

At the end of this worksheet you should be able to

- convert units within the metric system.
- apply how to correctly convert area and volume units.
- apply scientific notation.
- apply the definition of percent change.
- convert between a ratio statement and percent change statement.
- apply the two forms of proportionality statements to make predictions from dependent variable change.

1. How many meters are in a decameter and how do you know?
2. How many decameters are in a meter and why?
3. How many centimeters are in a meter? Draw on your paper approximately a centimeter.
4. How many millimeters are in a meter and how many meters are in a millimeter?
5. The diameter of the earth is 6,380,000 m. What is this in kilometers?
6. How many centimeters are in 3.2 km?
7. How many inches are in 1 meter? Do this using the conversion of 1 in = 2.54 cm.
8. If I say your desk has an area of 0.5 meters, then what is wrong with that statement?

9. Convert miles per hour to meters per second.

$$1 \frac{\cancel{\text{miles}}}{\cancel{\text{hour}}} \cdot \frac{\cancel{\text{hr}}}{\cancel{\text{min}}} \cdot \frac{\cancel{\text{min}}}{\cancel{\text{s}}} \cdot \frac{\text{meter}}{\cancel{\text{miles}}} = \frac{\text{meters}}{\cancel{\text{sec}}}$$

10. List as many formulas for the area of different shapes as you can remember (or look some up). What do these all have in common? What about volume formulas? What does this tell you about the units of these kinds of quantities?

11. If your desk has an area of 0.5 meters^2 , then what is its area in centimeters^2

$$0.5 \text{ m}^2 \cdot \frac{(100 \text{ cm})^2}{(1 \text{ m})^2} = 0.5 \cdot 10^4 \text{ cm}^2 = 5 \cdot 10^3 \text{ cm}^2$$

12. If a ball has a diameter of 18 cm, then what is the volume of the ball in meters^3 ?

$$V = \frac{4}{3} \pi r^3$$

$$3.05 \cdot 10^{-3} \text{ m}^3$$

13. Calculate your age in seconds on your last birthday.

14. Make up your own unit conversion problem that involves at least two conversions chained together.

15. Put the number 21,345,000,000 kg in scientific notation?

16. Put the number 0.0000000234 km in scientific notation?

17. Correct the scientific notation of 140×10^{-3} seconds

18. Correct the scientific notation of 0.012×10^{-3} meters

19. What is 0.000345 in micrometers μm ? *↑ meters*

20. What is $3.4 \times 10^5 \text{ m}$ in kilometers?

21. If I have three times as many marbles as you do then what is the ratio of my marbles to yours?
What is the ratio of your marbles to mine?

22. If I increase in speed from 25 mph to 40 mph, then by what percent has my speed changed?
By what ratio has the speed changed?

Percent Change $\frac{n\%}{100} = \frac{a_2 - a_1}{a_1}$ *final initial* $\frac{40 \text{ mph} - 25 \text{ mph}}{25 \text{ mph}} = \frac{15}{25} = \frac{3}{5} = 0.6 \rightarrow \boxed{60\%}$ *ratio* $\frac{\text{final}}{\text{initial}} = \frac{a_2}{a_1} = \frac{40}{25} = 1.6$

23. If my speed changes from 29 mph to 10 mph, then by what percent has my speed changed?
What is the negative sign in the answer tell you? By what factor has your speed changed from initially to finally? Could a negative ratio make sense ~~here~~?

$\boxed{-65\%}$ *negative means decrease*

24. If the generic variable (y) is inversely proportional to the a variable (x) , then write out this statement mathematically in two ways.

$$y \propto x^{-1} \quad \text{or} \quad y \propto \frac{1}{x}$$

$$\textcircled{1} \quad \frac{y_2}{y_1} = \left(\frac{x_2}{x_1} \right)^{-1} \Rightarrow \frac{y_2}{y_1} = \frac{x_1}{x_2}$$

$$\textcircled{2} \quad y = k \cdot x^{-1} \Rightarrow y = \frac{k}{x}$$

if x doubles
 $\frac{x_2}{x_1} = 2$
 $\frac{x_1}{x_2} = \frac{1}{2}$
Now
 $\frac{y_2}{y_1} = \frac{1}{2}$

direct $y \propto x^1$
inverse $y \propto x^{-1}$

square $y \propto x^2$

$$A \propto bh$$

$$A = kbh$$

$$\frac{A_2}{A_1} = \frac{b_2}{b_1} \text{ or } \frac{A_2}{A_1} = \frac{h_2}{h_1}$$

25. Since the area of a triangle is directly proportional to both the base and height, then how would an equation for this look like and what is the constant of proportionality?

$$A = k \cdot b \cdot h \quad k = \frac{1}{2}$$

26. The formula for the volume of a cylinder is $V = \pi r^2 h$. How would you write out a proportionality statement that was consistent with this formula? What is the constant of proportionality?

$$V \propto r^2 h \rightarrow \frac{V_2}{V_1} = \left(\frac{r_2}{r_1}\right)^2 \text{ if height is constant} \quad \left[\frac{V_2}{V_1} = \frac{h_2}{h_1} \text{ if } r \text{ is constant} \right]$$

27. If the radius of a sphere changes by a factor of 2.7, then by what factor does the volume change?

$$V = \frac{4}{3}\pi r^3 \rightarrow V \propto r^3 \rightarrow \frac{V_2}{V_1} = \left(\frac{r_2}{r_1}\right)^3 \quad \frac{r_2}{r_1} = 2.7 \quad \frac{V_2}{V_1} = (2.7)^3 = 19.68$$

28. How would you turn the previous problem "inside out"?

29. By what percent does the volume change in the previous two problems?

$$\frac{V_2}{V_1} = 19.68 \quad \frac{\%}{100} = \frac{V_2}{V_1} - 1$$

$$\boxed{\% = 1868\%}$$

$$\text{given } \frac{V_2}{V_1} = 19.68$$

$$\frac{V_2}{V_1} = \left(\frac{r_2}{r_1}\right)^3$$

$$\sqrt[3]{19.68} = \frac{r_2}{r_1}$$

$$(19.68)^{1/3} = \frac{r_2}{r_1}$$

Why does the constant not appear in a proportionality statement?

$$V_2 = \frac{4}{3}\pi r_2^3$$

$$V_1 = \frac{4}{3}\pi r_1^3$$

$$\frac{V_2}{V_1} = \frac{r_2^3}{r_1^3}$$

$$\frac{V_2}{V_1} = \left(\frac{r_2}{r_1}\right)^3$$

$$\underline{\underline{V \propto r^3}}$$

$$\% \rightarrow \text{ratio}$$

$$10 = \frac{x_2}{x_1 + 1}$$

$$\frac{x_2}{x_1} = 1.1$$