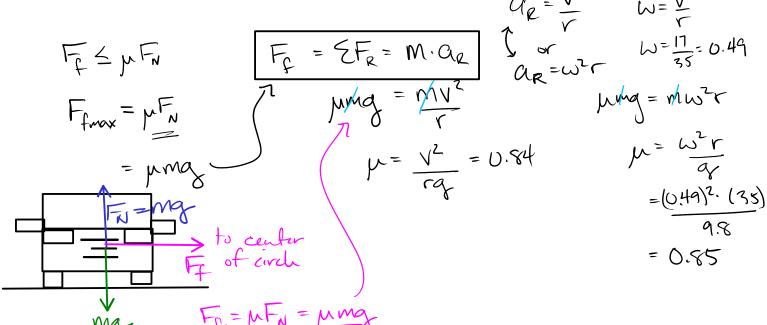
$$V = 10 \text{ rad}$$

$$V = 10 \text{ rad}$$

$$\Delta x = 7$$

$$\Delta t = 10 \text{ rad}$$

A car travels at 17 m/s without skidding around a level curved road with a radius of 35m. What is the static friction coefficient between the tires and the road if this speed is as fast as the car can go without sliding?



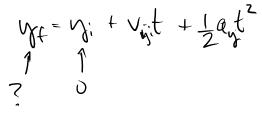
A arrow is released from a bow (ignore the height of the archer, so just assume it starts at ground level) with an initial velocity of 70.0 m/s at an angle of 30.0 degrees above the horizontal. How long does it take to reach the highest height of its flight?

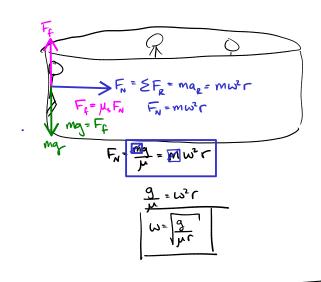
t=?  $V_{yi} = 70.5 \text{m} 30 = 35 \text{m/s}$   $V_{yf} = 0$  eat highest height

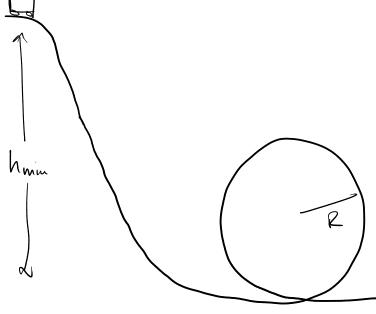
$$\rightarrow V_{yf} = V_{yi} + at$$

$$0 = 35\% + (-9.8) t$$

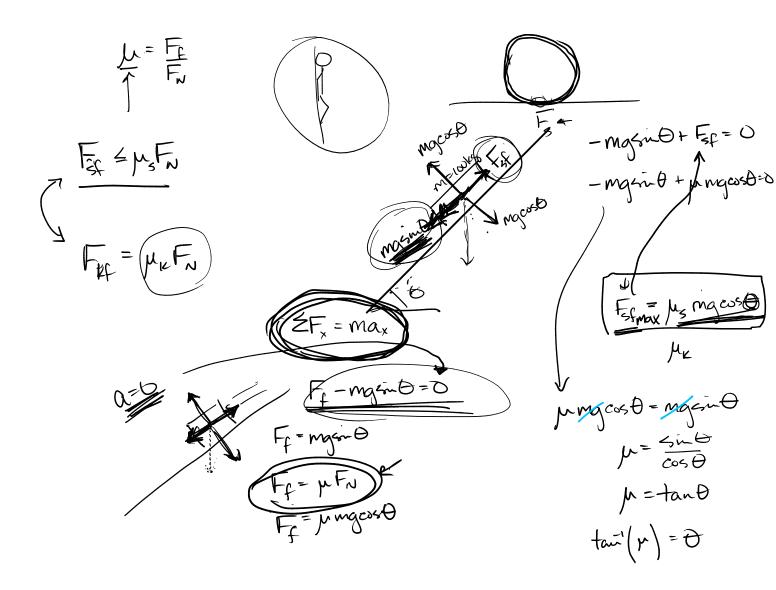
$$t \approx 3.56$$



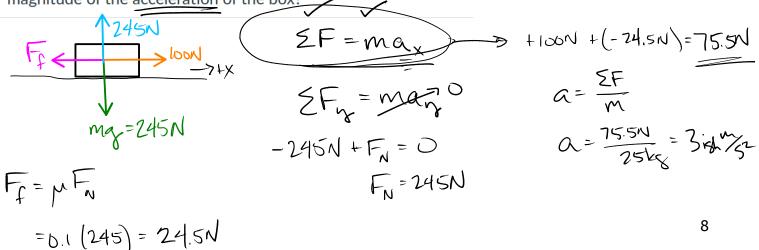




$$F_G = \frac{G_1 M_1 M_2}{C^2} = \frac{M_2 V^2}{C}$$



A 25 kg crate of apples is sliding across a level floor to the right with an applied force of 100 N, and a coefficient of friction between the crate and the floor being  $\mu=0.1$ . What is the magnitude of the acceleration of the box?



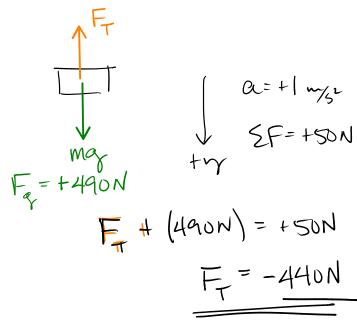
A 50 kg crate of apples is being lowered by a rope straight downwards and has an acceleration of 1 m/s^2 in the downward direction. What is the force the rope is applying ot the box? (magnitude and direction)

Steel Mag

$$a = -|w_{82}|$$
  
 $\Sigma F = m \cdot a$   
 $\Sigma F = -50 N$ 

$$F_{T} - 490N = -50N$$

$$F_{T} = +440N$$



440N upwart

In order to lift a certain box straight up at constant speed, I would need to exert a force of 1000 N on it. If I were to put the same box on an ramp inclined at 30 degrees to the horizontal, then what force would I need to exert to push it up the ramp at constant speed?