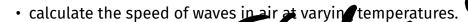
## At the end of this worksheet you should be able to



• operate the Kelvin temperature scale as an absolute temperature scale.

· alculate the intensity of a sound wave at any dictance from the source.

• talculate the loudness of any Sund source including the listener's distance from the source.

• apply the principles of standing wave to pipes of en on one end or open on both ends.

• use the principle of beat frequency to calculate tor an unlocky frequency.

1. According to the notes, the speed of sound in a granke air is proportional to the square root of the temperature. But much like when we taked about pressure, we need to use an *absolute* temperature scale. In the Al histem the Kelvin temperature scale is an absolute measure of temperature, because 0 K is the lowest conceivable temperature. The relationship of the Kelvin scale to the Celsius scale is that 0 K is  $-273.15\,^{\circ}$ C. So what is  $0\,^{\circ}$ C in Kelvin? What is  $20\,^{\circ}$ C in Kelvin? What is  $300\,^{\circ}$ C in Celsius?

$$\frac{DK}{=} - 273.15^{\circ}C \quad \text{Fabsolut. Zero}$$

$$\frac{213.15K}{=} 0^{\circ}C \qquad T_{K} = T_{C} + 273.15^{\circ}$$

$$\frac{293.15K}{=} 20^{\circ}C \qquad T_{C} = T_{K} - 273.15^{\circ}$$

$$\frac{313.15K}{=} 100^{\circ}C \qquad T_{C} = T_{K} - 273.15^{\circ}$$

2. The size of the degrees are the same in both the Kelvin and Celsius temperature scales. So if the air temperature changes from 10 °C to 36 °C, by how much does the temperature change in Kelvin? If the air temperature changes by 20 °C, then how much does the temperature change in Kelvin?

3. The Celsius scale has its zero point set at the freezing point of water. While this puts the temperatures that humans most commonly deal with at a useful size, it is not acceptable when using proportionality reasoning. For example, does it make sense to refer to doubling the temperature in the Celsius scale? Is 20 °C twice the temperature of 10 °C? If not, what is the proper ratio of these two temperatures? What is the percent change going from 10 °C to 20 °C?

4. So in these problems in order to find the speed of sound at any temperature, we need to use a known reference speed at a known temperature. We will use the reference speed of sound in air of  $v_0 = 331 \,\mathrm{m/s}$  at the temperature of  $T = 0 \,^{\circ}\mathrm{C}$  or 273.15 K. So what is the speed of sound at 20 °C? At what temperature would the speed of sound be 300 m/s? At what temperature would it be 400 m/s?

What temperature would it be 400 m/s?

$$V \propto T^{1/2}$$

$$V = K T^{1/2}$$

$$V = K T^{1/2}$$

$$V = 343 \text{ m/s}$$

$$V = 324 \text{ K}$$

$$V = 343 \text{ m/s}$$

$$V = 324 \text{ K}$$

5. If the temperature of air decreased by 10%, then by what percent would the speed of sound decrease?

7. 
$$\Delta \Rightarrow \text{ratio} \Rightarrow \text{proportion} \Rightarrow \text{proportion} \Rightarrow \text{ratio} \Rightarrow \text{proportion} \Rightarrow \text{ratio} \Rightarrow \text{proportion} \Rightarrow \text{pr$$

6. 40 °C is just about as hot as it ever gets in Alabama in the summer and -15 °C is just about as cold as it ever gets in the winter. What is this ratio of temperatures and what is the ratio of speeds of sound in the hottest day of the summer to speeds of sound in the coldest night in the winter? What is the speed of sound at these temperatures?

Im away from the explosion? What is the intensity 10 m away? 100 m away?

$$\frac{\Delta E}{\Delta t} = \frac{100,000 J}{0.0015} = 1 \cdot 10^8 \text{ Watts}$$

$$\frac{\times 0.10}{1 \cdot 10^7 \text{ Watts}} = \frac{1.10^7 \text{ Watts}}{1.10^7 \text{ Watts}} = 8 \cdot 10^5 \text{ W}$$

$$\frac{I_0}{I_0} = \frac{I_0}{I_0} = \frac{I_0}{I_0}$$

8. If the intensity of music from a loudspeaker at a concert is  $1 \text{W/m}^2$  at a distance of 1 m away, then what is the intensity 10 m away? 100 m away?

9. For all of the intensities in the previous problems, calculate their sound level (i.e loudness) relative to the threshold of hearing, 
$$I_0 = 10^{-12} \,\text{W/m}^2$$
.

$$\beta = 10 \cdot \log_{10} \left( \frac{I}{I_0} \right) \qquad \beta = 10 \cdot \log_{10} \left( \frac{9 \cdot 10^5}{10^{-12}} \right) \qquad \beta_{10...} = 10 \log_{10} \left( \frac{8 \cdot 10^3}{10^{-12}} \right)$$

$$\beta = \left[ \text{deci Bels} \right] \qquad \beta_{10...} = 159 \text{ JB}$$

$$\beta_{10...} = 10 \log_{10} \left( \frac{80}{10^{-12}} \right) = 139 \text{ JB}$$

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10. If the sound level at the location of your ear is 60 dB, what is the intensity of sound? If your eardrum (also apparently called the tympanic membrane)has a diameter of 0.5 cm, then what power is delivered to your eardrum? d=0.005m

$$60dB = 10 \cdot log_{10} \left(\frac{I}{I_0}\right)$$

$$6 = log_{10} \left(\frac{I}{I_0}\right)$$

$$10^6 = \frac{I}{I_0} \Rightarrow I = 10^6 \cdot 10^{12} \text{ Mg}$$

$$I = 10^6 \text{ Mg}$$

$$I = \frac{P}{A_{ra}} \longrightarrow P = I \cdot A$$

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11. The intensity of a sound is doubled. What is the difference in the sound level change? Hint: subtract the sound level of 21 and 1 and then use the properties of logarithms that  $\log A - \log B = \log (A/B)$ 

$$\frac{I_2}{I_1} = 2$$

$$\beta_1 = 10 \log \left(\frac{I_1}{I_2}\right)$$

$$\beta_2 = (0) \times \left(\frac{I_2}{I_2}\right)$$

$$\beta_{z} - \beta_{i} = 10 \log \left( \frac{I_{z}}{I_{o}} \right) - 10 \log \left( \frac{I_{z}}{I_{o}} \right)$$

$$= 10 \log \left( \frac{I_{z}}{I_{o}} \right)$$

$$\beta_{z} - \beta_{i} = 10 \log \left( \frac{I_{z}}{I_{i}} \right)$$

$$\beta_{z} - \beta_{i} = 10 \log \left( 2 \right) = 3 dB$$

12. The smallest change in sound level that humans can detect is about 1dB. What is the ratio of intensity does this represent?

$$\beta_{z} - \beta_{i} = 10 \cdot \log_{1}(\frac{\mathbb{I}_{z}}{\mathbb{I}_{i}})$$

$$|\beta_{z} - \beta_{i}| = 10 \cdot \log_{1}(\frac{\mathbb{I}_{z}}{\mathbb{I}_{i}})$$

$$0.1 = \log_{1}(\frac{\mathbb{I}_{z}}{\mathbb{I}_{i}})$$

$$|\delta_{i}| = \frac{\mathbb{I}_{z}}{\mathbb{I}_{i}} = 1.20$$

13. What is the sound level 1 m away from a 100 W sound source? What is it 2 m away? Plot this change in sound level as a function of distance away from the source. If you double your distance away from a source of sound how much does the sound level change?

$$\frac{297 \, \text{K}}{\text{V}_{0}} = \sqrt{\frac{\text{T}_{1}}{\text{T}_{0}}} \Rightarrow \text{V}_{0} = 331 \, \text{m/s} \quad \text{T}_{0} = 273.15 \, \text{K}$$

$$\Rightarrow \text{V}_{1} = 345 \, \text{m/s}$$

14. What is the fundamental frequency and wavelength of a 1 m long pipe open at both ends at 24°C? What is the fundamental frequency and wavelength of the same pipe if it is closed at one end? For each pipe, what is the next highest frequency that supports a standing wave in the pipe?

closed at one end? For each pipe, what is the next highest frequency that supports a standing wave in the pipe?

$$\frac{6\rho cv}{\lambda_n} \approx \frac{2L}{N} \qquad \lambda_n = \frac{2(1m)}{1} = 2m$$

$$\frac{2L}{N} \qquad \lambda_n = \frac{2L}{N} \qquad \lambda_n = \frac{2(1m)}{1} = 2m$$

$$\frac{2L}{N} \qquad \lambda_n = \frac{2L}{N} \qquad \lambda_n = \frac{2(1m)}{1} = 2m$$

$$\frac{2L}{N} \qquad \lambda_n = \frac{2L}{N} \qquad \lambda_n = \frac{2L}$$

- 15. On a guitar each string has a different mass density and tension, but also the fret board of the guitar allows you to shorten the length of each string. The frequency of the top E string at is full length of about a meter is about 164 Hz.
  - If I press the string on a fret to half the length of the string, then how much does the fundamental frequency change? State it as a difference, and a ratio, and a percent change.

• On a guitar, the frets are spaced so that there are 12 divisions. So if the divisions are equally spaced (they aren't for reasons that are outside the scope of this problem) then how much does the length change with each fret?

 So how much does each fret shorten the string by? If I press on the first fret by how much did the frequency change? As a difference and a percent change?

• What about the next fret as a difference and percent change?

$$\lambda_{1} = 2\frac{1}{2} = 2$$

$$\lambda_{1} = 2\frac{1}{2} = 2$$

$$\lambda_{2} = 34 \frac{1}{2} = 34 \frac{1}{2}$$

$$V_{15} = V_0 \left( \frac{T}{T_0} \right)^2 = 331 \text{ m/s} \left( \frac{298}{273} \right)^{1/2}$$

$$V_{25} = 346 \text{ m/s}$$

$$V_{25} = 346 \text{ m/s} = 6.92 \text{ m}$$

$$V_{3} = \frac{V_{3}}{V_{3}} = \frac{346 \text{ m/s}}{50 \text{ H/z}} = 6.92 \text{ m}$$

pressure wave? If the temperature drops to 10 °C, by how much does the fundamental frequency change?

$$f_{n} = \frac{nv}{2L} \qquad f_{1} = \frac{1.340 \text{ m/s}}{2(2 \text{ m})} = 85 \text{ Hz}$$

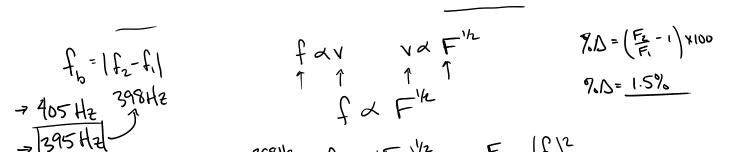
$$f_{2} = \frac{2.340}{2(2)} = 2.85 = 170 \text{ Hz}$$

$$f_{3} = 255 \text{ Hz}$$

frequency change?

$$rac{put}{2} = \frac{nv}{2L} \quad f_1 = \frac{1 \cdot 340 \text{ m/s}}{2(2 \text{ m})} = 85 \text{ Hz}$$
 $f_2 = \frac{2 \cdot 340}{2 \cdot (2)} = 2 \cdot 85 = 170 \text{ Hz}$ 
 $f_3 = 255 \text{ Hz}$ 
 $f_4 = 255 \text{ Hz}$ 
 $f_5 = 212.5 \text{ Hz}$ 
 $f_7 = 42.5 \text{ Hz}$ 
 $f_8 = 212.5 \text{ Hz}$ 
 $f_8 = 255 \text{ Hz}$ 

17. What are the three lowest standing wave frequencies of a 2 m long pipe that is open on both ends when the speed of sound is 340 m/s? What if the pipe were closed on one end?



18. Two strings of a guitar are being played at the same time. One string has a frequency of 400Hz. A beat frequency of 5 Hz can be heard. What are the possibilities for the frequency of the second string? If the tension in the second string increased, and the beat frequency decreases to 2Hz, then what can you conclude about the frequency of the second string before it was tightened? By what percent was the tension in the string increased? By what percent would the tension need to be increased in order to eliminate the beating?

19. Imagine the last problem if tightening the string had *increased* the beat frequency. What would you conclude about the original frequency then?

Table 12.2 Pressure Amplitudes, Intensities, and Intensity Levels of a Wide Range of Sounds in Air at 20°C (Room Temperature)

Sound	Pressure Amplitude (atm)	Pressure Amplitude (Pa)	Intensity (W/m²)	Intensity Level (dB)
Threshold of hearing	$3 \times 10^{-10}$	$3 \times 10^{-5}$	$10^{-12}$	0 6
Leaves rustling	$1 \times 10^{-9}$	$1 \times 10^{-4}$	$10^{-11}$	10
Whisper (1 m away)	$3 \times 10^{-9}$	$3 \times 10^{-4}$	$10^{-10}$	20
Library background noise	$1 \times 10^{-8}$	0.001	$10^{-9}$	30
Living room background noise	$3 \times 10^{-8}$	0.003	$10^{-8}$	40
Office or classroom	$1 \times 10^{-7}$	0.01	$10^{-7}$	50
Normal conversation at 1 m	$3 \times 10^{-7}$	0.03	$10^{-6}$	60
Inside a moving car, light traffic	$1 \times 10^{-6}$	0.1	$10^{-5}$	70
City street (heavy traffic)	$3 \times 10^{-6}$	0.3	$10^{-4}$	80
Shout (at 1 m); or inside a subway train; risk of hearing damage if	$1 \times 10^{-5}$	1	$10^{-3}$	90
exposure lasts several hours				
Car without muffler at 1 m	$3 \times 10^{-5}$	3	$10^{-2}$	100
Construction site	$1 \times 10^{-4}$	0	$10^{-1}$	110
Indoor rock concert; threshold of pain; hearing damage occurs rapidly	$3 \times 10^{-4}$	30	1	120
Jet engine at 30 m	$1 \times 10^{-3}$	100	10	130